
$K \rightarrow \pi \nu \bar{\nu}$ in and beyond the SM

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Technion

Some references

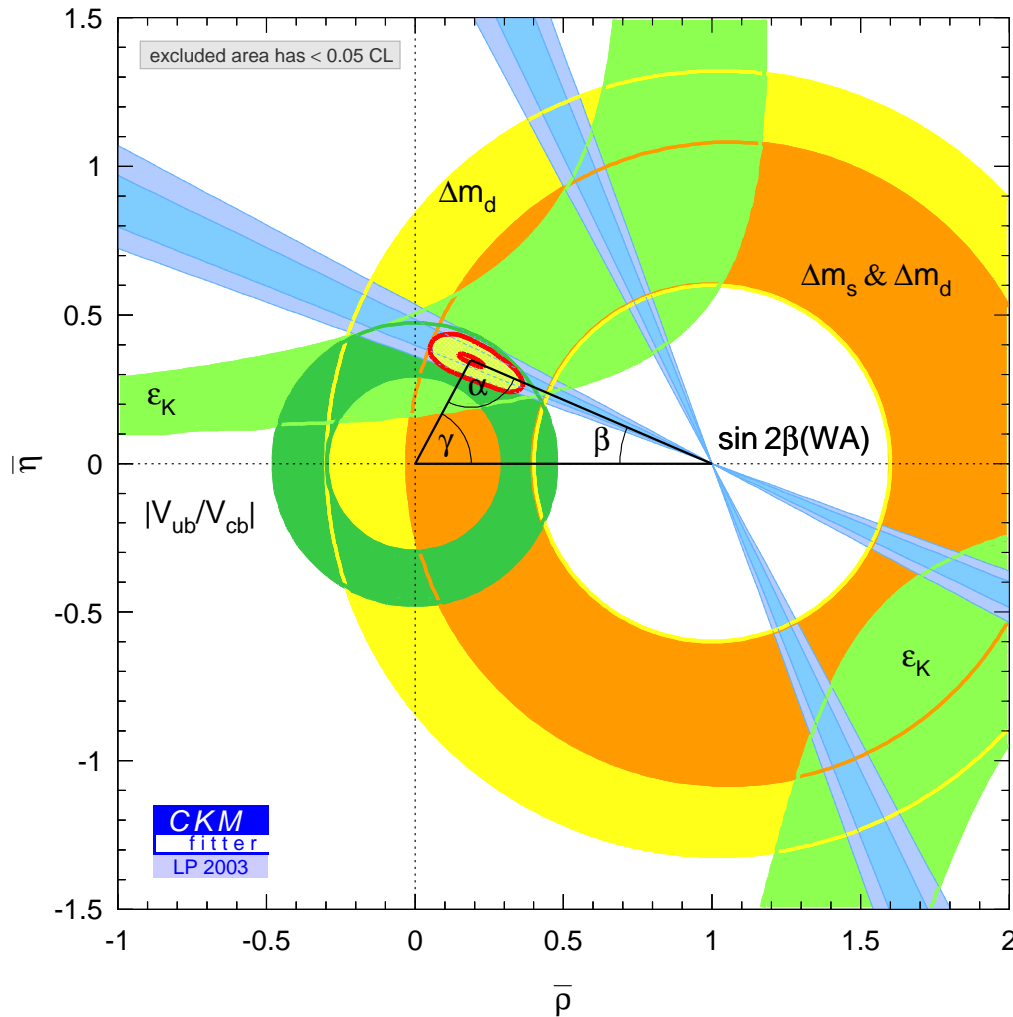
- Littenberg, 1989
- Buchalla and Buras, 1990s
- Grossman and Nir, 1997
- Nir and Worah, 1997
- Falk and Petrov, 2001
- D'Ambrosio and Isidori, 2001
- Grossman, Isidori and Murayama, 2003

Outline

- $K \rightarrow \pi \nu \bar{\nu}$ in specific models
 - General considerations
 - Standard Model
 - New physics
- General properties of $K_L \rightarrow \pi \nu \bar{\nu}$
 - Why is $K_L \rightarrow \pi \nu \bar{\nu}$ CP violating?
 - What kind of CP violation?
 - Possible CP conserving contributions
- Conclusions

$K \rightarrow \pi \nu \bar{\nu}$ in specific models

Setting the stage



Hocker et al. (CKMfitter)

- Present:
 $V_{cb}, V_{ub}/V_{cb}, \epsilon_K,$
 $\Delta m_d, \Delta m_s,$
 $a_{CP}(B \rightarrow \psi K_S)$
- Future:
 $\gamma, \alpha, K \rightarrow \pi \nu \bar{\nu}$
- Tiny Errors

What is an ultimate observable?

