

Appendix C

Quality of the Data

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Introduction

This appendix discusses several issues relating to the quality of the Residential Transportation Energy Consumption Survey (RTECS) data and to the interpretation of conclusions based on these data. The first section discusses under-coverage of the vehicle stock in the residential sector. The second section discusses the effects of using July 1991 as a time reference for the survey. The remainder of this appendix discusses the treatment of sampling and nonsampling errors in the RTECS, the quality of specific data items such as the Vehicle Identification Number (VIN) and fuel prices, and poststratification procedures used in the 1991 RTECS.

The quality of the data collection and the processing of the data affects the accuracy of estimates based on survey data. All the statistics published in this report such as total vehicle miles traveled (VMT) are estimates of population values. These estimates are based on observations from a randomly chosen subset of the entire population of occupied housing units. Consequently, the estimates always differ from the true population values. Because the RTECS is a sample survey, data from the 1991 RTECS are subject to various sources of nonsampling and sampling error.

Nonsampling error is a measure of variability due to the conduct of the survey. These errors can include: population undercoverage during sampling; questionnaire wording and format; response bias and variance; interviewer error; coding and/or keypunching error; and nonresponse bias. Nonsampling errors are treated in several sections of this appendix. The main section pertains to the imputation procedures used for item nonresponses, and the special treatment given to the fuel efficiency, reported in miles per gallon (MPG), of pre-1975 vehicles.

Sampling error is a measure of the variability in the data because a sample of households was surveyed rather than the entire population. The different samples that could be selected would each produce different values for the survey statistics. Because the survey used probability sampling techniques, it is possible to estimate the size of the sampling error for any statistic. These estimates can be used as a guide in making inferences from the sample estimates to the total population. The final section on sampling error pertains to estimating the magnitude of the error and the presentation of sampling errors as row and column factors in the detailed tables of this report.

Noncovered Residential Vehicles

The RTECS is a subsample of the Residential Energy Consumption Survey (RECS). Therefore, any type of household not covered in the RECS would affect the type of household vehicles not covered in the RTECS. The following types of individuals or families were not covered by RECS and, hence, the vehicles corresponding to these households were not covered by RTECS.

- Families or individuals living in group quarters such as college dormitories, military barracks, or large boarding houses (10 or more unrelated adults).
- Families or individuals living in recreation vehicles or other vehicles.

- Families or individuals with no fixed address.

The effect of these omissions is an underestimation of the total number of vehicles in the residential sector and an underestimation in the number of miles driven, gallons consumed, and dollars spent.

July 1991 as a Reference for Number of Households

The design of RTECS calls for households to be followed for the 1991 calendar year. Consequently, households formed during 1991 are represented in the sample by households that existed at the time the 1990 RECS was fielded. Hence, RTECS may have an over-representation of established households at the expense of newly formed households.

The decision to follow households for the entire year and not add a sample of households formed during 1991 means that as the survey progressed through 1991, the estimate of the number of vehicles accumulated a negative bias. This happens for several reasons.

- When established households separate, only part of the household is followed by RTECS. If the part of the household that is not followed takes a vehicle with them, that vehicle is counted as a disposed vehicle.
- Any vehicle acquired by a household member that leaves the household is not included in the RTECS.
- The number of households for the 1991 RTECS is set equal to the Current Population Survey (CPS) estimate of the number of households as of July 1991. (See the section below on poststratification.) RTECS does not provide for an increasing number of households from January to December. The household number for July is the number used for the entire year. This has the effect of overestimating the number of households and vehicles for January 1991 and underestimating the number for December 1991.

Nonsampling Error

Nonsampling errors are due to the conduct of the survey, and include both random errors and systematic errors or biases. The magnitudes of nonsampling biases cannot be estimated from the sample data. Thus, avoidance of systematic biases is a primary objective of all stages of survey design. (See Appendix A, "How the Survey was Conducted," for a discussion of procedures implemented to minimize all types of nonsampling errors.) Subsequent to conducting a survey, problems of unit nonresponse and item nonresponse need to be addressed. The treatment in the RTECS of these types of errors are discussed in separate sections below.

Unit Nonresponse

Unit nonresponse is the type of nonresponse that occurs when no data are available for an entire sampled household. Most unit nonresponse cases are caused by the respondent being unavailable or the respondent's refusal to cooperate.

