

# Thermodynamic Tabulations for Selected Phases in the System CaO-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub>-H<sub>2</sub>O at 101.325 kPa (1 atm) between 273.15 and 1800 K

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The standard thermodynamic properties of phases in the lime-alumina-silica-water system between 273.15 and 1800 K at 101.325 kPa (1 atm) were evaluated from published experimental data. Phases included in the compilation are boehmite, diaspore, gibbsite, kaolinite, dickite, halloysite, andalusite, kyanite, sillimanite, Ca-Al clinopyroxene, anorthite, gehlenite, grossular, prehnite, zoisite, margarite, wollastonite, cyclowollastonite (= pseudowollastonite), larnite, Ca olivine, hatrurite, and rankinite. The properties include heat capacity, entropy, relative enthalpy, and the Gibbs energy function of the phases and the enthalpies, Gibbs energies, and equilibrium constants for formation both from the elements and the oxides. Tabulated values are given at 50 K intervals with the 2-sigma confidence limit at 250 K intervals. Summaries for each phase give the temperature-dependent functions for heat capacity, entropy, and relative enthalpy and the experimental data used in the final evaluation.

Key words: Enthalpy; enthalpy of formation; entropy; equilibrium constant for formation; Gibbs energy function; Gibbs energy of formation; heat capacity; lime-alumina-silica-water; minerals; thermodynamic data.

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## 1. Introduction

The experimental data on the selected phases (table 1) in the lime-alumina-silica-water system were evaluated using the method of Haas and Fisher (1976). The goal was to produce a set of thermodynamic properties for each phase at a standard state of 1 atm (101.325 kPa) that is consistent with thermodynamic theory, the observed properties of each phase, and the observed phase relations among the phases. The experimental data used in the study came from a literature search through June 1979.

TABLE I. Phases for which evaluated data are presented in this study

| Chemical formula  | State                   | Mineral name   |
|---|-------------------------|--|
| Al(OH)  | orthorhombic            | boehmite   |
| Al(OH)  | orthorhombic            | diaspore   |
| Al(OH) <sub>3</sub>   | monoclinic              | gibbsite   |
| Al <sub>2</sub> Si <sub>4</sub> O <sub>10</sub> (OH) <sub>2</sub>                 | monoclinic              | pyrophyllite   |
| Al <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (OH) <sub>4</sub>                  | monoclinic              | dickite  |
| Al <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (OH) <sub>4</sub>                  | monoclinic              | halloysite   |
| Al <sub>2</sub> Si <sub>2</sub> O <sub>5</sub> (OH) <sub>4</sub>                  | monoclinic              | kaolinite  |
| Al <sub>2</sub> SiO <sub>5</sub>  | orthorhombic            | andalusite   |
| Al <sub>2</sub> SiO <sub>5</sub>  | triclinic               | kyanite  |
| Al <sub>2</sub> SiO <sub>5</sub>  | orthorhombic            | sillimanite  |
| CaAl <sub>2</sub> SiO <sub>6</sub>  | monoclinic              | (Ca-Al clinopyroxene)                                    |
| CaAl <sub>2</sub> Si <sub>2</sub> O <sub>8</sub>                                  | triclinic               | anorthite  |
| Ca <sub>2</sub> Al <sub>2</sub> SiO <sub>7</sub>                                  | tetragonal              | gehlenite  |
| Ca <sub>3</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>12</sub>                   | cubic                   | grossular  |
| Ca <sub>2</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>10</sub> (OH) <sub>2</sub> | orthorhombic            | prehnite   |
| Ca <sub>2</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>12</sub> (OH)              | orthorhombic            | zoisite  |
| CaAl <sub>4</sub> Si <sub>2</sub> O <sub>10</sub> (OH) <sub>2</sub>               | monoclinic              | margarite  |
| CaSiO <sub>3</sub>  | triclinic               | cyclowollastonite<br>("pseudowollastonite")              |
| CaSiO <sub>3</sub>  | triclinic               | wollastonite   |
| Ca <sub>2</sub> SiO <sub>4</sub> , $\alpha$                                       | hexagonal, $\alpha$     |  |
| Ca <sub>2</sub> SiO <sub>4</sub> , $\alpha'$                                      | orthorhombic, $\alpha'$ |  |
| Ca <sub>2</sub> SiO <sub>4</sub> , $\beta$  | monoclinic, $\beta$     | larnite<br>(Ca olivine)                                  |
| Ca <sub>2</sub> SiO <sub>4</sub> , $\gamma$                                       | orthorhombic, $\gamma$  | (hatrurite and other<br>polymorphs,<br>undifferentiated) |
| Ca <sub>3</sub> SiO <sub>5</sub>  | crystal                 |  |
| Ca <sub>3</sub> Si <sub>2</sub> O <sub>7</sub>                                    | monoclinic              | rankinite  |

## 2. Nomenclature

The following symbols were used in the text, tables, and data summaries.

| Symbol  | Units                | Meaning  |
|---|----------------------|--|
| $C_p^{\circ}$   | J/(mol·K)            | standard molar heat capacity   |
| $E^{\circ}$   | volts                | standard electrochemical potential in volts  |
| $[G^{\circ}(T) - H^{\circ}(Tr)]/T$                                | J/(mol·K)            | Gibbs energy function  |
| $\Delta G_{f,c}^{\circ}$  | J/mol                | standard molar Gibbs energy of formation from the elements                               |
| $\Delta G_{f,ox}^{\circ}$   | J/mol                | standard molar Gibbs energy of formation from the oxides                                 |
| $H^{\circ}$   | J/mol                | standard molar enthalpy  |
| $H^{\circ}(T) - H^{\circ}(298)$ or $H^{\circ}(T) - H^{\circ}(Tr)$ | J/mol                | relative standard molar enthalpy, base is $H^{\circ}$ at ( $Tr = 298.15$ K), 101.325 kPa |
| $\Delta H_{f,c}^{\circ}$  | J/mol                | standard molar enthalpy of formation from the elements                                   |
| $\Delta H_{f,ox}^{\circ}$   | J/mol                | standard molar enthalpy of formation from the oxides                                     |
| $\Delta H_r^{\circ}$  | J                    | standard enthalpy of reaction  |
| $\log K_{f,c}^{\circ}$  |                      | $\log_{10}$ of the standard equilibrium constant for formation from the elements         |
| $\log K_{f,ox}^{\circ}$   |                      | $\log_{10}$ of the standard equilibrium constant for formation from the oxides           |
| $P$   | Pa                   | absolute pressure in pascals   |
| $S^{\circ}$   | J/(mol·K)            | standard molar entropy   |
| $T$   | K                    | absolute temperature in kelvins  |
| $Tr$  | K                    | reference temperature, absolute scale, equals 298.15 K                                   |
| $V^{\circ}$   | cm <sup>3</sup> /mol | standard molar volume  |

Fundamental constants used in this evaluation are given in table 2.

Where possible, the data have been corrected to the International Practical Temperature Scale of 1968 (Comité International des Poids et Mesures, 1969). For most phase equilibria, however, this was not possible because the necessary temperature calibration data were not supplied.

The "formula weights" have been calculated to be consistent with the 1975 relative atomic masses for the elements (Commission on Atomic Weights, 1976).

Table 3 gives the sources of data for the thermodynamic properties of the elements and oxides that were used as reference phases in the evaluation procedure. In addition, the Gibbs-energy change for H<sub>2</sub>O(gas) between 101.325 kPa and the experimental pressure in experiments on phase equilibria were obtained from Fisher and Zen (1971).

TABLE 2. Fundamental constants and defined constants

| Name  | Symbol | Value of units                              |
|---|--------|---|
| Fundamental constants                         |        |   |
| Avogadro constant                             | $N$    | $6.022094 \times 10^{23}$ mol <sup>-1</sup> |
| Faraday constant                              | $F$    | 96,487.0 J/(volts·mol)                      |
| Gas constant                                  | $R$    | 8.3143 J/(mol·K)                            |
| Absolute temperature of the "ice point," 0 °C |        | 273.15 K                                    |
| Defined units                                 |        |   |
| Standard atmosphere                           | atm    | 101.325 kPa                                 |
| Standard bar                                  | b      | 100.000 kPa                                 |
| Thermochemical calorie                        | cal    | 4.1840 J                                    |

TABLE 3. Reference phases used in the evaluation and the sources for the thermodynamic values on these phases

| Phase   | $C_p^{\circ}(T)$ | $S^{\circ}(298), H_r^{\circ}(298), G_r^{\circ}(298)$ |
|---|------------------|--|
| Al (crystal, liquid)                                      | a                | b  |
| Ca ( $\alpha$ - and $\beta$ -crystals, liquid, ideal gas) | a                | b  |
| H <sub>2</sub> (ideal gas)                                | a                | b  |
| O <sub>2</sub> (ideal gas)                                | a                | b  |
| Si (crystal, liquid)                                      | a                | b  |
| Al <sub>2</sub> O <sub>3</sub> (corundum)                 | c                | b  |
| CaO (lime)  | c                | b  |
| H <sub>2</sub> O (liquid, ideal gas)                      | c                | b,d  |
| SiO <sub>2</sub> ( $\alpha$ - and $\beta$ -quartz)        | c                | b  |

<sup>a</sup>Hultgren and others (1973).

<sup>b</sup>CODATA Task Group (1978).

<sup>c</sup>Stull and Prophet (1971) and Chase and others (1974, 1975).

<sup>d</sup>Fisher and Zen (1971).

### 3.1. Introduction

The details of the approach and the procedure are described by Haas and Fisher (1976) and by Haas (1974). The approach and procedure given there have been followed closely and will not be described here in detail. The following description summarizes the evaluation procedure:

#### 1. Literature search

a. Review of literature for data that define thermodynamic properties of a phase or a group of phases.

- b. Close scrutiny of each citation to determine:
  - (1) What was physically observed.
  - (2) With what precision was it observed.
- 2. Refinement cycle
  - a. Comparison of related data (heat capacity, relative enthalpy, enthalpies of formation, enthalpies of reaction, Gibbs energy of reaction, entropies) for phases in a chemical system using weighted, simultaneous, multiple, least-squares regression.
  - b. Review of the pertinent literature where data are found not to be in agreement.
  - c. Removal of assumed or apparently erroneous data from the set of data being fit by the regression.
  - d. Repeat of steps a through c until all discordant data have been identified and removed.
  - 3. Preparation of tables using the smoothing functions and the variance-covariance matrix from the last execution of step 2a.

The mathematical model used in the regression in step 2a is based on eq (1) for the heat capacity at constant pressure and the known relations among heat capacity, enthalpy, entropy, and Gibbs energy for the  $i$ th phase in a group of chemically related phases. The constants  $a_{2,i}$  and  $a_{4,i}$  were reserved for the constants of integration to describe the enthalpy and entropy of the  $i$ th phase, respectively. Equation (1) is a restatement of Haas and Fisher's equation (6):

$$C_{p,i}^{\circ} = \frac{a_{1,i}}{T^2} + \frac{a_{3,i}}{T^{1/2}} + a_{5,i} + 2a_{6,i}T + a_{7,i}T^2 \quad (1)$$

Equation (1) has no theoretical basis. Equation (1) is a smoothing function only and must be so considered. At the absolute zero of temperature the function is indeterminate. In our work, data at temperatures below 200 K were not considered. Above 200 K, the function readily describes most data. In order to avoid overfitting of the data, non-significant constants have been eliminated from the general equation wherever they were not needed to describe the properties of a phase. This is particularly common for the last term,  $a_{7,i}T^2$ , in eq (1). Removal of this term eliminated any rapid excursions of the calculated values in the temperature region around and above the highest experimental temperature. For some phases (examples in this study are grossular, dickite, halloysite, and kaolinite), the fitting produced functions that contain maxima in the tabulated heat capacities. Each case was examined to determine whether these maxima should be eliminated because they are not theoretically possible without some additional phenomenon. For the clays, the maxima occur at the highest tabulated heat capacities where the functions supply estimates only and no action was taken. Equation (1) has been fit within the temperature range presented for each phase in the appendix and should not be extended indiscriminately to higher or lower temperatures.

For grossular, the experimental heat capacities were measured at or below 978 K. The estimated values used in the fitting for the heat capacity above 1000 K joined smoothly with the experimental data below 1000 K and did not contain a maximum. Therefore, the maximum in the fitted function was a result of the constraints imposed on the thermal data by the phase equilibria that included observations

up to 1523 K. In this case, no action was taken. The presence of the maximum emphasizes the need for measured high-temperature heat capacities. Until this has been accomplished, the tabulations are considered the best available.

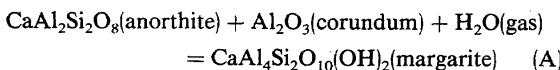
### 3.2. Data Entry

Haas (1974) described the mechanics used to fit the model to discrete experimental observations in detail. The typical problem includes the following information:

1. Title for problem.
2. Control codes to identify the options used.
3. Number and labels for the phases in the problem.
4. Sets of data being fit.
  - a. Name of the set and reference.
  - b. Control codes related to the observation and to data editing.
  - c. Label(s) for the phase(s), the stoichiometric coefficient(s) and any pertinent data on polymorphs.
  - d. Data as given in the reference.
    - (1) Temperature (and correction factor if needed to convert to kelvins).
    - (2) Observed value (and correction factor if needed to convert to joules, volts, moles, etc.).
    - (3) Precision.
    - (4) Second independent variable (if needed).
5. Constants of eq (1) above for each of the reference phases as well as the trial constants for the phases for which the properties are being refined.
6. Control parameters for the error plots.

The input format is designed to reduce manual conversions before entry into the computer for fitting.

The class of data that is not discussed by Haas consists of bracketed observations like those typical of phase equilibria studies. As an example, let us consider reaction A, below.



Chatterjee (1974) determined that the equilibrium at 100 MPa was located between 743.15 and 773.15 K. If we consider no additional information, there is an equal probability of equilibrium occurring at any temperature between these two bracketing temperatures at 100 MPa. Therefore, if we neglect the errors associated with the measurement of temperature and pressure, the probability curve is a square wave whose bounds are at 743.15 K and 773.15 K. To consider the reaction to occur at the midpoint of the bracket, 758.15 K, is unwarranted; this would cause the fitting algorithms to give too much weight to the midpoints of bracketed data. We evaluated the phase equilibrium data by calculating the Gibbs energy of reaction at 101.325 kPa for each two experimentally measured bracketing pressures and temperatures as if each bracketing pressure and temperature represented equilibrium. This procedure does not define a square probability curve between the bracketing values but does define a nearly uniform probability between the bracketing values and allows a sufficient probability of occurrence outside the bracketing values to compensate for errors in measurement of pressure and temperature. The Gibbs energy for the reac-

tion at 101.325 kPa for both bracketing temperatures (or bracketing pressures in some cases) is calculated using the following formula:

$$\Delta G^\circ(\text{reaction}) = \frac{1}{1000} \Delta V^\circ(\text{reaction, solids}) (101.325 - 10^5) + \frac{(-1)}{1000} \int_{10^5}^{101.325} V^\circ(\text{H}_2\text{O}) dP_T \quad (2)$$

where  $\Delta V^\circ$  (reaction, solids) is the volume change between the solid product, margarite, and the solid reactants, anorthite and corundum, expressed in  $\text{cm}^3/\text{mol}$ . The difference ( $101.325 - 10^5$ ) is the pressure difference in kPa. The factor 1000 is the conversion factor for  $\text{cm}^3/\text{mol}$  to  $\text{J}/(\text{kPa}\cdot\text{mol})$ . The integral represents the Gibbs energy difference of  $\text{H}_2\text{O}$  between  $10^5$  and 101.325 kPa. The term (-1) is the stoichiometric coefficient of  $\text{H}_2\text{O}(\text{gas})$  in reaction A. The Gibbs energy difference for  $\text{H}_2\text{O}$  at constant temperature was calculated from data in Fisher and Zen (1971). We expect to replace this method of estimation in the near future with one based on the  $P\text{-}V\text{-}T$  function proposed by Haar and others (in press). Equation 2 neglects the compressibility and thermal expansion of the solids. If thermal expansion and compressibility data are available for the solid phases, these corrections can be added.

### 3.3. Weighting of Experimental Data

Data were weighted by the reciprocal of the precision; the higher (smaller in magnitude) the precision, the higher (larger in magnitude) the weight. The use of weighting served two purposes. First, it allowed the simultaneous fitting of different properties that have large variations in magnitude. An example is the simultaneous fitting of enthalpy data that could exceed 7 MJ and electrochemical potentials that are more like 1.0 millivolt. Second, weighting constrained the solution towards the more precise observations. This was particularly desirable where precise data from low-temperature, adiabatic calorimetry were being matched with the less precise data from differential scanning calorimetry or from drop calorimetry.

In the first fitting of a data set from a particular reference, the author's stated precision was used. In subsequent cycles this would be modified if logic or other data showed the author's estimate to be unrealistically small.

Weighting of data within the above guideline was straightforward with two exceptions. The first exception is when the author makes many observations of a phenomenon but only reports an average value and the standard deviation. To enter one value, the average value, would underweight the work that went into the determination relative to the significance of discrete measurements on the same or other properties. We arbitrarily overcame this by making three entries: (1) the average value, (2) the average value less the deviation, and (3) the average value plus the deviation. All three entries had a weight equal to the stated standard deviation.

The second exception is related to the treatment of brackets in phase equilibria. As stated in the preceding section, the Gibbs energy at 101.325 kPa for both temperature limits (or pressure limits or their combination that defines the bracket) was entered. The weight was calculated from

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the arbitrary decision that the precision for each bracket was the difference in Gibbs energy for the bracket with the constraint that the magnitude of the assigned precision was equal to or greater than the precision associated with the determination of the temperature (or pressure) of the limit of the bracket. In this fashion, we reduced the tendency of the regression to settle on the midpoint of a bracket. We will return to this point again when we consider the topic of data rejection.

### 3.4. Data Rejection

Data were rejected during the literature search and during the refinement cycles. Data were rejected during the literature search if there was a clear error in the measurement technique or if there was ambiguity in the identification of the reactants or products.

During the refinement cycle, where all data for all phases in the chemical system are simultaneously fit by the model, the model returns the weighted average of all the data. Error plots such as figure 1 are part of the printed output. On the error plots for each source and type of data, the weighted difference, calculated as  $(\text{observed} - \text{calculated})/\text{precision}$ , is plotted as a function of temperature. These plots give a quick visual picture of the quality of the agreement between the function in the model, the other data in the refinement, and the specific data set. Ideally, the errors should be centered about the zero axis and should not exceed  $\pm 2$  units ( $\pm 2s$ ). Not attaining such an ideal plot can be the result of one or more of the following:

1. The function does not adequately describe the data.
2. Some set (or sets) of data is not consistent with the balance of the data considered.
3. The magnitude of the experimental precision is larger than that which the author stated. As a rule of thumb, if more than one third of the data plots outside the bounds of  $+1$  or  $-1$  (equal to  $\pm 1s$ ), this leads to overweighting of the data set. More realistic precisions were entered in this situation.

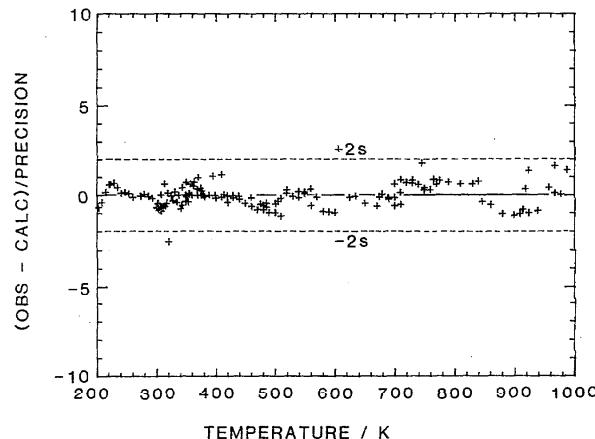
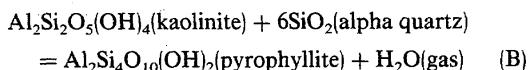


FIGURE 1. Parameter (observed value - calculated value)/precision as a function of temperature for the differential scanning calorimeter measurements of heat capacity for anorthite. Plus signs (+) indicate the data of Krupka and others (1979).

Error plots alert the evaluator to the existence of a conflict in the data sets. The evaluator must determine the source for the conflict and make the appropriate correction to the data. As an example, figure 2 is a combination of the error plots for reaction B. The relative errors for the silicic acid solubilities of Hemley and others (1980) and the reversed brackets of Thompson (1970) are shown. The data of Hemley and his coworkers plot systematically high for this reaction, but they are well within 1 sigma of the zero abscissa. The systematic discrepancy is caused by a minor misfit between these data and one or more of the enthalpies of solution and Gibbs energies of reaction in which either kaolinite or pyrophyllite is involved.



However, the reversed observations of Thompson (1970) lie well outside the 2 sigma limits. Figure 3 shows the calculated Gibbs energy for reaction B and the experimental data cited on figure 2. As expected, the data of Hemley and coworkers lie near the calculated values. Because the calculated line also reflects the other data in the problem, particularly entropies and other phase equilibria, we conclude that data of Hemley and coworkers are consistent. However, both the magnitude and the slope of the reversed brackets of Thompson are not in agreement with the other data. A review of the experimental method suggests that the error may be due to the finely ground kaolinite and pyrophyllite ("less than 300 mesh," p. 454) that was used in the study and to the relatively short duration of the experiments ("usually 28 days" at 100 MPa, "for 1 week" at 200 and 400 MPa, p. 455–456). These data were not included in the evaluation. The above conjecture on the part of the evaluators is not proven; only detailed discussions with the authors or repetition of the experiments could prove the data are in error.

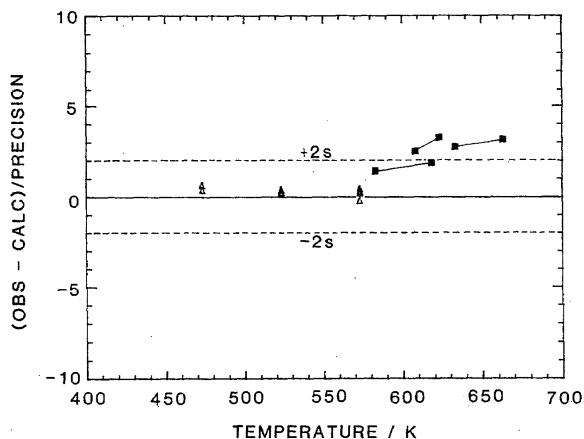


FIGURE 2. Parameter (observed value – calculated value)/precision as a function of temperature for the reaction: Kaolinite + 2 Quartz = Pyrophyllite + Steam. The open triangles were calculated from the silicic acid solubilities of Hemley and others (1980). The connected solid squares represent the brackets of Thompson (1970). The dashed lines represent two times the precision stated by the authors or two times the width of the Gibbs energy bracket, whichever is appropriate.

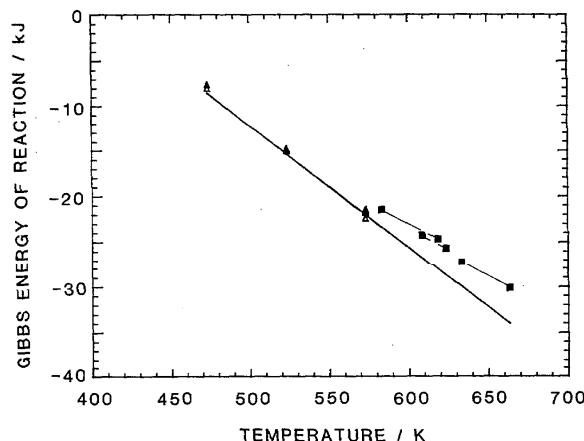


FIGURE 3. Gibbs energy of reaction as a function of absolute temperature for the reaction: Kaolinite + 2 Quartz = Pyrophyllite + Steam. The open triangles were calculated from the silicic acid solubilities of Hemley and others (1980). The connected solid squares represent the brackets of Thompson (1970). The solid line was calculated from the least-squares solution to the entire set of experimental observations.

Discordant data are readily identified. The cause of the disagreement is not always as straightforward as the identification. Fortunately, because sufficient related data were available for the phases in question, the right decision was made. In the discussions associated with the thermodynamic tables, all data used to produce the final results are given. Because of manpower and time, however, we have not included the much larger set of excluded data. The reference section contains all literature sources considered in the evaluation. References which contain indirect or supporting information on thermodynamic properties and references containing experimental data considered, but excluded from the evaluation, are marked with an asterisk (\*) at the beginning of the citation.

### 3.5. Preparation of Tables and Summaries

Tables of thermodynamic data at 101.325 kPa between 273.15 K and 1800 K were prepared from the functions in the fitted model. The commonly used thermodynamic functions given below were tabulated:

|                                      |  |
|--------------------------------------|--|
| $C_p^{\circ}$                        | heat capacity  |
| $S^{\circ}$                          | entropy  |
| $[G_T^{\circ} - H_{Tr}^{\circ}] / T$ | Gibb's function                                      |
| $H_T^{\circ} - H_{Tr}^{\circ}$       | relative enthalpy                                    |
| $\Delta H_{f,c}^{\circ}$             | enthalpy of formation from the elements              |
| $\Delta G_{f,c}^{\circ}$             | Gibbs energy of formation from the elements          |
| $\log K_{f,c}^{\circ}$               | equilibrium constant for formation from the elements |
| $\Delta H_{f,ox}^{\circ}$            | enthalpy of formation from the oxides                |
| $\Delta G_{f,ox}^{\circ}$            | Gibbs energy of formation from the oxides            |
| $\log K_{f,ox}^{\circ}$              | equilibrium constant for formation from the oxides   |

The summaries associated with each table contain functions for heat capacity, entropy, and relative enthalpy as obtained in fitting the model to the data. The summaries also cite those data used in the final evaluation that were directly pertinent to determine the properties of the phase in question. In the interest of saving manpower for more evaluations, data that were considered and rejected were not tabulated.

### 3.6. Confidence Limits

All evaluations must start with some base that is accepted without question. In this effort, the properties of the elements and the oxides cited in table 3 were used without question. The properties for the evaluated phases are determined relative to those reference values. In the course of the evaluation, we found no inconsistency of sufficient magnitude that would require us to consider reevaluating any of that reference base. This does not mean that the tabulated values are without error. For example, the uncertainty for the entropy at 298.15 K for Ca or CaO is about 1 percent (CODATA Task Group, 1978).

In preparing the tabulations, the 2-sigma confidence limits were given for the 298.15 K isotherm and for every isotherm that is a multiple of 250 K. These limits reflect only the variation in the final set of data on the chemical system. They do not include confidence limits on the reference data in table 3. For this reason the confidence limits for formation from the elements and the oxides is identical. If such a time arises when manpower is abundant or when other data centers adopt similar evaluation procedures, the imprecision in the reference base will be included in the tables.

## 4. Results

The appendix contains the thermodynamic properties and summaries for the phases listed in tables 1 and 3. The arrangement follows that of the JANAF Thermochemical Tables (Chase and others, 1974). The formula in the upper right of each table and summary is an alphabetical arrangement of atomic symbols. The more conventional formula is given elsewhere in the table or summary. In this set, aluminum (Al) compounds come first, followed by calcium, hydrogen, oxygen, and lastly silicon compounds. The index at the beginning of the appendix locates minerals within the alphabetized formulas.