- A good observable is
 1. Theoretically interesting
 2. Theoretically clean
 3. Experimentally accessible
- Not too many such observables

$$\begin{array}{ll} a_{CP}(B \rightarrow J/\psi K_S) & a_{CP}(B_s \rightarrow J/\psi \phi) \\ B \rightarrow DK (\gamma) & K \rightarrow \pi \nu \bar{\nu} \end{array}$$

- Interestingly, these are complementary to each other

Why is $K \rightarrow \pi \nu \bar{\nu}$ so clean?

The general problems with hadronic decays are:

- Hadronic matrix elements
- Long distance effects

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- Long distance effects \Leftarrow Neutrinos

Why is $K \rightarrow \pi\nu\bar{\nu}$ so clean?

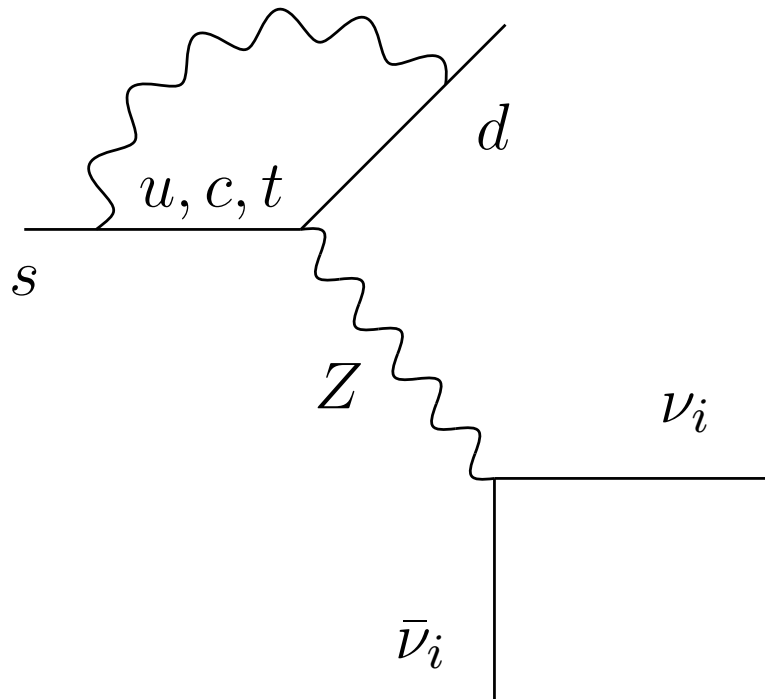
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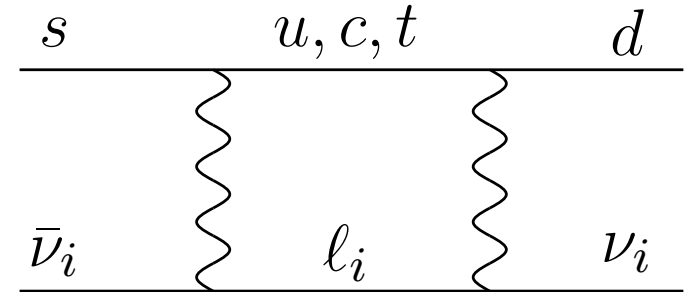
Therefore the $K \rightarrow \pi\nu\bar{\nu}$ decays are very interesting

- Exclusive hadronic decays that we can calculate in the SM and its extensions
- The measured rates are sensitive to fundamental parameters

