## 6 Discounting Future Benefits and Costs

Discounting renders costs and benefits that occur in different time periods comparable by expressing their values in present terms. In practice, it is accomplished by multiplying the changes in future consumption (broadly defined, including market and nonmarket goods and services) that will be caused by a policy by a discount factor. At a summary level, discounting reflects the fact that people prefer consumption today over consumption in the future, and the fact that invested capital is productive and provides greater consumption in the future. Properly applied, discounting can tell us how much future benefits and costs are worth today.

At a more technical level, as detailed later in this chapter, discounting reflects (1) the amount of time between the present and the point at which these changes occur, (2) the rate at which consumption is expected to change over time in the absence of the policy, (3) the rate at which the marginal value of consumption diminishes with increased consumption, and (4) the rate at which the future utility from consumption is discounted with time. Changes in these components or uncertainty about them can lead to a discount rate that changes over time, but for many analyses it may be sufficient to apply a fixed discount rate or rates without explicit consideration of the constituent components or uncertainty.

Social discounting, the type of discounting discussed in this chapter, is discounting from the broad society-as-a-whole point of view that is embodied in benefit-cost analysis. Private discounting, on the other hand, is discounting from the specific, limited perspective of private individuals or firms. Implementing this distinction in practice can be complex, as detailed in this chapter, but it is an important distinction to maintain because using a given private discount rate instead of a social discount rate may bias results as part of a benefit-cost analysis.

This chapter addresses discounting over the relatively short term, what has become known as "intragenerational discounting" as well as discounting over much longer time horizons, or inter-generational discounting. Intra-generational, or conventional, discounting applies to those contexts that may well have decades-long time frames, but do not explicitly confront impacts on unborn generations that may be beyond the private planning horizon of the current ones. Inter-generational discounting, by contrast, addresses extremely long time horizons and the impacts and preferences of generations to come. To some extent this distinction is a convenience because there is no discrete point at which one moves from one context to another. However, the relative importance of various issues can change as the time horizon lengthens leading to different recommendations across these two scenarios.

The chapter begins with a description of the mechanics of discounting, followed by overviews of the background and rationale for discounting, and key considerations for discounting in the inter-generational context. The chapter concludes with recommendations and guidance for discounting in EPA benefit-cost analyses. ${ }^{72}$

[^0]
### 6.1 The Mechanics of Summarizing Present and Future Costs and Benefits

There are several methods for discounting future values to the present, the most common of which involve estimating net present values and annualized values. An alternative is to estimate a net future value.

### 6.1.1 Net Present Value

The net present value (NPV) of a projected stream of current and future benefits and costs relative to the analytic baseline is estimated by multiplying the benefits and costs in each year by a time-dependent weight, or discount factor, $d$, and adding all of the weighted values as shown in the following equation:

$$
\begin{equation*}
N P V=N B_{0}+d_{1} N B_{1}+d_{2} N B_{2}+\ldots+d_{n} N B_{n} \tag{1}
\end{equation*}
$$

where $N B_{t}$ is the net difference between benefits and costs $\left(B_{t}-C_{t}\right)$ that accrue at the end of period $t$. The discounting weights, $d_{t}$, are given by:

$$
\begin{equation*}
d_{t}=1 /(1+r)^{t} \tag{2}
\end{equation*}
$$

where $r$ is the discount rate. The final period of the policy's future effects is designated as time $n$.
The NPV can be estimated using real or nominal benefits, costs, and discount rates. It is important that the same discount rate be used for both benefits and costs because any policy can be justified by choosing a sufficiently low discount rate for benefits, by choosing sufficiently high discount rates for costs, or by choosing a sufficiently long time horizon. The analyst can estimate the present value of costs and benefits separately and then compare them to arrive at net present value.

When estimating the NPV, it is important to explicitly state how time periods are designated and when, within each time period, costs and benefits accrue. Typically, time periods are years, but alternative time periods may be justified if costs or benefits accrue at irregular or non-annual intervals. The preceding formula assumes that $t=0$ designates the beginning of the first period. Therefore, the net benefits at time zero $\left(N B_{0}\right)$ include a $C_{0}$ term that captures startup or one-time costs such as capital costs that occur immediately upon implementation of the policy. The formula further assumes that no additional costs are incurred until the end of the first year of regulatory compliance. ${ }^{73}$ Any benefits also accrue at the end of each time period.

Figure 6.1 illustrates how net benefits (measured in dollars) are distributed over time. $\mathrm{NB}_{1}$ is the sum of benefits and costs that may have been spread evenly across the four quarters of the first year (i through iv) as shown in the bottom part of the figure. There may be a loss of precision by "rounding" a policy's effects in a given year to the end or beginning of that year, but this almost always extremely small in the scope of an entire economic analysis.

[^1]Figure 6.2

|  |  | 1 | 1 | T | T | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year $t$ | 0 | 1 | 2 | 3 | 4 | ... |
| \$ | $N B_{0}$ | $N B_{1}$ | $N B_{2}$ | $N B_{3}$ | $N B_{4}$ | ... $N B_{n}$ |

Time $\rightarrow$

Yeart 0

\$ $\quad \mathrm{NB}_{0 \mathrm{i}} \quad \mathrm{NB}_{0 \mathrm{ii}} \quad \mathrm{NB}_{0 \mathrm{iii}} \quad \mathrm{NB}_{0 \text { iv }}$

### 6.1.2 Annualized Values

An annualized value is the amount one would have to pay at the end of each time period $t$ so that the sum of all payments in present value terms equals the original stream of values. Producing annualized values of costs and benefits is useful because it converts the time varying stream of values to a constant stream. Comparing annualized costs to annualized benefits is equivalent to comparing the present values of costs and benefits. Costs and benefits each may be annualized separately by using a two-step procedure. While the formulas below illustrate the estimation of annualized costs, the formulas are identical for benefits. ${ }^{74}$

To annualize costs, the present value of costs is calculated using the above formula for net benefits, except the stream of costs alone, not the net benefits, is used in the calculation. The exact equation for annualizing depends on whether or not there are any costs at time zero (i.e., at $t=0$ ).

Annualizing costs when there is no initial cost at $t=0$ is estimated using the following equation:

$$
\begin{equation*}
A C=P V C * \frac{r^{*}(1+r)^{n}}{(1+r)^{n}-1} \tag{3}
\end{equation*}
$$

where
$A C=$ annualized cost accrued at the end of each of $n$ periods;
$P V C=$ present value of costs (estimated as in in equation 1, above);
$r=$ the discount rate per period; and
$n=$ the duration of the policy.

[^2]Annualizing costs when there is initial cost at $t=0$ is estimated using the following slightly different equation:

$$
\begin{equation*}
A C=P V C * \frac{r^{*}(1+r)^{n}}{(1+r)^{(n+1)}-1} . \tag{4}
\end{equation*}
$$

Note that the numerator is the same in both equations. The only difference is the " $n+1$ " term in the denominator.

Annualization is also useful when evaluating non-monetized benefits, such as reductions in emissions or reductions in health risks, when benefits are constant over time. The average cost-effectiveness of a policy or policy option can be calculated by dividing the annualized cost by the annual benefit to produce measures of program effectiveness, such as the cost per ton of emissions avoided.

### 6.1.3 Net Future Value

Instead of discounting all future values to the present, it is possible to estimate their value in some future time period, for example, at the end of the last year of the policy's effects, $n$. The net future value is estimated using the following equation:

$$
\begin{equation*}
N F V=d_{0} N B_{0}+d_{1} N B_{1}+d_{2} N B_{2}+\ldots+d_{n-1} N B_{n-1}+N B_{n} . \tag{5}
\end{equation*}
$$

$N B_{t}$ is the net difference between benefits and costs $\left(B_{t}-C_{t}\right)$ that accrue in year $t$ and the accumulation weights, $d_{t}$, are given by

$$
\begin{equation*}
d_{t}=(1+r)^{(n-t)} \tag{6}
\end{equation*}
$$

where $r$ is the discount rate.