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| Stull, D. R., and Prophet, H., 1971, JANAF thermochemical tables: U. S. National Bureau of Standards NSRDS-NBS 37.  | Boehmite, $\text{AlO(OH)}$  | $\text{AlHO}_2$  |
| Thompson, A. B., 1970, A note on the kaolinite-pyrophyllite equilibrium: American Journal of Science, <b>268</b> , 454-458.   | Ca-Al Clinopyroxene, $\text{CaAl}_2\text{SiO}_6$                        | $\text{Al}_2\text{CaO}_6\text{Si}$                         |
| Thompson, A. B., Perkins, Dexter, III, Sonderegger, U., and Newton, R. C., 1978, Heat capacities of synthetic $\text{CaAl}_2\text{SiO}_6\text{-CaMgSi}_2\text{O}_6\text{-Mg}_2\text{Si}_2\text{O}_8$ pyroxenes: EOS (American Geophysical Union Transactions), <b>59</b> , 395. | Corundum, $\text{Al}_2\text{O}_3$                                       | $\text{Al}_2\text{O}_3$                                    |
| Todd, S. S., 1950, Heat capacities at low temperatures and entropies at 298.16 °K of andalusite, kyanite, and sillimanite: American Chemical Society Journal, <b>72</b> , 4742-4743.  | Cyclowollastonite, $\text{CaSiO}_3$                                     | $\text{CaO}_3\text{Si}$                                    |
| Todd, S. S., 1951, Low-temperature heat capacities and entropies at 298.16 °K of crystalline calcium orthosilicate, zinc orthosilicate and tricalcium silicate: American Chemical Society Journal, <b>73</b> , 3277-3278.   | Diaspore, $\text{AlO(OH)}$  | $\text{AlHO}_2$  |
| *Topor, N. D., Kiseleva, I. A.; and Mel'chakova, L. V., 1972, Measurement of enthalpies of minerals by high temperature microcalorimetry: Geokhimiia, (3), 335-343.   | Dickite, $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$                | $\text{Al}_2\text{H}_4\text{O}_9\text{Si}_2$               |
| *Torgeson, D. R., and Sahama, Th. G., 1948, A hydrofluoric acid solution calorimeter and the determination of the heats of formation of $\text{Mg}_2\text{SiO}_4$ , $\text{MgSiO}_3$ , and $\text{CaSiO}_3$ : Journal of the American Chemical Society, <b>70</b> , 2156-2160.  | Gehlenite, $\text{Ca}_2\text{Al}_2\text{SiO}_7$                         | $\text{Al}_2\text{Ca}_2\text{O}_7\text{Si}$                |
| *Velde, Bruce, 1971, The stability and natural occurrence of margarite: Mineralogical Magazine, <b>38</b> , 317-323.  | Gibbsite, $\text{Al}(\text{OH})_3$                                      | $\text{AlH}_3\text{O}_3$                                   |
| Wagner, Hubert, 1932, Zur thermochemie der metasilikate des calciums und magnesiums und des diopside: Zeitschrift fur Anorganische und Allgemeine Chemie, <b>208</b> , 1-22.  | Grossular, $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$             | $\text{Al}_2\text{Ca}_3\text{O}_{12}\text{Si}_3$           |
| *Weill, D. F., 1966, Stability relations in the $\text{Al}_2\text{O}_3\text{-SiO}_2$ system calculated from solubilities in the $\text{Al}_2\text{O}_3\text{-SiO}_2\text{-Na}_3\text{AlF}_6$ system: Geochimica et Cosmochimica Acta, <b>30</b> , 223-237.                      | Hallyosite, $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$             | $\text{Al}_2\text{H}_4\text{O}_9\text{Si}_2$               |
| *Welch, J. H., and Gutt, W., 1959, Tricalcium silicate and its stability within the system $\text{CaO-SiO}_2$ : Journal of The American Ceramic Society, <b>42</b> , 11-15.   | Kaolinite, $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$              | $\text{Al}_2\text{H}_4\text{O}_9\text{Si}_2$               |
| Weller, W. W., and Kelley, K. K., 1963, Low-temperature heat capacities and entropies at 298.15 °K of akermanite, cordierite, gehlenite, and merwinite: U. S. Bureau of Mines, Report of Investigations 6343, 7 pp.   | Kyanite, $\text{Al}_2\text{SiO}_5$                                      | $\text{Al}_2\text{O}_5\text{Si}$                           |
| *West, E. D., and Ginnings, D. C., 1957, The heat capacity of aluminum oxide in the range 300 to 700 °K: Journal of Physical Chemistry, <b>61</b> , 1573-1574.  | Lime, $\text{CaO}$  | $\text{CaO}$   |
| Westrum, Edgar F., Jr., Essene, Eric J., and Perkins, Dexter, III, 1979, Thermophysical properties of the garnet, grossular: $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ : Journal of Chemical Thermodynamics, <b>11</b> , 57-66.  | Larnite, $\text{Ca}_2\text{SiO}_4$                                      | $\text{Ca}_2\text{O}_4\text{Si}$                           |
| White, W. P., 1919, Silicate specific heats. American Journal of Science, 2d series, <b>47</b> (277), 1-59.   | Margarite, $\text{CaAl}_4\text{Si}_2\text{O}_{10}(\text{OH})_2$         | $\text{Al}_4\text{CaH}_2\text{O}_{12}\text{Si}_2$          |
| *Windom, Kenneth Earl, 1976, The effect of reduced activity of anorthite on the reaction grossular + quartz = anorthite + wollastonite: a model for plagioclase in the earth's lower crust and upper mantle: Ph.D. Thesis, The Pennsylvania State University.                   | Ca Olivine, $\text{Ca}_2\text{SiO}_4$                                   | $\text{Ca}_2\text{O}_4\text{Si}$                           |
| *Windom, K. E., and Boettcher, A. L., 1976, The effect of reduced activity of anorthite on the reaction grossular + quartz = anorthite + wollastonite: a model for plagioclase in the earth's lower crust and upper mantle: American Mineralogist, <b>61</b> , 889-896.         | Prehnite, $\text{Ca}_2\text{Al}_2\text{Si}_3\text{O}_{10}(\text{OH})_2$ | $\text{Al}_2\text{Ca}_2\text{H}_2\text{O}_{12}\text{Si}_3$ |
| *Winkler, Helmut G. F., and Nitsch, K. H., 1962, Zoisitbildung bei der experimentellen metamorphose: Naturwissenschaften, <b>24</b> , 605.  | Quartz, $\text{SiO}_2$  | $\text{O}_2\text{Si}$                                      |
| Winter, John K., and Ghose, Subrata, 1979, Thermal expansion and high-temperature crystal chemistry of the $\text{Al}_2\text{SiO}_5$ polymorphs: American Mineralogist, <b>64</b> , 573-586.  | Rankinite, $\text{Ca}_3\text{Si}_2\text{O}_7$                           | $\text{Ca}_3\text{O}_7\text{Si}_2$                         |
| Yamaguchi, Goro, and Miyabe, Hisako, 1960, Precise determination of the $3\text{CaO-SiO}_2$ cells and interpretation of their x-ray diffraction patterns: American Ceramic Society Journal, <b>43</b> , 219-224.  | Sillimanite, $\text{Al}_2\text{SiO}_5$                                  | $\text{Al}_2\text{O}_5\text{Si}$                           |
|   | Wollastonite, $\text{CaSiO}_3$  | $\text{CaO}_3\text{Si}$                                    |
|   | Zoisite, $\text{Ca}_2\text{Al}_3\text{Si}_3\text{O}_{12}(\text{OH})$    | $\text{Al}_3\text{Ca}_2\text{HO}_{13}\text{Si}_3$          |

## 7.2. Index to Tables and Summaries

| Filing formula   | Table title  |
|--|--|
| Al   | Al (reference state)   |
| $\text{AlHO}_2$  | $\text{AlO(OH)}$ (reference state)                                       |
| $\text{AlHO}_2$  | $\text{AlO(OH)}$ , Boehmite  |
| $\text{AlHO}_2$  | $\text{AlO(OH)}$ , Diaspore  |
| $\text{AlH}_3\text{O}_3$                                   | $\text{Al}(\text{OH})_3$ , Gibbsite                                      |
| $\text{Al}_2\text{CaO}_6\text{Si}$                         | Ca $\text{Al}_2\text{SiO}_6$ , Clinopyroxene                             |
| $\text{Al}_2\text{CaO}_8\text{Si}_2$                       | $\text{CaAl}_2\text{Si}_2\text{O}_8$ , Anorthite                         |
| $\text{Al}_2\text{Ca}_2\text{H}_2\text{O}_{12}\text{Si}_3$ | $\text{Ca}_2\text{Al}_2\text{Si}_3\text{O}_{10}(\text{OH})_2$ , Prehnite |
| $\text{Al}_2\text{Ca}_2\text{O}_7\text{Si}$                | $\text{Ca}_2\text{Al}_2\text{SiO}_7$ , Gehlenite                         |
| $\text{Al}_2\text{Ca}_3\text{O}_{12}\text{Si}_3$           | $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ , Grossular             |
| $\text{Al}_2\text{H}_2\text{O}_{12}\text{Si}_4$            | $\text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2$ , Pyrophyllite        |
| $\text{Al}_2\text{H}_4\text{O}_9\text{Si}_2$               | $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ , Dickite                |
| $\text{Al}_2\text{H}_4\text{O}_9\text{Si}_2$               | $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ , Halloysite             |
| $\text{Al}_2\text{H}_4\text{O}_9\text{Si}_2$               | $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ , Kaolinite              |
| $\text{Al}_2\text{O}_3$                                    | $\text{Al}_2\text{O}_3$ , Corundum                                       |
| $\text{Al}_2\text{O}_5\text{Si}$                           | $\text{Al}_2\text{SiO}_5$ (reference state)                              |
| $\text{Al}_2\text{O}_5\text{Si}$                           | $\text{Al}_2\text{SiO}_5$ , Andalusite                                   |
| $\text{Al}_2\text{O}_5\text{Si}$                           | $\text{Al}_2\text{SiO}_5$ , Kyanite                                      |
| $\text{Al}_2\text{O}_5\text{Si}$                           | $\text{Al}_2\text{SiO}_5$ , Sillimanite                                  |
| $\text{Al}_3\text{Ca}_2\text{HO}_{13}\text{Si}_3$          | $\text{Ca}_2\text{Al}_3\text{Si}_3\text{O}_{12}(\text{OH})$ , Zoisite    |
| $\text{Al}_4\text{CaH}_2\text{O}_{12}\text{Si}_2$          | $\text{CaAl}_4\text{Si}_2\text{O}_{10}(\text{OH})_2$ , Margarite         |
| Ca   | Ca (reference state)   |
| CaO  | CaO, Lime  |
| $\text{CaO}_3\text{Si}$                                    | $\text{CaSiO}_3$ (reference state)                                       |
| $\text{CaO}_3\text{Si}$                                    | $\text{CaSiO}_3$ , Cyclowollastonite                                     |
| $\text{CaO}_3\text{Si}$                                    | ( = "Pseudowollastonite")  |
| $\text{Ca}_2\text{SiO}_4$                                  | $\text{CaSiO}_3$ , Wollastonite  |
| $\text{Ca}_2\text{SiO}_4$                                  | $\text{Ca}_2\text{SiO}_4$ (reference table, Ca Olivine base)             |

## 7. Appendix, Thermodynamic Tables, and Summaries

### 7.1. Mineral Index to Tables and Summaries

| Mineral name and formula                        | Filing formula                       |
|---|--------------------------------------|
| Andalusite, $\text{Al}_2\text{SiO}_5$           | $\text{Al}_2\text{O}_5\text{Si}$     |
| Anorthite, $\text{CaAl}_2\text{Si}_2\text{O}_8$ | $\text{Al}_2\text{CaO}_8\text{Si}_2$ |

|                                  |   |                                    |  |
|----------------------------------|---|------------------------------------|--|
| $\text{Ca}_2\text{O}_4\text{Si}$ | $\text{Ca}_2\text{SiO}_4$ (reference table,<br>Larnite base)  | $\text{Ca}_3\text{O}_7\text{Si}_2$ | $\text{Ca}_3\text{Si}_2\text{O}_7$ , Rankinite |
| $\text{Ca}_2\text{O}_4\text{Si}$ | $\text{Ca}_2\text{SiO}_4$ , ( $\alpha'$ crystal)              | $\text{H}_2$                       | $\text{H}_2$ (ideal gas)                       |
| $\text{Ca}_2\text{O}_4\text{Si}$ | $\text{Ca}_2\text{SiO}_4$ , Ca Olivine<br>( $\gamma$ crystal) | $\text{H}_2\text{O}$               | $\text{H}_2\text{O}$ (reference table)         |
| $\text{Ca}_2\text{O}_4\text{Si}$ | $\text{Ca}_2\text{SiO}_4$ , Larnite<br>( $\beta$ crystal)     | $\text{H}_2\text{O}$               | $\text{H}_2\text{O}$ (ideal gas)               |
| $\text{Ca}_3\text{O}_5\text{Si}$ | $\text{Ca}_3\text{SiO}_5$ (crystal)                           | $\text{O}_2$                       | $\text{O}_2$ (ideal gas)                       |
|                                  |   | $\text{O}_2\text{Si}$              | $\text{SiO}_2$ , Quartz (reference<br>table)   |
|                                  |   | Si                                 | Si (reference table)                           |

## 7.3. Tables and Summaries

Al

Issued September, 1979  
Reference state: crystals (face centered cubic) 273.15 K to 933 K  
liquid 933 K to 1800 K

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_T^o - H_{Tr}^o)/T$<br>J/mol | Formation from the Oxides   |                                   |                                   |
|--------------------|----------------------|--------------------|---------------------------------|-----------------------------|-----------------------------------|-----------------------------------|
|                    |                      |                    |                                 | $H_T^o - H_{Tr}^o$<br>J/mol | $\Delta G_f^o, \epsilon$<br>J/mol | $\Delta H_f^o, \epsilon$<br>J/mol |
| 273.15             | 23.844               | 26.241             | -28.445                         | -602.                       | 0.                                | 0.                                |
| 298.15             | 24.307               | 28.350             | -28.350                         | 0.                          | 0.                                | 0.                                |
| 300.               | 24.338               | 28.500             | -28.351                         | 45.                         | 0.                                | 0.                                |
| 350.               | 25.049               | 32.308             | -28.650                         | 1281.                       | 0.                                | 0.                                |
| 400.               | 25.625               | 35.691             | -29.322                         | 2548.                       | 0.                                | 0.                                |
| 450.               | 26.157               | 38.741             | -30.202                         | 3842.                       | 0.                                | 0.                                |
| 500.               | 26.692               | 41.524             | -31.197                         | 5163.                       | 0.                                | 0.                                |
| 550.               | 27.255               | 44.094             | -32.254                         | 6512.                       | 0.                                | 0.                                |
| 600.               | 27.863               | 46.491             | -33.342                         | 7890.                       | 0.                                | 0.                                |
| 650.               | 28.525               | 48.747             | -34.441                         | 9299.                       | 0.                                | 0.                                |
| 700.               | 29.249               | 50.887             | -35.440                         | 10743.                      | 0.                                | 0.                                |
| 750.               | 30.039               | 52.932             | -36.632                         | 12225.                      | 0.                                | 0.                                |
| 800.               | 30.898               | 54.898             | -37.712                         | 13748.                      | 0.                                | 0.                                |
| 850.               | 31.828               | 56.798             | -38.779                         | 15316.                      | 0.                                | 0.                                |
| 900.               | 32.831               | 58.645             | -39.832                         | 16932.                      | 0.                                | 0.                                |
| 933.               | 33.533               | 59.840             | -40.518                         | 18027.                      | 0.                                | 0.                                |
| 950.               | 31.756               | 71.405             | -40.518                         | 28817.                      | 0.                                | 0.                                |
| 1000.              | 31.756               | 71.978             | -41.076                         | 29357.                      | 0.                                | 0.                                |
| 1050.              | 31.756               | 75.157             | -44.173                         | 32532.                      | 0.                                | 0.                                |
| 1100.              | 31.756               | 76.634             | -45.615                         | 34120.                      | 0.                                | 0.                                |
| 1150.              | 31.756               | 78.045             | -46.395                         | 35708.                      | 0.                                | 0.                                |
| 1200.              | 31.756               | 79.397             | -48.317                         | 37296.                      | 0.                                | 0.                                |
| 1250.              | 31.756               | 80.693             | -49.586                         | 38884.                      | 0.                                | 0.                                |
| 1300.              | 31.756               | 81.939             | -50.807                         | 40472.                      | 0.                                | 0.                                |
| 1350.              | 31.756               | 83.137             | -51.982                         | 42059.                      | 0.                                | 0.                                |
| 1400.              | 31.756               | 84.292             | -53.116                         | 43647.                      | 0.                                | 0.                                |
| 1450.              | 31.756               | 85.407             | -54.210                         | 45235.                      | 0.                                | 0.                                |
| 1500.              | 31.756               | 86.483             | -55.268                         | 46823.                      | 0.                                | 0.                                |
| 1550.              | 31.756               | 87.525             | -56.292                         | 48411.                      | 0.                                | 0.                                |
| 1600.              | 31.756               | 88.533             | -57.284                         | 49999.                      | 0.                                | 0.                                |
| 1650.              | 31.756               | 89.510             | -58.246                         | 51586.                      | 0.                                | 0.                                |
| 1700.              | 31.756               | 90.458             | -59.179                         | 53174.                      | 0.                                | 0.                                |
| 1750.              | 31.756               | 91.319             | -60.086                         | 54762.                      | 0.                                | 0.                                |
| 1800.              | 31.756               | 92.273             | -60.968                         | 56350.                      | 0.                                | 0.                                |

Al

Al (reference state)      Aluminum, crystal; Aluminum, liquid      Formula weight = 26.982 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ ) (aluminum, crystal)

$$S^\circ = 28.350 \text{ J}/(\text{mol}\cdot\text{K}) \quad \Delta H_f^\circ = 0.0 \text{ kJ/mol}$$

$$V^\circ = 9.999 \pm 0.001 \text{ cm}^3/\text{mol} \quad \Delta G_f^\circ = 0.0 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

Aluminum, crystal (temperature range 200 to 933 K)

$$a_1 = -2.05250 \times 10^5 \quad a_4 = -1.28573 \times 10^2 \quad a_6 = -4.07067 \times 10^{-3}$$

$$a_2 = -8.70784 \times 10^3 \quad a_5 = 2.76424 \times 10^1 \quad a_7 = 1.57641 \times 10^{-5}$$

$$a_3 = 0.0$$

Aluminum, liquid (temperature range 933 to 1800 K)

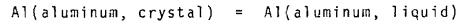
$$a_1 = 0.0 \quad a_4 = -1.45759 \times 10^2 \quad a_6 = 0.0$$

$$a_2 = -9.468 \times 10^3 \quad a_5 = 3.17565 \times 10^1 \quad a_7 = 0.0$$

$$a_3 = 0.0$$

Critical Reaction

Melting:



$$T_m = 933 \text{ K (observed)} \quad \Delta S_m^\circ = 11.565 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_m^\circ = 10.790 \text{ kJ/mol}$$

Sources for Thermodynamic Properties

The thermodynamic properties for aluminum were taken from the following sources:

| Property            | Source                     |
|---------------------|----------------------------|
| Heat capacity       | Hultgren and others (1973) |
| Entropy             | CODATA Task Group (1978)   |
| Enthalpy of melting | Hultgren and others (1973) |

$\text{Al}_2\text{H}_2\text{O}$ Issued September, 1979  
Reference state: Diaspore 273.15 K to 571.86 K  
Boehmite 571.86 K to 750 K

| Temperature<br>(K)  | $C_p^o$<br>$J/(mol \cdot K)$ | $S^o$<br>$J/(mol \cdot K)$ | $(G_f^o - H_f^o) / T$<br>$J/(mol)$ | Formation from the Elements  |                              |                        | Formation from the Oxides     |                               |                        |
|---------------------|------------------------------|----------------------------|------------------------------------|------------------------------|------------------------------|------------------------|-------------------------------|-------------------------------|------------------------|
|                     |                              |                            |                                    | $\Delta H_f^o, e$<br>$J/mol$ | $\Delta G_f^o, e$<br>$J/mol$ | $\log k_f^o, e$        | $\Delta H_f^o, ox$<br>$J/mol$ | $\Delta G_f^o, ox$<br>$J/mol$ | $\log K_f^o, ox$       |
| 273.15              | 49.137                       | 30.861                     | -35.543                            | -1279.                       | -999042.                     | -927511.               | 177.368                       | -18073.                       | -11819.                |
| 298.15<br>(2 sigma) | 53.098<br>$\pm 0.094$        | 35.339<br>$\pm 0.092$      | -35.339<br>$\pm 0.$                | 0.                           | -999456.<br>$\pm 366.$       | -920945.<br>$\pm 362.$ | 161.346<br>$\pm 0.063$        | -18697.<br>$\pm 366.$         | -11219.<br>$\pm 362.$  |
| 300.                | 53.374                       | 35.668                     | -35.340                            | 98.                          | -999484.                     | -920457.               | 160.266                       | -18741.<br>$\pm 19891.$       | -11172.<br>$\pm 9819.$ |
| 350.                | 60.067                       | 44.416                     | -36.015                            | 2940.                        | -100083.                     | -907235.               | 135.397                       | -19891.<br>$\pm 40815.$       | 1.465<br>$\pm 895.$    |
| 400.                | 65.574                       | 52.808                     | -37.594                            | 6085.                        | -1000438.                    | -893944.               | 116.137                       | -6856.<br>$\pm 40739.$        | 0.304<br>$\pm 0.000$   |
| 450.                | 70.202                       | 60.806                     | -39.332                            | 9483.                        | -1000594.                    | -880621.               | 102.220                       | -2615.<br>$\pm 40652.$        | 0.<br>$\pm 0.000$      |
| 487.90              | 72.717                       | 65.552                     | -41.440                            | 11692.                       | -1000607.                    | -872382.               | 94.157                        | -40585.<br>$\pm 371.$         | -0.169<br>$\pm 0.038$  |
| 500.<br>(2 sigma)   | 74.159<br>$\pm 0.369$        | 68.412<br>$\pm 0.130$      | -42.223<br>$\pm 0.093$             | 13095.<br>$\pm 39.$          | -1000587.<br>$\pm 371.$      | -867230.<br>$\pm 361.$ | 90.605<br>$\pm 0.038$         | -40360.<br>$\pm 689.$         | 1613.<br>$\pm 361.$    |
| 550.                | 77.591                       | 75.645                     | -44.935                            | 16890.                       | -1000447.                    | -853966.               | 81.03                         | -40360.<br>$\pm 689.$         | 5823.<br>$\pm 689.$    |
| 571.86              | 78.955                       | 78.696                     | -46.168                            | 18601.                       | -1000349.                    | -848146.               | 77.471                        | -40241.<br>$\pm 689.$         | 7656.<br>$\pm 689.$    |
| 571.86<br>600.      | 100.858<br>103.213           | 102.904<br>107.805         | -46.167<br>-48.944                 | 32446.<br>35317.             | -986505.<br>-985726.         | -848146.<br>-841346.   | 77.471<br>73.246              | -26397.<br>-25601.            | -0.699<br>-0.811       |
| 650.                | 107.047                      | 116.221                    | -53.797                            | 40575.                       | -984227.                     | -829385.               | 66.650                        | -24096.<br>-22484.            | -0.977<br>-1.111       |
| 700.                | 110.493                      | 124.282                    | -58.946                            | 46015.                       | -982603.                     | -817534.               | 61.005                        | -20774.<br>-17902.            | -1.219<br>-1.219       |
| 750.                | 113.611                      | 132.014                    | -63.188                            | 51619.                       | -90872.                      | -805803.               | 56.121                        | -20774.<br>-17902.            | -0.048<br>$\pm 689.$   |
|                     |                              |                            | $\pm 0.989$                        | $\pm 0.886$                  | $\pm 886.$                   | $\pm 689.$             | $\pm 0.048$                   |                               | $\pm 0.048$            |

$\text{AlHO}_2$  $\text{AlO(OH)}$  (reference state)

Diaspore, Boehmite

Formula weight = 59.988 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ ) (diaspore)

$S^\circ = 35.339 \pm 0.092 \text{ J/(mol}\cdot\text{K)}$

$\Delta H_f^\circ = -999.456 \pm 0.366 \text{ kJ/mol}$

$V^\circ = 17.760 \pm 0.052 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -920.945 \pm 0.362 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa

$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6T + a_7T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6T + a_7T^2/2$

$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3T^{0.5} + a_5T + a_6T^2 + a_7T^3/3$

Diaspore (temperature range 200 to 571.86 K)

$a_1 = 2.43069 \times 10^5$

$a_4 = -1.021486 \times 10^3$

$a_6 = 0.0$

$a_2 = 1.04719 \times 10^5$

$a_5 = 1.505560 \times 10^2$

$a_7 = 0.0$

$a_3 = -1.73002 \times 10^3$

Boehmite (temperature range 571.86 to 750 K)

$a_1 = 7.77111 \times 10^5$

$a_4 = -1.42636 \times 10^3$

$a_6 = 0.0$

$a_2 = 3.04561 \times 10^4$

$a_5 = 2.06903 \times 10^2$

$a_7 = 0.0$

$a_3 = -2.59274 \times 10^3$

Critical Reactions

## Inversion:

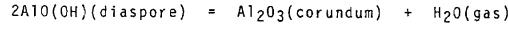


$T_i = 571.86 \text{ K (calculated)}$

$\Delta S_i^\circ = 24.208 \pm 1.8 \text{ J/(mol}\cdot\text{K)}$

$\Delta H_i^\circ = 13.844 \pm 0.7 \text{ kJ/mol}$

## Decomposition:



$T_d = 480.90 \text{ K (calculated)}$

$\Delta S_d^\circ = 169.066 \pm 1.54 \text{ J/(mol}\cdot\text{K)}$

$\Delta H_d^\circ = 81.304 \pm 0.74 \text{ kJ/mol}$

For detailed information on  $\text{AlO(OH)}$ , refer to the appropriate tables on the individual phases.

| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_{T^o}^o - H_{T^o}^o)/T$<br>J/mol | Formation from the Elements  |                              | Formation from the Oxides |                                      |        |
|---------------------|----------------------|--------------------|--------------------------------------|------------------------------|------------------------------|---------------------------|--------------------------------------|--------|
|                     |                      |                    |                                      | $\Delta H_{f, e}^o$<br>J/mol | $\Delta G_{f, e}^o$<br>J/mol | $\log K_f^o, \epsilon$    | $\Delta H_f^o, \epsilon$<br>J/mol    |        |
| 273.15              | 60.442               | 42.920             | -48.687                              | -1575.                       | -990306.                     | 176.328                   | -9337.                               |        |
| 298.15<br>(2 sigma) | 65.489<br>±0.218     | 48.435<br>±0.513   | -48.435<br>0.<br>±0.                 | -90424.<br>±725.             | -915817.<br>±882.            | 160.447<br>+0.119         | -9664.<br>±725.<br>-6337.            |        |
| 300.                | 65.846               | 48.841             | -48.436                              | 121.                         | -90428.                      | 159.377                   | -9686.<br>-10158.<br>-5456.<br>1.057 |        |
| 350.                | 74.659               | 59.672             | -49.271                              | 3640.                        | -90351.                      | 134.742                   | -102842.                             | 0.810  |
| 400.                | 82.123               | 70.142             | -51.230                              | 7565.                        | -99927.                      | 116.270                   | -890366.                             | 0.428  |
| 449.32              | 88.437               | 80.059             | -53.054                              | 11775.                       | -999222.                     | 102.085                   | -878130.                             | 0.000  |
| 450.                | 88.518               | 80.193             | -53.894                              | 11835.                       | -999210.                     | 101.911                   | -293565.                             | 0.005  |
| 500.                | 94.161               | 89.813             | -57.008                              | 16403.                       | -988247.                     | 90.434                    | -28244.                              | -0.340 |
| (2 sigma)           | ±1.005               | ±0.581             | ±0.515                               | ±114.                        | ±735.                        | ±670.                     | ±739.                                | ±610.  |
| 550.                | 98.917               | 99.011             | -60.412                              | 21230.                       | -987075.                     | 81.053                    | -26988.                              | 3253.  |
| 600.                | 103.213              | 107.805            | -63.397                              | 26285.                       | -957226.                     | 73.246                    | -25601.                              | -0.602 |
| 650.                | 107.047              | 116.221            | -67.693                              | 31543.                       | -94227.                      | 66.650                    | -24096.                              | -0.811 |
| 700.                | 110.493              | 124.282            | -71.449                              | 36983.                       | -922603.                     | 61.005                    | -22484.                              | -0.977 |
| 750.                | 113.611              | 132.014            | -75.31                               | 42587.                       | -817534.                     | 56.121                    | -20774.                              | -1.111 |
| (2 sigma)           | ±1.890               | ±0.989             | ±0.555                               | ±478.                        | ±886.                        | ±689.                     | ±886.                                | ±689.  |



AlO(OH)

Boehmite

Formula weight = 59.988 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 48.440 \pm 0.510 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -990.42 \pm 0.73 \text{ kJ/mol}$$

$$V^\circ = 19.535 \pm 0.052 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -915.82 \pm 0.68 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 7.77111 \times 10^5$$

$$a_4 = -1.42636 \times 10^3$$

$$a_6 = 0.0$$

$$a_2 = 3.04561 \times 10^4$$

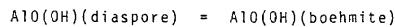
$$a_5 = 2.06903 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -2.59274 \times 10^3$$

Critical Reactions

## Inversion:

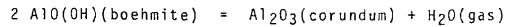


$$T_i = 571.86 \text{ K (calculated)}$$

$$\Delta S_i^\circ = 24.208 \pm 1.800 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 13.844 \pm 0.700 \text{ kJ/mol}$$

## Decomposition:



$$T_d = 449.32 \text{ K (calculated)}$$

$$\Delta S_d^\circ = 130.726 \pm 3.260 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_d^\circ = 58.738 \pm 1.464 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of boehmite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                        | Data Type     | Method                         | No. of Points | Range       |
|-------------------------------|---------------|--------------------------------|---------------|-------------|
| Shomate and Cook (1946)       | heat capacity | isothermal calorimetry         | 10            | 200 - 296 K |
| Estimated values <sup>a</sup> | heat capacity | corresponding states technique | 7             | 298 - 600 K |
| Shomate and Cook (1946)       | entropy       | isothermal calorimetry         | 1             | 298.15 K    |

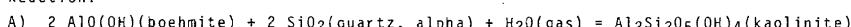
a The heat capacity was estimated by a corresponding states method (Lyon and Giaquie, 1949) from the heat-capacity data for diasporite from Perkins and others (1979) and the low-temperature heat capacity for boehmite from Shomate and Cook (1946).