Unit nonresponse for the 1991 RTECS must be addressed in the context of the unit nonresponse for the 1990 RECS, since the 1991 RTECS sample was drawn from households that responded to the 1990 RECS. Thus, in all cases, at least the RECS data were available for every RTECS household, therefore, no RTECS household was a total

nonrespondent. Generally, weight adjustment was the method used to reduce unit nonresponse bias in the RECS statistics and that adjustment carried over automatically to the RTECS subsample. (See *Housing Characteristics 1990* (published May 1992), DOE/EIA-0314(90) Appendix A, for a discussion of unit nonresponse adjustment.)

Imputation Procedures for Item Nonresponse

Item nonresponse occurs when the respondents do not know the answer or refuse to answer a question, or when an interviewer does not ask a question or does not record an answer. To facilitate "full-sample" data analyses, imputations were made to provide the most probable responses when responses were missing. The following imputation techniques were used: hot-decking, predictive mean matching, and regression.

Hot-Deck Procedure

The most commonly used technique of imputation for the RTECS was the hot-deck procedure. In hot-decking, when a certain response is missing for a given household or vehicle, another household or vehicle called a donor is randomly chosen to furnish its reported value for that missing item. The value is then assigned to the nonrespondent household or vehicle. To serve as a potential donor, a household or vehicle had to be similar to the nonrespondent in characteristics correlated with the missing item.

The RTECS items that were imputed using the hot-deck procedure were pre-1975 vehicle characteristics and fuel grade. Household demographic items such as family income and ethnic background were hot-decked as part of the RECS. (See *Housing Characteristics 1990* (published May 1992), DOE/EIA-0314(90), Appendix C, for a discussion of imputation of household characteristics.)

Predictive Mean Matching

Predictive mean matching was used for imputing changes in vehicle stock to households when those households were not followed for the complete duration of the RTECS. Changes to the vehicle stock were defined as acquisitions, dispositions, or a combination of both. In an ideal RTECS, a beginning vehicle stock inventory reported in the 1990 RECS interview would be followed throughout the 1991 RTECS calendar year and, at the time of each RTECS contact, changes in vehicle stock would be reported. However, because in some cases it was impossible to follow a household for the entire RTECS year due to attrition, it was unknown if, for these households, vehicle stock changes were made.

In the 1991 RTECS, 795 households (26 percent) were not followed for the entire RTECS calendar year. This figure represents the percentage of households that had imputations with respect to change in their vehicle stock. Within these households, 149 vehicles (2.4 percent) of the 6,084 total RTECS sample vehicles were imputed as acquisitions and 164 (2.7 percent) of the total sample vehicles were imputed as disposed vehicles.

To impute vehicle stock changes in the 1991 RTECS, logistic regression equations were used to compute a predicted probability (or propensity) of a household making a change in the vehicle stock during the RTECS data year. These propensities were computed for all households in the data set including households lost through attrition. For each household that was not followed during the year, a donor household was found by selecting the respondent household with a propensity closest in value to the "lost" household. This procedure of matching a donor and recipient using a prediction model is called "predictive mean matching." Once a donor household was found, it provided all vehicle

stock changes, if any, to the "lost" household.¹³ The independent variables were the following four household attributes: (1) age of head of household; (2) number of drivers in the household; (3) total number of vehicles; and (4) vintage of household's newest vehicle.

Backward elimination was used to fit the final models. The binary response variable took a value of 1 if the respondent changed vehicle stock, and 0 if otherwise. The equations were independently fitted and employed within categories defined by (1) time of last contact which could be the RECS interview, the RTECS Beginning-of-Year (B-O-Y) interview, or the RTECS Mid-Year (M-Y) interview, and (2) the number of vehicles in the household at the time of last contact (expressed as two categories: one vehicle, and more than one vehicle). Use of these categories excluded the possibility, for example, of a recipient household (one that was not tracked) with one vehicle being matched to a donor household that had disposed of two of its three vehicles. To achieve additional consistency, the matching procedure was carried out within geographic cells defined by the nine Census divisions and Metropolitan Statistical Area (MSA) versus non-MSA.

¹³R. Little, "Missing-Data Adjustments in Large Surveys," *Journal of Business and Economic Statistics*, pp. 287-301.

