# Measurement of $\Delta\Gamma_{\rm s}$ at CDFI

Along with  $\Delta M$ ,  $\Delta \Gamma$  and  $\phi$  are the other two parameters describing mixing in a system of the neutral *B* mesons.  $\Delta\Gamma \propto \Delta M$ , hence large  $\Delta M$  in the  $B_s - \overline{B}_s$  system predicted by the Standard Model means large  $\Delta\Gamma_s$ . While larger  $\Delta M$  is more difficult to determine experimentally, the larger  $\Delta\Gamma$  is the easier it is to measure. This presentation reviews a measurement of  $\Delta\Gamma_s$  accomplished by the CDF Collaboration using 260 pb<sup>-1</sup> of data.



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### 1. Motivation

$$egin{bmatrix} d' \ s' \ b' \end{bmatrix} = egin{bmatrix} V_{ud} & V_{us} & V_{ub} \ V_{cd} & V_{cs} & V_{cb} \ V_{td} & V_{ts} & V_{tb} \end{bmatrix} egin{bmatrix} d \ s \ b \end{bmatrix} \ V^\dagger = V^{-1} \ V^st_{ub}V_{ud} + V^st_{cb}V_{cd} + V^st_{tb}V_{td} = 0 \end{cases}$$



#### Over-constrain UT:

- measure  $lpha,eta,\gamma,R_u\,\&\,R_t$
- in particular, extract





#### B flavor oscillations





 $\Rightarrow$  MIXING with eff.  $H = \begin{bmatrix} M & M_{12} \\ M_{12}^* & M \end{bmatrix} - \frac{i}{2} \begin{bmatrix} \Gamma & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma \end{bmatrix}$ 

→ Diagonalize and get two eigenstates:  $|B^{L,H}\rangle = p|B^{0}\rangle \mp q|\overline{B}^{0}\rangle, \quad |p|^{2} + |q|^{2} = 1$   $\lambda_{L,H} = (M - \frac{i}{2}\Gamma) \mp \frac{q}{p}(M_{12} - \frac{i}{2}\Gamma_{12}), \quad \frac{q}{p} = \sqrt{\frac{M_{12}^{*} - \frac{i}{2}\Gamma_{12}^{*}}{M_{12} - \frac{i}{2}\Gamma_{12}}} = \begin{cases} e^{2i\beta}, B_{d} \\ 1, B_{s} \end{cases}$  $(e^{2i\beta_{s}}, \beta_{s} \approx 0.03)$ 

**B flavor oscillations** 2  

$$M_{L,H} = Re(\lambda_{L,H}) \Rightarrow \begin{cases} \Delta M = M_H - M_L = 2|M_{12}| \\ \Delta \Gamma = \Gamma_L - \Gamma_H = 2|\Gamma_{12}|\cos\phi \\ \phi = \arg(-M_{12}/\Gamma_{12}) - \text{small} \end{cases}$$

$$M_{12} = -\frac{\eta_{Bq}}{3\pi} \frac{m_W^2}{m_b^2} F S_0(m_t^2/m_W^2)(V_{tq}^*V_{tb})^2$$

$$\Gamma_{12} = \frac{\eta'_{Bq}}{2} F \left[ (V_{tq}^*V_{tb})^2 + V_{tq}^*V_{tb}V_{cq}^*V_{cb}\mathcal{O}\left(\frac{m_c}{m_b^2}\right) + (V_{cq}^*V_{cb})^2 \mathcal{O}\left(\frac{m_d}{m_b^4}\right) \right]$$
where  $F = \frac{G_F^2 m_b^2 M_{Bq} f_{Bq}^2 B_{Bq}}{A_B \text{ Buras, W Slominski, and H Steger, Nucl. Phys. B245 369-398}$   
 $\Rightarrow \Delta M, \Delta \Gamma \Rightarrow M_{12}, \Gamma_{12} \Rightarrow V_{td}, V_{ts} \qquad \boxed{\frac{\Delta \Gamma_s}{\Delta M_s} = (3.7 \frac{+0.8}{-1.5}) \times 10^{-3}}$   
 $\Rightarrow \text{ Measure } \Delta M_{d,s} \text{ and } \Delta \Gamma_{d,s}$   

$$\boxed{\frac{\Delta M}{B_d - \overline{B}_d}} \qquad 0.510 \pm 0.005 \text{ ps}^{-1} \qquad -0.007 \pm 0.038}$$

$$B_s - \overline{B}_s > 14.4 \text{ ps}^{-1} @95\% \text{ C.L.} \qquad \text{Today}}$$

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Today



## With the state of the art technologies $\Delta M_{\mathcal{S}}$ measurement may still be hostage to the (un)kindness of Nature