The standard error of estimate to the heat capacity of Shomate and Cook (1946) is 0.2 J/(mol·K). The estimated heat-capacity values are a smooth extension of the data of Shomate and Cook. The standard error of estimate of the estimated heat capacity is 0.15 J/(mol·K). The fitted entropy at 298.15 K is  $48.44 \pm 0.51 \text{ J}/(\text{mol}\cdot\text{K})$  or a departure of 0.01 from the experimental value of  $48.45 \pm 0.21$  determined by Shomate and Cook.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                    | Method  | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta G_f^\circ(298.15 \text{ K})$ |
|---|---|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Hemley and others (in press) <sup>b</sup> | H <sub>4</sub> SiO <sub>4</sub> concentration | A                     | 473-573   | 9             | -75.671 ± 1.059                      | -990.451                             |

## a Reaction:



b Hemley and others (in press) measured the silicic-acid content of water that was equilibrated with boehmite and kaolinite between 473 K and 573 K at 100 MPa. Using their data for the solubility of quartz at the same conditions, the molar volumes of the solid phases, and heat data for H<sub>2</sub>O(gas) of Fisher and Zen (1971), we calculated the free energy of reaction at 101.325 kPa and temperature for each of nine observations.

The phase-equilibrium study of Hemley and others (in press) was evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated and is shown in column 6 of Table 2. From this enthalpy of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for boehmite (column 7 of Table 2) was calculated and can be compared with the enthalpy of formation of  $-990.424 \pm 0.725 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of boehmite and presents the data in their poorest perspective.

The molar volume of boehmite was obtained from the compilation of Robie and others (1967).

Al<sub>10</sub>O<sub>2</sub>

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| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_T^o - H_{Tr}^o)/T$<br>J/(mol·K) | Formation from the Elements |                            |                   | Formation from the Oxides   |                  |                 |
|---------------------|----------------------|--------------------|-------------------------------------|-----------------------------|----------------------------|-------------------|-----------------------------|------------------|-----------------|
|                     |                      |                    |                                     | $H_{Tr}^o$<br>J/mol         | $\Delta H_f^o, e$<br>J/mol | $\log K_f^o, e$   | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, ox$ |                 |
| 273.15              | 49.137               | 30.861             | -35.543                             | -1279.                      | -999042.                   | -927511.          | -18073.                     | -11819.          | 2.260           |
| 298.15<br>(2 sigma) | 53.098<br>±0.094     | 35.339<br>±0.092   | -35.339<br>±0.                      | 0.<br>±0.                   | -99456.<br>±366.           | -920945.<br>±362. | -18697.<br>±366.            | -11219.<br>±362. | 1.966<br>±0.063 |
| 300.                | 53.374               | 35.668             | -35.340                             | 98.                         | -999484.                   | -920457.          | -160.266                    | -11172.          | 1.945           |
| 350.                | 60.067               | 44.416             | -36.015                             | 2940.                       | -1000083.                  | -907235.          | -135.397                    | -9819.           | 1.465           |
| 400.                | 65.574               | 52.808             | -37.594                             | 6085.                       | -1000438.                  | -893944.          | -116.137                    | -40815.          | 0.895           |
| 450.                | 70.202               | 60.806             | -39.732                             | 9483.                       | -1000594.                  | -880621.          | -102.220                    | -40739.          | 0.304           |
| 480.-90             | 72.717               | 65.552             | -41.240                             | 11692.                      | -1000607.                  | -872382.          | -94.757                     | -40652.          | 0.000           |
| 500.                | 74.159               | 68.412             | -42.223                             | 13095.                      | -1000587.                  | -87290.           | -90.605                     | -40585.          | -0.169          |
| (2 sigma)           | ±0.369               | ±0.130             | ±0.093                              | ±39.                        | ±371.                      | ±361.             | ±0.038                      | ±361.            | ±0.038          |
| 550.                | 77.591               | 75.645             | -44.935                             | 16390.                      | -1000447.                  | -853966.          | -81.103                     | -4036C.          | 5823.           |
| 600.                | 80.603               | 82.528             | -47.784                             | 20847.                      | -1000197.                  | -840660.          | -73.186                     | -40072.          | 10009.          |
| 650.                | 83.274               | 89.087             | -50.711                             | 24945.                      | -999858.                   | -87378.           | 66.489                      | -39727.          | 14148.          |
| 700.                | 83.663               | 95.348             | -53.677                             | 29165.                      | -994449.                   | -84126.           | 60.751                      | -39330.          | -1.1366         |
| 750.                | 87.817               | 101.333            | -56.656                             | 33501.                      | -99894.                    | -80904.           | 55.780                      | -38886C.         | 22401.          |
| (2 sigma)           | ±0.751               | ±0.323             | ±0.118                              | ±178.                       | ±420.                      | ±360.             | ±0.025                      | ±420.            | ±360.           |

$\text{Al}_2\text{O}_3$  $\text{Al}_2\text{O}_3(\text{OH})$ 

Diaspore

Formula weight = 59.988 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$S^\circ = 35.339 \pm 0.092 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_f^\circ = -999.456 \pm 0.366 \text{ kJ/mol}$

$V^\circ = 17.760 \pm 0.052 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -920.945 \pm 0.362 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 800 K)

$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$

$[\text{H}^\circ(T) - \text{H}^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

$a_1 = 2.43069 \times 10^5$

$a_4 = -1.021486 \times 10^3$

$a_6 = 0.0$

$a_2 = 1.04719 \times 10^5$

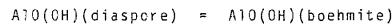
$a_5 = 1.50556 \times 10^2$

$a_7 = 0.0$

$a_3 = -1.73002 \times 10^3$

Critical Reactions

## Inversion:

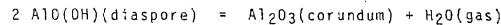


$T_i = 571.86 \text{ K (calculated)}$

$\Delta S_i^\circ = 24.208 \pm 1.8 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_i^\circ = 13.844 \pm 0.7 \text{ kJ/mol}$

## Decomposition:



$T_d = 480.90 \text{ K (calculated)}$

$\Delta S_d^\circ = 169.060 \pm 1.54 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_d^\circ = 81.304 \pm 0.74 \text{ kJ/mol}$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of diaspore.

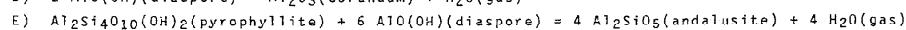
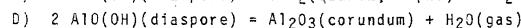
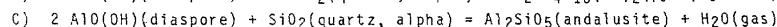
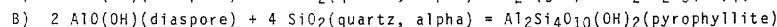
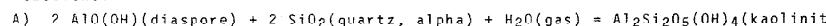
Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                    | Data Type     | Method                            | No. of Points | Range       |
|---------------------------|---------------|-----------------------------------|---------------|-------------|
| King and Weller (1961)    | heat capacity | isothermal calorimetry            | 10            | 206 - 296 K |
| Perkins and others (1979) | heat capacity | adiabatic calorimetry             | 15            | 203 - 345 K |
| Perkins and others (1979) | heat capacity | differential scanning calorimeter | 19            | 340 - 509 K |
| Perkins and others (1979) | entropy       | adiabatic calorimetry             | 1             | 298.15 K    |

The heat capacity measured by King and Weller (1961) was fit with a standard error of estimate of 0.25 J/(mol·K). The heat capacity of Perkins and others (1979) measured on an adiabatic calorimeter and differential scanning calorimeter were fit with a standard error of estimate of 0.26 and 0.78 J/(mol·K), respectively. The fitted entropy at 298.15 K is  $35.339 \pm 0.092 \text{ J}/(\text{mol}\cdot\text{K})$  or a departure of  $\pm 0.01$  from the experimental value of  $35.338 \pm 0.0377$  of Perkins and others.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                    | Method                                 | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta G_f^\circ(298.15 \text{ K})$ | kJ/mol |
|---|--|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|--------|
| Hemley and others (in press) <sup>b</sup> | $\text{H}_4\text{SiO}_4$ concentration | A                     | 473-573   | 6             | -57.885 $\pm$ 0.441                  | -999.421                             |        |
| Hemley and others (in press) <sup>b</sup> | $\text{H}_4\text{SiO}_4$ concentration | B                     | 523-598   | 4             | -1.678 $\pm$ 1.770                   | -999.837                             |        |
| Hemley and others (in press) <sup>b</sup> | $\text{H}_4\text{SiO}_4$ concentration | C                     | 623-663   | 2             | 78.164 $\pm$ 0.200                   | -999.855                             |        |
| Haas (1972)                               | gas-medium pressure apparatus          | D                     | 662-741   | 5 pair        | 81.322 $\pm$ 0.875                   | -999.465                             |        |
| Haas and Holdaway (1973)                  | gas-medium pressure apparatus          | E                     | 618-722   | 4             | 311.486 $\pm$ 3.224                  | -999.646                             |        |

<sup>a</sup> Reactions:

$\text{AlH}_3\text{O}_2$ 

b Henley and others (in press) measured the silicic-acid content of water equilibrated with the mineral pairs A) diaspore-kaolinite, B) diaspore-andalusite at 100 and 200 MPa between 450 K and 700 K. Using their data for the solubility of quartz at the same conditions, the molar volumes of the solid phases, and the free-energy data for  $\text{H}_2(\text{gas})$  of Fisher and Zen (1971), the free energy of reactions A, B, and C was calculated for each observation.

The phase-equilibrium studies of Haas (1972) and Haas and Holdaway (1973) were evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for  $\text{H}_2(\text{gas})$  from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 7 of Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 111.325 kPa was calculated for each source. These are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for diaspore (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-959.46 \pm 0.366 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of diaspore and presents the data in their poorest perspective. The phase-equilibria data cited above bracket the regression fit in free energy space.

The molar volume of diaspore was obtained from the compilation of Robie and others (1967).

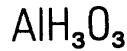
 $\text{Al}(\text{OH})_3$ 

Gibbsite (monoclinic, trimorphous with Bayerite and Nodstrandite)

 $\text{AlH}_3\text{O}_3$ 

Issued September, 1979

| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K)  | $S^o$<br>J/(mol·K)    | $(G_f^o - H_f^o)/T$<br>J/mol | Formation from the Elements  |                            |                          | Formation from the Oxides   |                             |                           |
|---------------------|-----------------------|-----------------------|------------------------------|------------------------------|----------------------------|--------------------------|-----------------------------|-----------------------------|---------------------------|
|                     |                       |                       |                              | $H_f^o - H_{f,r}^o$<br>J/mol | $\Delta H_f^o, e$<br>J/mol | $\log K_f^o, e$<br>J/mol | $\Delta H_f^o, ox$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, ox$<br>J/mol |
| 273.15              | 84.735                | 60.714                | -68.793                      | -2207.                       | -1292765.                  | -1166756.                | 223.119                     | -25183.                     | -9791.                    |
| 298.15<br>(2 s gma) | 91.729<br>$\pm 0.158$ | 68.440<br>$\pm 0.344$ | -68.440<br>$\pm 0.344$       | 0.<br>$\pm 0.$               | -1293334.<br>$\pm 628.$    | -1155197.<br>$\pm 637.$  | 202.385<br>$\pm 112.$       | -26766.<br>$\pm 628.$       | -8311.<br>$\pm 637.$      |
| 300.                | 92.226                | 69.009                | -68.442                      | 170.                         | -1293370.                  | -1154339.                | 200.388                     | -26879.<br>$\pm 112.$       | -8196.<br>$\pm 637.$      |
| 350.                | 104.706               | 84.185                | -69.612                      | 5101.                        | -129071.                   | -1131105.                | 168.308                     | -29700.<br>$\pm 644.$       | -4854.<br>$\pm 644.$      |
| 400.                | 115.656               | 98.896                | -72.558                      | 10615.                       | -129268.                   | -1107805.                | 144.564                     | -91780.<br>$\pm 644.$       | 3219.<br>$\pm 644.$       |
| 450.                | 125.423               | 113.093               | -76.100                      | 16647.                       | -129016.                   | -1084508.                | 125.386                     | -90793.<br>$\pm 644.$       | 15038.<br>$\pm 644.$      |
| 500.                | 134.262               | 126.772               | -80.488                      | 23142.                       | -1293364.                  | -1061260.                | 110.369                     | -89500.<br>$\pm 644.$       | 26731.<br>$\pm 644.$      |
| (2 s gma)           | $\pm 1.827$           | $\pm 0.473$           | $\pm 0.447$                  | $\pm 141.$                   | $\pm 644.$                 | $\pm 652.$               | $\pm 0.368$                 | $\pm 644.$                  | $\pm 632.$                |
| 550.                | 142.361               | 139.954               | -85.298                      | 30061.                       | -1292350.                  | -1038096.                | 98.590                      | -87923.<br>$\pm 1377.$      | 38280.<br>$\pm 1377.$     |
| 600.                | 149.861               | 152.666               | -90.386                      | 37368.                       | -129011.                   | -1015039.                | 88.367                      | -86082.<br>$\pm 1377.$      | 49673.<br>$\pm 1377.$     |
| 650.                | 156.868               | 164.941               | -95.551                      | 45038.                       | -128375.                   | -992105.                 | 79.727                      | -83993.<br>$\pm 1377.$      | 60933.<br>$\pm 1377.$     |
| 700.                | 163.464               | 176.810               | -101.027                     | 53048.                       | -128468.                   | -969308.                 | 72.331                      | -81668.<br>$\pm 1377.$      | 71966.<br>$\pm 1377.$     |
| 750.                | 169.716               | 188.303               | -106.464                     | 61379.                       | -1283312.                  | -946657.                 | 65.931                      | -79120.<br>$\pm 1377.$      | 82899.<br>$\pm 1377.$     |
| (2 s gma)           | $\pm 7.542$           | $\pm 2.016$           | $\pm 0.499$                  | $\pm 1225.$                  | $\pm 1225.$                | $\pm 1225.$              | $\pm 0.351$                 | $\pm 1377.$                 | $\pm 731.$                |

 $\text{Al}(\text{OH})_3$ 

Gibbsite

Formula weight = 78.003 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$$S^\circ = 68.440 \pm 0.344 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -1293.334 \pm 0.628 \text{ kJ/mol}$$

$$V^\circ = 31.9562 \pm 0.030 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -1155.197 \pm 0.637 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 6.617044 \times 10^5$$

$$a_4 = -1.513072 \times 10^3$$

$$a_6 = 3.006455 \times 10^{-2}$$

$$a_2 = 2.582430 \times 10^4$$

$$a_5 = 2.208509 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -2.667640 \times 10^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of gibbsite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

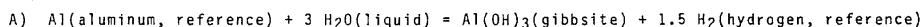
| Source                      | Data Type     | Method                | No. of Points | Range       |
|-----------------------------|---------------|-----------------------|---------------|-------------|
| Hemingway and others (1977) | heat capacity | adiabatic calorimetry | 23            | 200 - 480 K |
| Hemingway and others (1977) | entropy       | adiabatic calorimetry | 1             | 298.15 K    |

The heat-capacity measurements of Hemingway and others (1977) were fit with a standard error of estimate of 0.33  $\text{J}/(\text{mol}\cdot\text{K})$ . The fitted entropy at 298.15 K is  $68.440 \pm 0.344 \text{ J}/(\text{mol}\cdot\text{K})$ , which agrees with the experimental value of  $68.44 \pm 0.14 \text{ J}/(\text{mol}\cdot\text{K})$  reported by Hemingway and others (1977).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                  | Method                    | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ kJ | $\Delta H_f^\circ(298.15 \text{ K})$ kJ/mol |
|---|---------------------------|-----------------------|-----------|---------------|---|---|
| Hemingway and Robie (1977) <sup>b</sup> | solution calorimetry (HF) | A                     | 303.4     | 4             | -486.096 ± 2.514                        | -1293.578                                   |

a Reactions:



b Hemingway and Robie (1977) measured the enthalpy of solution of gibbsite in HF acid solution at 303.4 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of water, quartz, and aluminum metal in the HF acid solution. A correction was made for the enthalpy of vaporization of  $\text{H}_2$  gas evolved during the dissolution of aluminum metal.

The molar volume of gibbsite was obtained from the compilation of Robie and others (1967).

**THERMODYNAMIC DATA FOR MINERALS**

| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K)   | $S^o$<br>J/(mol·K)     | $(G_f^o - H_f^o)T$<br>J/mol | Formation from the Elements  |                            |                          | Formation from the Oxides          |                         |                                    |
|---------------------|------------------------|------------------------|-----------------------------|------------------------------|----------------------------|--------------------------|------------------------------------|-------------------------|------------------------------------|
|                     |                        |                        |                             | $H_f^o - H_{f,r}^o$<br>J/mol | $\Delta H_f^o, e$<br>J/mol | $\log K_f^o, e$          | $\Delta H_f^o, \text{ox}$<br>J/mol | $\log K_f^o, \text{ox}$ | $\Delta G_f^o, \text{ox}$<br>J/mol |
| 273.15              | 154.134                | 127.599                | -142.251                    | -4002.                       | -3298437.                  | -3137609.                | 600.007                            | -77415.                 | -80492.                            |
| 298.15<br>(2 sigma) | 165.658<br>$\pm 2.737$ | 141.611<br>$\pm 2.173$ | -141.611<br>$\pm 2.173$     | 0.<br>$\pm 0.$               | -3298956.<br>$\pm 1912.$   | -3122865.<br>$\pm 1465.$ | 547.113<br>$\pm 0.257$             | -77452.<br>$\pm 1912.$  | -80772.<br>$\pm 1468.$             |
| 300.                | 166.425                | 142.638                | -141.614                    | 307.                         | -3298986.                  | -3121772.                | 543.548                            | -77453.                 | -80793.                            |
| 350.                | 183.805                | 169.673                | -144.709                    | 9087.                        | -3298427.                  | -3092193.                | 461.484                            | -77430.                 | -81350.                            |
| 400.                | 196.556                | 195.089                | -148.561                    | 18611.                       | -3298333.                  | -3062589.                | 399.933                            | -77361.                 | -81914.                            |
| 450.                | 206.375                | 218.830                | -155.065                    | 28694.                       | -329878.                   | -3033020.                | 352.064                            | -77295.                 | -82488.                            |
| 500.                | 214.215                | 240.934                | -162.562                    | 39216.                       | -329878.                   | -30033516.               | 313.775                            | -77257.                 | -83067.                            |
| (2 sigma)           | $\pm 2.064$            | $\pm 1.809$            | $\pm 2.079$                 | $\pm 362.$                   | $\pm 1823.$                | $\pm 1272.$              | $\pm 0.133$                        | $\pm 1823.$             | $\pm 1272.$                        |
| 550.                | 220.652                | 261.723                | -170.645                    | 50093.                       | -3297315.                  | -2974090.                | 282.455                            | -77256.                 | -83448.                            |
| 600.                | 226.056                | 261.160                | -179.053                    | 61264.                       | -3296551.                  | -294748.                 | 286.363                            | -77299.                 | -8428.                             |
| 650.                | 230.675                | 299.441                | -187.618                    | 72685.                       | -3295336.                  | -2915489.                | 234.291                            | -77388.                 | -84002.                            |
| 700.                | 234.681                | 316.686                | -196.227                    | 84321.                       | -3294307.                  | -2886309.                | 215.379                            | -77524.                 | -85368.                            |
| 750.                | 238.198                | 333.000                | -204.806                    | 96145.                       | -3294334.                  | -2857165.                | 198.990                            | -77607.                 | -85922.                            |
| (2 sigma)           | $\pm 1.690$            | $\pm 1.540$            | $\pm 1.883$                 | $\pm 725.$                   | $\pm 1712.$                | $\pm 1173.$              | $\pm 0.082$                        | $\pm 1712.$             | $\pm 1173.$                        |
| 800.                | 241.318                | 348.474                | -213.306                    | 108135.                      | -3293065.                  | -2828059.                | 184.654                            | -77936.                 | -86162.                            |
| 850.                | 244.110                | 363.189                | -221.693                    | 120272.                      | -3292101.                  | -2799037.                | 172.008                            | -78930.                 | -86382.                            |
| 900.                | 246.629                | 377.215                | -222.947                    | 132541.                      | -3291162.                  | -2770058.                | 160.770                            | -78828.                 | -8758.                             |
| 950.                | 248.917                | 390.611                | -238.053                    | 144931.                      | -3312076.                  | -2740729.                | 150.696                            | -78708.                 | -87941.                            |
| 1000.               | 251.006                | 403.133                | -246.004                    | 157129.                      | -3311260.                  | -2710680.                | 141.591                            | -78570.                 | -88100.                            |
| (2 sigma)           | $\pm 2.651$            | $\pm 1.330$            | $\pm 1.711$                 | $\pm 99.$                    | $\pm 1653.$                | $\pm 1187.$              | $\pm 0.062$                        | $\pm 1653.$             | $\pm 1187.$                        |
| 1050.               | 252.925                | 415.727                | -253.795                    | 170028.                      | -3310493.                  | -2680670.                | 133.356                            | -78418.                 | -88957.                            |
| 1100.               | 254.695                | 427.534                | -261.426                    | 182119.                      | -3309881.                  | -2650605.                | 125.871                            | -78255.                 | -89431.                            |
| 1150.               | 256.335                | 438.933                | -268.896                    | 195196.                      | -3301000.                  | -2620471.                | 119.025                            | -78083.                 | -89593.                            |
| 1200.               | 257.860                | 449.835                | -276.209                    | 208351.                      | -3310466.                  | -2590220.                | 112.749                            | -77905.                 | -90633.                            |
| 1250.               | 259.283                | 460.330                | -283.366                    | 221260.                      | -3313094.                  | -2560034.                | 106.978                            | -77722.                 | -90990.                            |
| (2 sigma)           | $\pm 3.875$            | $\pm 1.385$            | $\pm 1.568$                 | $\pm 1515.$                  | $\pm 1872.$                | $\pm 1253.$              | $\pm 0.052$                        | $\pm 1872.$             | $\pm 1153.$                        |
| 1300.               | 260.615                | 470.586                | -290.372                    | 234278.                      | -3311286.                  | -2529911.                | 101.653                            | -77539.                 | -91524.                            |
| 1350.               | 261.865                | 480.445                | -291.230                    | 247310.                      | -3310443.                  | -250450.                 | 96.725                             | -77356.                 | -92655.                            |
| 1400.               | 263.042                | 489.990                | -303.945                    | 260463.                      | -3309868.                  | -249855.                 | 92.151                             | -77171.                 | -92633.                            |
| 1450.               | 264.152                | 499.240                | -310.521                    | 273643.                      | -330262.                   | -2439913.                | 87.895                             | -77003.                 | -93168.                            |
| 1500.               | 265.202                | 508.213                | -316.962                    | 286877.                      | -3305925.                  | -2410034.                | 83.925                             | -76839.                 | -93228.                            |
| (2 sigma)           | $\pm 4.952$            | $\pm 1.816$            | $\pm 1.461$                 | $\pm 2416.$                  | $\pm 2416.$                | $\pm 1370.$              | $\pm 0.048$                        | $\pm 2578.$             | $\pm 1570.$                        |
| 1550.               | 266.196                | 516.925                | -323.272                    | 300153.                      | -3303759.                  | -2380213.                | 80.213                             | -76685.                 | -94293.                            |
| 1600.               | 267.140                | 525.392                | -322.457                    | 313456.                      | -3301964.                  | -2350450.                | 76.734                             | -76545.                 | -94664.                            |
| 1650.               | 268.038                | 533.626                | -335.519                    | 326816.                      | -3309852.                  | -2320744.                | 73.469                             | -76421.                 | -95338.                            |
| 1700.               | 268.893                | 541.641                | -341.465                    | 340299.                      | -334899.                   | -2290653.                | 70.383                             | -76315.                 | -96016.                            |
| 1750.               | 269.709                | 549.447                | -341.296                    | 353764.                      | -3346777.                  | -2259550.                | 67.444                             | -76231.                 | -96597.                            |
| (2 sigma)           | $\pm 5.860$            | $\pm 2.463$            | $\pm 1.412$                 | $\pm 1.461$                  | $\pm 3641.$                | $\pm 1607.$              | $\pm 0.048$                        | $\pm 3711.$             | $\pm 1607.$                        |
| 1800.               | 270.488                | 557.056                | -353.017                    | 367210.                      | -3497557.                  | -2224591.                | 64.556                             | -76171.                 | -97180.                            |
| (2 sigma)           | $\pm 6.024$            | $\pm 2.605$            | $\pm 1.411$                 | $\pm 3918.$                  | $\pm 3377.$                | $\pm 1677.$              | $\pm 0.049$                        | $\pm 3977.$             | $\pm 1677.$                        |

CaAl<sub>2</sub>SiO<sub>6</sub>

Ca-Al Clinopyroxene

Formula weight = 218.125 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$$\begin{aligned} S^\circ &= 141.600 \pm 2.200 \text{ J/(mol}\cdot\text{K)} & \Delta H_f^\circ &= -3298.9 \pm 1.9 \text{ kJ/mol} \\ V^\circ &= 63.439 \pm 0.064 \text{ cm}^3/\text{mol} & \Delta G_f^\circ &= -3122.9 \pm 1.5 \text{ kJ/mol} \end{aligned}$$

Equations at Reference Pressure, 101.325 kPa

$$\begin{aligned} C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] &= a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2 \\ S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] &= -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2 \\ [H^\circ(T) - H^\circ(298.15\text{K})]/[\text{J}/\text{mol}] &= -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3 \\ a_1 &= -2.72024 \times 10^6 & a_4 &= -1.96633 \times 10^3 & a_6 &= 0.0 \\ a_2 &= 2.98963 \times 10^4 & a_5 &= 3.22040 \times 10^2 & a_7 &= 0.0 \\ a_3 &= -2.18582 \times 10^3 \end{aligned}$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of Ca-Al clinopyroxene.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                        | Data Type   | Method                            | No. of Points | Range           |
|-------------------------------|---|-----------------------------------|---------------|-----------------|
| Thompson and others (1978)    | heat capacity   | differential scanning calorimeter | 16            | 298.15 - 1000 K |
| Estimated values <sup>a</sup> | heat capacity   | component summation               | 11            | 1000 - 2000 K   |
| a                             | Above 1000 K, the heat capacity of Ca-Al clinopyroxene was estimated by a summation of the average heat capacities of CaO-, SiO <sub>2</sub> -, (Al <sup>IV</sup> ) <sub>2</sub> O <sub>3</sub> -, and (Al <sup>VI</sup> ) <sub>2</sub> O <sub>3</sub> -components derived from a number of sodium, potassium, and calcium aluminum silicates. (Al <sup>IV</sup> ) and (Al <sup>VI</sup> ) represent aluminum in tetrahedral and octahedral coordination, respectively. |                                   |               |                 |
|                               | The standard error of estimate of the fitted heat-capacity data of Thompson and others (1978) for synthetic Ca-Al clinopyroxene is 0.33 J/(mol·K). The estimated heat-capacity values above 1000 K were a smooth extension of the data of Thompson and others. The standard error of estimate for the estimated heat capacity from 1000 to 2000 K is 1.6 J/(mol·K).   |                                   |               |                 |

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                                | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15\text{ K})$ | $\Delta H_f^\circ(298.15\text{ K})$ |
|---------------------------------------|---------------------------------------|-----------------------|-----------|---------------|-------------------------------------|-------------------------------------|
| Charlu and others (1978) <sup>b</sup> | solution calorimetry<br>(borate salt) | A                     | 970       | 1             | 75.069 ± 1.006                      | -3301.339                           |
| Hays (1965)                           | solid-medium pressure apparatus       | B                     | 1473-1673 | 4 pair        | -11.841 ± 1.953                     | -3299.007                           |

a Reactions:

- A) CaAl<sub>2</sub>SiO<sub>6</sub>(clinopyroxene) = CaO(lime) + Al<sub>2</sub>O<sub>3</sub>(corundum) + SiO<sub>2</sub>(quartz, alpha)
- B) CaAl<sub>2</sub>Si<sub>2</sub>O<sub>6</sub>(anorthite) + Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>(gehlenite) + Al<sub>2</sub>O<sub>3</sub>(corundum) = 3 CaAl<sub>2</sub>SiO<sub>6</sub>(clinopyroxene)

b Charlu and others (1978) measured the enthalpy of solution of synthetic Ca-Al clinopyroxene in lead borate salt melt at 970 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of lime, quartz, and corundum in the salt melt; corrections were not made for the enthalpies of dilution and of mixing of the product melts.