If a recipient household was imputed to have acquired a vehicle, certain attributes for that vehicle were "borrowed" from the donor household. These attributes were date of acquisition, date of disposal, vehicle type, vehicle make, model and year, number of cylinders, type of transmission, type of fuel and MPG.

In addition to imputing vehicle acquisitions, some recipient households were imputed to have disposed of some of their vehicle stock. This occurred when a recipient household was matched to a donor that had disposed of some of its vehicle stock. The recipient household was imputed to have disposed of the same number of vehicles that the donor household had disposed of. The vehicles imputed as disposed of by the recipient household were chosen so that they occupied the same rank in terms of model year, as the vehicles disposed of by the donor household (for example, the oldest vehicle, or the next oldest).

The predictive mean matching procedure was validated by simulating the imputation task. Of the 2,366 1985 RTECS donor households, 600 households were randomly selected to act as recipient households. Since the actions of these 600 pseudo-recipient households were known, a direct comparison was made between the known action and the predicted action.

Overall, the prediction accuracy at the national level was 92.3 percent. That is, the distribution of the observed stock changes among the 600 recipient households differed from the distribution of the predicted vehicle stock changes by 46 households. At the regional level, the prediction accuracy was 78.4 percent in the Northeast Census Region, 84.4 percent in the Midwest Census Region, 71.5 percent in the South Census Region and 79.0 percent in the West Census Region.

Predictive mean matching could not be used for households with zero vehicles in stock. There was an insufficient number of households with zero vehicles to achieve significant estimates of parameters for the logistic regression models. For households without vehicles, that were lost from the survey through attrition, a hot-deck procedure was employed for imputing changes to the vehicle stock.

Regression Procedures

Multiple regressions were used to impute for annual VMT for vehicles imputed as acquired, since two odometer readings were not available in these cases. Simple linear and multiple regressions were also used to impute annual mileage for other vehicles when two odometer readings were not obtained. (See Appendix B, "Estimation Methodologies," for details on the imputation of VMT).

Imputation of Vehicle Characteristics for 1975 and Later

Vehicle characteristics that were missing for vehicle model years 1975 and later were imputed using either the VIN or the Environmental Protection Agency (EPA) certification files (CERT files) containing laboratory test results of MPG. When the vehicle characteristic was missing from the questionnaire, but the VIN was available, the characteristics from the VIN were used. Additionally, when there was a discrepancy between the VIN and the RTECS respondent's answer, the VIN generally overrode the response provided by the respondent. If both the VIN and questionnaire responses were missing, the vehicle characteristics were imputed from the CERT files. An individual record from the CERT files was chosen as a donor for a recipient sample vehicle by first narrowing the choice by using the known vehicle characteristics of the recipient vehicle, and then second, selecting a single CERT record according to probabilities proportional to vehicle sales. The type of fuel (gasoline or diesel) used in the vehicle was also imputed using the EPA CERT files (See Appendix B, "Estimation Methodologies," for more details on the use of EPA CERT files in the 1991 RTECS.)

Imputation of Vehicle Characteristics and MPG for Pre-1975 Vehicle Model Years

For all RTECS sample vehicles, the questionnaires and VIN's jointly provided the following vehicle characteristics: make, model, model year, number of cylinders, engine displacement (liters or cubic inches), transmission type (automatic or manual), and fuel system type (carbureted, gasoline fuel injected, or diesel). Many of these characteristics were used to assign EPA test MPG to the sample vehicles. EPA records, in the form of CERT files, were used to provide these MPG, as well as to provide any vehicle characteristics that were not obtained from the questionnaire or VIN (See Appendix B, "Estimation Methodologies," for more details.)

The EPA CERT files, however, have only been available since 1975. The 1991 RTECS file contained 556 pre-1975 vehicles (9 percent), and for these vehicles, missing characteristics were imputed by a hot-deck procedure using 1991 respondents as donor vehicles. Each donor and recipient vehicle was paired on as many of the following characteristics as possible: make, model, model year, transmission type, number of cylinders, and engine displacement.

The MPG for pre-1975 vehicles were imputed using a cold-deck procedure. The donor vehicles were respondents from the 1985 RTECS. Fuel purchase diaries were used in the 1985 RTECS; therefore, no shortfall adjustments were needed for the MPG. Cold-decking was performed within categories defined by make, model, model year, transmission type, and number of cylinders, with collapsing of categories performed where necessary. For example, MPG could be selected from donor vehicles of a certain size class in either the Pontiacs or the Chevrolets, if they shared similar model years, transmission type, and the General Motors 350 cubic inch V-8 engine. However, it appeared that a greater share of the variability in the 1985 RTECS MPG was due to individual driving habits, automotive maintenance and diary keeping, rather than to vehicle characteristics.