Example: the standard model



Penguin and box diagrams



$$A(K \rightarrow \pi \nu \bar{\nu}) = \sum_{q=u,c,t} A_q$$

$K \rightarrow \pi \nu \bar{\nu}$ in the SM

$$A(K \rightarrow \pi \nu \bar{\nu}) = \sum_{q=u,c,t} A_q$$

where

$$A_q \sim m_q^2 V_{qs}^* V_{qd} \sim \begin{cases} \Lambda_{QCD}^2 \lambda & up \\ m_c^2 (\lambda + i\lambda^5) & charm \\ m_t^2 (\lambda^5 + i\lambda^5) & top \end{cases}$$

- Hard GIM, negligible LD effects
- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$: top dominant, charm is important
- $K_L \rightarrow \pi \nu \bar{\nu}$: CP violating, almost pure top

$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ in the SM

The fundamental Wolfenstein parameters: λ , A , ρ and η

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = C_+ |A|^4 \times [\eta^2 + (\rho - \rho_c)^2] = O(10^{-10})$$

- C_+ is known
- ρ_c includes the charm effect, with small theoretical errors
- The largest error in extracting ρ and η is from A

$K_L \rightarrow \pi\nu\bar{\nu}$ in the SM

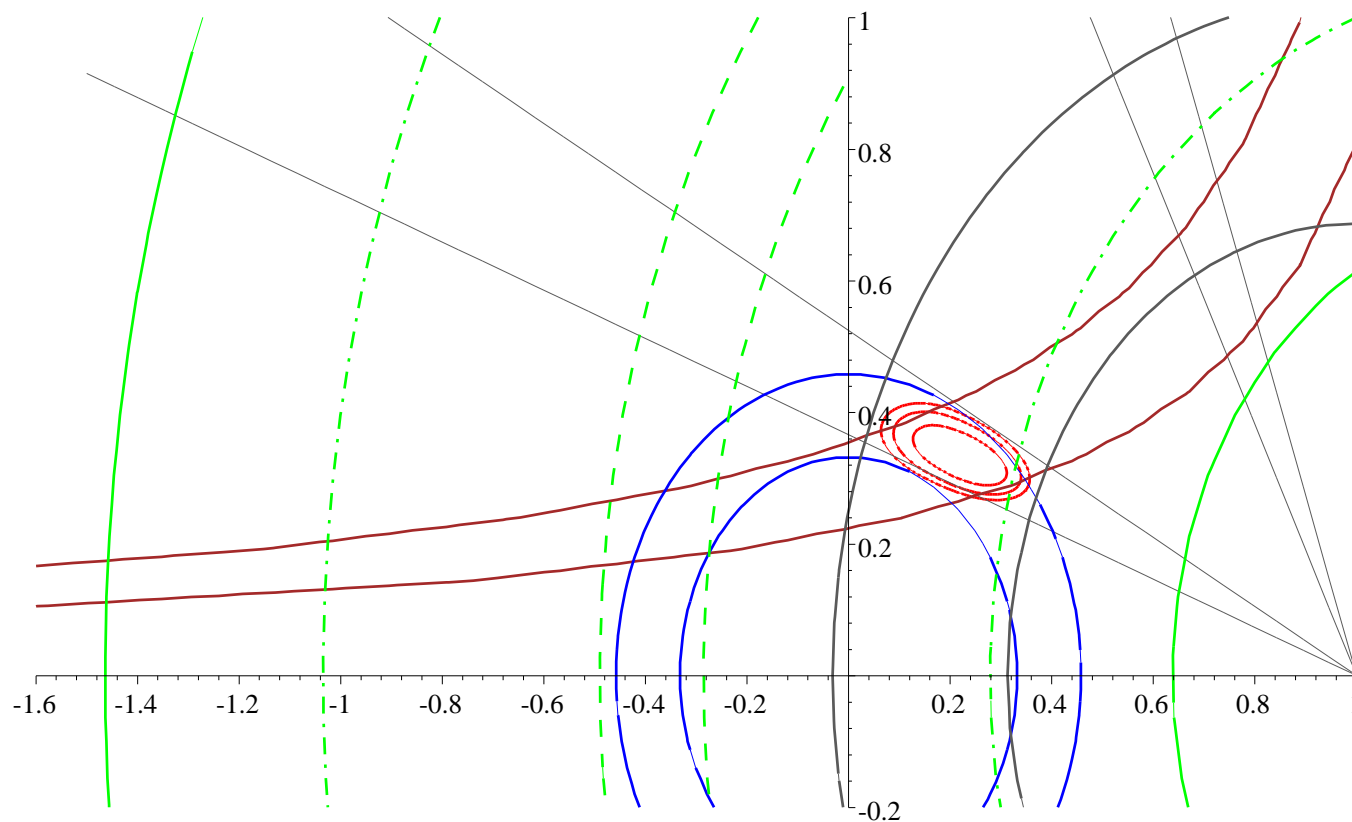
$$\mathcal{B}(K_L \rightarrow \pi\nu\bar{\nu}) = C_L |A|^4 \times \eta^2 = O(10^{-11})$$