### 6.1.4 Comparing the Methods

Each of the methods described above uses a discount factor to translate values across time, so the methods are not different ways to determine the benefits and costs of a policy, but rather are different ways to express and compare these costs and benefits in a consistent manner. Net present value represents the present value of all costs and benefits, annualization represents the value as spread smoothly through time, and net future value represents their future value. For a given stream of net benefits, the NPV will be lower with higher discount rates, the NFV will be higher with higher discount rates, and the annualized value may be higher or lower depending on the length of time over which they are annualized. Still, rankings among regulatory alternatives are unchanged across the methods.

Depending on the circumstances, one method might have certain advantages over the others. Discounting to the present to get a NPV is likely to be the most informative procedure when analyzing a policy that requires an immediate investment and offers a stream of highly variable future benefits. However, annualizing the costs of two machines with different service lives might reveal that the one with the higher total cost actually has a lower annual cost because of its longer lifetime.

Annualized values are sensitive to the annualization period; for any given present value the annualized value will be lower the longer the annualization period. Analysts should be careful when comparing annualized values from one analysis to those from another.

The analysis, discussion, and conclusions presented in this chapter apply to all methods of translating costs, benefits, and effects through time, even though the focus is mostly on net present value estimates.

### 6.1.5 Sensitivity of Present Value Estimates to the Discount Rate

The impact of discounting streams of benefits and costs depends on the nature and timing of benefits and costs. The discount rate is not likely to affect the present value of the benefits and costs for those cases in which:

- All effects occur in the same period (discounting may be unnecessary or superfluous because net benefits are positive or negative regardless of the discount rate used);
- Costs and benefits are largely constant over the relevant time frame (discounting costs and benefits will produce the same conclusion as comparing a single year's costs and benefits); and/or
- Costs and benefits of a policy occur simultaneously and their relative values do not change over time (whether the net present value is positive does not depend on the discount rate, although the discount rate may affect the relative present value if a policy is compared to another policy).

Discounting can, however, substantially affect the net present value of costs and benefits when there is a significant difference in the timing of costs and benefits, such as with policies that require large initial outlays or that have long delays before benefits are realized. Many of EPA's policies fit these profiles. Text Box 6.1 illustrates a case in which discounting and the choice of the discount rate have a significant impact on a policy's net present value.

## Text Box 6.1 - Potential Impact of Discounting

Suppose the cost of some environmental policy that is incurred entirely in the present is $\$ 1$ billion, and that after 30 years a benefit results that is estimated to be worth $\$ 5$ billion in the future. Without discounting, a policy that offers benefits five times its cost appears to be a very worthwhile social investment. Discounting the $\$ 5$ billion future benefits, however, can radically alter the economic assessment of the net present value of the policy. $\$ 5$ billion 30 years in the future discounted at $1 \%$ is $\$ 3.71$ billion, at $3 \%$ it is worth $\$ 2.06$ billion, at $7 \%$ it is worth $\$ 657$ million, and at $10 \%$ it is worth only $\$ 287$ million. In this case, the range of discount rates generates over an order of magnitude of difference in the present value of benefits. Longer time horizons will produce even more dramatic effects on a policy's net present value. For this reason, in this type of scenario, the choice of the discount rate determines whether this policy is considered on economic efficiency grounds to offer society positive or negative net benefits.

### 6.1.6 Some Issues in Application

There are several important analytic components that need to be considered when discounting: risk and valuation, placing effects in time, and the length of the analysis.

### 6.1.6.1 Risk and Valuation

There are two concepts that are often confounded when implementing social discounting, but should be treated separately. The first is the future value of environmental effects, which depends on many factors,
including the availability of substitutes and the level of wealth in the future. The second is the role of risk in valuing benefits and costs. For both of these components, the process of determining their values and then translating the values into present terms are two conceptually distinct procedures. Incorporating future values of risk into the social discount rate not only imposes specific and generally unwarranted assumptions, but it can also hide important information from decision makers.

### 6.1.6.2 Placing Effects in Time

Placing effects properly in time is essential for net present value calculations to characterize efficiency outcomes. Analyses should account for implementation schedules and the resulting changes in emissions or environmental quality, including possible changes in behavior between the announcement of policy and compliance. Additionally, there may be a lag time between changes in environmental quality and a corresponding change in welfare. It is the change in welfare that defines economic value, and not the change in environmental quality itself. Enumerating the time path of welfare changes is essential for proper valuation and benefit-cost analysis.

For environmental health risks there are at least two kinds of time lags between exposures and effects:

- Latency is the time difference between initial exposure to a contaminant and an increase in health risks, while
- Cessation lag is time difference between reduction in exposure and a reduction in observed health effects.

Thus, one can consider latency as applying to a newly exposed population and cessation lag applying to a population with prior exposure. These timeframes need not be identical, as noted by EPA's Science Advisory Board:

> A good example is cigarette smoking: the latency between initiation of exposure and an increase in lung cancer risk is approximately 20 years. However, after cessation of exposure, risk of lung cancer begins to decline rather quickly. A benefits analysis of smoking cessation programs based on the observed latency would greatly underestimate the actual benefits. ${ }^{75}$

Both latency and cessation lag should both be accounted for in an economic analysis. Assuming a benefit-transfer approach this can be done by valuing the changes in risk at the time of health effect impacts and not when exposure changes. These values should then be discounted along with other effects in the analysis. Ignoring cessation lag by assuming that benefits accrue immediately upon reduced exposure will produce an upper bound estimate of benefits.

EPA has received recommendations from Science Advisory Board consultations on how to estimate cessation lags, and this information would ideally come from the risk assessment process using consistent models. For carcinogens, the mechanism by which cancer occurs can be informative. ${ }^{76}$ However, cessation lag data is often very limited so EPA has been encouraged to pursue other models to examine the influence of the lag. EPA has estimated the benefits of reduced carcinogens in drinking water by modeling cessation lag with available data on contaminant-outcome combinations other than those

[^3]targeted in the regulation, such as smoking and lung cancer. ${ }^{77}$ This provides information on alternative cessation lags, but the applicability of these data for any particular contaminant is unknown.
Additionally, based on expert recommendations, lags have been implemented in estimating the benefits of particulate matter reductions. ${ }^{78}$

### 6.1.6.3 Length of the Analysis

While there is little theoretical guidance on the time horizon of economic analyses, a guiding principle is that the time span should be sufficient to capture major welfare effects from policy alternatives. This principle is consistent with the underlying requirement that benefit-cost analysis reflect the welfare outcomes of those affected by the policy. Another way to view this is to consider that the time horizon $T$ of an analysis should be chosen such that $\sum_{t=T}^{\infty}\left(B_{t}-C_{t}\right) e^{-r t} \leq \varepsilon$, where $\varepsilon$ is a tolerable estimation error for the $N P V$ of the policy. That is, the time horizon should be long enough that the net benefits for all future years (beyond the time horizon) are expected to be negligible when discounted to the present. In practice, however, it is not always obvious when this will occur because it may be unclear whether or when the policy will be renewed or retired by policy makers, whether or when the policy will become obsolete or "non-binding" due to exogenous technological changes, how long the capital investments or displacements caused by the policy will persist, etc. As a practical matter, reasonable alternatives for the time span of the analysis may be based on assumptions regarding:

As a practical matter, reasonable alternatives for the time span of the analysis may be based on:

- The expected life of capital investments required by or expected from the policy.
- The point at which benefits and costs reach a steady state.
- Statutory or other requirements for the policy or the analysis.
- The extent to which benefits and costs are separated by generations.

The choice should be explained and well-documented. In no case should the time horizon be arbitrary, and the analysis should highlight the extent to which the sign of net benefits or the relative rankings of policy alternatives are sensitive to the choice of time horizon.