Quality of Specific Data Items

Vehicle Identification Number

The VIN is a unique combination of numbers and letters that when decoded provide the characteristics of a particular vehicle. Since 1954, the VIN has been used by American automobile manufacturers. Beginning with the 1981 model year, a standard 17-character VIN was assigned to all vehicles sold in the United States. VIN's were obtained for most of the vehicles in the 1991 RTECS. The vehicle characteristics from decoded VIN's were employed in the 1991 RTECS to enhance the accuracy of reported vehicle characteristics. These characteristics were used in determining vehicle fuel efficiency based on the EPA certification files of test laboratory MPG estimates (See Appendix A, "How the Survey Was Conducted," for a discussion of the VIN.)

There were three occasions where attempts were made to obtain the VIN's: the RECS interview, the Beginning-of-Year (B-O-Y) interview, and the End-of-Year (E-O-Y) interview.

A computer software program, VINDICATOR, from the Highway Loss Data Institute, was used to decode the VIN's. For VIN's that could not be decoded immediately using this program, a computer routine was developed to correct for common errors in the transcription of VIN's. The vehicle characteristics produced for these "fixed" VIN's were then carefully compared to respondent information. Approximately 200 VIN's were salvaged using this routine.

Overall, the collection of the VIN was a highly successful endeavor that yielded quality data. VIN's were obtained

for 4,617 (76 percent) of the 6,084 total sample vehicles. Of the 4,617 obtained VIN's, 3,842 (83 percent) were considered "good" VIN's. In summary, "good" VIN's were obtained for 3,842 (63 percent) of the 6,084 sampled vehicles. (A good VIN was one that did not require correcting for common transcription error before it could be decoded.)

Vehicle Fuel Price and Expenditures

Vehicle Fuel Price: In the 1991 and 1988 RTECS, compared to previous RTECS, the fuel price data were not collected via fuel purchase diaries. Instead, fuel prices were determined from Bureau of Labor Statistics (BLS) Retail Pump Average Gasoline Prices and the Lundberg Survey, Inc., prices. (See Appendix B, "Estimation Methodologies" for a discussion of the sources of vehicle fuel prices and the assignment of specific prices to the RTECS data.)

To validate the 1988 and 1991 RTECS price methodology prior to the 1988 and 1991 RTECS, the 1985 RTECS gasoline prices were recalculated and analyzed using the new 1991 methodology (BLS price data). Results of this analysis suggest that if the 1985 BLS price data had been used in 1985 instead of fuel purchase diary data, the average vehicle fuel price reported for the 1985 RTECS would have increased by approximately 2 cents per gallon.

For this analysis, only the prices for unleaded regular gasoline, unleaded premium gasoline, and leaded regular gasoline were recalculated. The prices for leaded premium, diesel, and other fuels were left equal to the prices used in the 1985 RTECS.

The BLS prices that were used for recalculating the 1985 RTECS prices were monthly 1985 regional retail gasoline prices for leaded regular, unleaded regular, and unleaded premium. The prices were averaged across months for each of the above fuel types within each of the four Census regions. One of these average prices was assigned to each of the RTECS vehicles depending on Census region and on vehicle fuel type used.

Table C1 presents the BLS prices (monthly prices were for 1985) with the corresponding average prices from the 1985 RTECS. Overall, the BLS prices compared well with the corresponding average regional fuel prices from RTECS. The largest difference corresponded to unleaded premium gasoline.

While there was general consistency between the BLS prices and the 1985 RTECS prices, the differences that did exist may have stemmed from the differences in the two survey populations and survey collection procedures.

- The BLS population (approximately 85 percent of the total U.S. population) consisted of the U.S. urban, noninstitutional population excluding households living on military bases. The RTECS population represented both urban and rural areas and included military bases.
- BLS prices were based on prices gathered from service stations and sales volume. The 1985 RTECS prices were produced from fuel quantities and expenditures for individual vehicle refuelings.
- The BLS sample was a rotating sample of service stations. Every year approximately one-fifth of the service stations in the sample were replaced with service stations that consumers reported using in that year's "Point of Purchase Survey" conducted by the BLS. Thus, the BLS prices included service stations where consumers currently purchased fuel as well as stations where they had previously purchased fuel. The RTECS prices were based entirely on the service stations where consumers were currently purchasing their vehicle fuel.

