

SINGULAR VALUES

PURPOSE

Compute the singular values of a matrix.

DESCRIPTION

DATAPLOT uses the singular value decomposition (SVD) to compute the singular values.

If X is a matrix with row and column dimensions n and p respectively, then an n by n orthogonal matrix U and a p by p orthogonal matrix V can be found such that:

$$U^T X V = \begin{bmatrix} \Sigma \\ 0 \end{bmatrix} \quad (\text{EQ 4-73})$$

where Σ is a m by m diagonal matrix (m is the minimum of n and p). The diagonal elements of Σ are the singular values of X and they are stored from largest to smallest. The above assumes that $n \geq p$. A right hand side becomes $[\Sigma \ 0]$ if $N < p$. Singular values of zero (or near zero) indicate that the matrix is singular (i.e., not of full rank) or ill-conditioned. Chapters 2 and 14 of the Numerical Recipes book describe some applications of the SVD.

For large matrices, it can be impractical to compute U (which is n by n). However, U can be partitioned into

$$U = (U1, U2)$$

where $U1$ is n by p . Then

$$X = U1 \Sigma V'$$

is called the singular value factorization of X . Several multivariate statistical techniques are based on this factorization.

SYNTAX

LET <var> = SINGULAR VALUES <mat> <SUBSET/EXCEPT/FOR qualification>

where <mat> is a matrix for which the singular values are to be computed;

<var> is a variable where the resulting singular values are saved;

and where the <SUBSET/EXCEPT/FOR qualification> is optional and rarely used in this context.

EXAMPLES

LET C = SINGULAR VALUES A

NOTE 1

DATAPLOT uses the LINPACK routine SSVDC to calculate the singular values.

NOTE 2

DATAPLOT will calculate the singular value decomposition even if $N \leq p$. However, in practice this is almost never done.

DEFAULT

None

SYNONYMS

None

RELATED COMMANDS

MATRIX EIGENVALUES	=	Compute the matrix eigenvalues.
MATRIX EIGENVECTORS	=	Compute the matrix eigenvectors.
MATRIX MULTIPLICATION	=	Perform a matrix multiplication.
MATRIX SOLUTION	=	Solve a system of linear equations.
MATRIX TRACE	=	Compute a matrix trace.
MATRIX TRANSPOSE	=	Compute a matrix transpose.
CORRELATION MATRIX	=	Compute the correlation matrix of a matrix.
VARIANCE-COVA MATRIX	=	Compute the variance-covariance matrix of a matrix.
PRINCIPAL COMPONENTS	=	Compute the principal components of a matrix.
SINGULAR VALUE DECOM	=	Compute the singular value decomposition of a matrix.

SINGULAR VALUE FACT = Compute the singular value factorization of a matrix.

REFERENCE

“LINPACK User’s Guide,” Dongarra, Bunch, Moler, Stewart. Siam, 1979.

“Numerical Recipes: The Art of Scientific Programming (FORTRAN Version),” Press, Flannery, Teukolsky, and Vetterling, Cambridge University Press, 1989 (chapter 2).

APPLICATIONS

Linear Algebra, Multivariate Analysis

IMPLEMENTATION DATE

93/8

PROGRAM

```
DIMENSION 100 COLUMNS
SKIP 25
COLUMN LIMITS 20 132
READ MATRIX AUTO79.DAT X
LET S = SINGULAR VALUES X
SET WRITE FORMAT F15.5
PRINT S
```

The computed singular values are:

```
64127.84766
8772.52637
503.75061
208.19633
35.93915
33.60710
26.15010
17.76331
16.14256
5.89679
4.97285
2.48678
```