### 6.2 Background and Rationales for Social Discounting

The analytical and ethical foundation of the social discounting literature rests on the traditional test of a "potential" Pareto improvement in social welfare, in other words, the tradeoff between the gains to those who benefit and the losses to those who bear the costs. This framework casts the consequences of government policies in terms of individuals contemplating changes in their own consumption (broadly defined) over time. Tradeoffs (benefits and costs) in this context reflect the preferences of those affected by the policy, and the time dimension of those tradeoffs should reflect the intertemporal preferences of those affected. Thus, social discounting should seek to mimic the discounting practices of the affected individuals.

[^4]The literature on discounting uses a variety of terms and frameworks, often to describe identical or very similar key concepts. General themes throughout this literature, however, are the relationship between consumption rates of interest and the rate of return on private capital, the need for a social rate of time preference for benefit-cost analysis, and the importance of considering the opportunity cost of foregone capital investments.

### 6.2.1 Consumption Rates of Interest and Private Rates of Return

In a perfect capital market with no distortions the return to savings (the consumption rate of interest) equals the return on private sector investments. Therefore, if the government seeks to value costs and benefits in present day terms in the same way as the affected individuals, it should also discount using this single market rate of interest. In this kind of "first best" world the market interest rate would be an unambiguous choice for the social discount rate.

Real-world complications, however, make the issue much more complex. Among other things, private sector returns are taxed (often at multiple levels), capital markets are not perfect, and capital investments often involve risks reflected in market interest rates. These factors drive a wedge between the social rate at which consumption can be traded through time (the pre-tax rate of return to private investments) and the rate at which individuals can trade consumption over time (the post-tax consumption rate of interest). Text Box 6.2 illustrates how these rates can differ.

Text Box 6.2 - Social Rate and Consumption Rates of Interest
Suppose the market rate of interest, net of inflation, is $5 \%$, and that taxes on capital income amount to 40 percent of the net return. In this case, private investments will yield $5 \%$, of which $2 \%$ is paid in taxes to the government, with individuals receiving the remaining $3 \%$. From a social perspective, consumption can be traded from the present to the future at a rate of $5 \%$. But individuals effectively trade consumption through time at a rate of $3 \%$ because they owe taxes on investment earnings. As a result, the consumption rate of interest is $3 \%$, which is substantially less than the $5 \%$ social rate of return on private sector investments (also known as the social opportunity cost of private capital).

A large body of economic literature analyzes the implications for social discounting of divergences between the social rate of return on private sector investment and the consumption rate of interest. Most of this literature is based on the evaluation of public projects, but many of the insights still apply to regulatory benefit-cost analysis. The dominant approaches in this literature are briefly outlined here. More complete recent reviews can be found in Spackman (2004) and Moore, et al. (2004).

### 6.2.2 Social Rate of Time Preference

The goal of social discounting is to compare benefits and costs that occur at different times based on the rate at which society is willing to make such tradeoffs. If costs and benefits can be represented as changes in consumption profiles over time, then discounting should be based on the rate at which society is willing to postpone consumption today for consumption in the future. Thus, the rate at which society is willing to trade current for future consumption, or the social rate of time preference, is the appropriate discounting concept.

Generally a distinction is made between individual rates of time preference and that of society as a whole, which should inform public policy decisions. The individual rate of time preference includes factors such as the probability of death, whereas society can be presumed to have a longer planning horizon. Additionally, individuals routinely are observed to have several different types of savings, each possibly yielding different returns, while simultaneously borrowing at different rates of interest. For these and
other reasons, the social rate of time preference is not directly observable and may not equal any particular market rate.

### 6.2.2.1 Estimating a Social Rate of Time Preference Using Risk-Free Assets

One common approach to estimating the social rate of time preference is to approximate it from the market rate of interest from long-term, risk-free assets such as government bonds. The rationale behind this approach is that this market rate reflects how individuals discount future consumption, and government should value policy-related consumption changes as individuals do. In other words, the social rate of discount should equal the consumption rate of interest (i.e., an individual's marginal rate of time preference.)

In principle, estimates of the consumption rate of interest could be based on either after-tax lending or borrowing rates. Because individuals may be in different marginal tax brackets, have different levels of assets, and have different opportunities to borrow and invest, the type of interest rate that best reflects marginal time preference will differ among individuals. However, the fact that, on net, individuals generally accumulate assets over their working lives suggests that the after-tax returns on savings instruments generally available to the public will provide a reasonable estimate of the consumption rate of interest.

The historical rate of return, post-tax and after inflation is a useful measure because it is relatively riskfree, and benefit-cost analysis should address risk elsewhere in the analysis rather than through the interest rate. Also, because these are longer-term instruments they provide more information on how individuals value future benefits over these kinds of time frames.

### 6.2.2.2 Estimating a Social Rate of Time Preference Using the 'Ramsey' Framework

A second option is to construct the social rate of time preference in a framework originally developed by Ramsey (1928) to reflect (1) the value of additional consumption as income changes, and (2) a "pure rate of time preference" that weighs utility in one period directly against that later. These factors are combined in the equation:

$$
\begin{equation*}
r=\eta g+\rho \tag{7}
\end{equation*}
$$

where $(r)$ is the market interest rate, the first term is the elasticity of marginal utility $(\eta)$ times the consumption growth rate $\left({ }^{g}\right)$, and the second term is pure rate of time preference $(\rho)$. Estimating a social rate of time preference in this framework requires information on each of these arguments, and while the first two of these factors may be derived from data, the third is unobservable and must be determined. ${ }^{79}$ (A more detailed discussion of the Ramsey equation can be found in the inter-generational discounting section of this chapter.)

### 6.2.3 Social Opportunity Cost of Capital

The social opportunity cost of capital approach recognizes that funds for government projects, or those required to meet government regulations, have an opportunity cost in terms of foregone investments and therefore future consumption. When a regulation displaces private investments society loses the total pre-

[^5]tax returns from those foregone investments. In these cases, ignoring such capital displacements and discounting costs and benefits using a consumption rate of interest (the post-tax rate of interest) does not capture the fact that society loses the higher, social (pre-tax) rate of return on foregone investments.

Private capital investments might be displaced if, for example, public projects are financed with government debt or regulated firms cannot pass through capital expenses, and the supply of investment capital is relatively fixed. The resulting demand pressure in the investment market will tend to raise interest rates and squeeze out private investments that would otherwise have been made. ${ }^{80}$ Applicability of the social opportunity cost of capital depends upon full crowding out of private investments by environmental policies.

The social opportunity cost of capital may be estimated by the pre-tax marginal rate of return on private investments observed in the marketplace. There is some debate as to whether it is best to use only corporate debt, equity (e.g., returns to stocks) or some combination of the two. In practice, we typically observe average returns which are likely to be higher than marginal return given that firms will make the most profitable investments first; it is not clear how to estimate marginal returns. These rates also reflect risks faced in the private sector, which may not be relevant for public sector evaluation.

### 6.2.4 Shadow Price of Capital Approach

Under the shadow price of capital approach costs are adjusted to reflect the social costs of altered private investments but discounting for time itself is accomplished using the social rate of time preference which represents how society trades and values consumption over time. ${ }^{81}$ The adjustment factor is referred to as the "shadow price of capital." ${ }^{82}$ Many sources recognize this method as the preferred analytic approach to social discounting for public projects and policies. ${ }^{83}$

The shadow price, or social value, of private capital is intended to capture the fact that a unit of private capital produces a stream of social returns at a rate greater than that at which individuals discount them. If the social rate of discount is the consumption rate of interest, then the social value of a $\$ 1$ private sector investment will be greater than $\$ 1$. The investment produces a rate of return for its owners equal to the post-tax consumption rate of interest, plus a stream of tax revenues (generally considered to be consumption) for the government. Text Box 6.3 illustrates this idea of the shadow price of capital.