The phase-equilibrium study of Hays (1965) (utilizing solid-medium pressure apparatus) was evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for H<sub>2</sub>O(gas) from Fisher and Zen (1971) were used in the conversion. This study complies with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated. These are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for Ca-Al clinopyroxene (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of -3298.956 ± 1.902 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of Ca-Al clinopyroxene and presents the data in their poorest perspective. Most of the phase-equilibria data cited above bracket the regression fit in free-energy space.

The molar volume of Ca-Al clinopyroxene was obtained from the compilation of Robie and others (1967).

$\text{CaAl}_2\text{Si}_2\text{O}_8$   
Anorthite (triclinic, member of the Feldspar Group)

$\text{Al}_2\text{CaO}_8\text{Si}_2$

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| Temperature<br>(K)                                     | $C_p^o$<br>$\text{J}/(\text{mol} \cdot \text{K})$                   | $S^o$<br>$\text{J}/(\text{mol} \cdot \text{K})$                    | $(G_T^o - H_{\text{Tr}}^o)/T$<br>$\text{J}/(\text{mol} \cdot \text{K})$ | Formation from the Elements   |  |   | Formation from the Oxides   |  |  |  |
|--|---|--|---|---|--|---|---|--|--|--|
|  |   |  |   | $\Delta H_f^o$<br>$\text{J}/\text{mol}$                             | $\Delta G_f^o$<br>$\text{J}/\text{mol}$                                      | $\log K_f^o, e$   | $\Delta H_f^o, \text{ox}$<br>$\text{J}/\text{mol}$                  | $\Delta G_f^o, \text{ox}$<br>$\text{J}/\text{mol}$                     | $\log K_f^o, \text{ox}$  |  |
| 273.15   | 199.778   | 181.275  | -200.110  | -5145.  | -4227236.  | -4021095.   | 768.956   | -95649.  | -103103.   | 19.716   |
| 298.15<br>(2 signs)                                    | 211.600<br>$\pm 0.146$  | 199.290<br>$\pm 0.145$   | -199.290<br>$\pm 0.145$   | 0.  | -4227833.<br>$\pm 1118.$   | -4002200.<br>$\pm 1117.$  | 701.168<br>$\pm 0.196$  | -95631.<br>$\pm 1118.$   | -103786.<br>$\pm 1117.$  | 18.183<br>$\pm 0.156$  |
| 300.<br>350.<br>400.<br>450.<br>500.<br>(2 signs)      | 212.425<br>232.294<br>248.139<br>260.828<br>271.072<br>$\pm 0.417$  | 200.601<br>234.897<br>266.989<br>296.975<br>325.005<br>$\pm 0.179$ | -199.294<br>-201.957<br>-208.103<br>-216.330<br>-225.812<br>$\pm 0.145$ | 392.<br>11529.<br>2355.<br>3690.<br>4997.<br>$\pm 145.$             | -4227869.<br>-4228466.<br>-4228460.<br>-4228007.<br>-4227233.<br>$\pm 1119.$ | -40020800.<br>-3962298.<br>-3924554.<br>-3887039.<br>-3849193.<br>$\pm 1117.$ | 696.601<br>591.430<br>512.546<br>451.195<br>402.122<br>$\pm 0.117.$ | -95630.<br>-95610.<br>-95604.<br>-95626.<br>-95703.<br>$\pm 0.117.$    | -103837.<br>-105206.<br>-105678.<br>-107948.<br>-109314.<br>$\pm 0.117.$ | 18.030<br>15.701<br>13.918<br>12.530<br>11.420<br>$\pm 0.117.$ |
| 550.<br>600.<br>650.<br>700.<br>750.<br>(2 signs)      | 279.430<br>286.333<br>292.117<br>297.049<br>301.337<br>$\pm 0.162$  | 351.246<br>326.365<br>399.019<br>420.852<br>441.496<br>$\pm 0.333$ | -236.035<br>-246.673<br>-257.510<br>-268.405<br>-279.262<br>$\pm 0.162$ | 63366.<br>77515.<br>91818.<br>106713.<br>121675.<br>$\pm 174.$      | -4226238.<br>-4228103.<br>-4223890.<br>-422649.<br>-4226255.<br>$\pm 1122.$  | -3811436.<br>-3733776.<br>-3736214.<br>-3698147.<br>-3661332.<br>$\pm 0.078$  | 361.980<br>328.536<br>300.246<br>276.004<br>254.998<br>$\pm 0.078$  | -95850.<br>-96087.<br>-96424.<br>-96871.<br>-97429.<br>$\pm 0.078$     | -110669.<br>-112006.<br>-113320.<br>-114603.<br>-115951.<br>$\pm 0.078$  | 10.510<br>9.751<br>9.106<br>8.552<br>8.059<br>$\pm 0.078$      |
| 800.<br>850.<br>900.<br>950.<br>1000.<br>(2 signs)     | 305.152<br>308.631<br>311.888<br>315.015<br>318.091<br>$\pm 1.322$  | 461.068<br>479.673<br>497.407<br>514.354<br>530.591<br>$\pm 0.471$ | -290.019<br>-300.632<br>-311.076<br>-331.392<br>-331.392<br>$\pm 0.204$ | 136639.<br>152185.<br>16798.<br>183371.<br>199199.<br>$\pm 324.$    | -4220960.<br>-4219765.<br>-4218685.<br>-4219245.<br>-4218152.<br>$\pm 1155.$ | -36323980.<br>-3586706.<br>-3549199.<br>-3511956.<br>-3473106.<br>$\pm 1135.$ | 236.621<br>220.412<br>206.007<br>193.101<br>181.448<br>$\pm 0.059$  | -98101.<br>-100317.<br>-100356.<br>-102362.<br>-100331.<br>$\pm 1135.$ | -117058.<br>-118209.<br>-119260.<br>-120310.<br>-121360.<br>$\pm 0.059$  | 7.643<br>7.264<br>6.922<br>6.615<br>6.339<br>$\pm 0.059$       |
| 1050.<br>1100.<br>1150.<br>1200.<br>1250.<br>(2 signs) | 321.182<br>324.344<br>327.625<br>331.066<br>334.703<br>$\pm 4.280$  | 546.185<br>561.199<br>575.688<br>589.704<br>603.292<br>$\pm 0.729$ | -341.251<br>-350.909<br>-360.369<br>-369.634<br>-378.710<br>$\pm 0.248$ | 215181.<br>231318.<br>247617.<br>264683.<br>280127.<br>$\pm 47.$    | -4231076.<br>-4236011.<br>-424820.<br>-424806.<br>-423666.<br>$\pm 1384.$    | -3435510.<br>-3397165.<br>-3589388.<br>-3320603.<br>-3282205.<br>$\pm 1156.$  | 170.907<br>161.327<br>152.570<br>144.542<br>137.160<br>$\pm 0.048$  | -100257.<br>-100132.<br>-99964.<br>-99358.<br>-99138.<br>$\pm 1156.$   | -122413.<br>-123471.<br>-124561.<br>-125610.<br>-126697.<br>$\pm 0.048$  | 6.090<br>5.863<br>5.657<br>5.468<br>5.294<br>$\pm 0.048$       |
| 1300.<br>1350.<br>1400.<br>1450.<br>1500.<br>(2 signs) | 338.566<br>342.884<br>347.079<br>351.774<br>356.186<br>$\pm 9.904$  | 616.494<br>629.347<br>641.889<br>654.149<br>666.158<br>$\pm 1.759$ | -387.603<br>-396.320<br>-404.867<br>-413.252<br>-421.483<br>$\pm 0.330$ | 297558.<br>314588.<br>331331.<br>349301.<br>367013.<br>$\pm 224.$   | -4236387.<br>-423954.<br>-421349.<br>-4228556.<br>-4225555.<br>$\pm 2674.$   | -3240495.<br>-3205976.<br>-3167950.<br>-3130020.<br>-3092190.<br>$\pm 1196.$  | 130.349<br>124.047<br>118.198<br>112.755<br>107.680<br>$\pm 0.042$  | -98927.<br>-99837.<br>-97724.<br>-96922.<br>-95964.<br>$\pm 1196.$     | -1229798.<br>-123471.<br>-124561.<br>-125610.<br>-126697.<br>$\pm 0.042$ | 5.135<br>4.988<br>4.853<br>4.727<br>4.612<br>$\pm 0.042$       |
| 1550.<br>1600.<br>1650.<br>1700.<br>1750.<br>(2 signs) | 362.132<br>367.828<br>373.186<br>380.318<br>387.336<br>$\pm 18.260$ | 677.944<br>689.530<br>700.940<br>712.196<br>723.318<br>$\pm 3.779$ | -429.566<br>-437.510<br>-445.320<br>-453.004<br>-460.569<br>$\pm 0.595$ | 384985.<br>396132.<br>404854.<br>4132104.<br>421774.<br>$\pm 5706.$ | -4222328.<br>-423954.<br>-421349.<br>-4228556.<br>-4225555.<br>$\pm 5926.$   | -3054463.<br>-3205976.<br>-3167950.<br>-3130020.<br>-3092190.<br>$\pm 1455.$  | 102.935<br>98.490<br>94.318<br>90.367<br>86.584<br>$\pm 0.043$      | -94836.<br>-93518.<br>-91993.<br>-90244.<br>-88252.<br>$\pm 0.043$     | -133662.<br>-134935.<br>-130061.<br>-13230.<br>-132429.<br>$\pm 0.043$   | 4.504<br>4.405<br>4.313<br>4.229<br>4.150<br>$\pm 0.043$       |
| 1800.<br>(2 signs)                                     | 394.348<br>$\pm 20.267$   | 734.324<br>$\pm 4.307$   | -468.020<br>$\pm 0.680$   | 479447.<br>$\pm 6656.$  | -4455352.<br>$\pm 6862.$   | -2856748.<br>$\pm 1576.$  | 82.901<br>$\pm 0.046$   | -85998.<br>$\pm 6862.$   | -140523.<br>$\pm 1576.$  | 4.078<br>$\pm 0.046$   |

CaAl<sub>2</sub>O<sub>8</sub>Si<sub>2</sub>

Anorthite

Formula weight = 278.209 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 199.29 \pm 0.15 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -4227.8 \pm 1.1 \text{ kJ/mol}$$

$$V^\circ = 100.79 \pm 0.10 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -4002.2 \pm 1.1 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1800 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{ K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 3.18591 \times 10^6$$

$$a_4 = -5.35832 \times 10^3$$

$$a_6 = -1.46450 \times 10^{-1}$$

$$a_2 = 1.10301 \times 10^5$$

$$a_5 = 8.00971 \times 10^2$$

$$a_7 = 1.05663 \times 10^{-4}$$

$$a_3 = -9.44981 \times 10^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of anorthite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                   | Data Type         | Method                            | No. of Points | Range         |
|--------------------------|-------------------|-----------------------------------|---------------|---------------|
| Robie and others (1978)  | heat capacity     | adiabatic calorimetry             | 49            | 202 - 381 K   |
| Krupka and others (1979) | heat capacity     | differential scanning calorimetry | 95            | 349 - 966 K   |
| White (1919)             | relative enthalpy | drop calorimetry                  | 9             | 1173 - 1673 K |
| Robie and others (1978)  | entropy           | adiabatic calorimetry             | 1             | 298.15 K      |

The heat capacities of Robie and others (1978) and of Krupka and others (1979) were fit with a standard error of estimate of 0.4 and 1.36 J/(mol·K), respectively. The relative enthalpy measurements of White (1919) were fit with a standard error of estimate of 980 J/mol, or approximately 0.3 percent of the observed value. The fitted entropy value at 298.15 K is  $199.29 \pm 0.15 \text{ J}/(\text{mol}\cdot\text{K})$  or a departure of 0.01 from the experimental value of  $199.3 \pm 0.3 \text{ J}/(\text{mol}\cdot\text{K})$ .

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                  | Method                                      | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H^\circ(298.15 \text{ K})$ | $\Delta H^\circ(298.15 \text{ K})$ |
|---|---|-----------------------|-----------|---------------|------------------------------------|------------------------------------|
|   |   |                       |           |               | Third Law, kJ                      | kJ/mol                             |
| Kracek and Neuvonen (1952) <sup>b</sup> | solution calorimetry(HF)                    | A                     | 347-895   | 1             | 43.275 $\pm$ 1.447                 | -4226.665                          |
| Charlu and others (1978) <sup>c</sup>   | solution calorimetry<br>(borate salt)       | B                     | 970       | 2             | 95.089 $\pm$ 1.988                 | -4228.375                          |
| Newton (1965)                           | gas- and solid-medium<br>pressure apparatus | C                     | 843-1113  | 6 pair        | -94.454 $\pm$ 1.738                | -4228.919                          |
| Boettcher (1970)                        | gas-medium pressure apparatus               | C                     | 898-928   | 1 pair        | -306.468 $\pm$ 2.790               | -4227.725                          |
| Strens (1968)                           | gas-medium pressure apparatus               | D                     | 770-823   | 1 pair        | -220.561 $\pm$ 5.976               | -4226.920                          |
| Boettcher (1970)                        | gas-medium pressure apparatus               | D                     | 853-933   | 2 pair        | -213.025 $\pm$ 2.944               | -4228.428                          |
| Shmulovich (1974)                       | gas-medium pressure apparatus               | E                     | 1133-1153 | 1 pair        | 159.942 $\pm$ 1.763                | -4226.727                          |
| Huckenholz (1974)                       | unspecified                                 | E                     | 1125-1423 | 6 pair        | 158.750 $\pm$ 2.236                | -4227.919                          |
| Hays (1965)                             | solid-medium pressure apparatus             | E                     | 1473-1523 | 2 pair        | 156.099 $\pm$ 6.608                | -4230.570                          |
| Huckenholz (1974)                       | unspecified                                 | F                     | 848-858   | 1 pair        | -49.366 $\pm$ 0.328                | -4228.137                          |
| Newton (1966b)                          | gas-medium pressure apparatus               | F                     | 803-923   | 2 pair        | -51.708 $\pm$ 3.042                | -4225.795                          |
| Huckenholz (1974)                       | unspecified                                 | G                     | 888-958   | 2 pair        | -50.101 $\pm$ 0.499                | -4227.971                          |
| Newton (1966b)                          | gas-medium pressure apparatus               | G                     | 973-1023  | 2 pair        | -49.103 $\pm$ 1.847                | -4228.969                          |
| Boettcher (1970)                        | gas-medium pressure apparatus               | G                     | 893-1053  | 2 pair        | -50.328 $\pm$ 1.454                | -4227.744                          |
| Storre and Nitsch (1974)                | gas- and solid-medium<br>pressure apparatus | H                     | 788-833   | 2 pair        | -89.818 $\pm$ 1.710                | -4228.388                          |
| Chatterjee (1971)                       | gas-medium pressure apparatus               | I                     | 763-893   | 3 pair        | -94.087 $\pm$ 0.931                | -4227.976                          |
| Hays (1965)                             | solid-medium pressure apparatus             | J                     | 1473-1673 | 4 pair        | -11.814 $\pm$ 1.953                | -4227.678                          |
| Boettcher (1970)                        | gas-medium pressure apparatus               | K                     | 1033-1053 | 1 pair        | -102.037 $\pm$ 0.996               | -4228.292                          |
| Huckenholz (1974)                       | unspecified                                 | K                     | 1028-1263 | 3 pair        | -102.895 $\pm$ 1.257               | -4227.434                          |
| Liou (1971)                             | gas-medium pressure apparatus               | L                     | 708-828   | 5 pair        | -89.180 $\pm$ 0.496                | -4227.848                          |
| Kay and Taylor (1960) <sup>d</sup>      | silica activity                             | M                     | 1653      | 1             | 83.137 $\pm$ 2.584                 | -4227.859                          |
| Kay and Taylor (1960) <sup>d</sup>      | silica activity                             | N                     | 1543      | 1             | 59.386 $\pm$ 2.412                 | -4223.667                          |

$\text{Al}_2\text{CaO}_8\text{Si}_2$ 

## Reactions:

- A)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) + 3  $\text{H}_2\text{O}$ (liquid) =  $\text{CaO}$ (lime) + 2  $\text{Al}(\text{OH})_3$ (gibbsite) + 2  $\text{SiO}_2$ (quartz, alpha)
- B)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) =  $\text{CaO}$ (lime) +  $\text{Al}_2\text{O}_3$ (corundum) + 2  $\text{SiO}_2$ (quartz, alpha)
- C) 2  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$ (grossular) + 6  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{Al}_2\text{O}_3$ (corundum) + 3  $\text{H}_2\text{O}$ (gas)  
= 6  $\text{Ca}_2\text{Al}_3\text{Si}_3\text{O}_12(\text{OH})(\text{zoisite})$
- D)  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$ (grossular) + 5  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) + 2  $\text{H}_2\text{O}$ (gas)  
= 4  $\text{Ca}_2\text{Al}_3\text{Si}_3\text{O}_12(\text{OH})(\text{zoisite})$  +  $\text{SiO}_2$ (quartz, alpha)
- E) 2  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$ (grossular) =  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) + 3  $\text{CaSiO}_3$ (wollastonite) +  $\text{Ca}_2\text{Al}_2\text{Si}_1\text{O}_7$ (gehlenite)
- F)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) + 2  $\text{CaSiO}_3$ (wollastonite) =  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$ (grossular) +  $\text{SiO}_2$ (quartz, alpha)
- G)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) + 2  $\text{CaSiO}_3$ (wollastonite) =  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$ (grossular) +  $\text{SiO}_2$ (quartz, beta)
- H)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{Al}_2\text{Si}_1\text{O}_5$ (andalusite) +  $\text{H}_2\text{O}$ (gas) =  $\text{CaAl}_4\text{Si}_2\text{O}_{10}(\text{OH})_2$ (margarite) +  $\text{SiO}_2$ (quartz, alpha)
- I)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{Al}_2\text{O}_3$ (corundum) +  $\text{H}_2\text{O}$ (gas) =  $\text{CaAl}_4\text{Si}_2\text{O}_{10}(\text{OH})_2$ (margarite)
- J)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{Ca}_2\text{Al}_2\text{Si}_1\text{O}_7$ (gehlenite) +  $\text{Al}_2\text{O}_3$ (corundum) = 3  $\text{CaAl}_2\text{Si}_1\text{O}_6$ (clinopyroxene)
- K)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{Ca}_2\text{Al}_2\text{Si}_1\text{O}_7$ (gehlenite) =  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$ (grossular) +  $\text{Al}_2\text{O}_3$ (corundum)
- L)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{CaSiO}_3$ (wollastonite) +  $\text{H}_2\text{O}$ (gas) =  $\text{Ca}_2\text{Al}_2\text{Si}_3\text{O}_{10}(\text{OH})_2$ (prehnite)
- M) 2  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) =  $\text{Ca}_2\text{Al}_2\text{Si}_1\text{O}_7$ (gehlenite) +  $\text{Al}_2\text{O}_3$ (corundum) + 3  $\text{SiO}_2$ (cristobalite, beta)
- N)  $\text{CaAl}_2\text{Si}_2\text{O}_8$ (anorthite) +  $\text{CaSiO}_3$ (cyclowollastonite) =  $\text{Ca}_2\text{Al}_2\text{Si}_1\text{O}_7$ (gehlenite) + 2  $\text{SiO}_2$ (cristobalite, beta)
- b) Kracek and Neuvonen (1952) measured the enthalpy of solution of lime and synthetic anorthite in HF acid at 374.15 K. To complete the thermodynamic cycle, their data were evaluated in combination with the recent data for the enthalpies of solution of water, quartz, and gibbsite in similar solutions (Barany, 1963; Bennington and others, 1978; Hemingway and Robie, 1977; Barany and Kelley, 1961; and Koehler and others, 1961).
- c) Charlu and others (1978) measured the enthalpy of solution of two samples of synthetic anorthite in lead borate salt melt at 970 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of lime, quartz, and corundum in the salt melt; corrections were not made for the enthalpies of dilution and of mixing of the product melts.
- d) Kay and Taylor (1960) determined the activity of silica in the silicate liquid for the lime-alumina-silica system. Using the silica activity from their study and the measured temperatures and compositions of the silicate melts in equilibrium with either anorthite, gehlenite, and corundum or anorthite, cyclowollastonite, and gehlenite, we obtained the equilibrium constants for reactions M and N at the melt temperature and 101.325 kPa.

Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for  $\text{H}_2\text{O}$ (gas) from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for anorthite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of -4227.8±1.1 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of anorthite and presents the data in their poorest perspective.

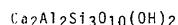
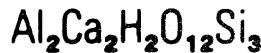
Most of the phase-equilibria data cited above bracket the regression fit in free-energy space. However, the phase-equilibria studies lack sufficient precision to constrain the fit, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate. The phase-equilibria studies also lack the precision to discriminate among the experimental enthalpies of solution; therefore, the three experimental enthalpies of solution were included in the study.

The molar volume of anorthite was obtained from the compilation of Robie and others (1967).