### Measuring large $\Delta\Gamma_{\rm S}$ ... is easy!

$$rac{\Delta\Gamma_s}{\Gamma_s}\!=\!0.12\!\pm\!0.06$$

• 
$$\sigma_t = au_{B_s}/10$$
 is all right

no tagging required

- effective signal size is much better than  $S/100\,$ 

If you run a risk, it makes sense to have insurance — measure  $\Delta\Gamma_s$ 

Straightforward approach facilitated by:  $\frac{q}{p} = 1 \Rightarrow \begin{cases} |B_s^L\rangle = p|B_s\rangle - q|\overline{B}_s\rangle = \frac{1}{\sqrt{2}} \Big[ |B_s\rangle - |\overline{B}_s\rangle \Big] & CP\text{-even} \\ |B_s^H\rangle = p|B_s\rangle + q|\overline{B}_s\rangle = \frac{1}{\sqrt{2}} \Big[ |B_s\rangle + |\overline{B}_s\rangle \Big] & CP\text{-odd} \\ \end{cases}$ Phase convention:  $CP|B_s\rangle = -|\overline{B}_s\rangle$ 

- statistically separate  $B_s^H$  from  $B_s^L$  using parity of the angular correlations in  $B_s \to J/\psi\phi$  decay
- fit distinct lifetimes to  $B_s^H$  and  $B_s^L$  components
- cross-check the analysis by performing similar one on a  $B_d o J/\psi K^{*0}$  sample

#### Analysis of $P \rightarrow VV$ decays

 $egin{aligned} B_d &
ightarrow J/\psi K^{st 0} \ B_S &
ightarrow J/\psi \phi \ _{J/\psi 
ightarrow \mu\mu, \ \phi 
ightarrow KK, \ K^{st 0} 
ightarrow K\pi \end{aligned}$ 



Need three amplitudes to describe

 $S, D \ wave = P- ext{even}$  $(CP- ext{even for } B_s)$  $P \ wave = P- ext{odd}$  $(CP- ext{odd for } B_s)$ 





### Angular analysis time-dependent kind

 $rac{d^4 \mathcal{P}}{dec{\omega} \, dt} \propto |A_0|^2 \cdot g_1(t) \cdot f_1(ec{\omega})$  $+|A_{\parallel}|^2 \!\cdot\! g_2(t) \!\cdot\! f_2(ec\omega)$  $+|A_{+}|^{2} \cdot g_{3}(t) \cdot f_{3}(\vec{\omega})$  $\pm Im(A_{\parallel}^{*}A_{\perp})\!\cdot\!g_{4}(t)\!\cdot\!f_{4}(ec{\omega})$  $+Re(A_0^*A_{\parallel})\!\cdot\!g_5(t)\!\cdot\!f_5(ec\omega)$  $\pm Im(A_0^*A_\perp) \cdot g_6(t) \cdot f_6(ec\omega)$  $\equiv \sum^6 {\cal A}_i \!\cdot\! g_i(t) \!\cdot\! f_i(ec\omega)$ i=1

$$egin{aligned} f_1(ec{\omega}) &= & 2\cos^2\psi(1-\sin^2 heta\cos^2\phi) \ f_2(ec{\omega}) &= & \sin^2\psi(1-\sin^2 heta\sin^2\phi) \ f_3(ec{\omega}) &= & \sin^2\psi\sin^2 heta \ f_4(ec{\omega}) &= & -\sin^2\psi\sin2 heta\sin\phi \ f_5(ec{\omega}) &= & rac{1}{\sqrt{2}}\sin2\psi\sin^2 heta\sin2\phi \ f_6(ec{\omega}) &= & rac{1}{\sqrt{2}}\sin2\psi\sin2 heta\cos\phi \end{aligned}$$

 $g_i(t)$  different for  $B_d$ and  $B_s$  and are rather non-trivial

A. Dighe et. al., Eur. Phys. J. C 6, 647-662

### Angular analysis time-dependent kind

 $B_s 
ightarrow J/\psi\phi$ :

$$egin{aligned} &rac{d^4 \mathcal{P}}{dec \omega \, dt} \propto |A_0|^2 \cdot e^{-\Gamma_L t} \cdot f_1(ec \omega) \ &+ |A_{\parallel}|^2 \cdot e^{-\Gamma_L t} \cdot f_2(ec \omega) \ &+ |A_{\perp}|^2 \cdot e^{-\Gamma_H t} \cdot f_3(ec \omega) \ &+ Re(A_0^*A_{\parallel}) \cdot e^{-\Gamma_L t} \cdot f_5(ec \omega) \end{aligned}$$