[^6]
## Text Box 6.3 - Shadow Price of Capital

Suppose that the consumption rate of interest is $3 \%$, the pre-tax rate of return on private investments is $5 \%$, the net-of-tax earnings from these investments are consumed in each period, and the investment exists in perpetuity (amortization payments from the gross returns of the investment are devoted to preserving the value of the capital intact). A $\$ 1$ private investment under these conditions will produce a stream of private consumption of $\$ .03$ per year, and tax revenues of $\$ .02$ per year. Discounting the private post-tax stream of consumption at the $3 \%$ consumption rate of interest yields a present value of $\$ 1$. Discounting the stream of tax revenues at the same rate yields a present value of about $\$ .67$. The social value of this $\$ 1$ private investment - the shadow price of capital - is thus $\$ 1.67$, which is substantially greater than the $\$ 1$ private value that individuals place on it.

If compliance with environmental policies displaces private investments, the shadow price of capital approach suggests first adjusting the project or policy cost upward by the shadow price of capital, and then discounting all costs and benefits using a social rate of discount equal to the social rate of time preference. The most complete frameworks for the shadow price of capital also note that while the costs of regulation might displace private capital, the benefits could encourage additional private sector investments. In principle, a full analysis of shadow price of capital adjustments would treat costs and benefits symmetrically in this sense.

The first step in applying this approach is determining whether private investment flows will be altered by a policy. Next, all of the altered private investment flows (positive and negative) are multiplied by the shadow price of capital to convert them into consumption-equivalent units. All flows of consumption and consumption-equivalents are then discounted using the social rate of time preference. A simple illustration of this method applied to the costs of a public project and using the consumption rate of interest is shown in Text Box 6.4. ${ }^{84}$

## Text Box 6.4 - Shadow Price of Capital Approach

Suppose that the pre-tax rate of return from private investments is $5 \%$, and the post-tax rate is $3 \%$, with the difference attributable to taxation of capital income. Assume as well that increases in government debt displace private investments dollar-for-dollar, and that increased taxes reduce individuals' current consumption also on a one-for-one basis. Finally, assume that the $\$ 1$ current cost of a public project is financed $75 \%$ with government debt and $25 \%$ with current taxes, and that this project produces a benefit 40 years from now that is estimated to be worth $\$ 5$ in the future.

Using the shadow price of capital approach, first multiply $75 \%$ of the $\$ 1$ current cost (which is the amount of displaced private investment) by the shadow price of capital (assume this is the 1.67 figure from above). This yields $\$ 1.2525$, to which is added the $\$ .25$ amount by which the project's costs displace current consumption. The total social cost is therefore $\$ 1.5025$. This results in a net social present value of about $\$ .03$, which is the present value of the future $\$ 5$ benefit discounted at the $3 \%$ consumption rate of interest ( $\$ 1.5328$ ) minus the $\$ 1.5025$ social cost.

[^7]
### 6.2.4. $\quad$ Estimating the Shadow Price of Capital

The shadow price of capital approach is data intensive, requiring, among other things, estimates of the social rate of time preference, the social opportunity cost of capital, as well as estimates of the extent to which regulatory costs displace private investment and benefits stimulate it. While the first two components can be estimated as described earlier, information on regulatory effects on capital formation is more difficult. As a result empirical evidence for the shadow price of capital is less concrete, making the approach difficult to implement. ${ }^{85}$

Whether or not this adjustment is necessary appears to depend largely on whether the economy in question is assumed to be open or closed, and on the magnitude of the intervention or program considered relative to the flow of investment capital from abroad. ${ }^{86}$

Some argue that early analyses implicitly assumed that capital flows into the nation were either nonexistent or very insensitive to interest rates, known as the "closed economy" assumption. ${ }^{87}$ Some empirical evidence suggests, however, that international capital flows are quite large and are sensitive to interest rate changes. In this case, the supply of investment funds to the U.S. equity and debt markets may be highly elastic (the "open economy" assumption) and, thus, private capital displacement would be much less important than previously thought.

Under this alternative view, it would be inappropriate to assume that financing a public project through borrowing would result in dollar-for-dollar crowding out of private investment. If there is no crowding out of private investment, then no adjustments using the shadow price of capital are necessary; benefits and costs should be discounted using the social rate of time preference alone. However, the literature to date is not conclusive on the degree of crowding out, providing little detailed empirical evidence as to the relationship between the nature and size of projects and capital displacement. Thus, while the approach is often recognized as being technically superior to simpler methods, it is difficult to implement in practice.

## Text Box 6.5: Alternative Social Discounting Perspectives

Some of the social discounting literature questions basic premises underlying the conventional social discounting analysis. For example, some studies of individual financial and other decision making contexts suggest that even a single individual may appear to value and discount different actions, goods, and wealth components differently. This "mental accounts" or "self-control" view suggests that individuals may evaluate some aspects of the future differently from other consequences. The discount rate an individual might apply to a given future benefit or cost, as a result, may not be observable from market prices, interest rates, or other phenomena. This may be the case if the future consequences in question are not tradable commodities. Some evidence from experimental economics also indicates that discount rates appear to be lower the larger the magnitude of the underlying effect being valued is, higher for gains than for losses, and tend to decline as the length of time to the event increases. Further, individuals may have preferences about whether sequences of environmental outcomes are generally improving or declining. Some experimental evidence suggests that individuals tend discount hyperbolically rather than exponentially, a structure that raises time-consistency concerns. Additional studies have attempted to address the

[^8]87 See Lind (1990) for this revision of the shadow price of capital approach.
time-consistency problems that emerge from hyperbolic discounting. Approaches to social discounting based on alternative perspectives and ecological structures have also been developed, but these have yet to be fully incorporated into the environmental economics literature. ${ }^{88}$

### 6.2.5 Evaluating the Alternatives

The empirical literature for choosing a social discount rate focuses largely on estimating the consumption rate of interest at which individuals translate consumption through time with reasonable certainty. For this, historical rates of return, post-tax and after inflation, on "safe" assets, such as U.S. Treasury securities, are normally used, although some may use the return to private savings. Recent studies and reports have generally found government borrowing rates in the range of around $2-4 \%{ }^{89}$ Some studies have expanded this portfolio to include other bonds, stocks, and even housing, and this generally raises the range of rates slightly. It should be noted that these rates are realized rates of return, not anticipated, and they are somewhat sensitive to the time periods selected and the classes of assets considered. ${ }^{90}$ Studies of the social discount rate for the United Kingdom place the consumption rate of interest at approximately $2 \%$ to $4 \%$, with the balance of the evidence pointing toward the lower end of the range. ${ }^{91}$

Others have constructed a social rate of time preference by estimating the individual arguments in the Ramsey equation. These estimates necessarily require judgments about the pure rate of time preference. Moore, et al. (2004) and Boardman et al. (2008), for example, estimate an intra-generational rate to be $3.5 \%$. Other studies base the pure rate of time preference on individual mortality risks in order to arrive at a discount rate estimate. As noted earlier, this may be useful for an individual, but is not generally appropriate from a societal standpoint. The Ramsey equation has been used more frequently in the context of inter-generational discounting, which we address in the next section.

The social opportunity cost of capital represents a situation where investment is crowded out dollar-fordollar by the costs of environmental policies. This is an unlikely outcome, but can be useful for sensitivity analysis and special cases. Estimates of the social opportunity costs of capital are typically in the $4.5 \%$ to $7 \%$ range depending upon the type of data used. ${ }^{92}$
${ }^{88}$ See Thaler (1990) and Laibson (1998) for more information on mental accounts; Guyse, Keller, and Eppell (2002) on preferences for sequences; Gintis (2000) and Karp (2005) on hyperbolic discounting; and Sumaila and Waters (2005) and Voinov and Farley (2007) for additional treatments on discounting.