Table C1. Average Bureau of Labor Statistics Gasoline Prices and 1985 Residential Transportation Energy Consumption Survey Prices by Census Region and Fuel Type

Census Region and Fuel Type	Average Price (dollars per gallon)	
	1985 RTECS	1985 BLS ^a
Total U.S.		
Total	\$1.1805	\$1.1969
Unleaded Regular	1.1848	1.2001
Unleaded Premium	1.2945	1.3396
Leaded Regular	1.1080	1.1128
Leaded Premium	1.3087	b
Diesel	1.1845	b
Other	1.1702	b
Northeast		
Total	1.2033	1.2082
Unleaded Regular	1.1931	1.2000
Unleaded Premium	1.3151	1.3327
Leaded Regular	1.1358	1.1243
Leaded Premium	1.3220	b
Diesel	1.2123	b
Other	1.2209	b
Midwest		
Total	1.1831	1.2098
Unleaded Regular	1.1916	1.2185
Unleaded Premium	1.2838	1.3572
Leaded Regular	1.1244	1.1333
Leaded Premium	1.2495	b
Diesel	1.1862	b
Other	1.1965	b
South		
Total	1.1620	1.1847
Unleaded Regular	1.1615	1.1805
Unleaded Premium	1.2795	1.3302
Leaded Regular	1.0806	1.0927
Leaded Premium	1.2333	b
Diesel	1.1706	b
Other	1.1112	b
West		
Total	1.1909	1.1938
Unleaded Regular	1.2075	1.2091
Unleaded Premium	1.3300	1.3562
Leaded Regular	1.1170	1.1153
Leaded Premium	1.3985	b
Diesel	1.1885	b
Other	1.2040	b

^aBLS average prices in this table were derived by assigning BLS prices to the 1985 RTECS sample vehicles, then producing national averages using the 1985 RTECS sample weights.

^bPrices for these fuels were not collected by BLS; therefore, the 1985 RTECS prices were used.

Vehicle Fuel Expenditures: Vehicle fuel expenditures were calculated by multiplying the price paid for fuel by the quantity of fuel used. Expenditures per household were the sum of the expenditures for each vehicle in the household. To assess the effect of the 1988 RTECS price methodology on vehicle fuel expenditures, the 1985 household vehicle fuel expenditures were recalculated using the 1985 BLS price data. Table C2 compares average expenditures by fuel type and Census region using both sources of price data.

The use of BLS prices for the 1985 RTECS would have increased the per household expenditures for vehicle fuel from \$1,274 per year to \$1,292 per year. The changes in expenditures reflect differences in the average price of gasoline between the new 1988 methodology and the 1985 RTECS methodology since the average consumption used to calculate the expenditures comes from the RTECS data under the new and original methodologies. The estimated total 1985 U.S. expenditures for vehicle fuel increased from 99.1 billion dollars to 100.4 billion dollars when the 1988 methodology was applied to the 1985 RTECS data.

The 1988 RTECS price methodology seemed to have little effect on the standard errors of expenditure statistics. When the 1985 RTECS prices were recalculated using 1985 BLS price data, the standard errors of the expenditures were close to the standard errors reported using the 1985 RTECS fuel purchase diary data. While the standard errors of the fuel prices were reduced, in some cases by 50 percent, the variability in fuel prices was very small relative to the variability in gallons of fuel consumed. Therefore, the standard errors of the vehicle fuel expenditures were largely controlled by the variability in gallons of fuel consumed.

Gasohol

In the 1991 RTECS, a little over 1.6 million households reported that they purchased gasohol. In the 1988 RTECS, there was no category for "gasohol" in the detailed tables showing "Type of Fuel Purchased" but there is reason to believe that a small portion of the 81.1 billion gallons of gasoline was gasohol since an estimated 8,138 gallons of gasohol was sold in 1988. This estimate was derived from Federal Highway Administration Statistics (Department of Transportation, Washington, D.C., *Monthly Gasohol Reported by States--1988*, Table MF-33GLA). Only a few 1988 RTECS households reported purchasing gasohol. Gasohol, a mixture of 10 percent ethanol and 90 percent gasoline, is not sold under the name "gasohol". It is sold as "ethanol blends." Given the disparity between the few households reporting purchasing gasohol and the amount of gasohol sold, it does seem likely that some households that reported purchasing gasoline actually bought "gasohol" or "ethanol blends," resulting in an underestimation of the amount of gasohol consumed in 1988. Whether the use of "ethanol blend" in the questionnaire in place of "gasohol" would have increased reports of the alcohol fuel is speculative.