- CP violating decay
- Very small theoretical error in C_L
- The largest error in extracting ρ and η is from A
- In the ratio A cancels

$$\frac{\mathcal{B}(K_L \rightarrow \pi\nu\bar{\nu})}{\mathcal{B}(K^+ \rightarrow \pi^+\nu\bar{\nu})} = \frac{C_L}{C_+} \times \frac{\eta^2}{\eta^2 + (\rho - \rho_c)^2}$$

$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ effects on CKM fits

G. Isidori



- The green lines: central value, 1σ and 90% CL

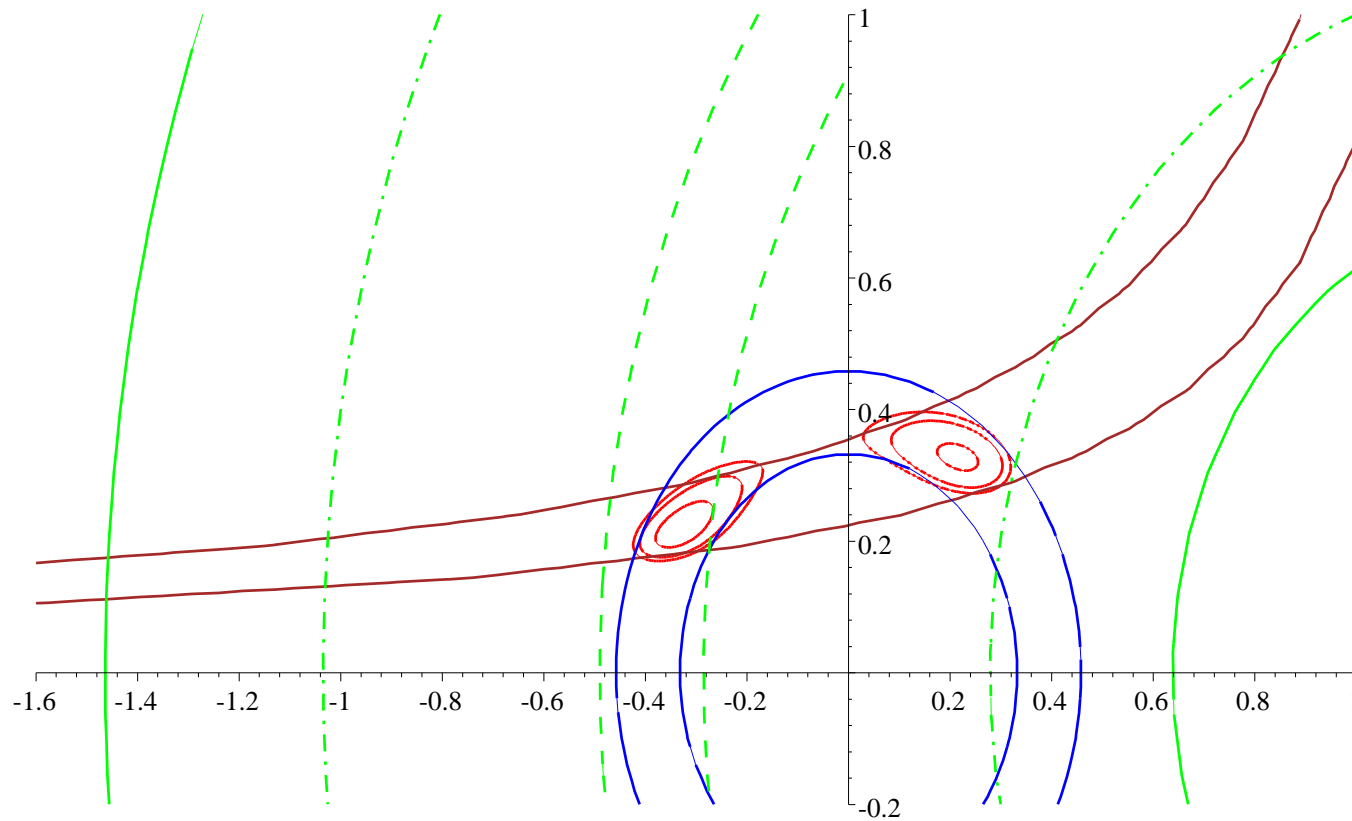
New physics effects