OMB (2003) cites evidence of a $3.1 \%$ pre-tax rate for 10-year Treasury notes. ).According to the US CBO (2005), funds continuously reinvested in 10-year U.S. Treasury bonds from 1789 to the present would have earned an average inflation-adjusted return of slightly more than 3 percent a year. Boardman et al. (2005) suggest 3.71 percent as the real rate of return on 10-year Treasury notes. Newell and Pizer (2003) find rates slightly less than 4\% for 30-year Treasury securities. Nordhaus (2008) reports a real rate of return of $2.7 \%$ for 20-year Treasury securities. The Congressional Budget Office estimates the cost of government borrowing to be $2 \%$, a value used as the social discount rate in their analyses (US CBO 1998).
90 Ibbotson and Sinquefield (1984 and annual updates) provide historical rates of return for various assets and for different holding periods.

91 Lind (1982b) offers some empirical estimates of the consumption rate of interest. Pearce and Ulph (1994) provide estimates of the consumption rate of interest for the United Kingdom. Lyon (1994) provides estimates of the shadow price of capital under a variety of assumptions.
92 OMB (2003) recommends a real, pre-tax opportunity cost of capital of 7\% and refers to Circular A-94 (1992) as the basis for this conclusion. Moore, et al. (2004) estimate a rate of $4.5 \%$ based on AAA corporate bonds In recent reviews of EPA's plans to estimate the costs and benefits of the Clean Air Act, the SAB advisory Council (US EPA 2004c; US EPA 2007b) recommends using a single central rate of $5 \%$ as intermediate between, $3 \%$ and $7 \%$ rates based generally on the consumption rate of interest and the cost of capital, respectively.

The utility of the shadow price of capital approach hinges on the magnitude of altered capital flows from the environmental policy. If the policy will substantially displace private investment then a shadow price of capital adjustment is necessary before discounting consumption and consumption equivalents using the social rate of time preference. The literature does not provide clear guidance on the likelihood of this displacement, but it has been suggested that if a policy is relatively small and capital markets fit an "open economy" model, then there is probably little displaced investment. ${ }^{93}$ Because changes in yearly U.S. government borrowing during the past several decades have been in the many billions of dollars, it may be reasonable to conclude that EPA programs and policies costing a fraction of these amounts are not likely to result in significant crowding out of U.S. private investments. Primarily for these reasons, some argue that for most environmental regulations it is sufficient to discount using a government bond rate with some sensitivity analysis. ${ }^{94}$

## 6.3 "Inter-generational" Social Discounting

Policies designed to address long-term environmental problems such as global climate change, radioactive waste disposal, groundwater pollution, or biodiversity will likely involve significant impacts on future generations. This section focuses on social discounting in the context of policies with very long time horizons involving multiple generations, typically referred to in the literature as inter-generational discounting.

Discounting over very long time horizons is complicated by at least three factors: (1) the "investment horizon" is longer than what is reflected in observed interest rates that are used to guide private discounting decisions; (2) future generations without a voice in the current policy process are affected; and (3) compared to intra-generational time horizons, inter-generational investment horizons involve greater uncertainty. Greater uncertainty implies rates lower than those observed in the marketplace, regardless of whether or not the estimated rates are measured in private capital or consumption terms. Policies with very long time horizons often involve costs imposed mainly on the current generation to achieve benefits that will accrue mainly to unborn, future generations, making it important to consider how to incorporate these impacts into decision-making. However, there is less agreement in the literature on the precise approach for discounting over very long time horizons.

This section presents a discussion of the main issues associated with inter-generational social discounting. As a starting point, the section first lays out the Ramsey discounting framework that underlies most of the current literature on the subject. It then discusses how the "conventional" discounting procedures described so far in this chapter might need to be modified when analyzing policies with very long ("intergenerational") time horizons. The need for such modifications arises from several simplifying assumptions behind the conventional discounting procedures described above that will likely become less realistic the longer is the relevant time horizon of the policy. This discussion will focus on the social discount rate itself; other issues such as shadow price of capital adjustments, while still relevant under certain assumptions, will be only briefly touched upon.

Clearly, economics alone cannot provide definitive guidance for selecting the "correct" social welfare function or the social rate of time preference. Nevertheless, economics can offer important insights concerning discounting over very long time horizons, the implications and consequences of alternative

[^9]discounting methods, and some advice on the appropriate and consistent use of the social welfare function approach as a policy evaluation tool in an inter-generational context.

### 6.3.1 The Ramsey Framework

A common approach to intergenerational discounting is based upon methods economists have used for many years in optimal growth modeling. In this framework, the economy is assumed to operate as if a "representative agent" chooses a time path of consumption and savings that maximizes the net present value of the flow of utility from consumption over time. ${ }^{95}$ Note that this framework can be viewed in normative terms, as a device to investigate how individuals should consume and reinvest economic output over time, or it can be viewed in positive terms, as a description (or "first order approximation") of how the economy actually works in practice. It is a "first order approximation" only from this positive perspective because it typically excludes numerous real-world departures from the idealized assumptions of perfect competition and full information that are required for a competitive market system to produce a Pareto optimal allocation of resources. If the economy worked exactly as described by optimal growth models-i.e., there were no taxes, market failures, or other distortions - the social discount rate as defined in these models would be equal to the market interest rate. And the market interest rate, in turn, would also be equal to the social rate of return on private investments and the consumption rate of interest.

It is worth noting, however, that the optimal growth literature is only one strand of the substantial body of research and writing on inter-temporal social welfare. This literature extends from the economics and ethics of interpersonal and intergenerational wealth distribution to the more specific environment-growth issues raised in the "sustainability" literature, and even to the appropriate form of the social welfare function, e.g., utilitarianism, or Rawls' maxi-min criterion.

As noted earlier, the basic model of optimal economic growth, due to Ramsey (1928), implies an equivalence between the market interest rate $\left({ }^{r}\right)$ and the elasticity of marginal utility $\left({ }^{\eta}\right)$ times the consumption growth rate $\left({ }^{g}\right)$ plus the pure rate of time preference $\left({ }^{\rho}\right)$ :

$$
r=\eta g+\rho .
$$

The first term reflects the fact that the marginal utility of consumption will change over time as the level of consumption changes. The second term, the pure rate of time preference, measures the rate at which individuals discount their own utility over time (taking a positive view of the optimal growth framework) or the rate at which society should discount utilities over time (taking a normative view). Note that if consumption grows over time-as it has at a fairly steady rate at least since the industrial revolution (e.g., Valdés 1999)-then future generations will be richer than the current generation and therefore increments to consumption will be valued less highly in the future than today due to the diminishing marginal utility of consumption. Thus, in a growing economy changes in future consumption would be given a lower weight (i.e., discounted at a positive rate) than changes in present consumption in this framework, even setting aside discounting due to the pure rate of time preference $\rho$.

There are two primary approaches typically used in the literature to specify the individual parameters of the Ramsey equation: the descriptive approach, and the normative (or prescriptive) approach. The descriptive approach attempts to derive likely estimates of the underlying parameters in the Ramsey equation, based on the argument that economic models should be based on actual behavior and that

95 Key literature on this topic includes Arrow et al. (1996), Lind (1994), Schelling (1995), Solow (1992), Manne (1994), Toth (1994), Sen (1982), Dasgupta (1982), and Pearce and Ulph (1994).
models should be able to predict this behavior. By specifying a given utility function and modeling the economy over time one can obtain empirical estimates for the marginal utility and for the change in growth rate. While the pure rate of time preference cannot be estimated directly, the other components of the Ramsey equation may be estimated, allowing $\rho$ to be inferred.

Other economists take what is referred to as a normative approach and assign parameters to the Ramsey equation to match what they believe to be ethically correct. ${ }^{96}$ For instance, there has been a long debate on whether the pure rate of time preference should be greater than zero (starting with Ramsey himself). The main responses to the normative approach are (1) people (individually and societally) do not make decisions that match this approach and (2) using this approach would lead to an over investment in climate change mitigation at the expense of investments that would actually make future generations better off (and would make intervening generations better off as well). There is also an argument that a very low discount rate advocated by some adherents to the normative approach leads to unethical shortchanging of current and close generations.

