

**POIPDF****PURPOSE**

Compute the Poisson probability density function.

**DESCRIPTION**

The Poisson distribution is the distribution of the number of events in the interval  $(0, \lambda)$  when the waiting time between events is exponentially distributed with mean 1 and standard deviation 1 (there are alternate interpretations as well). The Poisson distribution has the following probability density function:

$$p(x, \lambda) = \frac{e^{-\lambda} \lambda^x}{x!} \quad (\text{EQ 8-304})$$

where  $x$  is a non-negative integer. The mean is  $\lambda$  and the standard deviation is  $\sqrt{\lambda}$ .

**SYNTAX**

LET <y2> = POIPDF(<y1>,<lambda>) <SUBSET/EXCEPT/FOR qualification>  
 where <y1> is a non-negative integer variable, number, or parameter (a warning message is printed if it is not);  
 <y2> is a variable or a parameter (depending on what <y1> is) where the computed Poisson pdf value is stored;  
 <lambda> is a positive number or parameter that specifies the shape parameter of the Poisson distribution;  
 and where the <SUBSET/EXCEPT/FOR qualification> is optional.

**EXAMPLES**

```
LET A = POIPDF(3,0.5)
LET Y = POIPDF(X1,0.3)
```

**DEFAULT**

None

**SYNONYMS**

None

**RELATED COMMANDS**

|        |   |   |
|--------|---|---|
| POICDF | = | Compute the Poisson cumulative distribution function.           |
| POIPPF | = | Compute the Poisson percent point function.                     |
| BINCDF | = | Compute the binomial cumulative distribution function.          |
| BINPDF | = | Compute the binomial probability density function.              |
| BINPPF | = | Compute the binomial percent point function.                    |
| NBCDF  | = | Compute the negative binomial cumulative distribution function. |
| NBPDF  | = | Compute the negative binomial probability density function.     |
| NBPPF  | = | Compute the negative binomial percent point function.           |
| GEOCDF | = | Compute the geometric cumulative distribution function.         |
| GEOPDF | = | Compute the geometric probability density function.             |
| GEOPPF | = | Compute the geometric percent point function.                   |

**REFERENCE**

"Discrete Univariate Distributions," Johnson and Kotz, Houghton Mifflin, 1970 (chapter 4).

"Statistical Distributions," 2nd ed., Evans, Hastings, and Peacock, Wiley and Sons, 1993 (chapter 31).

**APPLICATIONS**

Queueing theory, analysis of count data

**IMPLEMENTATION DATE**

94/4

**PROGRAM**

```
MULTIPLY 2 2; MULTIPLY CORNER COORDINATES 0 0 100 100
YLIMITS 0 0.2
XLIMITS 0 50
XTIC OFFSET 0.5 0.5
LINE BLANK
SPIKE ON
SPIKE THICKNESS 0.3
TITLE AUTOMATIC
X1LABEL NUMBER OF SUCCESSES
Y1LABEL PROBABILITY
TITLE SIZE 3
PLOT POIPDF(X,5) FOR X = 0 1 50
PLOT POIPDF(X,15) FOR X = 0 1 50
PLOT POIPDF(X,25) FOR X = 0 1 50
PLOT POIPDF(X,35) FOR X = 0 1 50
END OF MULTIPLY
```