$\text{Ca}_2\text{Al}_2\text{Si}_3\text{O}_{10}(\text{OH})_2$   
Prehnite (orthorhombic)

$\text{Al}_2\text{Ca}_2\text{H}_2\text{O}_{12}\text{Si}_3$   
Issued September, 1979

| Temperature<br>(K)  | $\zeta_p$<br>J/(mol·K) | $S^\circ$<br>J/(mol·K) | $(G_f^\circ - H_f^\circ)/T_r$<br>J/(mol·K) | Formation from the Elements          |                                |                         | Formation from the Oxides              |  |                             |
|---------------------|------------------------|------------------------|--|--------------------------------------|--------------------------------|-------------------------|--|--|-----------------------------|
|                     |                        |                        |  | $H_f^\circ - H_{f,r}^\circ$<br>J/mol | $\Delta G_f^\circ, e$<br>J/mol | $\log K_f^\circ, e$     | $\Delta H_f^\circ, \text{ox}$<br>J/mol | $\Delta G_f^\circ, \text{ox}$<br>J/mol | $\log K_f^\circ, \text{ox}$ |
| 273.15              | 312.544                | 264.558                | -294.028                                   | -8050.                               | -1192637.                      | -5848224.               | 1118.359                               | -228741.                               | -221950.                    |
| 298.15<br>(2 s gma) | 331.110<br>$\pm 0.538$ | 292.745<br>$\pm 0.639$ | -292.745<br>$\pm 0.659$                    | 0.<br>$\pm 0.659$                    | -1193631.<br>$\pm 832.$        | -5816655.<br>$\pm 729.$ | 1019.053<br>$\pm 0.128$                | -229828.<br>$\pm 832.$                 | -221279.<br>$\pm 729.$      |
| 300.                | 332.405                | 294.797                | -292.751                                   | 614.                                 | -1193591.                      | -5814315.               | 1012.362                               | -229906.                               | -221226.                    |
| 350.                | 363.758                | 348.478                | -296.919                                   | 18046.                               | -1194713.                      | -5759990.               | 858.288                                | -231888.                               | -219620.                    |
| 400.                | 389.191                | 398.769                | -306.441                                   | 36891.                               | -1194738.                      | -5681589.               | 742.722                                | -273429.                               | -214842.                    |
| 450.                | 410.022                | 445.852                | -319.433                                   | 56888.                               | -1193996.                      | -5622433.               | 652.443                                | -273009.                               | -207543.                    |
| 500.                | 427.230<br>(2 s gma)   | 489.971<br>$\pm 0.322$ | -334.305<br>$\pm 0.670$                    | 77833.<br>$\pm 232.$                 | -1192673.<br>$\pm 0.670$       | -5566992.<br>$\pm 667.$ | 580.952<br>$\pm 0.070$                 | -272505.<br>$\pm 0.070$                | -200295.<br>$\pm 667.$      |
| 550.                | 441.543                | 531.382                | -350.358                                   | 99563.                               | -1190923.                      | -5491905.               | 522.147                                | -271968.                               | -193100.                    |
| 600.                | 453.505                | 570.330                | -367.083                                   | 121948.                              | -1186571.                      | -5431992.               | 473.158                                | -271443.                               | -185953.                    |
| 650.                | 463.534                | 607.037                | -384.142                                   | 144881.                              | -1186625.                      | -5372559.               | 431.120                                | -270971.                               | -178849.                    |
| 700.                | 471.950                | 641.706                | -401.313                                   | 168275.                              | -1184224.                      | -5303704.               | 396.215                                | -270588.                               | -171778.                    |
| 750.                | 479.006                | 674.515                | -418.443                                   | 192054.                              | -1183569.                      | -5247244.               | 365.050                                | -270325.                               | -164730.                    |
|                     | +1.721<br>(2 s gma)    | +1.047                 | +0.726                                     | $\pm 412.$                           | $\pm 10.11.$                   | $\pm 615.$              | $\pm 0.043$                            | $\pm 1011.$                            | $\pm 615.$                  |
| 800.                | 481.904                | 705.623                | -435.428                                   | 216156.                              | -1181015.                      | -5184907.               | 338.539                                | -270210.                               | -157695.                    |
| 850.                | 489.808                | 735.172                | -452.198                                   | 240528.                              | -1178628.                      | -5122724.               | 314.804                                | -272418.                               | -150646.                    |
| 900.                | 493.848                | 763.287                | -468.706                                   | 265122.                              | -1176453.                      | -506676.                | 293.714                                | -271399.                               | -143512.                    |
| 950.                | 497.135                | 790.079                | -484.321                                   | 289900.                              | -1196013.                      | -4993349.               | 274.828                                | -270395.                               | -136435.                    |
| 1000.               | 493.759                | 815.648                | -500.823                                   | 314825.                              | -1194336.                      | -4933363.               | 257.97                                 | -269333.                               | -129409.                    |
|                     | +1.589<br>(2 s gma)    | +1.621                 | +0.793                                     | $\pm 1184.$                          | $\pm 1184.$                    | $\pm 673.$              | $\pm 0.035$                            | $\pm 1509.$                            | $\pm 673.$                  |
| 1050.               | 501.798                | 840.083                | -516.401                                   | 339866.                              | -1192430.                      | -4872467.               | 242.392                                | -268537.                               | -122431.                    |
| 1100.               | 503.316                | 863.464                | -531.649                                   | 364996.                              | -1190946.                      | -480647.                | 228.391                                | -267727.                               | -115493.                    |
| 1150.               | 504.368                | 885.862                | -546.666                                   | 390190.                              | -605447.                       | -474329.                | 215.385                                | -267023.                               | -108589.                    |
| 1200.               | 505.001                | 907.342                | -561.154                                   | 415426.                              | -620257.                       | -468951.                | 203.043                                | -266442.                               | -101713.                    |
| 1250.               | 505.257                | 927.964                | -575.417                                   | 440684.                              | -619977.                       | -461691.                | 193.046                                | -260000.                               | -94859.                     |
|                     | +2.005<br>(2 s gma)    | +4.369                 | +1.029                                     | $\pm 4560.$                          | $\pm 4671.$                    | $\pm 1097.$             | $\pm 0.046$                            | $\pm 4671.$                            | $\pm 1097.$                 |



Prehnite

Formula weight = 412.388 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$$S^\circ = 292.745 \pm 0.659 \text{ J}/(\text{mol}\cdot\text{K}) \quad \Delta H_f^\circ = -6193.631 \pm 0.832 \text{ kJ/mol}$$

$$V^\circ = 140.326 \pm 0.650 \text{ cm}^3/\text{mol} \quad \Delta G_f^\circ = -5816.655 \pm 0.729 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 298.15 to 1250 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/[\text{J}/\text{mol}] = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 2.755226 \times 10^6 \quad a_4 = -6.270704 \times 10^3 \quad a_6 = -5.753272 \times 10^{-2}$$

$$a_2 = 1.842781 \times 10^5 \quad a_5 = 9.460222 \times 10^2 \quad a_7 = 0.0$$

$$a_3 = -1.056051 \times 10^4$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of prehnite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

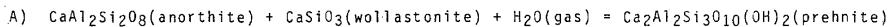
| Source                    | Data Type     | Method                            | No. of Points | Range       |
|---------------------------|---------------|-----------------------------------|---------------|-------------|
| Perkins and others (1980) | heat capacity | adiabatic calorimetry             | 8             | 200 - 298 K |
| Perkins and others (1980) | heat capacity | differential scanning calorimetry | 12            | 298 - 800 K |
| Perkins and others (1980) | entropy       | adiabatic calorimetry             | 1             | 298.15 K    |

The compositionally adjusted heat capacities that were obtained from measurements on a natural prehnite sample by Perkins and others (1980) were fit with a standard error of estimate of 0.32 J/(mol·K). The fitted entropy at 298.15 K is 292.745 ± 0.659 J/(mol·K) or a departure of 0.01 J/mol from the compositionally adjusted value of 292.75 ± 0.29 J/(mol·K) reported by Perkins and others.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source      | Method                        | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_r^\circ(298.15\text{K})$ | $\Delta H_f^\circ(298.15\text{K})$ |
|-------------|-------------------------------|-----------------------|-----------|---------------|------------------------------------|------------------------------------|
| Liou (1971) | gas-medium pressure apparatus | A                     | 708-828   | 5 pair        | -89.180 ± 0.496                    | -6193.616                          |

a Reaction:



The phase-equilibrium study of Liou (1971) (utilizing gas-medium pressure apparatus) was evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for H<sub>2</sub>O(gas) from Fisher and Zen (1971) were used in the conversion. The study cited in Table 2 complies with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated and is shown in column 6 of Table 2. From this enthalpy of reaction and the calculated enthalpies of formation of other phases in the reaction, the enthalpy of formation for prehnite (column 7 of Table 2) was calculated and can be compared with the enthalpy of formation of -6193.631 ± 0.832 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of prehnite and presents the data in their poorest perspective. Most of the phase-equilibria data cited above bracket the regression fit in free-energy space.

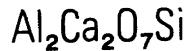
The molar volume for prehnite was taken from the study of Liou (1971).

$\text{Ca}_2\text{Al}_2\text{SiO}_7$   
Gehlenite (tetragonal, member of the Melilite Group)

$\text{Al}_2\text{Ca}_2\text{O}_7\text{Si}$

Issued September, 1979

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K)    | $S^o$<br>J/(mol·K)      | $(H_f^o - H_{f,r}^o)/T$<br>J/mol | Formation from the Elements |                            |                           | Formation from the Oxides   |                             |                          |
|--------------------|-------------------------|-------------------------|----------------------------------|-----------------------------|----------------------------|---------------------------|-----------------------------|-----------------------------|--------------------------|
|                    |                         |                         |                                  | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$           | $\Delta H_f^o, ox$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, ox$         |
| 273.15             | 195.177                 | 192.348                 | -210.688                         | -5010.                      | -3981198.                  | -3799542.                 | 726.607                     | -125045.                    | -135392.                 |
| (2 sigma)          | 205.387<br>$\pm 0.571$  | 209.891<br>$\pm 0.972$  | -209.891<br>$\pm 0.972$          | 0.<br>$\pm 0.$              | -3981707.<br>$\pm 2158.$   | -3783001.<br>$\pm 2329.$  | 652.766<br>$\pm 0.408$      | -125110.<br>$\pm 2458.$     | -137428.<br>$\pm 2329.$  |
| 300.               | 206.095                 | 211.163                 | -212.895                         | 381.                        | -398138.                   | -3781768.                 | 658.464                     | -125116.                    | -137504.                 |
| 350.               | 223.063                 | 244.258                 | -212.466                         | 11126.                      | -398221.                   | -378392.                  | 559.416                     | -125302.                    | -139555.                 |
| 400.               | 236.577                 | 274.959                 | -218.386                         | 2263.                       | -398209.                   | -3714983.                 | 435.127                     | -125531.                    | -14156.                  |
| 450.               | 247.476                 | 303.476                 | -226.275                         | 34746.                      | -3981819.                  | -3681500.                 | 427.349                     | -12792.                     | -14356.                  |
| 500.               | 256.370                 | 330.026                 | -235.338                         | 47344.                      | -3981176.                  | -368274.                  | 381.132                     | -126086.                    | -145526.                 |
| (2 sigma)          | 261.044                 | 330.026<br>$\pm 1.044$  | -235.338<br>$\pm 1.044$          | 4161..<br>$\pm 0.975$       | -3981274.<br>$\pm 2187.$   | -368274.<br>$\pm 2253.$   | 381.132<br>$\pm 0.235$      | -126086.<br>$\pm 2253.$     | -145526.<br>$\pm 0.235$  |
| 550.               | 263.707                 | 354.815                 | -245.085                         | 60351.                      | -3980375.                  | -3615022.                 | 343.326                     | -126418.                    | -147454.                 |
| 600.               | 269.821                 | 378.031                 | -255.207                         | 73694.                      | -3979491.                  | -3581347.                 | 311.827                     | -126794.                    | -149350.                 |
| 650.               | 274.966                 | 399.837                 | -265.502                         | 8731..                      | -3978587.                  | -3544747.                 | 285.181                     | -127220.                    | -15020.                  |
| /00.               | 279.336                 | 420.378                 | -275.839                         | 101178.                     | -3977715.                  | -3515715.                 | 262.346                     | -127699.                    | -153041.                 |
| 750.               | 282.086                 | 439.782                 | -286.127                         | 115241..                    | -3978590.                  | -3482670.                 | 242.555                     | -128236.                    | -154832.                 |
| (2 sigma)          | 287.138                 | 439.782<br>$\pm 1.138$  | -286.127<br>$\pm 1.178$          | 115241..<br>$\pm 1.178$     | -3978590.                  | -3482670.<br>$\pm 2166.$  | 242.555<br>$\pm 0.151$      | -128236.<br>$\pm 2166.$     | -154832.<br>$\pm 0.151$  |
| 800.               | 286.336                 | 458.158                 | -296.310                         | 129478.                     | -3977689.                  | -3449539.                 | 225.238                     | -128833.                    | -155586.                 |
| 850.               | 289.184                 | 475.004                 | -306.348                         | 134866.                     | -3977601.                  | -3416659.                 | 209.962                     | -130209.                    | -153266.                 |
| 900.               | 291.711                 | 492.206                 | -316.216                         | 153391.                     | -3976447.                  | -3383711.                 | 196.385                     | -130507.                    | -153939.                 |
| 950.               | 293.982                 | 508.040                 | -325.899                         | 173034..                    | -397856.                   | -3353390.                 | 184.217                     | -130802.                    | -161566.                 |
| (1000.             | 296.051                 | 523.173                 | -335.387                         | 187786.                     | -3977647.                  | -3316319.                 | 173.227                     | -131097.                    | -163118.                 |
| (2 sigma)          | 298.884                 | 523.173<br>$\pm 1.884$  | -335.387<br>$\pm 1.226$          | 187786.<br>$\pm 1.026$      | -3977647.<br>$\pm 2103.$   | -3316319.<br>$\pm 2103.$  | 173.227<br>$\pm 0.110$      | -131097.<br>$\pm 2103.$     | -163118.<br>$\pm 0.110$  |
| 1050.              | 297.965                 | 537.664                 | -344.676                         | 202637..                    | -3977596.                  | -3282255.                 | 163.283                     | -131392.                    | -164775.                 |
| 1100.              | 299.763                 | 551.567                 | -353.767                         | 217581..                    | -3997709.                  | -3248189.                 | 154.244                     | -131392.                    | -166357.                 |
| 1150.              | 301.477                 | 564.930                 | -362.659                         | 23261..                     | -4013731.                  | -3213554.                 | 145.364                     | -131392.                    | -167927.                 |
| 1200.              | 302.136                 | 577.996                 | -371.357                         | 262925..                    | -4012289.                  | -312288.                  | 138.369                     | -132583.                    | -169433.                 |
| 1250.              | 304.764                 | 590.204                 | -379.864                         | 2798..                      | -4010804.                  | -3144095.                 | 131.384                     | -132583.                    | -171027.                 |
| (2 sigma)          | 306.383                 | 602.188                 | -388.186                         | 273204..                    | -402455.                   | -2971497.                 | 103.477                     | -132645..<br>$\pm 0.087$    | -171027..<br>$\pm 0.087$ |
| 1300.              | 308.011                 | 613.182                 | -396.328                         | 293563..                    | -4009276..                 | -3109457.                 | 124.939                     | -132879.                    | -172558..                |
| 1350.              | 309.664                 | 625.013                 | -401.295                         | 309005..                    | -4007701..                 | -304378.                  | 118.974                     | -133171..                   | -174059..                |
| 1400.              | 311.358                 | 635.909                 | -412.095                         | 324531..                    | -4004395..                 | -3005399.                 | 113.437                     | -134455..                   | -175559..                |
| 1450.              | 313.104                 | 646.494                 | -419.733                         | 340142..                    | -4002656..                 | -2971497.                 | 108.284                     | -133731..                   | -177059..                |
| (2 sigma)          | 313.847                 | 646.494<br>$\pm 3.847$  | -419.733<br>$\pm 1.312$          | 340142..<br>$\pm 1.062$     | -4002656..<br>$\pm 2645.$  | -2971497..<br>$\pm 2102.$ | 103.477<br>$\pm 0.073$      | -133731..<br>$\pm 2102.$    | -177059..<br>$\pm 0.073$ |
| 1550.              | 314.914                 | 656.790                 | -427.215                         | 355842..                    | -4000853..                 | -2937155.                 | 98.981                      | -134241..                   | -180061..                |
| 1600.              | 316.798                 | 666.818                 | -431.546                         | 37163..                     | -3998978..                 | -2902372.                 | 94.769                      | -134469..                   | -181556..                |
| 1650.              | 318.765                 | 676.996                 | -441.733                         | 38752..                     | -3997028..                 | -2866548.                 | 90.814                      | -134674..                   | -183030..                |
| 1700.              | 320.823                 | 686.142                 | -448.782                         | 403512..                    | -4045503..                 | -2834035.                 | 87.079                      | -134852..                   | -184465..                |
| 1750.              | 322.980                 | 695.473                 | -455.698                         | 41960..                     | -4043237..                 | -2798437.                 | 83.529                      | -135056..                   | -185922..                |
| (2 sigma)          | 325.241                 | 704.603                 | -466.485                         | 435810..                    | -4346538..                 | -2756057..                | 79.950                      | -135112..                   | -187375..                |
| 1800.              | 325.241                 | 704.603                 | -466.485                         | 435810..                    | -4346538..                 | -2756057..                | 79.950                      | -135112..                   | -187375..                |
| (2 sigma)          | 325.241<br>$\pm 11.442$ | 704.603<br>$\pm 11.442$ | -466.485<br>$\pm 1.753$          | 435810..<br>$\pm 2313.$     | -4346538..<br>$\pm 3367.$  | -2756057..<br>$\pm 2191.$ | 79.950                      | -135112..<br>$\pm 3367.$    | -187375..<br>$\pm 2191.$ |

Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>

Gehlenite

Formula weight = 274.204 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 209.89 \pm 0.97 \text{ J/(mol}\cdot\text{K)} \quad \Delta H_f^\circ = -3981.7 \pm 2.5 \text{ kJ/mol}$$

$$V^\circ = 90.24 \pm 0.18 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -3783.0 \pm 2.3 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1800 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^{2/2}$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^{3/3}$$

$$a_1 = 1.51047 \times 10^6 \quad a_4 = -3.82222 \times 10^3 \quad a_6 = -6.71533 \times 10^{-2}$$

$$a_2 = 5.19543 \times 10^4 \quad a_5 = 5.88351 \times 10^2 \quad a_7 = 3.89086 \times 10^{-5}$$

$$a_3 = -6.27433 \times 10^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of gehlenite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                     | Data Type         | Method                 | No. of Points | Range        |
|----------------------------|-------------------|------------------------|---------------|--------------|
| Weller and Kelley (1963)   | heat capacity     | isothermal calorimeter | 10            | 206 - 296 K  |
| Pankratz and Kelley (1964) | relative enthalpy | drop calorimeter       | 15            | 402 - 1801 K |
| Hemingway and Robie (1977) | entropy           | adiabatic calorimeter  | 1             | 298.15 K     |

The standard error of estimate of the fitted heat-capacity data of Weller and Kelley (1963) for synthetic gehlenite is 0.14 J/(mol·K). The standard error of estimate of the fitted relative enthalpy measurements of Pankratz and Kelley (1964) is 420 J/(mol·K) or approximately 0.2 percent of the observed value. Hemingway and Robie (1977) calculated an entropy for gehlenite from the low-temperature heat-capacity data of Weller and Kelley (1963) after correcting their temperature scale. The fitted entropy at 298.15 K is 209.89 ± 0.97 J/(mol·K) or a departure of 0.09 from the experimental value of 209.8 ± 0.4 J/(mol·K) determined by Hemingway and Robie.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                             | Method                          | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H^\circ(298.15\text{ K})$ | $\Delta H_f^\circ(298.15\text{ K})$ |
|------------------------------------|---------------------------------|-----------------------|-----------|---------------|-----------------------------------|-------------------------------------|
| Shmulovich (1974)                  | gas-medium pressure apparatus   | A                     | 1133-1153 | 1 pair        | 159.942±1.763                     | -3980.604                           |
| Huckenholz (1974)                  | unspecified                     | A                     | 1125-1423 | 6 pair        | 158.750±2.236                     | -3982.796                           |
| Hays (1965)                        | solid-medium pressure apparatus | A                     | 1473-1523 | 2 pair        | 156.099±6.608                     | -3984.447                           |
| Hays (1965)                        | solid-medium pressure apparatus | B                     | 1473-1673 | 4 pair        | -11.814±1.953                     | -3981.555                           |
| Boettcher (1970)                   | gas-medium pressure apparatus   | C                     | 1033-1053 | 2 pair        | -102.037±0.996                    | -3982.169                           |
| Huckenholz (1974)                  | unspecified                     | C                     | 1028-1263 | 3 pair        | -102.895±1.257                    | -3981.311                           |
| Kay and Taylor (1960) <sup>b</sup> | silica activity                 | D                     | 1653      | 1             | 83.137±2.584                      | -3981.557                           |
| Kay and Taylor (1960) <sup>b</sup> | silica activity                 | E                     | 1643      | 1             | 59.386±2.412                      | -3985.876                           |

## a Reactions:

- A) 2 Ca<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>(grossular) = CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + 3 CaSiO<sub>3</sub>(wollastonite) + Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>(gehlenite)
- B) CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>(gehlenite) + Al<sub>2</sub>O<sub>3</sub>(corundum) = 3 CaAl<sub>2</sub>SiO<sub>6</sub>(clinopyroxene)
- C) CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>(gehlenite) = Ca<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>(grossular) + Al<sub>2</sub>O<sub>3</sub>(corundum)
- D) 2 CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) = Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>(gehlenite) + Al<sub>2</sub>O<sub>3</sub>(corundum) + 3 SiO<sub>2</sub>(cristobalite, beta)
- E) CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + CaSiO<sub>3</sub>(cyclo wollastonite) = Ca<sub>2</sub>Al<sub>2</sub>SiO<sub>7</sub>(gehlenite) + 2 SiO<sub>2</sub>(cristobalite, beta)

b Kay and Taylor (1960) determined the activity of silica in the silicate liquid for the lime-alumina-silica system. Using the silica activity from their study and the measured temperatures and compositions of the silicate melts in equilibrium with either anorthite, gehlenite, and corundum or anorthite, cyclo wollastonite, and gehlenite, we obtained the equilibrium constants for reactions D and E at the melt temperature and 101.325 kPa.

Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for H<sub>2</sub>O(gas) from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for gehlenite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of -3981.707±2.458 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of gehlenite and presents the data in their poorest perspective.

Most of the phase-equilibria data cited above bracket the regression fit in free-energy space. However, the phase-equilibria studies lack sufficient precision to constrain the fit tightly, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate. However, the phase-equilibria studies have sufficient precision to indicate that they are incompatible with the enthalpy of formation of gehlenite at 298.15 K of -4007.570 ± 2.820 kJ/mol calculated from the enthalpy of solution measurements of Barany (1963). The sample-preparation procedure of Barany (1963) may have produced a contaminated sample, and his data were not used here.

The molar volume of gehlenite was obtained from the compilation of Robie and others (1967).

$\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12$   
Grossular (cubic, member of the Garnet Group)

$\text{Al}_2\text{Ca}_3\text{O}_{12}\text{Si}_3$

Issued September, 1979

| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K)   | $S^o$<br>J/(mol·K)      | $(G_T^o - H_{T,r}^o)/T$<br>J/(mol·K) | $H_T^o - H_{T,r}^o$<br>J/mol | Formation from the Elements       |                                   |                         |                                    | $\Delta G_f^o, \epsilon$<br>J/mol | $\log K_f^o, \epsilon$ | $\Delta H_f^o, \text{ox}$<br>J/mol | $-\log K_f^o, \text{ox}$ |
|---------------------|------------------------|-------------------------|--------------------------------------|------------------------------|-----------------------------------|-----------------------------------|-------------------------|------------------------------------|-----------------------------------|------------------------|------------------------------------|--------------------------|
|                     |                        |                         |                                      |                              | $\Delta H_f^o, \epsilon$<br>J/mol | $\Delta G_f^o, \epsilon$<br>J/mol | $\log K_f^o, \epsilon$  | $\Delta H_f^o, \text{ox}$<br>J/mol |                                   |                        |                                    |                          |
| 273.15              | 310.918                | 227.878                 | -257.251                             | -8023.                       | -6635402.                         | -6305187.                         | 1205.744                | -322988.                           | -314053.                          | 60.057                 |                                    |                          |
| 298.15<br>(2 sigma) | 330.509<br>$\pm 0.149$ | 255.971<br>$\pm 2.946$  | -255.971<br>$\pm 2.946$              | 0.<br>$\pm 0$                | -6636338.<br>$\pm 2383.$          | -6274919.<br>$\pm 2383.$          | 1039.339<br>$\pm 0.453$ | -323240.<br>$\pm 2383.$            | -312244.<br>$\pm 2383.$           | 54.875<br>$\pm 0.453$  |                                    |                          |
| 300.                | 331.858                | 258.020                 | -255.978                             | 613.                         | -6636393.                         | -6272675.                         | 1092.169                | -323267.                           | -313161.                          | 54.526                 |                                    |                          |
| 350.                | 363.923                | 311.687                 | -260.142                             | 18041.                       | -6637245.                         | -6211974.                         | 922.086                 | -323366.                           | -311444.                          | 46.480                 |                                    |                          |
| 400.                | 389.093                | 361.991                 | -269.164                             | 36891.                       | -6637106.                         | -6151220.                         | 803.266                 | -323956.                           | -309677.                          | 40.440                 |                                    |                          |
| 450.                | 409.151                | 409.021                 | -282.654                             | 56865.                       | -6636253.                         | -6090523.                         | 706.970                 | -324426.                           | -307819.                          | 35.737                 |                                    |                          |
| 500.<br>(2 sigma)   | 425.320<br>$\pm 0.159$ | 452.996<br>$\pm 2.947$  | -297.514<br>$\pm 2.946$              | 77741.<br>$\pm 24.$          | -6634901.<br>$\pm 2247.$          | -6029662.<br>$\pm 2247.$          | 629.945<br>$\pm 0.235$  | -324426.<br>$\pm 2247.$            | -306053.<br>$\pm 2247.$           | 31.973<br>$\pm 0.235$  |                                    |                          |
| 550.                | 438.472                | 494.171                 | -313.540                             | 99347.                       | -6633217.                         | -5969548.                         | 566.940                 | -324705.                           | -304203.                          | 28.891                 |                                    |                          |
| 600.                | 449.239                | 532.800                 | -330.219                             | 121549.                      | -6633337.                         | -5909255.                         | 514.450                 | -325069.                           | -302333.                          | 26.320                 |                                    |                          |
| 650.                | 458.092                | 569.120                 | -347.213                             | 146239.                      | -6633737.                         | -5849255.                         | 470.048                 | -325551.                           | -300409.                          | 24.141                 |                                    |                          |
| 700.                | 465.391                | 603.344                 | -364.298                             | 167332.                      | -667416.                          | -5789256.                         | 432.000                 | -326179.                           | -29853.                           | 22.271                 |                                    |                          |
| 750.<br>(2 sigma)   | 471.415<br>$\pm 0.602$ | 635.664<br>$\pm 2.937$  | -381.322<br>$\pm 2.945$              | 190757.<br>$\pm 83.$         | -6628051.<br>$\pm 23216.$         | -5729355.<br>$\pm 2004.$          | 339.027<br>$\pm 0.140$  | -326974.<br>$\pm 2004.$            | -29646.<br>$\pm 2004.$            | 20.646<br>$\pm 0.140$  |                                    |                          |
| 800.                | 476.384                | 666.253                 | -398.183                             | 214456.                      | -6626003.                         | -5669510.                         | 370.181                 | -327958.                           | -294319.                          | 19.221                 |                                    |                          |
| 850.                | 480.473                | 695.260                 | -414.812                             | 238381.                      | -662462.                          | -5609784.                         | 344.735                 | -32910.                            | -289938.                          | 17.958                 |                                    |                          |
| 900.                | 483.826                | 722.821                 | -431.165                             | 262491.                      | -6622868.                         | -550151.                          | 322.122                 | -331431.                           | -289938.                          | 16.827                 |                                    |                          |
| 950.                | 486.559                | 749.056                 | -447.211                             | 286753.                      | -6643366.                         | -5490192.                         | 301.872                 | -331597.                           | -28768.                           | 15.814                 |                                    |                          |
| 1000.<br>(2 sigma)  | 498.769<br>$\pm 1.190$ | 774.072<br>$\pm 2.928$  | -462.933<br>$\pm 2.939$              | 311138.<br>$\pm 294.$        | -6662485.<br>$\pm 23211.$         | -5429523.<br>$\pm 2015.$          | 233.609<br>$\pm 0.105$  | -331813.<br>$\pm 105.$             | -285258.<br>$\pm 2015.$           | 14.902<br>$\pm 0.095$  |                                    |                          |
| 1050.               | 490.538                | 797.963                 | -478.323                             | 335622.                      | -6661917.                         | -5368830.                         | 267.087                 | -323094.                           | -282955.                          | 14.077                 |                                    |                          |
| 1100.               | 491.933                | 820.816                 | -493.375                             | 360186.                      | -6641676.                         | -5308277.                         | 252.069                 | -332454.                           | -280618.                          | 13.325                 |                                    |                          |
| 1150.               | 493.013                | 842.709                 | -508.091                             | 384811.                      | -665387.                          | -5246826.                         | 238.318                 | -332905.                           | -27822.                           | 12.639                 |                                    |                          |
| 1200.               | 493.827                | 863.709                 | -522.474                             | 409483.                      | -6660370.                         | -5185201.                         | 222.706                 | -331597.                           | -27584.                           | 12.008                 |                                    |                          |
| 1250.               | 494.419                | 883.881                 | -536.529                             | 434190.                      | -6660657.                         | -5123674.                         | 214.106                 | -334114.                           | -273452.                          | 11.427                 |                                    |                          |
| (2 sigma)           | $\pm 1.531$            | $\pm 2.947$             | $\pm 2.933$                          | $\pm 630.$                   | $\pm 3233.$                       | $\pm 2276.$                       | $\pm 0.095$             | $\pm 3233.$                        | $\pm 2276.$                       | $\pm 0.095$            |                                    |                          |
| 1300.               | 494.826                | 903.281                 | -550.264                             | 458921.                      | -6658360.                         | -5062240.                         | 203.403                 | -334888.                           | -271010.                          | 10.889                 |                                    |                          |
| 1350.               | 495.080                | 921.961                 | -563.87                              | 483670.                      | -6661115.                         | -500894.                          | 193.496                 | -335784.                           | -26857.                           | 10.390                 |                                    |                          |
| 1400.               | 495.209                | 939.968                 | -576.806                             | 508427.                      | -66613923.                        | -4939630.                         | 184.300                 | -336808.                           | -266038.                          | 9.926                  |                                    |                          |
| 1450.               | 495.239                | 957.347                 | -589.630                             | 53189.                       | -6661784.                         | -4878443.                         | 177.740                 | -337963.                           | -263400.                          | 9.492                  |                                    |                          |
| 1500.<br>(2 sigma)  | 495.192<br>$\pm 1.687$ | 974.135<br>$\pm 2.992$  | -602.169<br>$\pm 2.929$              | 557950.<br>$\pm 1002.$       | -6649699.<br>$\pm 3300.$          | -481729.<br>$\pm 219.$            | 167.754<br>$\pm 0.095$  | -339253.<br>$\pm 3300.$            | -260800.<br>$\pm 219.$            | 9.085<br>$\pm 0.095$   |                                    |                          |
| 1550.               | 495.087                | 990.371                 | -614.431                             | 582707.                      | -6647666.                         | -4756284.                         | 160.286                 | -340681.                           | -258255.                          | 8.703                  |                                    |                          |
| 1600.               | 494.942                | 1006.087                | -626.126                             | 607458.                      | -6655684.                         | -4695303.                         | 153.286                 | -342251.                           | -255571.                          | 8.344                  |                                    |                          |
| 1650.               | 494.772                | 1021.315                | -638.163                             | 63201.                       | -6653750.                         | -4634334.                         | 146.712                 | -343963.                           | -252856.                          | 8.004                  |                                    |                          |
| 1700.               | 494.592                | 1036.083                | -649.650                             | 656935.                      | -67533388.                        | -4572113.                         | 140.486                 | -345819.                           | -25007.                           | 7.683                  |                                    |                          |
| 1750.<br>(2 sigma)  | 494.414<br>$\pm 2.223$ | 1050.417<br>$\pm 3.046$ | -660.897<br>$\pm 2.929$              | 681660.<br>$\pm 1356.$       | -6791115.<br>$\pm 3309.$          | -4506816.<br>$\pm 3278.$          | 131.523<br>$\pm 0.098$  | -347820.<br>$\pm 3278.$            | -24722.                           | 7.377                  |                                    |                          |
| 1800.<br>(2 sigma)  | 494.250<br>$\pm 2.440$ | 1064.343<br>$\pm 3.058$ | -671.911<br>$\pm 2.930$              | 706377.<br>$\pm 1428.$       | -727367.<br>$\pm 3437.$           | -442973.<br>$\pm 3399.$           | 126.551<br>$\pm 0.099$  | -349968.<br>$\pm 3437.$            | -244297.                          | 7.089<br>$\pm 0.099$   |                                    |                          |