While use of the Ramsey discounting framework is quite common and is based on an intuitive description of the general problem of trading off current and future consumption, it has some limitations. In particular, it ignores differences in income within generations (at least in the basic single representative agent version of the model). Arrow (1996) contains detailed discussion of descriptive and prescriptive approaches to discounting over long time horizons, including examples of rates that emerge under various assumptions about components of the Ramsey equation.

## Text Box 6.6 Applying these approaches to the Ramsey Equation

Most climate economists adopt a descriptive approach to identify long-term real interest rates and likely estimates of the underlying parameters in the Ramsey equation. William Nordhaus argues that economic models should be based on actual behavior and that models should be able to predict this behavior. His DICE model, for example, uses interest rates, growth rates, etc., to calibrate the model to match actual historic levels of investment, consumption, and other variables. In the most recent version of the DICE model (Nordhaus 2008), he specifies the current rate of productivity growth to be 5.5 percent per year, the rate of time preference to be 1.5 percent per year, and the elasticity of marginal utility to be 2 . (In an earlier version (Nordhaus 1994), he estimate the initial return on capital (and social discount) to be 6 percent, the rate of time preference to be 2, and the elasticity of marginal utility to be 3). Because the model predicts that economic and population growth will slow, the social discount rate will decline.

Other analyses have adopted at least aspects of a prescriptive approach. For example, the Stern Review (see Text Box 6.7) sets the pure rate of time preference at a value of 0.1 percent and the elasticity of marginal utility as 1.0 . With an assumed population growth rate of 1.3 percent, the social discount rate is 1.4 percent. Guo, et al. (2006) evaluate the effects of uncertainty and discounting on the social cost of carbon where the social discount rate is constructed from the Ramsey equation. A number of different discount rate schedules are estimated depending on the adopted parameters.

### 6.3.2 Key Considerations

There are a number of important ways in which inter-generational social discounting differs from intragenerational social discounting, essentially due to the length of the time horizon. Over a very long time horizon, it is much more difficult - if not impossible - for analysts to judge whether current generation preferences also reflect those of future generations and how per capita consumption will change over

[^10]time. This section discusses efficiency and intergenerational equity concerns, and uncertainty in this context

### 6.3.2.1 Efficiency and Intergenerational Equity

A principal problem with policies that span long time horizons is that many of the people affected are not yet alive. Hence, while the preferences of each affected individual are knowable (if perhaps unknown in practice) in an intra-generational context, the preferences of future generations in an inter-generational context are essentially unknowable. This is not always a severe problem for practical policymaking, especially when policies impose relatively modest costs and benefits, or when the costs and benefits begin immediately or in the not too distant future. Most of the time, it suffices to assume future generations will have preferences much like those of present generations.

The more serious challenge posed by long time horizon situations arises primarily when costs and benefits of an action or inaction are very large and distributed asymmetrically over vast expanses of time. Here the crux of the problem is that future generations are not present to participate in making the relevant social choices. Instead, these decisions will be made only by existing generations. Social discounting in these cases can no longer be thought of as a process of consulting the preferences of all affected parties concerning their valuation today of effects they will experience in different time periods.

Moreover, compounding interest over very long time horizons can have profound impacts on the intergenerational distribution of welfare. An extremely large benefit or cost far into the future has essentially zero present value when discounted at even a low rate. But a modest sum invested today at the same low interest rate can grow to a staggering amount given enough time. Therefore, mechanically discounting very large distant future effects of a policy without thinking carefully about the implications is not advised. ${ }^{97}$

For example, in the climate change context, Pearce et al. (2003) show that decreasing the discount rate from a constant $6 \%$ to a constant $4 \%$ nearly doubles the estimate of the marginal benefits from CO 2 emission reductions. Weitzman (2001) shows that moving from a constant $4 \%$ discount rate to a declining discount rate approach nearly doubles the estimate again. Newell and Pizer (2003) show that constant discounting can substantially undervalue the future given uncertainty in economic growth and the overall investment environment (e.g., a constant discount rate could undervalue net present benefits by $21 \%$ to $95 \%$ depending on the model of interest rate uncertainty with an initial rate of $7 \%$, and $440 \%$ to $700 \%$ with an initial rate of $4 \%$.

Using observed market interest rates for inter-generational discounting in the representative agent Ramsey framework essentially substitutes the pure rate of time preference exhibited by individuals for the weight placed on the utilities of future generations relative to the current generation (see OMB 2003 and Arrow et al. 1996). Many argue that the discount rate should be below market rates ${ }^{98}$ - though not necessarily zero - to (1) correct for market distortions and inefficiencies in inter-generational transfers, and (2) so that generations are treated equally based on ethical principles (Arrow et al., 1996; Weyant and Portney, 1999).

[^11]
## Inter-Generational Transfers

The notion of Pareto compensation attempts to identify the appropriate social discount rate in an intergenerational context by asking whether the distribution of wealth across generations could be adjusted to compensate the losers under an environmental policy and still leave the winners better off than they would have been absent the policy. Whether winners could compensate losers across generations hinges on the rate of interest at which society (the U.S. presumably, or perhaps the entire world) can transfer wealth across hundreds of years. Some argue that in the U.S. context, a good candidate for this rate is the Federal government's borrowing rate. Some authors also consider the infeasibility of intergenerational transfers to be a fundamental problem for discounting across generations. ${ }^{99}$

## Equal Treatment Across Generations

Environmental policies that affect distant future generations can be considered to be altruistic acts. ${ }^{100}$ As such, some argue that they should be valued by current generations in exactly the same way as other acts of altruism are valued. For this reason, the relevant discount rate is not that applied to an individual's consumption, but instead that applicable for an individual's valuation of the consumption or welfare of someone else, identified by the analyst through either revealed or stated preference.

At least some altruism is apparent from international aid programs, private charitable giving, and bequests within overlapping generations of families. But the evidence suggests that the importance of other people's welfare to an individual appears to grow weaker as temporal, cultural, geographic, and other measures of "distance" increase. The implied discount rates survey respondents appear to apply in trading off present and future lives also is relevant under this approach. One such survey (Cropper, Aydede, and Portney, 1994) suggests that these rates are positive on average, which is consistent with the rates at which people discount monetary outcomes, and decline as the time horizon involved lengthens.

### 6.3.2.2 Uncertainty

A longer time horizon in an inter-generational policy context also implies greater uncertainty about the investment environment and economic growth over time, and a greater potential for environmental feedbacks to economic growth (and consumption and welfare), which - in turn -further increases uncertainty when attempting to estimate the social discount rate.

This additional uncertainty has been shown to imply effective discount rates lower than what that based on the observed average market interest rates, regardless of whether or not the estimated investment effects are predominantly measured as private capital or consumption terms (Weitzman 1998, 2001; Newell and Pizer, 2003; Groom et al. 2005). ${ }^{101}$ The rationale for this conclusion is that consideration of uncertainty in the discount rate should be based on the average of discount factors (i.e., $\left.1 /(1+r)^{t}\right)$ rather than the standard discount rate (i.e., $r$ ). From the expected discount factor over any period of time we can infer a constant, certainty-equivalent discount rate that yields the discount factor (for any given distribution of $r$ ). Several methods for accounting for uncertainty into inter-generational discounting are discussed in more detail in the next section.

[^12]
### 6.3.3 Evaluating Alternatives

There are a wide range of options available to the analyst for discounting inter-generational costs and benefits. We describe several of these below, ordered from simplest to most analytically complex. Which option is utilized in the analysis is left to expert judgment, but should be based on the likely consequences of undertaking a more complex analysis for the bottom-line estimate of expected net benefits. This will be a function of the proportion of the costs and benefits occurring far out on the time horizon and the separation of costs and benefits over the planning horizon. When it is unclear which method should be utilized, we encourage the analyst to explore a variety of approaches.