New physics can affect the rates in many ways

- Significant new physics only in the B sector
- Minimal flavor violation: flavor violation is confined to the SM Yukawa couplings
- Significant new physics in $K \rightarrow \pi \nu \bar{\nu}$ decays

New physics only in the B sector

G. Isidori

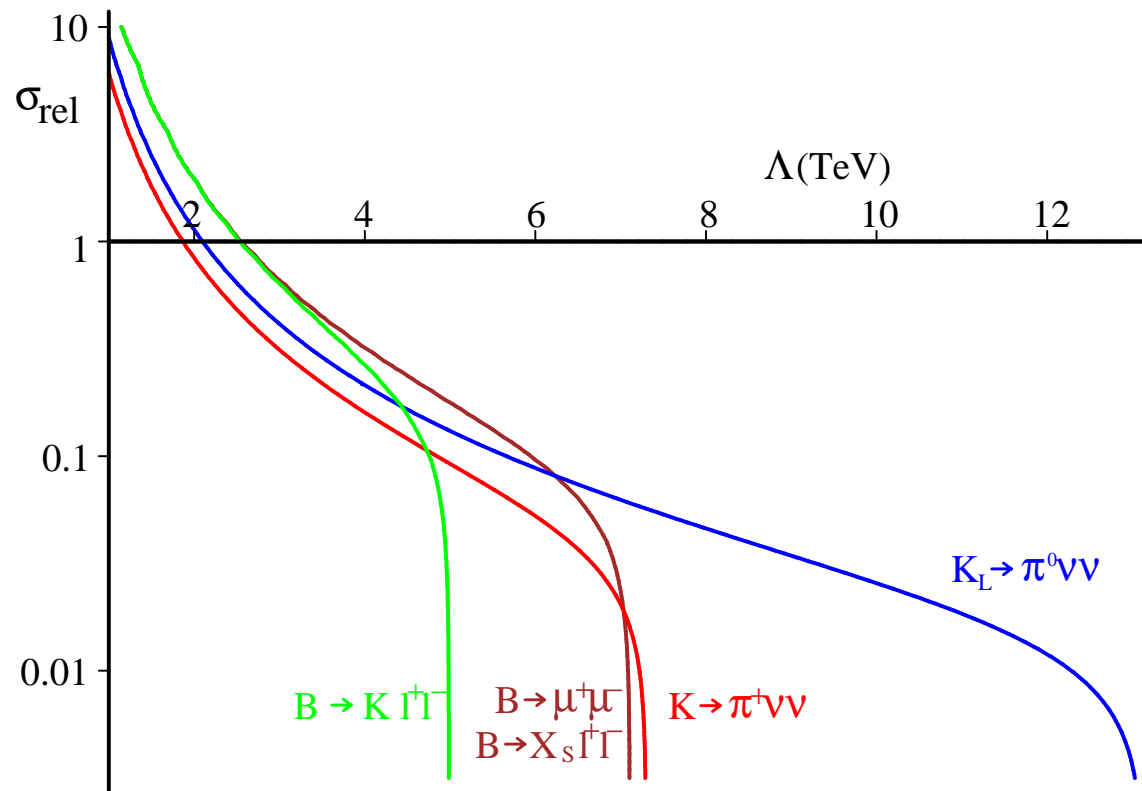


- The green lines: central value, 1σ and 90% CL

Minimal flavor violation

- One effective new parameter: the new physics scale
- Small effects, but $K \rightarrow \pi\nu\bar{\nu}$ have very high sensitivity

