SEMCDF

PURPOSE

Compute the semi-circular cumulative distribution function.

DESCRIPTION

The semi-circular distribution is the distribution of the projection onto one axis of the points uniformly distributed within the unit circle. As such, it is useful for testing 2-dimensional uniformity. The semi-circular probability density function is:

$$f(x) = \sqrt{1-x^2}$$
 for $-1 \le x \le 1$ (EQ 8-311)

The semi-circular cumulative distribution function is:

$$F(x) = \frac{1}{2} + \left(\frac{1}{\pi}\right) \left(\arctan\left(\frac{x}{\sqrt{1 - x^2}}\right) + x\sqrt{1 - x^2}\right)$$
 for $-1 \le x \le 1$ **(EQ 8-312)**

SYNTAX

LET < y2 > = SEMCDF(< y1 >)

<SUBSET/EXCEPT/FOR qualification>

where <y1> is a variable, a number, or a parameter in the range -1 to 1;

<y2> is a variable or a parameter (depending on what <y1> is) where the computed semi-circular cdf value is stored; and where the <SUBSET/EXCEPT/FOR qualification> is optional.

EXAMPLES

LET A = SEMCDF(3)LET Y = SEMCDF(X1)

DEFAULT

None

SYNONYMS

None

RELATED COMMANDS

SEMPDF Compute the semi-circular probability density function. **SEMPPF** Compute the semi-circular percent point function. UNIPDF Compute the uniform probability density function. UNICDF Compute the uniform cumulative distribution function. UNIPPF Compute the uniform percent point function.

NORCDF Compute the normal cumulative distributing function. Compute the normal probability density function. **NORPDF NORPPF** Compute the normal percent point function.

REFERENCE

"Continuous Univariate Distributions - 2," Johnson and Kotz, Houghton Mifflin, 1970 (chapter 25).

"Simple and Robust Linear Estimation of the Location Parameter of a Symmetric Distribution," Filliben, unpublished Ph.d dissertation, Princeton University, 1969 (pp. 21-44, 229-231).

APPLICATIONS

Data Analysis

IMPLEMENTATION DATE

94/4

PROGRAM

YLIMITS 0 1
MAJOR YTIC NUMBER 6
MINOR YTIC NUMBER 1
YTIC DECIMAL 1
XLIMITS -1 1
XTIC OFFSET 0.1 0.1
TITLE AUTOMATIC
X1LABEL X
Y1LABEL PROBABILITY
PLOT SEMCDF(X) FOR X = -1 0.01 1