Sampling Error

The random differences between the survey estimates and the true population value that occur because of the particular sample that was selected are known as sampling errors. The average sampling error, averaged over all possible samples, should be zero. Although the sampling error is nonzero and unknown for the particular sample chosen, the sample design permits sampling errors to be estimated. The typical magnitude of the sampling error is measured by the "standard error" of the estimate. Standard errors in this report are given as percents of their estimated values, that is, as relative standard errors (RSE). The RSE is also known as the coefficient of variation.

Table C2. Average Bureau of Labor Statistics Vehicle Fuel Expenditures and 1985 Residential Transportation Energy Consumption Survey Vehicle Fuel Expenditures by Census Region and Fuel Type

Census Region and Fuel Type	Average Expenditures	
	1985 RTECS	1985 BLS ^a
Total U.S.		
Total	\$1,274	\$1,292
Unleaded Regular	686	695
Unleaded Premium	213	220
Leaded Regular	341	342
Leaded Premium	10	b
Diesel	22	b
Other	2	b
Northeast		
Total	1,169	1,174
Unleaded Regular	694	698
Unleaded Premium	225	228
Leaded Regular	232	229
Leaded Premium	6	b
Diesel	12	b
Other	1	b
Midwest		
Total	1,266	1,294
Unleaded Regular	724	741
Unleaded Premium	164	174
Leaded Regular	352	355
Leaded Premium	5	b
Diesel	17	b
Other	3	b
South		
Total	1,321	1,347
Unleaded Regular	659	670
Unleaded Premium	281	292
Leaded Regular	348	352
Leaded Premium	10	b
Diesel	21	b
Other	2	b
West		
Total	1,304	1,307
Unleaded Regular	678	679
Unleaded Premium	147	149
Leaded Regular	418	417
Leaded Premium	21	b
Diesel	39	b
Other	2	b

^aBLS average expenditures in this table were derived by assigning BLS prices by fuel type and region to the 1985 RTECS sample vehicles, then producing expenditure averages by using the 1985 RTECS quantities of vehicle fuel consumed.

^bPrices for these fuels were not collected by BLS; therefore, the 1985 RTECS prices were used in the computations.

For a given survey statistic, Y , the relative standard error, $RSE(Y)$ is given by:

$$RSE(Y) = (S_y/Y) \times 100. \quad (1)$$

The standard error of Y is S_y . Therefore:

$$S_y = RSE(Y) \times Y/100. \quad (2)$$

The following sections provide a discussion of the procedure used to estimate sampling variances as well as an explanation and example of the procedures used to calculate approximate RSE's for each statistic shown in Tables 6 through 23 in the "Detailed Tables" section of this publication.

Balanced Half-Sample Replication

For some surveys, a convenient algebraic formula for computing variances can be obtained. However, the RECS (of which the RTECS is a subsample) used a multistage area sample design of such complexity that it is virtually impossible to construct an exact algebraic expression for estimating variances (See *Housing Characteristics 1990* (published May 1992), DOE/EIA-0314(90) Appendix A). Instead, the method used to estimate sampling variances for this survey was balanced half-sample replication. This numerical method involves pairing primary sampling units (PSU) in the strata so that differences between the members of each pair can be used to build an estimate of sampling variance. The strata were collapsed to 85 new strata to achieve this pairing of PSU's. Of these 85 strata, 44 each contained two nonself-representing PSU's belonging to the same Census division, with one PSU constituting each member of a pair. Of the remaining 41 strata, 32 were each composed of one self-representing PSU; that is, they consisted of large metropolitan areas that came into the sample with certainty. In each of the latter strata, all of the PSU's were treated as a composite PSU, while the segments within the composite PSU were segregated into two groups representing the two members of a pair. There was no between-PSU component of variance for self-representing PSU's. The nine remaining strata contained nonself-representing PSU's that were treated as if they were self-representing PSU's. These nine strata were in separate Census divisions, and were not collapsed to form pairs of nonself-representing PSU's due to a desire to restrict pairing to within the nine Census divisions, and also due to the desire to treat Alaska and Hawaii as two separate and unique strata.