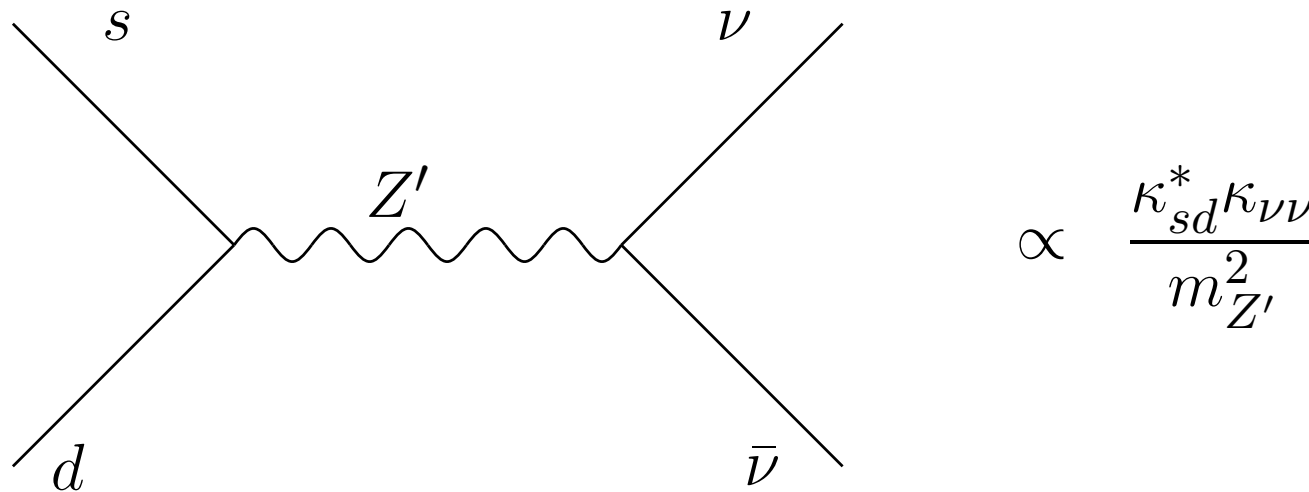
D'Ambrosio, et al.



Non minimal new physics effects

Generic new physics can have large effect with

1. Low scale new physics
2. New flavor violation



Generically, new physics affects B and K differently

General properties of $K_L \rightarrow \pi\nu\bar{\nu}$

Why is $K_L \rightarrow \pi\nu\bar{\nu}$ CP violating decay?

- In general, three body decays do not have definite CP
- $\pi^+\pi^-$ is CP even
- $\pi^+\pi^-\pi^0$ can have both CP even and CP odd components

Is $K_L \rightarrow \pi\nu\bar{\nu}$ a true CP violating decay?

CP violation in $K_L \rightarrow \pi\nu\bar{\nu}$

We neglect ε_K and

1. Consider only left handed neutrinos
2. Assume lepton flavor conservation
3. Neglect small m_K/m_W effects

The only dimension 6 operator that mediate $K_L \rightarrow \pi\nu\bar{\nu}$ is

$$O_{sd}^{ii} = \bar{s}\gamma_\mu d \times \bar{\nu}_L^i \gamma^\mu \nu_L^i$$

- This operator produces $\pi^0 \nu_i \bar{\nu}_i$ in a CP even state
- We can think of it as $K_L \rightarrow \pi Z^*$ two body decay
- Since K_L is CP-odd, $K_L \rightarrow \pi\nu\bar{\nu}$ is CP violating

CP properties of the operators

- We choose

$$|K_L\rangle = |K\rangle + |\bar{K}\rangle$$

- The hadronic matrix element that enter $K_L \rightarrow \pi\nu\bar{\nu}$ transform under CP as

$$\langle\pi|\bar{s}d + \bar{d}s|K_L\rangle \xrightarrow{CP} \langle\pi|\eta_{CP}(\bar{s}d + \bar{d}s)|K_L\rangle$$

- Since we consider only vector interaction where $\eta_{CP}(V) = -1$, $K_L \rightarrow \pi\nu\bar{\nu}$ requires CP violation

What is the kind of CP violation?