### 6.3.3.1 Constant Discount Rate

One possible approach is to simply make no distinction between inter-generational and intra-generational social discounting. For example, models of infinitely-lived individuals suggest the consumption rate of interest as the social discount rate. Of course, individuals actually do not live long enough to experience distant future consequences of a policy and cannot report today the present values they place on those effects. However, it is equally sufficient to view this assumption as a proxy for family lineages in which the current generation treats the welfare of all its future generations identically with the current generation. It is not so much that the individual lives forever as that the family spans many generations (forever) and that the current generation discounts consumption of future generations at the same rate as its own future consumption.

Models based on constant discount rates over multiple generations essentially ignore potential differences in economic growth and income and/or preferences for distant future generations. Since economic growth is unlikely to be constant over long time horizons, the assumption of a constant discount rate is unrealistic. Interest rates are a function of economic growth; thus, increasing (declining) economic growth implies an increasing (decreasing) discount rate.

A constant discount rate assumption also does not adequately account for uncertainty. Uncertainty regarding economic growth increases as one goes further out in time, which implies increasing uncertainty in the interest rate and a declining certainty equivalent rate of return to capital (Hansen 2006).

### 6.3.3.2 Step Functions

Some modelers and government analysts have experimented with varying the discount rate with the time horizon to reflect non-constant economic growth, intergeneration equity concerns, and/or heterogeneity in future preferences. For instance, in the U.K., the Treasury recommends the use of a $3.5 \%$ discount rate for the years $0-30$, declining to a rate of $3 \%$ for years $31-75$. This method acknowledges that a constant discount rate does not adequately reflect the reality of fluctuating and uncertain growth rates over long time horizons. However, application of this method also raises several potential analytic complications. First, there is no empirical evidence to suggest the point(s) at which the discount rate declines, so any year selected for a change in the discount rate will be necessarily ad-hoc. Second, this method can suffer from a time inconsistency problem. Time inconsistency means that an optimal policy today may look sub-optimal in the future when using a different discount rate and vice versa. Some have argued that time inconsistency is a relatively minor problem relative to other conditions imposed (Heal 1998, Henderson and Bateman 1995, and Spackman 2002).

### 6.3.3.3 Declining or Non-constant Discount Rate

Using a constant discount rate in benefit-cost analysis (BCA) is technically correct only if the rate of economic growth will remain fixed over the time horizon of the analysis. If economic growth is changing over time, then the discount rate, too, will fluctuate. In particular, one may assume that the growth rate is declining systematically over time (perhaps to reflect some physical resource limits), which will lead to a declining discount rate. This is the approach taken in some models of climate change. ${ }^{102}$ In principle, any set of known changes to income growth, the elasticity of marginal utility of consumption, or the pure rate of time preference will lead to a discount rate that changes accordingly.

### 6.3.3.4 Uncertainty-Adjusted Discounting

If there is uncertainty about the future growth rate, then the correct procedure for discounting must account for this uncertainty in the calculation of the expected net present value of the policy. Over the long time horizons investment uncertainty and risk will naturally increase, which results in a decline in the imputed discount rate. If the time horizon of the policy is very long, then eventually a low discount rate will then dominate the expected net present value calculations for benefits and cost far in the future (Weitzman1999).

Newell and Pizer (2003) expand on this observation, using historical data on U.S. interest rates and assumptions regarding their future path to characterize uncertainty and compute a certainty equivalent rate. In this case, uncertainty in the individual components of the Ramsey equation is not being modeled explicitly. Their results illustrate that a constant discount rate could substantially undervalue net present benefits when compared to one that accounts for uncertainty. For instance, a constant discount rate of seven percent could undervalue net present benefits by between 21 and 95 percent depending on the way in which uncertainty is modeled.

A key advantage of this treatment of the discount rate over the step function and simple declining rate discounting approaches is that the analyst is not required to arbitrarily designate the discount rate transitions over time nor ignore the effects of uncertainty in economic growth over time. Thus, this approach is not subject to the time inconsistency problems of some of these other approaches.

## Text Box 6.7: What's the Big Deal with the Stern Report?

In autumn 2006, the UK government released a detailed report titled The Economics of Climate Change: The Stern Review, headed by Nobel Laureate Sir Nicholas Stern (2006). The report drew mainly on published studies to estimate that damages from climate change could result in a $5 \%$ to $20 \%$ decline in global output by 2100 , while costs to mitigate these impacts were significantly less (about $1 \%$ of GDP). Stern's findings led him to say that "climate change is the greatest and widest-ranging market failure ever seen," and that "the benefits of strong early action considerably outweigh the cost." The Review recommended that policies aimed towards sharp reduction in greenhouse-gas emissions should be enacted immediately.

While lauded for its thoroughness and accurate use of current climate science, the Review drew significant criticism and discussion of how future benefits were calculated, namely Stern's assumptions about the discount rate (Tol and Yohe, 2006; Nordhaus, 2008). The Review used the Ramsey discounting equation (see section 6.3.1), applying rates of $0.1 \%$ for the annual pure rate of time preference, $1.3 \%$ for the annual growth rate, and a elasticity of

[^13]marginal utility of consumption equal to 1 . Combining these parameter values reveals an estimated equilibrium real interest rate of $1.4 \%$, a rate arguably lower than most returns to standard investments, but not outside the range of values suggested in these Guidelines for intergenerational discount rates.

So, why is the issue on the value of the discount rate so contentious? Perhaps the biggest concern is that climate change is expected to cause significantly greater damages in the far future than it is today, and thus benefits are sensitive to discounting assumptions. A low social discount rate means the Stern Review places a much larger weight on the benefits of reducing climate change damages in 2050 or 2100 relative to the standard $3 \%$ or $7 \%$ commonly observed in market rates. Furthermore, Stern's relatively low values of $\rho$ and $\eta$ imply that the current generation should operate at a higher savings rate than what is observed, thus implying that we should save more today to compensate losses incurred by future generations.

Why did Stern use these particular parameter values? First, he argues that we have an ethical obligation to place similar weights on the pure rate of time for future generations. Second, a marginal elasticity of consumption of unity implies a relatively low inequality aversion, which reduces the transfer of benefits between the rich and the poor relative to a higher elasticity. Finally, there are significant risks and uncertainties associated with climate change, which could imply using a lower than market rate. Stern's (2007) concluding remarks for using a relatively low discount rate are clear, "However unpleasant the damages from climate change are likely to appear in the future, any disregard for the future, simply because it is in the future, will suppress action to address climate change."

There is little consensus in the economic literature on social discounting for inter-generational policies. In particular, the fundamental choice of what moral perspective should guide inter-generational social discounting - a social planner who weighs the utilities of present and future generations, the preferences of the current generations regarding future generations - cannot be made on economic grounds alone. Additionally, the rule of uncertainty is more important in an inter-generational context, which can have a profound effect on discount rates over the very long run.

### 6.4 Recommendations and Guidance

As summed up by Freeman (2003 p. 206), "economists have not yet reached a consensus on the appropriate answers" to all of the issues surrounding intergenerational discounting. And while there may be more agreement on matters of principle for discounting in the context of intragenerational policies, there is still some disagreement on the magnitude of capital displacement and the need to account for the opportunity costs of capital in practice. Thus, the recommendations provided here are intended as practical and plausible default assumptions rather than comprehensive and precise estimates of social discount rates that must be applied without adjustment in all situations.

These recommendations can be used as a starting point for benefit-cost analyses, but if the analysts can develop a more realistic model and bring to bear more accurate empirical estimates of the various factors that are most relevant to the specific policy scenario under consideration, then they should do so and provide the rationale in the description of their methods. With this caveat in mind, our default recommendations for discounting are below.