Balanced half-sample replication involved repeatedly drawing pair members from the 85 strata. Each replication is called a "half-sample" because only one member of the pair within each of the 85 strata was selected. The poststratification procedure described in Appendix A, "How the Survey Was Conducted," was performed independently for each half-sample, so that the resulting variance estimates would reflect the benefits of poststratification. The sample units drawn into each half-sample and adjusted by poststratification can produce unbiased survey statistics based on roughly one-half of the data. Using different combinations of members from the 85 pairs, it is possible to produce a total of $2^{85} = 3.9 \times 10^{25}$ unique half-samples.

Although desirable for good variance estimation, a large number of half-samples would be computationally infeasible. However, the method of balanced half-sample replication allows a small number of half-samples (approximately equal to the number of strata) to produce estimates of variance that are identical to estimates based on all possible unique half-samples for linear survey statistics. The use of ratio adjustments such as poststratification means that even a statistic giving the number of households in a category is not a linear statistic. For nonlinear survey statistics,

the variance estimate computed using the method of balanced half-samples is approximately equal to the variance estimate computed using all possible half-samples. With this balancing method each half-sample is constructed by using an orthogonal matrix to control the selection of pair members from strata. For the RTECS, 128 balanced half-samples were used in variance estimation.

The variances are estimated from the 128 half-sample-based statistics in the following way. Let Y' be a survey estimate of characteristic Y for a certain category of housing units (for example, total consumption of vehicle fuel in the West Census Region). Then, the estimated variance of Y' is given by:

$$S_{y'}^2 = \frac{1}{128} \sum_{i=1}^{128} (Y'_i - Y')^2, \quad (3)$$

where Y'_i is the i^{th} half-sample estimate of Y . The standard error of Y' is given by:

$$S_{y'} = \sqrt{S_{y'}^2} \quad (4)$$

Row and Column Factors

RSE's were calculated for all statistics in this publication, although they cannot be presented due to space limitations. However, the RSE's are presented in a generalized form. The method of presenting generalized RSE's of statistics uses sets of row and column factors inserted in the top row and right-most column of figures in each table. This method of presentation allows the readers to calculate an approximate RSE for each statistic. To estimate the RSE of a statistic in the i^{th} row and j^{th} column of a particular table, the approximation $RSEA_{ij}$ for the original RSE_{ij} is given by:

$$RSEA_{ij} = R_i \times C_j \quad (5)$$

Where: R_i is the RSE row factor given at the right-most margin of row i in the tables, and C_j is the RSE column factor given at the top of column j .

The following example illustrates this procedure:

Referencing the second row of the table (Figure C1) labeled "Northeast," and the third column labeled "Vehicle Miles Traveled (billion)," yields an estimate of 295 billion miles driven. The RSE row factor is $R_2 = 4.4$, and the RSE column factor is $C_3 = 1.1$. The approximate RSE for the estimate is, therefore,

$$RSEA_{2,3} = 4.4 \times 1.1 = 4.84 \text{ percent.} \quad (6)$$

The standard error derived from row and column factors can be used to construct confidence intervals as in Figure C1, and to perform hypothesis tests by standard statistical methods. However, because the generalized variance procedure gives only approximate RSE's, such confidence intervals and statistical tests must also be regarded as only approximate.

For the example above, the RSE determined directly by the half-sample method is actually 5.20 percent, not 4.84 percent.

Figure C1. Use of RSE Row and Column Factors

Total Vehicle Miles Traveled in the Northeast Census Region = 295 billion miles

R (Northeast Census Region) = 4.4
C (Vehicle Miles Traveled) = 1.1

Approximate RSE
(Total Vehicle Miles Traveled in the Northeast Census Region) = (4.4) X (1.1)
= 4.84 percent

Approximate Standard Error
(Total Vehicle Miles Traveled in the Northeast Census Region) = (4.4) X (1.1) X 295/100
= 14.29 billion miles

Approximate 2 Standard Errors
(95 percent confidence interval) = (1.96) X (14.29)
= 28.01 billion miles

Therefore, with approximately 95 percent confidence, the total vehicle miles traveled in the Northeast Census Region in 1991 was between 267 billion and 323 billion miles (295 ± 28)

Source: Energy Information Administration, Office of Energy Markets and End Use, the 1991 Residential Transportation Energy Consumption Survey.