In B physics we talk about three types of CPV

1. “Direct” $|\bar{A}/A| \neq 1$
2. “Indirect” $|q/p| \neq 1$
3. Interference between mixing and decay

$$\arg \left(\frac{q\bar{A}}{pA} \right) \neq 0$$

● $K_L \rightarrow \pi\nu\bar{\nu}$ is of the third type \Rightarrow the clean type

The third type of CPV

$$\lambda \equiv \frac{A(\bar{K} \rightarrow \pi\nu\bar{\nu})}{A(K \rightarrow \pi\nu\bar{\nu})} \frac{q}{p}$$

Then we get

$$\frac{\Gamma(K_L \rightarrow \pi\nu\bar{\nu})}{\Gamma(K_S \rightarrow \pi\nu\bar{\nu})} = \frac{1 + \lambda^2 - 2\mathcal{R}e\lambda}{1 + \lambda^2 + 2\mathcal{R}e\lambda} \xrightarrow{|\lambda|=1} \tan^2 \theta$$

where

$$\theta \equiv \arg(\lambda)$$

In the SM $\theta \approx \beta$, up to calculable charm contribution

Bounding the $K_L \rightarrow \pi\nu\bar{\nu}$ rate

$\Gamma(K_S \rightarrow \pi\nu\bar{\nu})$ may never be measured. We thus use isospin

$$\sqrt{2}A(K^0 \rightarrow \pi^0\nu\bar{\nu}) = A(K^+ \rightarrow \pi^+\nu\bar{\nu})$$

Then we get

$$R \equiv r_{is} \frac{\Gamma(K_L \rightarrow \pi\nu\bar{\nu})}{\Gamma(K^+ \rightarrow \pi^+\nu\bar{\nu})} = \sin^2 \theta$$

with $r_{is} = 0.954$ takes care of isospin breaking

- R measured θ cleanly assuming only isospin
- Using $\sin^2 \theta \leq 1$ we get a model independent bound

More general $K_L \rightarrow \pi \nu \bar{\nu}$

We can have CP conserving contribution once we relax each of the above mentioned assumptions

1. Consider also right handed neutrinos
2. Allow for lepton flavor violation
3. Include small m_K/m_W effects

Right handed neutrinos

Consider right-handed neutrinos. Then there are new dimension 6 scalar and tensor operators. For example

$$(\bar{s} \Gamma_S d) \times \bar{\nu}_R \Gamma_S \nu_L$$

- Γ_S is a scalar operator
- Under CP $\Gamma_S \xrightarrow{CP} \Gamma_S$ $\Gamma_V \xrightarrow{CP} -\Gamma_V$
- Scalar operators generate $K_L \rightarrow \pi \nu \bar{\nu}$ in the CP limit, with one LH and one RH neutrino (SM: both are LH)
- The effect due to neutrino masses is tiny
- The spectrum is different from the standard spectrum

m_K/m_W effects

Under CP

$$\nu(k_1)\bar{\nu}(k_2) \xrightarrow{CP} \nu(k_2)\bar{\nu}(k_1)$$

- For a CP eigenstate the ν and $\bar{\nu}$ must have the same spectrum
- The standard dimension 6 operator generates a symmetric spectrum
- Dimension 8 operators do not necessarily generate a symmetric spectrum
- A general spectrum is a sum of a symmetric and a antisymmetric spectrum. That is CP-even and CP-odd
- In the SM this operator comes from the box diagram as long as we keep the external momenta