Ca<sub>3</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>12</sub>

Grossular

Formula weight = 450.452 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 256.00 \pm 2.90 \text{ J/(mol·K)} \quad \Delta H_f^\circ = -6636.3 \pm 3.2 \text{ kJ/mol}$$

$$V^\circ = 125.30 \pm 0.06 \text{ cm}^3/\text{mol} \quad \Delta G_f^\circ = -6274.9 \pm 2.6 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1600 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol} \cdot \text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol} \cdot \text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 1.77080 \times 10^6 \quad a_4 = -6.53238 \times 10^3 \quad a_6 = -9.66435 \times 10^{-2}$$

$$a_2 = 9.02292 \times 10^4 \quad a_5 = 9.05002 \times 10^2 \quad a_7 = 3.35314 \times 10^{-5}$$

$$a_3 = -1.07077 \times 10^4$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of grossular.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

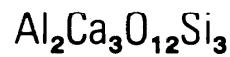
| Source                        | Data Type     | Method                            | No. of Points | Range         |
|-------------------------------|---------------|-----------------------------------|---------------|---------------|
| Westrum and others (1979)     | heat capacity | adiabatic calorimeter             | 57            | 200 - 596 K   |
| Krupka and others (1979)      | heat capacity | differential scanning calorimeter | 50            | 350 - 978 K   |
| Estimated values <sup>a</sup> | heat capacity | component summation               | 11            | 1000 - 1800 K |
| Westrum and others (1979)     | entropy       | adiabatic calorimeter             | 1             | 298.15        |

a Above 1000 K, the heat capacity of grossular was estimated by totaling the average heat capacities of CaO-, SiO<sub>2</sub>-, (Al<sup>IV</sup>)<sub>2</sub>O<sub>3</sub>-, and (Al<sup>VI</sup>)<sub>2</sub>O<sub>3</sub>-components derived from a number of sodium, potassium, and calcium aluminum silicates. (Al<sup>IV</sup>) and (Al<sup>VI</sup>) represent aluminum in tetrahedral and octahedral coordination.

The standard error of estimate of the fitted heat capacity of Westrum and others (1979) on a natural grossular and Krupka and others (1979) on a synthetic grossular is 0.84 and 6.4 J/(mol·K), respectively. The estimated heat-capacity values above 1000 K is a smooth extension of the data of Krupka and others (1979). The estimated heat capacity was fit with a standard error of estimate of 2.7 J/(mol·K). Westrum and others derived an entropy for grossular at 298.15 K of 254.68 ± 1.26 J/(mol·K), which has a departure of 1.32 from the fitted value of 256.0 ± 2.9 J/(mol·K). Haselton and Westrum (1979) reported heat-capacity data on synthetic grossular and obtained an entropy of 260.12 J/(mol·K) at 298.15 K. Neither the heat capacity nor entropy reported by Haselton and Westrum were used because the entropy is inconsistent with the phase-equilibria studies.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                                   | Reaction <sup>a</sup> | Range T/K  | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta G_f^\circ(298.15 \text{ K})$ |
|---------------------------------------|--|-----------------------|------------|---------------|--------------------------------------|--------------------------------------|
| Charlu and others (1978) <sup>b</sup> | solution calorimetry<br>(borate salt)    | A                     | 970        | 2             | -316.703 ± 5.089                     | -6642.885                            |
| Boettcher (1970)                      | gas-medium pressure apparatus            | B                     | 898-928    | 1 pair        | -318.334 ± 5.146                     | -6641.254                            |
| Newton (1965)                         | gas- and solid-medium pressure apparatus | B                     | 843-1113   | 6 pair        | -308.308 ± 4.088                     | -6635.093                            |
| Boettcher (1970)                      | gas- and solid-medium pressure apparatus | C                     | 853-933    | 2 pair        | -306.468 ± 2.790                     | -6636.013                            |
| Strens (1968)                         | medium apparatus                         | C                     | 770-823    | 1 pair        | -213.025 ± 2.944                     | -6639.311                            |
| Shmulovich (1974)                     | gas-medium pressure apparatus            | D                     | 1133-1153  | 1 pair        | -220.561 ± 5.976                     | -6631.774                            |
| Huckenholz (1974)                     | unspecified                              | D                     | 1125-1423  | 6 pair        | -159.942 ± 1.763                     | -6636.890                            |
| Hays (1965)                           | solid-medium pressure apparatus          | D                     | 11473-1523 | 2 pair        | -158.750 ± 2.236                     | -6636.294                            |
| Huckenholz (1974)                     | unspecified                              | E                     | 848-858    | 1 pair        | -156.099 ± 0.608                     | -6634.968                            |
| Newton (1966b)                        | gas-medium pressure apparatus            | E                     | 803-923    | 2 pair        | -49.366 ± 0.328                      | -6636.033                            |
| Huckenholz (1974)                     | unspecified                              | F                     | 888-958    | 2 pair        | -50.708 ± 3.042                      | -6637.375                            |
| Newton (1966b)                        | solid-medium pressure apparatus          | F                     | 973-1023   | 2 pair        | -50.101 ± 0.499                      | -6636.199                            |
| Boettcher (1970)                      | gas-medium pressure apparatus            | F                     | 893-1053   | 2 pair        | -49.103 ± 1.867                      | -6635.201                            |
| Huckenholz (1974)                     | unspecified                              | G                     | 1028-1263  | 3 pair        | -50.328 ± 1.454                      | -6636.426                            |
| Boettcher (1970)                      | gas-medium pressure apparatus            | G                     | 1033-1053  | 1 pair        | -102.895 ± 1.751                     | -6636.736                            |



## a Reactions:

- A)  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) = 3 CaO(lime) + Al<sub>2</sub>O<sub>3</sub>(corundum) + 3 SiO<sub>2</sub>(quartz, beta)  
 B) 2  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) + 6 CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + Al<sub>2</sub>O<sub>3</sub>(corundum) + 3 H<sub>2</sub>O(gas)  
     = 6 Ca<sub>2</sub>Al<sub>3</sub>Si<sub>3</sub>O<sub>12</sub>(OH)(zoisite)  
 C)  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) + 5 CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + 2 H<sub>2</sub>O(gas)  
     = 4 Ca<sub>2</sub>Al<sub>3</sub>Si<sub>3</sub>O<sub>12</sub>(OH)(zoisite) + SiO<sub>2</sub>(quartz, alpha)  
 D) 2  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) = CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + 3 CaSiO<sub>3</sub>(wollastonite) + Ca<sub>2</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>7</sub>(gehlenite)  
 E) 2 CaSiO<sub>3</sub>(wollastonite) + CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) =  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) + SiO<sub>2</sub>(quartz, alpha)  
 F) 2 CaSiO<sub>3</sub>(wollastonite) + CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) =  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) + SiO<sub>2</sub>(quartz, beta)  
 G) CaAl<sub>2</sub>Si<sub>2</sub>O<sub>8</sub>(anorthite) + Ca<sub>2</sub>Al<sub>2</sub>Si<sub>3</sub>O<sub>7</sub>(gehlenite) =  $\text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{12}$ (grossular) + Al<sub>2</sub>O<sub>3</sub>(corundum)

b Charlu and others (1978) measured the enthalpy of solution of two samples of synthetic grossular in lead borate salt melt at 970 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of lime, quartz, and corundum in the salt melt; corrections were not made for the enthalpies of dilution and of mixing of the product melts.

Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for H<sub>2</sub>O(gas) from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for grossular (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of -6636.338±3.220 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of grossular and presents the data in their poorest perspective.

Most of the phase-equilibria data cited above bracket the regression fit in free-energy space. However, the phase-equilibria studies lack sufficient precision to constrain the fit tightly, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate.

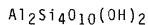
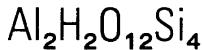
The molar volume of grossular was obtained from the compilation of Robie and others (1967).

$\text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2$   
Pyrophyllite (monoclinic)

$\text{Al}_2\text{H}_2\text{O}_{12}\text{Si}_4$

Issued September, 1979

| Temperature<br>(K)                                     | $C_p^{\circ}$<br>J/(mol·K)   | $S^{\circ}$<br>J/(mol·K)  | $(G_f^{\circ}-H_f^{\circ})/T$<br>J/(mol·K)   | $H_f^{\circ}-H_{f_r}^{\circ}$<br>J/mol   | Formation from the Elements   |  | Formation from the Oxides  |  |
|--|--|---|--|--|---|--|--|--|
|  |  |   |  |  | $\Delta G_f^{\circ}, e$<br>J/mol  | $\log K_f^{\circ}, e$<br>J/mol   | $\Delta G_f^{\circ}, \text{ox}$<br>J/mol   | $\log K_f^{\circ}, \text{ox}$<br>J/mol                             |
| 273.15   | 275.556  | 214.466   | -240.562   | -7128.   | -5640881.   | -5299642.  | 1013.453   | -36683.  |
| 298.15<br>(2 sigma)                                    | 294.349<br>$\pm 0.318$   | 239.424<br>$\pm 0.992$  | -239.424<br>$\pm 0.992$  | 0.<br>$\pm 0.$   | -5642023.<br>$\pm 1158.$  | -5263357.<br>$\pm 1043.$   | 922.994<br>$\pm 0.183$   | -37708.<br>$\pm 1158.$   |
| 300.<br>350.<br>400.<br>450.<br>500.<br>(2 sigma)      | 295.656<br>327.053<br>351.979<br>372.025<br>383.509<br>$\pm 1.312$   | 241.249<br>289.276<br>334.638<br>377.293<br>417.369<br>$\pm 1.03$                                       | -239.429<br>-243.150<br>-251.780<br>-263.380<br>-276.796<br>$\pm 0.994$  | 546.<br>16144.<br>33143.<br>51261.<br>70287.<br>$\pm 121.$   | -5642094.<br>-5643428.<br>-5643786.<br>-5643393.<br>-5642421.<br>$\pm 1170.$              | -5266038.<br>-5203441.<br>-5140322.<br>-5077406.<br>-5014666.<br>$\pm 1007.$ | 916.998<br>776.541<br>671.257<br>589.370<br>523.868<br>$\pm 105.$                      | -37781.<br>-39506.<br>-81004.<br>-80498.<br>-79981.<br>$\pm 1170.$ |
| 550.<br>600.<br>650.<br>700.<br>750.<br>(2 sigma)      | 402.465<br>411.699<br>422.837<br>435.374<br>446.704<br>$\pm 9.594$   | 455.069<br>490.623<br>524.262<br>556.208<br>586.667<br>$\pm 1.013$                                      | -291.306<br>-306.449<br>-321.921<br>-337.525<br>-353.127<br>$\pm 1.013$  | 90070.<br>110504.<br>131521.<br>153078.<br>175155.<br>$\pm 806.$   | -5640993.<br>-5639196.<br>-5637085.<br>-5634694.<br>-5632033.<br>$\pm 1417.$              | -4951846.<br>-4889274.<br>-4826664.<br>-4764427.<br>-4702970.<br>$\pm 1023.$ | 470.287<br>425.659<br>387.591<br>355.541<br>327.516<br>$\pm 0.71$                      | -79504.<br>-79092.<br>-7853.<br>-7848.<br>-7845.<br>$\pm 117.$     |
| 800.<br>850.<br>900.<br>950.<br>1000.<br>(2 sigma)     | 457.143<br>467.948<br>473.332<br>491.469<br>504.506<br>$\pm 4.080$   | 515.828<br>543.864<br>570.930<br>597.168<br>722.704<br>$\pm 7.811$                                      | -368.640<br>-384.011<br>-399.203<br>-411.198<br>-428.988<br>$\pm 1.401$  | 197750.<br>220876.<br>244555.<br>268821.<br>293717.<br>$\pm 6808.$   | -5629101.<br>-5625882.<br>-5622349.<br>-563980.<br>-563543.<br>$\pm 6890.$                | -4640700.<br>-4579022.<br>-4517443.<br>-4453716.<br>-4393670.<br>$\pm 1470.$ | 303.006<br>281.392<br>262.191<br>245.001<br>229.502<br>$\pm 0.077$                     | -78023.<br>-80638.<br>-78612.<br>-76190.<br>-73333.<br>$\pm 6830.$ |
| 1050.<br>1150.<br>1250.<br>1250.<br>1250.<br>(2 sigma) | 513.566<br>533.754<br>551.161<br>567.863<br>585.927<br>$\pm 113.181$ | 747.655<br>772.125<br>-457.950<br>796.208<br>-472.135<br>319.932<br>343.555<br>-499.960<br>$\pm 24.351$ | 319289.<br>345592.<br>-5624619.<br>-5618218.<br>-4208653.<br>-5611065.<br>-4144744.<br>-4086000.<br>-429494.<br>$\pm 25776.$ | -4431705.<br>-4231105.<br>-4263996.<br>-191.159<br>-180.533<br>-170.770<br>-167.466<br>-167.466<br>$\pm 4859.$ | -69957.<br>-66035.<br>-66035.<br>-61493.<br>-56264.<br>-50279.<br>-50279.<br>$\pm 25776.$ | 215.490<br>202.765<br>191.159<br>180.533<br>170.770<br>167.466<br>$\pm 203$  | 88211.<br>95653.<br>102903.<br>109941.<br>109941.<br>116746.<br>116746.<br>$\pm 4859.$ |  |



## Pyrophyllite

Formula weight = 360.314 g/mol

## Summary of Critical Data

## Data at Reference Temperature, 298.15 K (±2s)

$$S^\circ = 239.424 \pm 0.992 \text{ J/(mol·K)}$$

$$\Delta H_f^\circ = -5642.023 \pm 1.158 \text{ kJ/mol}$$

$$V^\circ = 127.82 \pm 0.29 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -5268.357 \pm 1.043 \text{ kJ/mol}$$

## Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1000 K)

$$C_p(T)/[\text{J}/(\text{mol·K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol·K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/[\text{J}/\text{mol}] = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 6.069358 \times 10^6 \quad a_4 = -9.850236 \times 10^3 \quad a_6 = -3.960932 \times 10^{-1}$$

$$a_2 = 2.311270 \times 10^5 \quad a_5 = 1.454512 \times 10^3 \quad a_7 = 3.971889 \times 10^{-4}$$

$$a_3 = -1.774285 \times 10^4$$

## Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of pyrophyllite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                   | Data Type     | Method                            | No. of Points | Range       |
|--------------------------|---------------|-----------------------------------|---------------|-------------|
| Robie and others (1976)  | heat capacity | adiabatic calorimetry             | 20            | 200 - 370 K |
| Krupka and others (1979) | heat capacity | differential scanning calorimetry | 48            | 335 - 680 K |
| Robie and others (1976)  | entropy       | adiabatic calorimetry             | 1             | 298.15 K    |

The heat-capacity measurements of Robie and others (1976) and Krupka and others (1979) were fit with standard errors of estimate of 0.31 and 2.0 J/(mol·K), respectively. The fitted entropy at 298.15 K is  $239.424 \pm 0.992$  J/(mol·K), which agrees with the experimental value of  $239.4 \pm 0.4$  reported by Robie and others (1976).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                    | Method                                 | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---|--|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
|   |  |                       |           |               | Third Law, kJ                        | kJ/mol                               |
| Hemley and others (in press) <sup>b</sup> | $\text{H}_4\text{SiO}_4$ concentration | A                     | 523-598   | 4             | -1.678 ± 1.644                       | -5643.386                            |
| Hemley and others (in press) <sup>b</sup> | $\text{H}_4\text{SiO}_4$ concentration | B                     | 613-673   | 11            | -78.080 ± 1.616                      | -5642.283                            |
| Haas and Holdaway (1973)                  | gas-medium pressure apparatus          | B                     | 643-737   | 4             | -76.968 ± 0.615                      | -5642.872                            |
| Kerrick (1968)                            | gas-medium pressure apparatus          | B                     | 668-718   | 2             | -79.382 ± 1.273                      | -5643.589                            |
| Hemley and others (in press) <sup>b</sup> | $\text{H}_4\text{SiO}_4$ concentration | C                     | 473-573   | 10            | 57.792 ± 0.323                       | -5642.550                            |
| Haas and Holdaway (1973)                  | gas-medium pressure apparatus          | D                     | 618-722   | 4             | 311.486 ± 3.224                      | -5643.168                            |

## a Reactions:

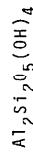
- A)  $2 \text{Al}_2\text{O}(\text{OH})(\text{diaspore}) + 4 \text{SiO}_2(\text{quartz, alpha}) = \text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite})$
- B)  $\text{Al}_2\text{Si}_4\text{O}_5(\text{andalusite}) + 3 \text{SiO}_2(\text{quartz, alpha}) + \text{H}_2\text{O}(\text{gas}) = \text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite})$
- C)  $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4(\text{kaolinite}) + 2 \text{SiO}_2(\text{quartz, alpha}) = \text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite}) + \text{H}_2\text{O}(\text{gas})$
- D)  $\text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite}) + 6 \text{Al}_2\text{O}(\text{OH})(\text{diaspore}) = 4 \text{Al}_2\text{Si}_4\text{O}_5(\text{andalusite}) + 4 \text{H}_2\text{O}(\text{gas})$

b Hemley and others (in press) measured the silicic-acid content of water equilibrated with the mineral pairs 1) pyrophyllite-diaspore, 2) pyrophyllite-andalusite, and 3) pyrophyllite-kaolinite between 500 K and 700 K at 100 and 200 MPa. Using their data for the solubility of quartz under the same conditions, the molar volumes of the solid phases, and the free-energy data for  $\text{H}_2\text{O}(\text{gas})$  of Fisher and Zen (1971), we calculated the free energy of reaction at 101.325 kPa and temperature for reactions A, B, and C for each observation.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for pyrophyllite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-5642.023 \pm 1.158$  kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of pyrophyllite and presents the data in their poorest perspective.

The phase-equilibria data cited above bracket the regression fit in free-energy space.

The molar volume of pyrophyllite was obtained from the study by Krupka and others (1979).

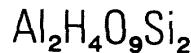


Dickite (monoclinic, polymorphous with Kaolinite, Nacrite, and Halloysite, member of the Kaolinite - Serpentine Group)

Issued September, 1979



| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K)   | $S^o$<br>J/(mol·K)     | $(G_T^o - H_{T_r}^o)/T$<br>J/(mol·K) | $H_T^o - H_{T_r}^o$<br>J/mol | Formation from the Elements |                            | Formation from the Oxides |                                    |
|---------------------|------------------------|------------------------|--------------------------------------|------------------------------|-----------------------------|----------------------------|---------------------------|------------------------------------|
|                     |                        |                        |                                      |                              | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$           | $\Delta H_f^o, \text{ox}$<br>J/mol |
| 273.15              | 224.241                | 176.737                | -197.985                             | -5804.                       | -4117368.                   | -3823141.                  | 731.101                   | -47687.                            |
| 298.15<br>(2 sigma) | 239.787<br>$\pm 0.736$ | 197.058<br>$\pm 3.067$ | -197.058<br>$\pm 0.$                 | -4118475.<br>$\pm 1237.$     | -3796160.<br>$\pm 1538.$    | 666.071<br>$\pm 0.269$     | -49750.<br>$\pm 1237.$    | -26906.<br>$\pm 1538.$             |
| 300.                | 240.872                | 198.545                | -197.063                             | 445.                         | -4118545.                   | -3794160.                  | 660.621                   | -49897.                            |
| 350.                | 267.038                | 237.716                | -200.097                             | 13167.                       | -4119921.                   | -3739973.                  | 558.160                   | -53639.<br>$\pm 160.$              |
| 400.                | 287.841                | 274.786                | -207.138                             | 27059.                       | -4120419.                   | -3685652.                  | 481.296                   | -136540.<br>$\pm 19.$              |
| 450.                | 304.298                | 309.677                | -216.613                             | 41879.                       | -4120241.                   | -3633131.                  | 421.511                   | -135510.<br>$\pm 19.$              |
| 500.                | 317.245                | 342.436                | -227.575                             | 57430.                       | -4119539.                   | -3577018.                  | 373.688                   | -134476.<br>$\pm 18.$              |
| (2 sigma)           | $\pm 1.677$            | $\pm 3.131$            | $\pm 3.070$                          | $\pm 256.$                   | $\pm 1263.$                 | $\pm 1971.$                | $\pm 0.206$               | $\pm 1.977.$                       |
| 550.                | 327.337                | 373.166                | -239.429                             | 73556.                       | -4118516.                   | -3522812.                  | 334.568                   | -133345.<br>$\pm 12.$              |
| 600.                | 335.085                | 401.996                | -251.787                             | 90125.                       | -411723.                    | -3468112.                  | 301.978                   | -132254.<br>$\pm 12.$              |
| 650.                | 340.886                | 429.058                | -261.394                             | 107032.                      | -4115815.                   | -3414125.                  | 274.410                   | -131266.<br>$\pm 15.$              |
| 700.                | 345.052                | 454.482                | -277.073                             | 124187.                      | -4114346.                   | -3360850.                  | 250.790                   | -130438.<br>$\pm 10.$              |
| 750.                | 347.833                | 478.391                | -289.705                             | 141514.                      | -4112991.                   | -3307080.                  | 230.325                   | -129815.<br>$\pm 8.$               |
| (2 sigma)           | $\pm 4.150$            | $\pm 3.286$            | $\pm 3.090$                          | $\pm 650.$                   | $\pm 1397.$                 | $\pm 627.$                 | $\pm 0.183$               | $\pm 1397.$                        |
| 800.                | 349.429                | 500.896                | -302.208                             | 158950.                      | -4111545.                   | -3253403.                  | 212.425                   | -129439.<br>$\pm 12.$              |
| 850.                | 350.002                | 522.102                | -311.526                             | 176440.                      | -4110334.                   | -319807.                   | 196.636                   | -130779.<br>$\pm 12.$              |
| 900.                | 349.686                | 542.103                | -326.619                             | 193936.                      | -4109320.                   | -3146277.                  | 182.605                   | -130150.<br>$\pm 10.$              |
| 950.                | 348.591                | 560.983                | -330.462                             | 211396.                      | -4130058.                   | -3094405.                  | 170.032                   | -129730.<br>$\pm 8.$               |
| 1000.               | 346.811                | 578.821                | -350.038                             | 228783.                      | -4129220.                   | -30378.2.                  | 158.779                   | -129557.<br>$\pm 6.$               |
| (2 sigma)           | $\pm 11.337$           | $\pm 3.129$            | $\pm 4.041$                          | $\pm 2209.$                  | $\pm 2532.$                 | $\pm 3364.$                | $\pm 0.176$               | $\pm 2332.$                        |

 $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ 

Dickite

Formula weight = 258.160 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$$S^\circ = 197.058 \pm 3.067 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -4118.475 \pm 1.237 \text{ kJ/mol}$$

$$V^\circ = 99.300 \pm 0.140 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -3796.160 \pm 1.538 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1000 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 3.804450 \times 10^6$$

$$a_4 = -6.190732 \times 10^3$$

$$a_6 = -1.056632 \times 10^{-1}$$

$$a_2 = 1.379448 \times 10^5$$

$$a_5 = 9.083598 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -1.119531 \times 10^4$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of dickite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                        | Data Type     | Method                 | No. of Points | Range       |
|-------------------------------|---------------|------------------------|---------------|-------------|
| King and Weller (1961)        | heat capacity | isothermal calorimetry | 10            | 206 - 296 K |
| Estimated values <sup>a</sup> | heat capacity |                        | 27            | 340 - 800 K |
| King and Weller (1961)        | entropy       | isothermal calorimetry | 1             | 298.15 K    |

a Heat-capacity values for kaolinite from Hemingway and others (1978) were used.