Derivation of Row and Column Factors

The row and column factors are determined from a two-factor analysis of the table of RSE's on the basis of the two-way model,

$$\begin{aligned}
m &= \overline{(\log RSE)} \\
a_i &= \overline{(\log RSE)_{i.}} - \overline{(\log RSE)} \\
b_j &= \overline{(\log RSE)_{.j}} - \overline{(\log RSE)}
\end{aligned}
\tag{7}$$

Where:

- $\overline{(\log RSE)}$ = the mean of log RSE_{i,j} over all rows i and columns j,
- $\overline{(\log RSE)_{i.}}$ = the mean over all columns j for a particular row i, and
- $\overline{(\log RSE)_{.j}}$ = the mean over all rows i for a particular column j.

The row and column RSE factors are then computed as:

The RSE row factor, R_i, is the geometric mean of the RSE's in row i. The RSE column factor, C_j, is an adjustment

factor with geometric mean equal to 1.0.¹⁴

$$R_i = \text{antilog}(m + a_i) = \text{antilog}(\overline{(\log RSE)_i}) \quad (8)$$

Statistics in the tables in the

$$C_j = \text{antilog} b_j = \text{antilog}(\overline{(\log RSE)_j} - \overline{(\log RSE)}) . \quad (9)$$

"Detailed Tables" section are suppressed by the footnote symbol "Q" if (1) the RSE exceeds 50 percent, or (2) for tables showing household counts, fewer than 10 sample households were used to compute the statistics, or (3) for tables showing vehicle counts, fewer than 18 sample vehicles were used to compute the statistics. The estimation procedure used to obtain the row and column factors does not use RSE's for statistics that were suppressed by the footnote "Q" or for statistics with RSE's that are less than 1.0 percent. In addition, if the statistic for a cell is not listed for any other reason, the RSE for that cell is not used in the procedure. This convention is used because the product of the row and column factors frequently is an inaccurate estimate for these RSE's.

Using these cells in the calculation of the row and column factors may result in factors that give inaccurate RSE estimates for other cells actually presented in the table.

Whenever a household count is a poststratification control total, its RSE estimate is zero. An example is the cell in the first row and first column of Table 25. This cell contains an estimate of the national total of households as of July 1991 (that is, households with and without vehicles). Because the RSE is zero, this cell was not used in the computation of row and column factors. Zero RSE's are never used in row and column calculations, because their inclusion would make the row and column factors inappropriately low for the bulk of the statistics in the tables. Therefore, RSE's calculated from row and column factors for the total household count in Table 25 or for any other poststratification control total, will be inappropriately overestimated.

Determination of the Standard Error of the Difference Between Two Statistics

The procedure used to compute the standard error of the difference between two statistics follows:

$$SE(x_1 - x_2) = \sqrt{[SE(x_1)]^2 + [SE(x_2)]^2} . \quad (10)$$

This procedure assumes the two statistics are not correlated. The following example illustrates this procedure. Households with children drove an average of 22,800 miles per household in 1991. Households without children drove an average of 16,500 miles, for a difference of 6,300 miles. The RSE's for households with and without children are 2.9 and 2.3, respectively. The corresponding standard errors are 661 miles and 380 miles, respectively. Therefore, the standard error for the difference is:

$$SE(6,300) = \sqrt{[661]^2 + [380]^2} = 762 \text{ miles} . \quad (11)$$

If 1.96 times the standard error is greater than the difference between the statistics, the difference is not statistically significant at the .05 level of significance (the level used to test significance of inferences in this report). In this example, 1.96 times the standard error equals 1,494 miles, while the difference is 6,300 miles. Therefore, the con-

¹⁴For detailed discussions of the accuracy of the RSE approximation, the procedure for estimating confidence intervals, and the statistical tests of hypotheses, see Nonresidential Buildings Energy Consumption Survey: Commercial Buildings, Consumption and Expenditures, 1983, DOE/EIA-0318(83) (Washington, DC, October 1986).

clusion is that, in 1991, there was a significant difference in average mileage driven per household, between households with and without children.