Lepton number violation

Consider CP conserving new physics model where

$$A(K \rightarrow \pi\nu_i\bar{\nu}_j) \neq 0 \quad A(K \rightarrow \pi\nu_j\bar{\nu}_i) = 0$$

Due to CP

$$A(K \rightarrow \pi\nu_j\bar{\nu}_i) = -A(\bar{K} \rightarrow \pi\nu_i\bar{\nu}_j)$$

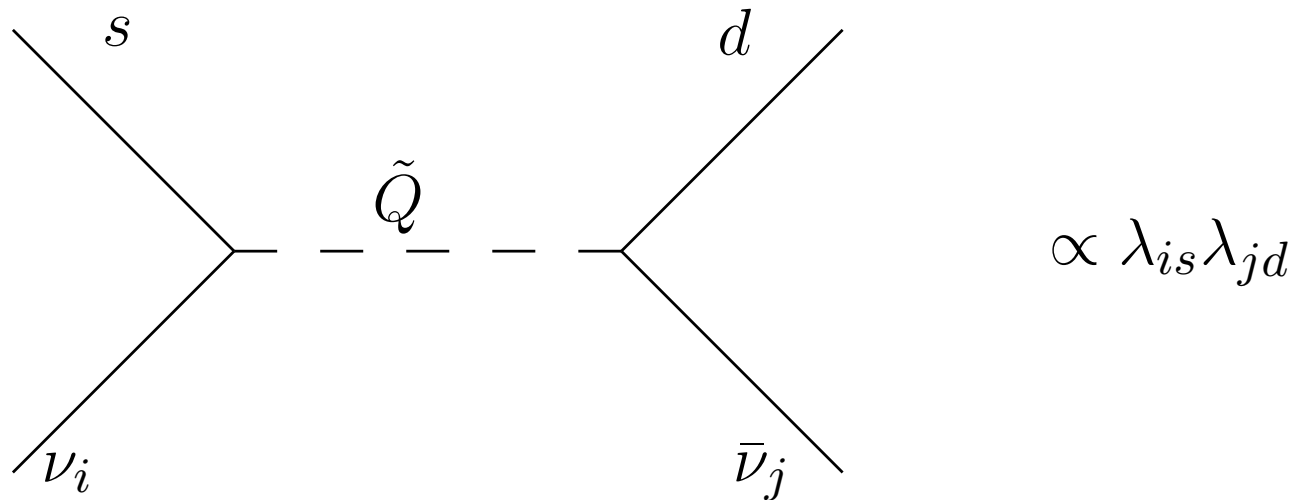
Then

$$\sqrt{2} A(K_L \rightarrow \pi\nu_i\bar{\nu}_j) = A(K \rightarrow \pi\nu_i\bar{\nu}_j) + A(\bar{K} \rightarrow \pi\nu_i\bar{\nu}_j) \neq 0$$

- In the standard CP conserving case, $A(K_L \rightarrow \pi\nu\bar{\nu}) = 0$ since K and \bar{K} cancel each other
- This cancelation does not occur once these decay amplitudes have different magnitudes

Example: SUSY without R-parity

We get an effective leptoquark interaction: $\lambda_{ik}\bar{L}_i Q_k S$



• Then

$$A(K_L \rightarrow \pi \nu_i \bar{\nu}_j) \propto (\lambda_{is}\lambda_{jd} - \lambda_{id}\lambda_{js})$$

that, in general, is finite in the CP limit

Lepton number violation: mass matrices

We know that lepton number is violated by neutrino mass

Q: Can it generate CP conserving contribution to $K_L \rightarrow \pi\nu\bar{\nu}$?

A: No. we can always rotate to interaction basis

Can the CP violating contribution be sensitive to the mixing matrix?

- Neutrino mixing: The effects are proportional to m_ν
- Sneutrino mixing: The $K_L \rightarrow \pi\nu\bar{\nu}$ rate depends on the sneutrino masses but not their mixing angles
- Sneutrino and Slepton mixing. The rate depends on the product of the two rotation matrices

Conclusions

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- The $K \rightarrow \pi\nu\bar{\nu}$ decays are very clean and interesting
- It would be nice to know their rates
- Even in the era when flavor physics is dominated by B 's, kaons are important