$$egin{aligned} &B_d 
ightarrow J/\psi K^{st 0}\colon \ &rac{d^4 \mathcal{P}}{dec \omega \, dt} \propto \left\{ |A_0|^2 \cdot f_1(ec \omega) 
ight. \ &+ |A_\parallel|^2 \cdot f_2(ec \omega) \ &+ |A_\perp|^2 \cdot f_3(ec \omega) \ &+ |A_\perp|^2 \cdot f_3(ec \omega) \ &\pm Im(A_\parallel^st A_\perp) \cdot f_4(ec \omega) \ &+ Re(A_0^st A_\parallel) \cdot f_5(ec \omega) \ &\pm Im(A_0^st A_\perp) \cdot f_6(ec \omega) 
ight\} \cdot e^{-\Gamma_d t} \end{aligned}$$

• flavor blind decay -  $\pm Im(...)$  terms average out • flavor specific decay - no linear sensitivity to  $\Delta\Gamma$ 

### Use these to extract $A_0, A_{\parallel}, A_{\perp}, \text{ and } \Gamma_{(L,H)}$ from data (set $arg(A_0) = 0$ )

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### 2. Measurement



 $J/\psi \rightarrow \mu^+ \mu^-$  trigger to collect samples of:

- $B_u 
  ightarrow J/\psi K^+$
- $B_d \rightarrow J/\psi K^{*0}$
- $B_s \to J/\psi \phi$

 $260\,\mathrm{pb}^{-1}$  of data

- B candidate: { $(m, \sigma_m), (ct, \sigma_{ct}), \vec{\omega}$ }
  - m separate signal
     from background
  - ct lifetime fit +
     addt-l S/B separa tion
  - $\vec{\omega}$  angular analysis
- cross-checks in other B samples:
  - models
  - techniques





#### Modeling $\vec{\omega}$ - sculpting 3 does it work this way?

#### YES, IT DOES!

Indeed, no need to
parametrize/integrate
the acceptance

#### note:

 $|\xi_{1,2,3} \gg |\xi_5| > |\xi_{4,6}| \simeq 0$ 

i	$\xi_i^{B_s}$	$\xi_i^{B_d}$
1	3.81e-02	3.48e-02
2	4.06e-02	4.23e-02
3	4.07e-02	4.27e-02
5	-7.43e-05	-7.26e-04

#### Monte Carlo tests:

$B_s$ prm.	input	fit result	diff., $\sigma$	
$ A_0 ^2$	0.5625	$0.5627 \pm 0.0019$	0.0	
$ oldsymbol{A}_{\parallel} ^2$	0.2025	$0.2048 \pm 0.0029$	+0.8	
$arg(A_{\parallel})$	2.0	$1.980\pm0.014$	-1.4	
$c au_L,\mu{ m m}$	330.0	$332.1 \pm 1.4$	+1.5	
$\Delta\Gamma/\Gamma,\%$	50.0	$49.6\pm0.9$	-0.4	
$N_{sig}$		132129		

$B_d$ prm.	input	fit result	diff., $\sigma$
$ A_0 ^2$	0.597	$0.5912 \pm 0.0020$	-2.9
$ A_{\parallel} ^2$	0.243	$0.2469 \pm 0.0030$	+1.3
$arg(A_{\parallel})$	<b>2.5</b>	$2.5356 \pm 0.0170$	+2.1
$arg(A_{\perp})$	-0.17	$-0.1743 \pm 0.0128$	-0.3
$N_{sig}$		132866	

### 3. Results

 $au_{B_u} = (1.659 \pm 0.033 \stackrel{+0.007}{_{-0.008}}) \,\mathrm{ps}$ PDG'04:  $au_{B_u} = (1.671 \pm 0.018) ext{ ps}$  $au_{B_d} = (1.549 \pm 0.051 \stackrel{+0.007}{_{-0.008}}) \,\mathrm{ps}$ 

PDG'04:  $au_{B_d} = (1.536 \pm 0.014) ext{ ps}$ 

 $au_{B_s} = (1.363 \pm 0.100 \stackrel{+0.007}{_{-0.010}}) \, \mathrm{ps}$ 

- $\rightarrow \tau_{B_u}$  and  $\tau_{B_d}$  are in excellent agreement with PDG
- $\rightarrow \tau_{B_s}$  indicative of large  $\Delta \Gamma_s$ :

$$-\frac{2c\tau_H\tau_L}{\tau_H+\tau_L} = 460 \,\mu\text{m} \,\left(\Gamma_s = \Gamma_d\right)$$

 $-0.23c\tau_H$ +0.77 $c\tau_L$ =409  $\mu$ m (CDF I)