- Display the time paths of benefits and costs as they are projected to occur over the time horizon of the policy, i.e., without discounting.
- Using the shadow price of capital approach is the analytically preferred method for discounting, but there is some disagreement on the extent to which private capital is displaced by EPA regulatory requirements. EPA will undertake additional research and analysis to investigate important aspects of this issue, including the elasticity of capital supply, and will update guidance accordingly. In the interim analysts should conduct a bounding exercise as follows:
o Calculate the NPV using the consumption rate of interest. This is appropriate for situations where all costs and benefits occur as changes in consumption flows rather than changes in capital stocks, i.e., capital displacement effects are negligible. As of the date of this publication, current estimates of the consumption rate of interest, based on recent returns to Government-backed securities, are close to $3 \%$.
o Also calculate the NPV using the rate of return to private capital. This is appropriate for situations where all costs and benefits occur as changes in capital stocks rather than consumption flows. The Office of Management and Budget estimates a rate of 7\% for the opportunity cost of private capital.
o EPA intends to review the empirical basis for the consumption discount rate and the rate of return to private capital at regular intervals.

In most cases the results of applying the more detailed "shadow price of capital" approach will lie somewhere between the NPV estimates ignoring the opportunity costs of capital displacements and discounting all costs and benefits using these two alternative discount rates.

- If the policy has a long time horizon (more than 50 years or so) where net benefits vary substantially over time - e.g., most benefits accrue to one generation and most costs to another -then also calculate the expected present value of net benefits using the schedule of discount factors estimated by Newell and Pizer (2003) based a stochastic "random walk" model of interest rates (shown in the fourth column of their Table 2; see also Newell and Pizer 2004). This approach is relatively straightforward to implement and accounts for discount rate uncertainty and variability, which are known to have potentially large effects on net present value estimates for policies with long time horizons. EPA will provide an empirical supplement that provides specific rates based on this approach. This does not preclude the use of more detailed approaches that, for example, might construct the discount rate from estimating the individual parameters in the Ramsey equation. However, these alternatives should be fully described, supported, and justified.

When implementing any discounting approach the following principles should be kept in mind:

- In all cases social benefits and costs should be discounted in the same manner, although private discount rates may be used to predict behavior and to evaluate economic impacts.
- The discount rate should reflect time preferences and should not be confounded with factors such as uncertainty in benefits and costs or the value of environmental goods or other commodities in the future (i.e., the "current price" in future years).
- Cessation lag and latency should be accounted for in the economic analysis, with the monetary benefits from the expected future impacts--be they changes in human health, environmental conditions, ecosystem services, etc.--discounted at the same rate as other benefits and costs in the analysis.


[^0]:    ${ }^{72}$ This chapter is intended to summarizes some key aspects from the core literature on social discounting;, it is not a detailed review of the vast and varied social discounting literature on the topic. Excellent sources for additional information are Lind (1982a, b; 1990; 1994), Lyon (1990, 1994), Kolb and Scheraga (1990), Scheraga (1990), Arrow, et al (1996), Pearce and Turner (1990), Pearce and Ulph (1994), Groom, et al (2005), Cairns (2006), Frederick, et al. (2002), Moore, et al. (2004), Spackman (2004), and Portney and Weyant (1999).

[^1]:    ${ }^{73}$ See EPA (1995) for an example in which operating and monitoring costs are assumed to be spread out evenly throughout each year of compliance. While the exponential function above is the most accurate way of modeling the relationship between the present value and a continuous stream of benefits and costs, simple adjustments to the equations above can sometimes adapt them for use under alternative assumptions about the distribution of monetary flows over time.

[^2]:    ${ }^{74}$ Variants of these formulas may be common in specific contexts. See, for example, the Equivalent Uniform Annual Cost approach in EPA's Air Pollution Control Cost Manual (US EPA, 2002). [6 $6^{\text {th }}$ Edition, EPA/452/B-02-001, January 2002, OAQPS].

[^3]:    ${ }^{75}$ Arsenic Rule Benefits Analysis: A Review (US EPA 2001c).
    ${ }^{76}$ See Arsenic Rule Benefits Analysis: A Review (US EPA 2001c).

[^4]:    ${ }^{77}$ See EPA's economic analysis for the Final Stage 2 Disinfection and Disinfection Byproducts Rule (US EPA 2005a)
    ${ }^{78}$ See, for example the recommendations on the distributed lag for particulate matter benefits in EPA-COUNCIL-LTR-05-001 as applied in EPA's Regulatory Impact Analysis for the 2006 Particulate Matter NAAQS www.epa.gov/ttn/ecas/ria.html )

[^5]:    79 The SAB Council defines discounting based on a Ramsey equation as the "demand-side" approach, noting that the value judgments required for the pure social rate of time preference make it an inherently subjective concept. (US EPA 2004c).

[^6]:    ${ }^{80}$ Another justification for using the social opportunity cost of capital argues that the government should not invest (or compel investment through its policies) in any project that offers a rate of return less than the social rate of return on private investments. While it is true that social welfare will be improved if the government invests in projects that have higher values rather than lower ones, it does not follow that rates of return offered by these alternative projects define the level of the social discount rate. If individuals discount future benefits using the consumption rate of interest, the correct way to describe this project is that it offers substantial present value net benefits.
    ${ }^{81}$ Because the consumption rate of interest is often used as a proxy for the social rate of time preference this method is sometimes known as the "consumption rate of interest - shadow price of capital" approach. However, as Lind (1982) notes, what is really needed is the social rate of time preference, so we use more general terminology. Discounting based on the shadow price of capital is referred to as a "supply side" approach by EPA's SAB Council. (US EPA, 2004c).
    ${ }^{82}$ A "shadow price" can be viewed as a good's opportunity cost, which may not equal the market price. Lind (1982a) remains the seminal source for this approach in the social discounting literature.
    83 See OMB Circular A-4, Freeman (2003), and the report of EPA's Advisory Council on Clean Air Compliance Analysis (US EPA 2004c).

[^7]:    ${ }^{84}$ An alternative approach for addressing the divergence between the higher social rate of return on private investments and lower consumption rate of interest is to set the social discount rate equal to a weighted average of the two. The weights would equal the proportions of project financing that displace private investment and consumption respectively. This approach has enjoyed considerable popularity over the years, but it is technically incorrect and can produce net present value results substantially different from the shadow price of capital approach. (For an example of these potential differences see Spackman 2004.)

[^8]:    85 Depending on the magnitudes of the various factors, shadow prices from close to 1 to $3,20,100$, and infinity can result. Lyon (1990) and Moore, et al. (2004) contain excellent reviews of how to calculate the shadow price of capital and possible settings for the various parameters that determine its magnitude.
    ${ }^{86}$ Studies suggesting that increased U.S. government borrowing does not crowd out U.S. private investment generally examine the impact of changes in the level of government borrowing on interest rates. The lack of a significant positive correlation of government borrowing and interest rates is the foundation of this conclusion.

[^9]:    93 Lind (1990) first suggested this.
    94 See, in particular, Lesser and Zerbe (1994) and Moore, et al. (2004).

[^10]:    96 Arrow, et al. 1996.

[^11]:    97 OMB's Circular A-4 (OMB 2003) requires the use of constant three and seven percent for both intra- and intergenerational discounting for benefit-cost estimation of economically significant rules but allows for lower, positive consumption discount rates if there are important intergenerational benefits/costs.

    98 Another issue is that there are no market rates for intergenerational time periods.

[^12]:    99 See Lind (1990) and a summary by Freeman (2003).
    100 Schelling (1995) and Birdsall and Steer (1993) are good references for these arguments.
    101 Gollier and Zeckhauser (2005) reach a similar result using a model with decreasing absolute risk aversion.

[^13]:    102
    E.g., Nordhaus 2008.