The heat-capacity measurements of King and Weller (1961) were fit with a standard error of estimate of 0.27  $\text{J}/(\text{mol}\cdot\text{K})$ . The estimated heat-capacity values were fit with a standard error of estimate of 1.66  $\text{J}/(\text{mol}\cdot\text{K})$ . The fitted entropy at 298.15 K is  $197.058 \pm 3.067 \text{ J}/(\text{mol}\cdot\text{K})$ , which agrees with the experimental value of  $197.058 \pm 1.255$  reported by King and Weller (1961).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                    | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_r^\circ(298.15 \text{ K})$ kJ | $\Delta H_f^\circ(298.15 \text{ K})$ kJ/mol |
|---------------------------------------|---------------------------|-----------------------|-----------|---------------|---|---|
| Barany and Kelley (1961) <sup>b</sup> | solution calorimetry (HF) | A                     | 346.85    | 6             | -3.642 $\pm$ 1.215                      | -4118.615                                   |

a Reaction:



b Barany and Kelley (1961) measured the enthalpy of solution of dickite in HF acid solution at 346.85 K. To complete the thermodynamic cycle, their data were evaluated in combination with the recent data for the enthalpies of solution of water, quartz, and gibbsite in similar solutions (Barany, 1963; Bennington and others, 1978; Hemingway and Robie, 1977; Barany and Kelley, 1961; and Koehler and others, 1961).

The molar volume of dickite was obtained from the compilation of Robie and others (1967).

## THERMODYNAMIC DATA FOR MINERALS

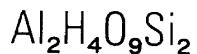


$\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$

Halloysite (monoclinic, polymorphs with Kaolinite, Nacrite, and Dickite, member of the Kaolinite - Serpentine Group)

Issued September, 1979

| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K)   | $S^o$<br>J/(mol·K)     | $(G_f^o - H_f^o)_{\text{Tr}}/T$<br>J/mol | $H_f^o - H_{\text{Tr}}^o$<br>J/mol | Formation from the Elements |                            |                        | Formation from the Oxides          |                                    |                         |
|---------------------|------------------------|------------------------|--|------------------------------------|-----------------------------|----------------------------|------------------------|------------------------------------|------------------------------------|-------------------------|
|                     |                        |                        |  |                                    | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$        | $\Delta H_f^o, \text{ox}$<br>J/mol | $\Delta G_f^o, \text{ox}$<br>J/mol | $\log K_f^o, \text{ox}$ |
| 273.15              | 230.416                | 182.502                | -204.283                                 | -5950.                             | -410066.                    | -3807414.                  | 728.094                | -30385.                            | -13007.                            | 2.487                   |
| 298.15<br>(2 sigma) | 245.245<br>$\pm 0.755$ | 203.334<br>$\pm 3.067$ | -203.334<br>$\pm 3.067$                  | 0.<br>$\pm 0.$                     | -4101028.<br>$\pm 1200.$    | -3780584.<br>$\pm 1508.$   | 662.342<br>$\pm 0.264$ | -32303.<br>$\pm 1200.$             | -11330.<br>$\pm 1508.$             | 1.985<br>$\pm 0.264$    |
| 300.                | 246.270                | 204.854                | -203.339                                 | 455.                               | -4101088.                   | -3778555.                  | 657.911                | -32440.                            | -11200.                            | 1.950                   |
| 350.                | 270.688                | 244.728                | -206.432                                 | 1340.                              | -4102237.                   | -3724743.                  | 555.887                | -35955.                            | -7377.                             | 1.101                   |
| 400.                | 289.860                | 282.175                | -213.585                                 | 27436.                             | -4102594.                   | -367083.                   | 479.355                | -118715.                           | 2733.                              | -0.357                  |
| 450.                | 305.023                | 317.226                | -221.175                                 | 42323.                             | -4102350.                   | -3616816.                  | 419.829                | -117639.                           | 17853.                             | -2.072                  |
| 500.                | 317.065<br>(2 sigma)   | 350.011<br>$\pm 1.683$ | -234.237<br>$\pm 3.132$                  | 57887.<br>$\pm 3.069$              | -4101656.<br>$\pm 257.$     | -3562902.<br>$\pm 1227.$   | 372.214<br>$\pm 0.204$ | -116512.<br>$\pm 1227.$            | 32853.<br>$\pm 1948.$              | -3.432<br>$\pm 0.204$   |
| 550.                | 326.629                | 380.696                | -246.172                                 | 73988.                             | -4100636.                   | -3509073.                  | 333.264                | -115465.                           | 47741.                             | -4.534                  |
| 600.                | 334.194                | 409.444                | -258.594                                 | 90516.                             | -4093396.                   | -3455348.                  | 300.815                | -114415.                           | 62531.                             | -5.444                  |
| 650.                | 340.121                | 436.448                | -271.247                                 | 107380.                            | -4098019.                   | -340173.                   | 273.366                | -113470.                           | 77238.                             | -6.207                  |
| 700.                | 347.686                | 461.828                | -283.963                                 | 124506.                            | -4095279.                   | -3348226.                  | 249.848                | -112611.                           | 91877.                             | -6.856                  |
| 750.                | 348.105<br>(2 sigma)   | 485.172<br>$\pm 4.156$ | -296.625<br>$\pm 3.286$                  | 141830.<br>$\pm 3.090$             | -4095137.<br>$\pm 1365.$    | -3294823.<br>$\pm 2609.$   | 229.472<br>$\pm 0.182$ | -112052.<br>$\pm 1365.$            | 106464.<br>$\pm 2609.$             | -4.415<br>$\pm 0.182$   |
| 800.                | 350.551                | 508.281                | -309.156                                 | 159300.                            | -4093747.                   | -3241514.                  | 211.649                | -111642.                           | 121017.                            | -7.902                  |
| 850.                | 352.162                | 529.585                | -321.502                                 | 176871.                            | -4092456.                   | -3188290.                  | 195.928                | -112900.                           | 135562.                            | -8.331                  |
| 900.                | 353.050                | 549.743                | -333.627                                 | 194504.                            | -4091394.                   | -3135131.                  | 181.959                | -112114.                           | 150155.                            | -8.715                  |
| 950.                | 353.307                | 568.841                | -345.508                                 | 212166.                            | -4111840.                   | -3081652.                  | 169.441                | -111512.                           | 164709.                            | -9.056                  |
| 1000.               | 353.010<br>(2 sigma)   | 586.998<br>$\pm 1.384$ | -357.132<br>$\pm 4.043$                  | 229826.<br>$\pm 2213.$             | -4110800.<br>$\pm 2517.$    | -3027459.<br>$\pm 3351.$   | 158.138<br>$\pm 0.175$ | -111057.<br>$\pm 3351.$            | 179235.<br>$\pm 2517.$             | -9.362<br>$\pm 0.175$   |

 $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ 

Halloysite

Formula weight = 258.160 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 203.334 \pm 3.067 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -4101.028 \pm 1.200 \text{ kJ/mol}$$

$$V^\circ =$$

$$\Delta G_f^\circ = -3780.584 \pm 1.503 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1000 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/[\text{J}/\text{mol}] = -a_1/T + a_2 + 2a_3 T^{-0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 1.936712 \times 10^6$$

$$a_4 = -5.153860 \times 10^3$$

$$a_6 = -7.258844 \times 10^{-2}$$

$$a_2 = 8.41514 \times 10^4$$

$$a_5 = 7.723004 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -8.729481 \times 10^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of halloysite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                        | Data Type     | Method                 | No. of Points | Range       |
|-------------------------------|---------------|------------------------|---------------|-------------|
| King and Weller (1961)        | heat capacity | isothermal calorimetry | 10            | 206 - 296 K |
| Estimated values <sup>a</sup> | heat capacity |                        | 27            | 340 - 800 K |
| King and Weller (1961)        | entropy       | isothermal calorimetry | 1             | 298.15 K    |

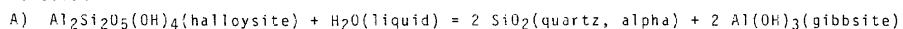
a Heat-capacity values for kaolinite from Hemingway and others (1978) were used.

The heat capacity measured by King and Weller (1961) was fit with a standard error of estimate of 0.23 J/(mol·K). The estimated heat-capacity values were fit with a standard error of estimate of 1.5 J/(mol·K). The fitted entropy at 298.15 K is  $203.334 \pm 3.067 \text{ J}/(\text{mol}\cdot\text{K})$ , which agrees with the experimental value of  $203.334 \pm 1.255 \text{ J}/(\text{mol}\cdot\text{K})$  reported by King and Weller (1961).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                   | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ kJ | $\Delta G_f^\circ(298.15 \text{ K})$ kJ/mol |
|---------------------------------------|--------------------------|-----------------------|-----------|---------------|---|---|
| Bareny and Kelley (1961) <sup>b</sup> | solution calorimetry(HF) | A                     | 346.85    | 5             | -21.089 $\pm$ 1.177                     | -4101.168                                   |

a Reaction:



b Bareny and Kelley (1961) measured the enthalpy of solution of halloysite in HF acid solution at 346.85 K. To complete the thermodynamic cycle, their data were evaluated in combination with the recent data for the enthalpies of solution of water, quartz, and gibbsite in similar solutions (Bareny, 1963; Bennington and others, 1978; Hemingway and Robie, 1977; Bareny and Kelley, 1961; and Koehler and others, 1961).



$\text{Al}_2\text{S}_2\text{O}_5(\text{OH})_4$   
Kaolinite (monoclinic, polymorphous with Dickite, Nacrite, and Halloysite, member of the Kaolinite - Serpentine Group)

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# THERMODYNAMIC DATA FOR MINERALS

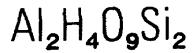
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Kaolinite (monoclinic, polymorphous with Dickite, Nacrite, and Halloysite, member of the Kaolinite - Serpentine Group)

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| Temperature<br>(K)  | $C_p^{\circ}$<br>J/(mol·K) | $S^{\circ}$<br>J/(mol·K) | $(G_f^{\circ} - H_f^{\circ})/T$<br>J/mol | Formation from the Elements   |                                  | Formation from the Oxides        |  |
|---------------------|----------------------------|--------------------------|--|-------------------------------|----------------------------------|----------------------------------|--|
|                     |                            |                          |  | $\Delta H_f^{\circ}$<br>J/mol | $\Delta G_f^{\circ}, e$<br>J/mol | $\log K_f^{\circ}$ , e           | $\Delta G_f^{\circ}, \text{ox}$<br>J/mol |
| 273.15              | 231.273                    | 184.057                  | -205.919                                 | -5972.                        | -4118841.                        | -3826613.                        | -49160.                                  |
| 298.15<br>(2 sigma) | 246.135<br>±0.771          | 204.966<br>±1.022        | -204.966<br>±1.022                       | 456.<br>0.<br>±0.             | -4119780.<br>-411065.<br>±1065.  | -3799823.<br>-379838.<br>±982.   | -51056.<br>-51056.<br>±0.172             |
| 300.                | 247.159                    | 206.492                  | -204.971                                 | 1344.7.                       | -4119839.                        | -3797838.                        | -51191.                                  |
| 350.                | 271.445                    | 246.495                  | -208.074                                 | 1344.7.                       | -4120946.                        | -3744071.                        | -54665.                                  |
| 400.                | 290.400                    | 284.030                  | -215.249                                 | 27512.                        | -4121271.                        | -3698202.                        | -137332.                                 |
| 450.                | 305.345                    | 319.131                  | -224.863                                 | 42420.                        | -4121005.                        | -3636329.                        | -13634.                                  |
| 500.                | 317.201                    | 351.940                  | -235.949                                 | 57995.                        | -4120299.                        | -3582510.                        | -13526.                                  |
| (2 sigma)           | 311.682                    | 311.196                  | -235.949                                 | ±257.                         | ±1110.                           | ±975.                            | ±1110.                                   |
| 550.                | 326.624                    | 382.631                  | -247.904                                 | 74100.                        | -4119277.                        | -3528779.                        | -134106.                                 |
| 600.                | 334.093                    | 411.384                  | -260.342                                 | 90625.                        | -4118040.                        | -3475150.                        | -133059.                                 |
| 650.                | 339.968                    | 438.368                  | -273.009                                 | 107483.                       | -4116670.                        | -3421631.                        | -132121.                                 |
| 700.                | 344.523                    | 463.736                  | -285.736                                 | 124600.                       | -4115238.                        | -3362220.                        | -13130.                                  |
| (2 sigma)           | 347.969<br>±4.157          | 487.629<br>±4.157        | -298.407<br>±1.555                       | 141917.<br>141917.<br>±650.   | -4113804.<br>-4113804.<br>±1265. | -3314912.<br>-3314912.<br>±1050. | -13078.<br>-13078.<br>±1255.             |
| 800.                | 350.476                    | 510.171                  | -310.944                                 | 159381.                       | -4112419.                        | -3261698.                        | -13033.                                  |
| 850.                | 352.178                    | 531.473                  | -323.296                                 | 176951.                       | -411129.                         | -3208568.                        | -13153.                                  |
| 900.                | 353.184                    | 551.335                  | -335.426                                 | 194588.                       | -4109973.                        | -3155510.                        | -13083.                                  |
| 950.                | 353.585                    | 570.744                  | -347.313                                 | 212259.                       | -4130560.                        | -3102119.                        | -130171.                                 |
| 1000.<br>(2 sigma)  | 353.453<br>±11.389         | 588.879<br>±2.826        | -358.942<br>±1.190                       | 229937.<br>22214.             | -4129412.<br>-4129412.<br>±2444. | -3048022.<br>-3048022.<br>±1274. | -129659.<br>-129659.<br>±0.067           |

 $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4$ 

Kaolinite

Formula weight = 258.160 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$S^\circ = 205.0 \pm 1.00 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_f^\circ = -4119.8 \pm 1.1 \text{ kJ/mol}$

$V^\circ = 99.52 \pm 0.52 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -3799.8 \pm 1.0 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1000 K)

$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$

$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

$a_1 = 1.49195 \times 10^6$

$a_4 = -4.97366 \times 10^3$

$a_6 = -6.77102 \times 10^{-2}$

$a_2 = 7.35514 \times 10^4$

$a_5 = 7.49175 \times 10^2$

$a_7 = 0.0$

$a_3 = -8.27864 \times 10^3$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of kaolinite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                              | Data Type     | Method                 | No. of Points | Range       |
|-------------------------------------|---------------|------------------------|---------------|-------------|
| King and Weller (1961) <sup>a</sup> | heat capacity | isothermal calorimeter | 10            | 206 - 296 K |
| Hemingway and others (1978)         | heat capacity | differential scanning  | 27            | 340 - 800 K |
| King and Weller (1961) <sup>a</sup> | entropy       | calorimeter            | 1             | 298.15 K    |

<sup>a</sup> The measurements were made on an impure natural sample of kaolinite. The observed heat-capacity and entropy values were assumed to equal the molar sum of the heat capacities and entropies, respectively, of the components. The stoichiometry used was: kaolinite, 0.970; pyrophyllite, 0.016; boehmite, 0.014.

The heat-capacity measurements of King and Weller (1961) and Hemingway and others (1978) were fit with a standard error of estimate of 0.52 and 1.6  $\text{J}/(\text{mol}\cdot\text{K})$ , respectively. The fitted entropy for 298.15 K is  $205.0 \pm 1.0 \text{ J}/(\text{mol}\cdot\text{K})$ , or a departure of 0.33  $\text{J}/\text{mol}$  from the experimental value, corrected for composition, of  $204.67 \pm 0.42 \text{ J}/(\text{mol}\cdot\text{K})$  reported by King and Weller.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                    | Method  | Reaction <sup>d</sup> | Range T/K | No. of Points | $\Delta H^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---|---|-----------------------|-----------|---------------|------------------------------------|--------------------------------------|
| Barany and Kelley (1961) <sup>b</sup>     | solution calorimetry (HF) <sup>b</sup>          | A                     | 346.85    | 10            | -2.362 ± 1.304                     | -4119.894                            |
|   |   | B                     | 573-573   | 9             | -2.403 ± 1.116                     | -4119.853                            |
| Hemley and others (in press) <sup>c</sup> | $\text{H}_4\text{Si}_4\text{O}_4$ concentration | C                     | 473-573   | 6             | -75.671 ± 1.059                    | -4119.572                            |
| Hemley and others (in press) <sup>c</sup> | $\text{H}_4\text{Si}_4\text{O}_4$ concentration | D                     | 473-573   | 10            | -57.885 ± 0.441                    | -4119.844                            |
|   |   |                       |           |               | 57.792 ± 0.323                     | -4120.515                            |

a Reactions:

- A)  $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4(\text{kaolinite}) + \text{H}_2\text{O}(\text{gas}) = 2 \text{SiO}_2(\text{quartz, alpha}) + 2 \text{Al}(\text{OH})_3(\text{gibbsite})$
- B)  $2 \text{Al}(\text{OH})(\text{boehmite}) + 2 \text{SiO}_2(\text{quartz, alpha}) + \text{H}_2\text{O}(\text{gas}) = \text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4(\text{kaolinite})$
- C)  $2 \text{Al}(\text{OH})(\text{diaspore}) + 2 \text{SiO}_2(\text{quartz, alpha}) + \text{H}_2\text{O}(\text{gas}) = \text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4(\text{kaolinite})$
- D)  $\text{Al}_2\text{Si}_2\text{O}_5(\text{OH})_4(\text{kaolinite}) + 2 \text{SiO}_2(\text{quartz, alpha}) = \text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite}) + \text{H}_2\text{O}(\text{gas})$

<sup>b</sup> Barany and Kelley (1961) measured the enthalpy of solution of kaolinite in HF acid solution at 346.85 K. To complete the thermodynamic cycle, their data were evaluated in combination with the recent data for the enthalpies of solution of water, quartz, and gibbsite in similar solutions (Barany, 1963; Bennington and others, 1978; Hemingway and Robie, 1977; Barany and Kelley, 1961; and Koehler and others, 1961).

<sup>c</sup> Hemley and others (in press) measured the silicic-acid content of water equilibrated with the mineral pairs A) boehmite-kaolinite, B) diaspor-kaolinite, and C) pyrophyllite-kaolinite at 100 and 200 MPa between 450 K and 600 K. Using their data for the solubility of quartz under the same conditions, the molar volumes of the solid phases, and the free-energy data for  $\text{H}_2\text{O}(\text{gas})$  of Fisher and Zen (1971), we calculated the gibbs energies of reactions B, C, and D for each observation.

The phase-equilibrium studies of Hemley and others (in press) were evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for kaolinite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-4119.780 \pm 1.065 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of kaolinite and presents the data in their poorest perspective.

Most of the phase-equilibria data cited above bracket the regression fit in free-energy space. However, the phase-equilibria studies lack sufficient precision to constrain the fit tightly, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate. The phase-equilibria studies are consistent with the experimental enthalpy of solution of Barany and Kelley (1961).

The molar volume of kaolinite was obtained from the compilation of Robie and others (1967).

$\text{Al}_2\text{O}_3$   
Corundum (trigonal)

$\text{Al}_2\text{O}_3$

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| Temperature<br>(K) | $C_p$<br>$J/(mol \cdot K)$ | $S^\circ$<br>$J/(mol \cdot K)$ | $(G_f^\circ - H_f^\circ)T$<br>$J/mol$ | Formation from the Elements            |                                  |                     | Formation from the Oxides               |   |                            |
|--------------------|----------------------------|--------------------------------|---------------------------------------|--|----------------------------------|---------------------|---|---|----------------------------|
|                    |                            |                                |                                       | $H_f^\circ - H_{f,r}^\circ$<br>$J/mol$ | $\Delta G_f^\circ, e$<br>$J/mol$ | $\log K_f^\circ, e$ | $\Delta H_f^\circ, \alpha_x$<br>$J/mol$ | $\Delta G_f^\circ, \alpha_x$<br>$J/mol$ | $\log K_f^\circ, \alpha_x$ |
| 273.15             | 73.847                     | 44.204                         | -51.223                               | -1917.                                 | -1675326.                        | -1590109.           | 304.077                                 | 0.                                      | 0.                         |
| 298.15             | 79.393                     | 50.917                         | -50.917                               | 0.                                     | -1675711.                        | -1552291.           | 277.211                                 | 0.                                      | 0.                         |
| 300.               | 79.772                     | 51.409                         | -50.918                               | 147.                                   | -1675736.                        | -1581712.           | 275.400                                 | 0.                                      | 0.                         |
| 350.               | 88.678                     | 64.405                         | -51.924                               | 438.                                   | -1676206.                        | -1565999.           | 233.712                                 | 0.                                      | 0.                         |
| 400.               | 95.583                     | 76.716                         | -54.261                               | 8942.                                  | -1676183.                        | -1550240.           | 202.440                                 | 0.                                      | 0.                         |
| 450.               | 101.075                    | 88.303                         | -57.406                               | 13933.                                 | -1676343.                        | -1534473.           | 178.117                                 | 0.                                      | 0.                         |
| 500.               | 105.528                    | 99.190                         | -61.046                               | 19072.                                 | -1676144.                        | -1558719.           | 158.659                                 | 0.                                      | 0.                         |
| 550.               | 109.195                    | 109.425                        | -64.984                               | 24443.                                 | -1675833.                        | -1502991.           | 142.742                                 | 0.                                      | 0.                         |
| 600.               | 112.254                    | 119.062                        | -69.093                               | 29981.                                 | -1675445.                        | -1487254.           | 129.480                                 | 0.                                      | 0.                         |
| 650.               | 114.833                    | 128.151                        | -73.289                               | 35660.                                 | -1675011.                        | -1471632.           | 118.262                                 | 0.                                      | 0.                         |
| 700.               | 117.029                    | 136.744                        | -77.518                               | 41458.                                 | -1674557.                        | -1456045.           | 108.648                                 | 0.                                      | 0.                         |
| 750.               | 118.914                    | 144.884                        | -81.740                               | 47358.                                 | -1674103.                        | -1440410.           | 100.319                                 | 0.                                      | 0.                         |
| 800.               | 120.545                    | 152.612                        | -85.930                               | 53346.                                 | -1673370.                        | -1424845.           | 93.033                                  | 0.                                      | 0.                         |
| 850.               | 121.967                    | 159.163                        | -90.070                               | 59409.                                 | -1673275.                        | -1409345.           | 86.605                                  | 0.                                      | 0.                         |
| 900.               | 123.217                    | 166.971                        | -94.150                               | 65539.                                 | -1672332.                        | -1393788.           | 80.893                                  | 0.                                      | 0.                         |
| 950.               | 124.323                    | 173.663                        | -98.160                               | 71728.                                 | -1674468.                        | -137895.            | 75.762                                  | 0.                                      | 0.                         |
| 1000.              | 125.310                    | 180.066                        | -102.096                              | 779.0.                                 | -1693639.                        | -1301261.           | 71.105                                  | 0.                                      | 0.                         |
| 1050.              | 126.197                    | 186.201                        | -105.956                              | 84258.                                 | -1693201.                        | -1344652.           | 66.893                                  | 0.                                      | 0.                         |
| 1100.              | 127.003                    | 192.091                        | -109.738                              | 90588.                                 | -1692619.                        | -1326066.           | 63.065                                  | 0.                                      | 0.                         |
| 1150.              | 127.740                    | 197.753                        | -113.443                              | 96957.                                 | -1692334.                        | -1311505.           | 59.857                                  | 0.                                      | 0.                         |
| 1200.              | 128.421                    | 203.204                        | -117.070                              | 103361.                                | -1691570.                        | -1284968.           | 56.368                                  | 0.                                      | 0.                         |
| 1250.              | 129.056                    | 208.460                        | -120.621                              | 109798.                                | -1690386.                        | -128455.            | 53.424                                  | 0.                                      | 0.                         |
| 1300.              | 129.655                    | 213.533                        | -124.098                              | 116266.                                | -1690185.                        | -124626.            | 50.706                                  | 0.                                      | 0.                         |
| 1350.              | 130.226                    | 218.137                        | -127.501                              | 122763.                                | -168976.                         | -1245499.           | 48.191                                  | 0.                                      | 0.                         |
| 1400.              | 130.774                    | 223.183                        | -130.834                              | 129288.                                | -1689130.                        | -1249057.           | 45.857                                  | 0.                                      | 0.                         |
| 1450.              | 131.307                    | 227.781                        | -134.098                              | 135840.                                | -1688477.                        | -1242637.           | 43.984                                  | 0.                                      | 0.                         |
| 1500.              | 131.829                    | 232.242                        | -137.296                              | 142419.                                | -1687807.                        | -1196240.           | 41.657                                  | 0.                                      | 0.                         |
| 1550.              | 132.345                    | 236.573                        | -140.429                              | 14903.                                 | -1687120.                        | -119866.            | 39.761                                  | 0.                                      | 0.                         |
| 1600.              | 132.859                    | 240.783                        | -143.499                              | 155653.                                | -1686443.                        | -1163514.           | 37.985                                  | 0.                                      | 0.                         |
| 1650.              | 133.376                    | 244.379                        | -146.510                              | 162304.                                | -1685687.                        | -1147184.           | 36.317                                  | 0.                                      | 0.                         |
| 1700.              | 133.898                    | 248.868                        | -149.462                              | 168991.                                | -1684930.                        | -11087.             | 34.48                                   | 0.                                      | 0.                         |
| 1750.              | 134.428                    | 252.757                        | -152.358                              | 175699.                                | -1684172.                        | -1114592.           | 33.269                                  | 0.                                      | 0.                         |
| 1800.              | 134.969                    | 256.552                        | -155.200                              | 182434.                                | -1683380.                        | -1098330.           | 31.873                                  | 0.                                      | 0.                         |



## Corundum

Formula weight = 101.926 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 50.917 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -1675.711 \text{ kJ/mol}$$

$$V^\circ = 25.575 \pm 0.007 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -1582.291 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (temperature range 200 to 1800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 0.0$$

$$a_4 = -1.55092 \times 10^3$$

$$a_6 = -1.95913 \times 10^{-2}$$

$$a_2 = 1.7321 \times 10^4$$

$$a_5 = 2.33004 \times 10^2$$

$$a_7 = 9.44410 \times 10^{-6}$$

$$a_3 = -2.46518 \times 10^3$$

Sources for Thermodynamic Properties

The thermodynamic properties for corundum were taken from the following sources:

| <u>Property</u>                         | <u>Source</u>   |
|---|---|
| Heat capacity                           | Stull and Prophet (1971), Chase and others (1974, 1975) |
| Entropy                                 | CODATA Task Group (1978)                                |
| Enthalpy of formation from the elements | CODATA Task Group (1978)                                |

The molar volume for corundum was taken from the compilation of Robie and others (1967).