#### Avg. lifetime measurements



 $-\frac{0.16\tau_H}{0.16\tau_H + 0.84\tau_L}c\tau_H + \frac{0.84\tau_L}{0.16\tau_H + 0.84\tau_L}c\tau_L = 409\,\mu\text{m}\,\,(\text{SU(3)})$ 

## t-dep. angular analysis fit results





#### Fit projections



side-band subtracted, sculpting corrected signal. ct>0 cut applied

#### **Cross-checks**

#### 1. " $\Delta\Gamma/\Gamma$ " from $B_d$

$B_d$ sample	$\Delta\Gamma/\Gamma,\%$	$c au_{(L)}, \mu{ m m}$
Full, one c $ au$		$461 \pm 15$
Full	$14.5\pm12.1$	$444 \pm 21$
Sub-sample 1	$13.7\pm27.9$	$422 \pm 34$
Sub-sample 2	$25.1 \pm 22.3$	$437\pm39$
Sub-sample 3	$26.1 \pm 23.0$	$437\pm50$
Sub-sample 4	$-7.6\pm27.6$	$475\pm41$

2. 
$$f_{CP_{odd}}$$
 vs.  $ct$  cut

$B_s$ : fitted	$B_s$ : pred.	$B_d$ : fitte
$f_{CP_{odd}},\%$	$f_{CP_{odd}},\%$	$f_{P_{odd}}, ?$
$20.1\pm9.0$	-20.1-	$21.6\pm4.4$
$24.2\pm10.3$	24.1	$23.0\pm3.$
$29.6 \pm 12.7$	28.6	$23.0\pm4.$
$38.7 \pm 11.6$	33.6	$23.6 \pm 4.$
	$B_s:  ext{ fitted } \ f_{CP_{odd}}, \%$ 20.1 $\pm$ 9.0 24.2 $\pm$ 10.3 29.6 $\pm$ 12.7 38.7 $\pm$ 11.6	$egin{array}{llllllllllllllllllllllllllllllllllll$



### Systematic uncertainty summary

$B_d$	$  c au, \mu m$	$ A_0 ^2$	$ m{A}_{  } ^2$	$ A_{\perp} ^2$	$arg(A_{\parallel})$	$arg(A_{\perp})$
Bkg. angular model	$\pm 3.9$	$\pm 0.013$	$\pm 0.006$	$\pm 0.007$	$\pm 0.01$	$\pm 0.01$
Eff. and acc.						
$\mathrm{K} \leftrightarrow \pi$ swap		$\pm 0.006$	$\pm 0.004$	$\pm 0.002$	$\pm 0.04$	
Non-resonant decays		$\pm 0.010$	$\pm 0.001$	$\pm 0.003$	$\pm 0.07$	$\pm 0.04$
Lft. fit model	$\pm 1.7$					
SVX alignment	$\pm 1.0$					
Detector bias	-1.2					
$B_s$ cross feed						
Total	$\begin{array}{c} +4.4 \\ -4.6 \end{array}$	$\pm 0.017$	$\pm 0.007$	$\pm 0.007$	$\pm 0.08$	$\pm 0.04$
$B_s$	$c au_L,\mu{ m m}$	$\Delta\Gamma/\Gamma$	$ A_0 ^2$	$ oldsymbol{A}_{\parallel} ^2$	$ m{A}_{\perp} ^2$	$arg(A_{\parallel})$
Bkg. angular model	$\pm 3.7$	$\pm 0.007$	$\pm 0.011$	$\pm 0.013$	$\pm 0.002$	$\pm 0.03$
Eff. and acc.						
Unequal $\# B_s, \bar{B}_s$						
Lft. fit model	$\pm 1.7$					
SVX alignment	$\pm 1.0$					
Detector bias	-1.2					
$B_d$ cross feed	-5.0	$\pm 0.008$		$\pm 0.003$	$\pm 0.003$	
Total	$\begin{array}{c}+4.2\\-6.7\end{array}$	$\pm 0.011$	$\pm 0.011$	$\pm 0.013$	$\pm 0.004$	$\pm 0.03$

### Final results



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### Comparison

#### 1



#### CDF can do lifetimes (exceptionally) well

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CDF can do amplitudes very well too

and even see some SU(3) symmetry :o)



Comparison

#### Summary



- PRL 94 101803 (2005)
- a lot of excitement in the community and even some controversy
- additional motivation for measurements of  $\Delta M_s$ ,  $au_s^{fsp}$  $Br(B_s o D_s^{(*)+}D_s^{(*)-})$
- more careful averaging farstriang of  $B_s$  lifetime measurements



#### → Don't stop here!

- improve technique
- get better precision with more statistics
- use alternative methods and combine results

### **BACKUP SLIDES**

#### MC-Data agreement know for $B_u$ • check for $B_d$ • assume for $B_s$



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#### MC-Data agreement

