

## PLNPDF

### PURPOSE

Compute the standard power-normal probability density function.

### DESCRIPTION

The standard lognormal distribution has the following probability density function:

$$f(x, \sigma, p) = \left( \frac{p}{x\sigma} \right) \phi\left( \frac{\ln(x)}{\sigma} \right) \left( \Phi\left( \frac{-\ln(x)}{\sigma} \right) \right)^{p-1} \quad x > 0, \sigma > 0, p > 0 \quad (\text{EQ Aux-264})$$

where  $\sigma$  is the shape parameter,  $p$  is the power parameter, and  $\Phi$  and  $\phi$  are the cumulative distribution function and the probability density function for the standard normal distribution respectively.

If  $p$  is 1, this distribution reduces to the lognormal distribution.

### SYNTAX

LET <y2> = PLNPDF(<y1>,<p>,<s>) <SUBSET/EXCEPT/FOR qualification>

where <y1> is a non-negative number, parameter, or variable;

<p> is a positive number, parameter, or variable that specifies the power parameter;

<s> is an optional positive number, parameter, or variable that specifies the shape parameter;

<y2> is a variable or a parameter (depending on what <y1> is) where the computed power-lognormal pdf value is stored; and where the <SUBSET/EXCEPT/FOR qualification> is optional.

If the <s> parameter is omitted, it defaults to 1.

### EXAMPLES

LET A = PLNPDF(3,2,1)

LET X2 = PLNPDF(X1,POW,SD)

LET X2 = PLNPDF(X1,0.5,0.5)

### NOTE

The general power-lognormal distribution has the following probability density function:

$$f(x, \mu, \sigma, p) = \left( \frac{p}{x\sigma} \right) \phi\left( \frac{\ln(x) - \mu}{\sigma} \right) \left( \Phi\left( \frac{-\ln(x) - \mu}{\sigma} \right) \right)^{p-1} \quad x > 0, \sigma > 0, p > 0 \quad (\text{EQ Aux-265})$$

where  $\mu$  is the location parameter,  $\sigma$  is the shape parameter and  $p$  is the power parameter.

### DEFAULT

None

### SYNOMYS

None

### RELATED COMMANDS

PLNCDF	=	Compute the power-lognormal cumulative distribution function.
PLNPPF	=	Compute the power-lognormal percent point function.
PNRCDF	=	Compute the power-normal cumulative density function.
PNRPDF	=	Compute the power-normal probability density function.
PNRPPF	=	Compute the power-normal percent point function.
LGNCDF	=	Compute the lognormal cumulative distribution function.
LGNPDF	=	Compute the lognormal probability density function.
LGNPPF	=	Compute the lognormal percent point function.
NORCDF	=	Compute the normal cumulative distribution function.
NORPDF	=	Compute the normal probability density function.
NORPPF	=	Compute the normal percent point function.

**REFERENCE**

"A Computer Program POWNOR for Fitting the Power-Normal and -Lognormal Models to Life or Strength Data from Specimens of Various Sizes," Nelson and Doganaksoy, NIST-IR 4760, March 1992.

**APPLICATIONS**

Reliability

**IMPLEMENTATION DATE**

95/5

**PROGRAM**

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TITLE SD=1, P=10000, 3000, 1000, 300, 100, 50, 20, 5, 1, 0.5, 0.2 0.1
TITLE SIZE 2
X1LABEL PDF's
YLIMITS 0 1
YTIC OFFSET 0 0.1
MAJOR YTIC MARK NUMBER 6

PLOT PLNPDF(X,10000,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,3000,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,1000,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,300,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,100,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,50,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,20,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,5,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,1,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,0.5,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,0.2,1) FOR X = 0.01 .05 3 AND
PLOT PLNPDF(X,0.1,1) FOR X = 0.01 .05 3

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