Al<sub>2</sub>SiO<sub>5</sub>

Reference state:

Kyanite  
Andalusite  
Sillimanite

273.15 K to 430.46 K

430.46 K to 1016.9 K

1016.9 K to 1800 K

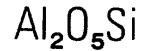
Al<sub>2</sub>O<sub>5</sub>Si

Issued September, 1979

## THERMODYNAMIC DATA FOR MINERALS

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| Temperature<br>(K) | C <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K) | (G <sub>T</sub> <sup>°</sup> -H <sub>T</sub> <sup>°</sup> ) <sub>f</sub> /T<br>J/mol | H <sub>T</sub> <sup>°</sup> -H <sub>Tr</sub><br>J/mol | Formation from the Elements               |   | Formation from the Oxides                    |  |
|--------------------|-----------------------------|-----------------|--|---|---|---|--|--|
|                    |                             |                 |  |   | ΔH <sub>f</sub> <sup>°</sup> , e<br>J/mol | ΔG <sub>f</sub> <sup>°</sup> , e<br>J/mol | log K <sub>f</sub> <sup>°</sup> , e<br>J/mol | ΔH <sub>f</sub> <sup>°</sup> , ox<br>J/mol |
| 273.15             | 113.775                     | 74.123          | -84.937  | -2954.  | -2593700.                                 | -2456680.                                 | 469.792                                      | -7809.                                     |
| 298.15             | 122.348                     | 84.465          | -84.465  | 0.  | -259269.                                  | -2444113.                                 | 428.198                                      | -7859.                                     |
| (2 sigma)          | ±0.154                      | ±0.339          | ±0.  | ±433.   | ±339.                                     | ±0.068                                    | ±433.  | ±389.                                      |
| 300.               | 122.936                     | 85.224          | 84.468   | 227.  | -2593305.                                 | -243181.                                  | 425.395                                      | -7862.                                     |
| 300.               | 136.874                     | 105.666         | -86.018  | 6337.   | -2593999.                                 | -2417932.                                 | 360.856                                      | -7934.                                     |
| 400.               | 147.857                     | 124.288         | -89.624  | 13865.  | -259250.                                  | -2392615.                                 | 311.443                                      | -7984.                                     |
| 430.46             | 153.475                     | 135.347         | -92.471  | 18456.  | -259323.                                  | -2377184.                                 | 288.462                                      | -8009.                                     |
| (2 sigma)          | 153.273                     | 144.555         | -92.471  | 22120.  | -2591268.                                 | -2377184.                                 | 288.462                                      | -8009.                                     |
| 450.               | 156.475                     | 151.431         | -94.882  | 25447.  | -2591204.                                 | -2367448.                                 | 274.808                                      | -8045.                                     |
| 500.               | 163.491                     | 168.234         | -101.389   | 3352.   | -2590880.                                 | -2342623.                                 | 244.732                                      | -8127.                                     |
| (2 sigma)          | ±0.268                      | ±0.729          | ±0.769   | ±615.   | ±643.                                     | ±410.                                     | ±643.  | ±410.                                      |
| 550.               | 169.117                     | 184.150         | -108.199   | 4173.   | -2590381.                                 | -2317821.                                 | 220.128                                      | -8219.                                     |
| 600.               | 173.663                     | 199.067         | -115.156   | 50346.  | -2589764.                                 | -2293065.                                 | 199.629                                      | -8355.                                     |
| 650.               | 177.367                     | 213.118         | 59.25.   | 59346.  | -2589764.                                 | -2268372.                                 | 182.288                                      | -8456.                                     |
| 700.               | 180.419                     | 226.378         | -129.132   | 68012.  | -2583357.                                 | -2243779.                                 | 167.429                                      | -8486.                                     |
| 750.               | 182.969                     | 238.315         | -136.037   | 77.59.  | -2586334.                                 | -2219138.                                 | 154.554                                      | -8513.                                     |
| (2 sigma)          | ±0.316                      | ±0.             | ±0.486   | ±614.   | ±642.                                     | ±380.                                     | ±642.  | ±380.                                      |
| 800.               | 185.138                     | 250.794         | -142.841   | 86363.  | -2586933.                                 | -2194595.                                 | 143.292                                      | -8533.                                     |
| 850.               | 187.024                     | 262.076         | -149.526   | 95668.  | -2588274.                                 | -2170094.                                 | 133.358                                      | -8673.                                     |
| 900.               | 188.708                     | 272.815         | -156.079   | 105062.   | -2585671.                                 | -2145631.                                 | 121.529                                      | -8723.                                     |
| 950.               | 190.256                     | 283.059         | -162.495   | 114536.   | -2606651.                                 | -2108086.                                 | 116.610                                      | -8844.                                     |
| 1000.              | 191.726                     | 292.836         | -166.770   | 124066.   | -2609325.                                 | -2095254.                                 | 109.445                                      | -8957.                                     |
| (2 sigma)          | ±0.492                      | ±0.730          | ±0.429   | ±615.   | ±644.                                     | ±434.                                     | ±644.  | ±434.                                      |
| 1016.90            | 192.213                     | 296.073         | -170.859   | 127330.   | -2605672.                                 | -2086626.                                 | 107.183                                      | -7138.                                     |
| 1016.90            | 194.962                     | 298.932         | -170.859   | 13028.  | -2602704.                                 | -2086626.                                 | 107.183                                      | -7138.                                     |
| 1050.              | 195.912                     | 305.552         | -174.997   | 136168.   | -260107.                                  | -209837.                                  | 102.969                                      | -74170.                                    |
| 1100.              | 197.210                     | 314.397         | -181.127   | 146596.   | -2601180.                                 | -2044512.                                 | 97.086                                       | -7452.                                     |
| 1150.              | 198.361                     | 323.189         | -187.114   | 156186.   | -260227.                                  | -2019231.                                 | 91.716                                       | -7486.                                     |
| 1200.              | 199.379                     | 331.653         | -192.961   | 166420.   | -259353.                                  | -1993991.                                 | 86.796                                       | -7527.                                     |
| 1250.              | 200.278                     | 339.811         | -190.673   | 17612.  | -2593262.                                 | -1987792.                                 | 82.271                                       | -7573.                                     |
| (2 sigma)          | ±0.572                      | ±0.562          | ±0.433   | ±552.   | ±551.                                     | ±513.                                     | ±551.  | ±513.                                      |
| 1300.              | 201.069                     | 347.681         | -204.254   | 18646.  | -259756.                                  | -1943633.                                 | 78.096                                       | -8159.                                     |
| 1350.              | 201.763                     | 345.83          | -201.707   | 196527.   | -2596240.                                 | -1918513.                                 | 74.232                                       | -8452.                                     |
| 1400.              | 202.368                     | 362.632         | -215.038   | 206631.   | -2595216.                                 | -1893430.                                 | 70.645                                       | -8724.                                     |
| 1450.              | 202.892                     | 369.143         | -220.251   | 216753.   | -2594187.                                 | -1868385.                                 | 67.306                                       | -8734.                                     |
| 1500.              | 203.342                     | 376.629         | -225.349   | 226917.   | -2593154.                                 | -1843375.                                 | 64.192                                       | -8742.                                     |
| (2 sigma)          | ±0.879                      | ±0.             | ±0.437   | ±527.   | ±612.                                     | ±611.                                     | ±612.  | ±611.                                      |
| 1550.              | 203.723                     | 383.303         | -230.338   | 237096.   | -2592118.                                 | -1818399.                                 | 61.280                                       | -878.                                      |
| 1600.              | 204.042                     | 389.776         | -235.219   | 247220.   | -2591083.                                 | -1793457.                                 | 58.550                                       | -8753.                                     |
| 1650.              | 204.303                     | 396.059         | -239.999   | 257459.   | -2590048.                                 | -176854.                                  | 55.987                                       | -8724.                                     |
| 1700.              | 204.510                     | 402.161         | -244.679   | 26770.  | -2639125.                                 | -1743219.                                 | 53.563                                       | -8703.                                     |
| 1750.              | 204.668                     | 408.092         | -244.263   | 277949.   | -2638354.                                 | -1716874.                                 | 51.246                                       | -8730.                                     |
| (2 sigma)          | ±1.208                      | ±0.668          | ±0.448   | ±702.   | ±67.                                      | ±730.                                     | ±672.  | ±730.                                      |
| 1800.              | 204.779                     | 413.559         | -253.756   | 288186.   | -2637782.                                 | -1690563.                                 | 49.059                                       | -8753.                                     |
| (2 sigma)          | ±1.276                      | ±0.688          | ±0.450   | ±751.   | ±811.                                     | ±756.                                     | ±811.  | ±756.                                      |

 $\text{Al}_2\text{SiO}_5$  (reference state)

Kyanite, Andalusite, Sillimanite

Formula weight = 162.046 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K (+2s) (kyanite)

$$S^\circ = 84.47 \pm 0.44 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -2594.27 \pm 0.43 \text{ kJ/mol}$$

$$V^\circ = 44.22 \pm 0.02 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -2444.11 \pm 0.39 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

## Kyanite (temperature range 200 to 430.46 K)

$$a_1 = 0.0$$

$$a_4 = -2.23489 \times 10^3$$

$$a_6 = -1.29800 \times 10^{-2}$$

$$a_2 = 2.37951 \times 10^4$$

$$a_5 = 3.36114 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -3.55746 \times 10^3$$

## Andalusite (temperature range 430.46 to 1016.9 K)

$$a_1 = 2.28751 \times 10^6$$

$$a_4 = -3.71202 \times 10^3$$

$$a_6 = -1.03545 \times 10^{-1}$$

$$a_2 = 8.75787 \times 10^4$$

$$a_5 = 3.134705 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -6.75436 \times 10^3$$

## Sillimanite (temperature range 1016.9 to 1800 K)

$$a_1 = 0.0$$

$$a_4 = -2.050871 \times 10^3$$

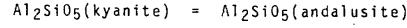
$$a_6 = -9.470810 \times 10^{-3}$$

$$a_2 = 1.667620 \times 10^4$$

$$a_5 = 3.134705 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -3.164868 \times 10^3$$

Critical ReactionsInversions:

$$T_i = 430.46 \text{ K (calculated)}$$

$$\Delta S_i^\circ = 9.20 \pm 1.80 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_i^\circ = 3.96 \pm 0.77 \text{ kJ/mol}$$



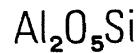
$$T_i = 1016.9 \text{ K (calculated)}$$

$$\Delta S_i^\circ = 2.92 \pm 0.83 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_i^\circ = 2.97 \pm 0.84 \text{ kJ/mol}$$

For detailed information on  $\text{Al}_2\text{SiO}_5$ , refer to the appropriate tables on the individual phases.

| Temperature<br>(K)  | C <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K)  | (G <sub>T</sub> <sup>°</sup> -H <sub>Tf</sub> <sup>°</sup> )/T<br>J/mol | Formation from the Elements   |                            |                               | Formation from the Oxides   |                             |                                |
|---------------------|-----------------------------|------------------|---|---|----------------------------|-------------------------------|-----------------------------|-----------------------------|--------------------------------|
|                     |                             |                  |   | H <sub>T</sub> <sup>°</sup> -H <sub>Tr</sub> <sup>°</sup> /T<br>J/mol | ΔG <sub>f,e</sub><br>J/mol | log K <sub>f,e</sub><br>J/mol | ΔH <sub>f,ox</sub><br>J/mol | ΔG <sub>f,ox</sub><br>J/mol | log K <sub>f,ox</sub><br>J/mol |
| 273.15              | 113.630                     | 83.456           | -94.246   | -2947.  | -2589694.                  | -2455224.                     | 469.514                     | -3803.                      | -4239.                         |
| 298.15<br>(2 sigma) | 121.991<br>±0.262           | 93.775<br>±0.728 | -93.715<br>±0.728   | 0.<br>±0.   | -2590270.<br>±641.         | -2442889.<br>±884.            | 427.984<br>±0.085           | -3860.<br>±641.             | -4277.<br>±484.                |
| 300.                | 122.573                     | 94.531           | -93.777   | 226.  | -2590307.                  | -2441975.                     | 425.185                     | -3864.                      | -4279.                         |
| 350.                | 136.577                     | 114.519          | -95.323   | 6718.   | -2510119.                  | -2417109.                     | 360.746                     | -3853.                      | -4341.                         |
| 400.                | 147.672                     | 133.509          | -98.921   | 13335.  | -2591281.                  | -2392334.                     | 312.407                     | -4014.                      | -4342.                         |
| 450.                | 156.475                     | 151.431          | -103.769  | 21448.  | -2591204.                  | -2367463.                     | 274.808                     | -4065.                      | -4336.                         |
| 500.                | 163.491                     | 168.294          | -109.387  | 29553.  | -2590880.                  | -2342623.                     | 244.732                     | -4127.                      | -4474.                         |
| (2 sigma)           | ±0.268                      | ±0.729           | ±38.  | ±410.   | ±643.                      | ±410.                         | ±643.                       | ±643.                       | ±410.                          |
| 550.                | 169.117                     | 184.150          | -115.471  | 37774.  | -2590381.                  | -2317821.                     | 220.128                     | -4219.                      | -4219.                         |
| 600.                | 173.663                     | 199.067          | -121.822  | 46347.  | -259764.                   | -2293059.                     | 199.629                     | -4355.                      | -4505.                         |
| 650.                | 177.367                     | 213.118          | -128.309  | 55126.  | -259077.                   | -2268372.                     | 182.288                     | -4348.                      | -4532.                         |
| 700.                | 180.419                     | 226.378          | -134.845  | 64073.  | -2588357.                  | -2243779.                     | 167.429                     | -4006.                      | -4522.                         |
| 750.                | 182.969                     | 238.915          | -141.369  | 73159.  | -2581634.                  | -2219133.                     | 154.554                     | -5133.                      | -4490.                         |
| (2 sigma)           | ±0.316                      | ±0.729           | ±78.  | ±642.   | ±890.                      | ±890.                         | ±642.                       | ±380.                       | ±0.026                         |
| 800.                | 185.138                     | 250.794          | -147.840  | 82363.  | -2586933.                  | -2194695.                     | 143.292                     | -5633.                      | -4435.                         |
| 850.                | 187.024                     | 262.076          | -154.831  | 91668.  | -2586274.                  | -2170034.                     | 133.358                     | -6723.                      | -4347.                         |
| 900.                | 188.708                     | 272.815          | -160.523  | 101062.   | -2585671.                  | -2145631.                     | 124.529                     | -6944.                      | -4204.                         |
| 950.                | 190.256                     | 292.856          | -166.705  | 1120087.  | -2606651.                  | -2120086.                     | 116.610                     | -6688.                      | -4053.                         |
| 1000.               | 191.726                     | 328.326          | -172.769  | 120087.   | -2605925.                  | -2095254.                     | 109.445                     | -7095.                      | -3897.                         |
| (2 sigma)           | ±0.492                      | ±0.730           | ±126.   | ±126.   | ±644.                      | ±444.                         | ±0.023                      | ±644.                       | ±434.                          |
| 1050.               | 193.163                     | 302.245          | -178.713  | 129709.   | -2605167.                  | -2069739.                     | 102.964                     | -6723.                      | -3734.                         |
| 1100.               | 194.607                     | 311.264          | -184.534  | 139003.   | -2604374.                  | -2044261.                     | 97.074                      | -7342.                      | -3565.                         |
| 1150.               | 196.094                     | 319.947          | -190.234  | 149170.   | -2603544.                  | -2038820.                     | 91.698                      | -7454.                      | -3391.                         |
| 1200.               | 197.652                     | 328.326          | -195.814  | 159014.   | -2602670.                  | -1993415.                     | 86.771                      | -7551.                      | -3212.                         |
| 1250.               | 199.307                     | 336.427          | -201.273  | 168337.   | -2601747.                  | -1968043.                     | 82.240                      | -7625.                      | -3029.                         |
| (2 sigma)           | ±0.568                      | ±0.738           | ±187.   | ±187.   | ±657.                      | ±545.                         | ±0.023                      | ±657.                       | ±516.                          |
| 1300.               | 201.080                     | 344.279          | -206.628  | 178946.   | -2600767.                  | -1942720.                     | 78.070                      | -7669.                      | -2845.                         |
| 1350.               | 202.993                     | 351.903          | -211.868  | 189048.   | -2599721.                  | -1917430.                     | 74.190                      | -7676.                      | -2659.                         |
| 1400.               | 205.061                     | 359.322          | -217.002  | 199248.   | -2598600.                  | -1892180.                     | 70.598                      | -7636.                      | -2474.                         |
| 1450.               | 207.299                     | 366.556          | -222.035  | 209556.   | -2591394.                  | -1866912.                     | 67.256                      | -7551.                      | -2291.                         |
| 1500.               | 209.721                     | 373.624          | -226.970  | 219981.   | -2596092.                  | -1841807.                     | 64.137                      | -7381.                      | -2112.                         |
| (2 sigma)           | ±1.915                      | ±0.756           | ±724.   | ±724.   | ±683.                      | ±683.                         | ±0.024                      | ±703.                       | ±639.                          |
| 1550.               | 212.339                     | 380.543          | -231.813  | 230532.   | -2594683.                  | -1816687.                     | 61.222                      | -7146.                      | -1940.                         |
| 1600.               | 215.164                     | 387.329          | -236.567  | 241219.   | -2533155.                  | -1791611.                     | 58.490                      | -6836.                      | -1777.                         |
| 1650.               | 218.204                     | 393.996          | -241.237  | 252052.   | -251496.                   | -1766591.                     | 55.920                      | -6410.                      | -1625.                         |
| 1700.               | 221.469                     | 400.558          | -245.827  | 263043.   | -260203.                   | -1741171.                     | 53.500                      | -5881.                      | -1438.                         |
| 1750.               | 224.967                     | 407.027          | -250.340  | 274203.   | -2688102.                  | -1714759.                     | 51.183                      | -5247.                      | -1358.                         |
| (2 sigma)           | ±4.592                      | ±0.951           | ±727.   | ±727.   | ±969.                      | ±852.                         | ±0.025                      | ±1182.                      | ±852.                          |
| 1800.               | 228.703                     | 413.417          | -254.782  | 28543.  | -2635825.                  | -1688411.                     | 48.996                      | -448.                       | -2845.                         |
| (2 sigma)           | ±5.280                      | ±1.040           | ±729  | ±1205.  | ±1387.                     | ±883.                         | ±0.026                      | ±1387.                      | ±838.                          |

 $\text{Al}_2\text{SiO}_5$ 

Andalusite

Formula weight = 162.046 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 93.78 \pm 0.73 \text{ J}/(\text{mol}\cdot\text{K}) \quad \Delta H_f^\circ = -2590.27 \pm 0.64 \text{ kJ/mol}$$

$$V^\circ = 51.58 \pm 0.02 \text{ cm}^3/\text{mol} \quad \Delta G_f^\circ = -2442.89 \pm 0.48 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1800 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

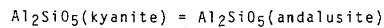
$$a_1 = 2.28751 \times 10^6 \quad a_4 = -3.71202 \times 10^3 \quad a_6 = -1.03545 \times 10^{-1}$$

$$a_2 = 8.75787 \times 10^4 \quad a_5 = 5.43227 \times 10^2 \quad a_7 = 6.68935 \times 10^{-5}$$

$$a_3 = -6.75436 \times 10^3$$

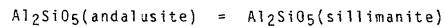
Critical Reactions

## Inversion:



$$T_i = 430.46 \text{ K (calculated)} \quad \Delta S_i^\circ = 9.2 \pm 1.80 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 3.96 \pm 0.77 \text{ kJ/mol}$$



$$T_i = 1016.9 \text{ K (calculated)} \quad \Delta S_i^\circ = 2.92 \pm 0.83 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 2.97 \pm 0.84 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of andalusite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                                 | Data Type         | Method                 | No. of Points | Range        |
|--|-------------------|------------------------|---------------|--------------|
| Todd (1950) <sup>a</sup>               | heat capacity     | isothermal calorimetry | 10            | 206 - 296 K  |
| Pankratz and Kelly (1964) <sup>a</sup> | relative enthalpy | drop calorimetry       | 13            | 397 - 1600 K |
| Todd (1950) <sup>a</sup>               | entropy           | isothermal calorimetry | 1             | 298.15 K     |

a The measurements were made on an impure natural sample of andalusite. The observed heat-capacity and entropy values were assumed to equal the molar sum of the heat capacities and entropies, respectively, of the components. The stoichiometry used was: andalusite, 0.9925; corundum, 0.0226; hematite, 0.00112; lime, 0.00058.

The heat capacity of Todd (1950) was fit with a standard error of estimate of 0.15 J/(mol·K). The relative enthalpy measured by Pankratz and Kelley (1964) was fit with a standard error of estimate of 93 J/mol or approximately 0.18 percent of the observed value. The fitted entropy at 298.15 K is  $93.78 \pm 0.73 \text{ J}/(\text{mol}\cdot\text{K})$  or a departure of 0.56 J/mol from the experimental value of  $93.22 \pm 0.42 \text{ J}/(\text{mol}\cdot\text{K})$  calculated from the data of Todd (1950).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                    | Method                                 | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---|--|-----------------------|-----------|---------------|------------------------------------|--------------------------------------|
| Anderson and others (1977) <sup>b</sup>   | solution calorimetry<br>(borate salt)  | A                     | 973       | 1             | -1.110 ± 0.948                     | -2593.020                            |
| Hemley and others (in press) <sup>c</sup> | $\text{H}_4\text{SiO}_4$ concentration | B                     | 723-773   | 10            | -4.876 ± 0.204                     | -2591.209                            |
| Hemley and others (in press) <sup>c</sup> | $\text{H}_4\text{SiO}_4$ concentration | C                     | 623-663   | 2             | 78.164 ± 0.200                     | -2589.472                            |
| Hemley and others (in press) <sup>c</sup> | $\text{H}_4\text{SiO}_4$ concentration | D                     | 613-673   | 11            | -78.080 ± 1.616                    | -2590.320                            |
| Haas and Holdaway (1973)                  | gas-medium pressure apparatus          | D                     | 643-737   | 4             | -76.968 ± 0.615                    | -2591.119                            |
| Kerrick (1968)                            | gas-medium pressure apparatus          | D                     | 668-718   | 2             | -79.383 ± 1.273                    | -2588.704                            |
| Holdaway (1971)                           | gas-medium pressure apparatus          | E                     | 764-917   | 4             | 2.483 ± 0.063                      | -2590.245                            |
| Holdaway (1971)                           | gas-medium pressure apparatus          | F                     | 650-858   | 6             | 4.215 ± 0.179                      | -2590.032                            |
| Newton (1966a)                            | gas-medium pressure apparatus          | F                     | 973-1123  | 7             | 4.021 ± 0.218                      | -2590.226                            |
| Storre and Nitsch (1974)                  | gas-medium pressure apparatus          | G                     | 788-833   | 4             | -89.818 ± 1.710                    | -2590.825                            |
| Haas and Holdaway (1973)                  | gas-medium pressure apparatus          | H                     | 618-722   | 4             | 311.486 ± 3.224                    | -2589.982                            |

$\text{Al}_2\text{O}_5\text{Si}$ 

## a Reactions:

- A)  $\text{Al}_2\text{O}_3(\text{corundum}) + \text{SiO}_2(\text{quartz, beta}) = \text{Al}_2\text{SiO}_5(\text{andalusite})$   
 B)  $\text{Al}_2\text{O}_3(\text{corundum}) + \text{SiO}_2(\text{quartz, alpha}) = \text{Al}_2\text{SiO}_5(\text{andalusite})$   
 C)  $2 \text{AlO(OH)}(\text{diaspore}) + \text{SiO}_2(\text{quartz, alpha}) = \text{Al}_2\text{SiO}_5(\text{andalusite}) + \text{H}_2\text{O}(\text{gas})$   
 D)  $\text{Al}_2\text{SiO}_5(\text{andalusite}) + 3 \text{SiO}_2(\text{quartz, alpha}) + \text{H}_2\text{O}(\text{gas}) = \text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite})$   
 E)  $\text{Al}_2\text{SiO}_5(\text{andalusite}) = \text{Al}_2\text{SiO}_5(\text{sillimanite})$   
 F)  $\text{Al}_2\text{SiO}_5(\text{kyanite}) = \text{Al}_2\text{SiO}_5(\text{andalusite})$   
 G)  $\text{CaAl}_2\text{Si}_2\text{O}_8(\text{anorthite}) + \text{Al}_2\text{SiO}_5(\text{andalusite}) + \text{H}_2\text{O}(\text{gas}) = \text{CaAl}_4\text{Si}_2\text{O}_{10}(\text{OH})_2(\text{margarite}) + \text{SiO}_2(\text{quartz, alpha})$   
 H)  $\text{Al}_2\text{Si}_4\text{O}_{10}(\text{OH})_2(\text{pyrophyllite}) + 6 \text{AlO(OH)}(\text{diaspore}) = 4 \text{Al}_2\text{SiO}_5(\text{andalusite}) + 4 \text{H}_2\text{O}(\text{gas})$

- b Anderson and others (1977) measured the enthalpy of solution of andalusite in lead borate salt melt at 974.15 K. To complete the thermodynamic cycle, their data were evaluated in combination with the enthalpies of solution of quartz and corundum (Charlu and others, 1978) and the changes in enthalpy of solution with temperature (Shearer and Kleppa, 1973) in the salt melt. Corrections were not made for the enthalpies of dilution and of mixing of the product melts.
- c Hemley and others (in press) measured the silicic-acid content of water equilibrated with the mineral pairs: 1) andalusite-corundum, 2) andalusite-pyrophyllite, and 3) andalusite-diaspore between 600 K and 800 K at 100 and 200 MPa. Using their data for the solubility of quartz under the same conditions, the molar volumes of the solid phases, and the free-energy data for  $\text{H}_2\text{O}(\text{gas})$  of Fisher and Zen (1971), we calculated the free energy of reaction at 101.325 kPa and temperature for reactions A, B, and C for each observation.

The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for andalusite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-2590.270 \pm 0.641$  kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of andalusite and presents the data in their poorest perspective.

Most of the phase-equilibria data cited above bracket the regression fit in free-energy space. However, the phase-equilibria studies lack sufficient precision to constrain the fit tightly, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate.

The molar volume of andalusite was obtained from the work of Winter and Ghose (1979).

$\text{Al}_2\text{O}_5\text{Si}$ 

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$\text{Al}_2\text{SiO}_5$   
Kyanite (triclinic, polymorphous with Andalusite and Sillimanite)

| Temperature<br>(K)  | $C_p^\circ$<br>J/(mol·K) | $S^\circ$<br>J/(mol·K) | $(G_T^\circ - H_{T_f}^\circ)/T$<br>J/mol | Formation from the Elements          |                                |                         |  | Formation from the Oxides              |                             |  |                             |
|---------------------|--------------------------|------------------------|--|--------------------------------------|--------------------------------|-------------------------|--|--|-----------------------------|--|-----------------------------|
|                     |                          |                        |  | $H_T^\circ - H_{T_f}^\circ$<br>J/mol | $\Delta G_f^\circ, e$<br>J/mol | $\log K_f^\circ, e$     | $\Delta H_f^\circ, \text{ox}$<br>J/mol | $\Delta G_f^\circ, \text{ox}$<br>J/mol | $\log K_f^\circ, \text{ox}$ | $\Delta H_f^\circ, \text{ox}$<br>J/mol | $\log K_f^\circ, \text{ox}$ |
| 273.15              | 113.775                  | 74.123                 | -84.937                                  | -2954.                               | -2593700.                      | -2456680.               | 469.792                                | -7809.                                 | -5696.                      | 1.089                                  |                             |
| 298.15<br>(2 sigma) | 122.348<br>$\pm 0.154$   | 84.465<br>$\pm 0.439$  | -84.465<br>$\pm 0.439$                   | 0.<br>$\pm 0.$                       | -2594269.<br>$\pm 433.$        | -2444113.<br>$\pm 389.$ | 428.198<br>$\pm 0.068$                 | -7859.<br>$\pm 433.$                   | -5500.<br>$\pm 389.$        | 0.964<br>$\pm 0.068$                   |                             |
| 300.                | 122.936                  | 85.224                 | -84.468                                  | 227.                                 | -2594305.                      | -2443181.               | 425.395                                | -7862.                                 | -5486.                      | 0.955                                  |                             |
| 350.                | 136.874                  | 105.266                | -86.018                                  | 6737.                                | -2594939.                      | -2447932.               | 360.856                                | -7934.                                 | -5084.                      | 0.759                                  |                             |
| 400.                | 147.857                  | 124.288                | -89.624                                  | 13865.                               | -2595250.                      | -232615.                | 312.443                                | -7984.                                 | -4673.                      | 0.610                                  |                             |
| 450.                | 156.732                  | 142.233                | -94.483                                  | 21488.                               | -2595164.                      | -2367288.               | 274.787                                | -8025.                                 | -4256.                      | 0.494                                  |                             |
| 500.                | 164.039                  | 159.136                | -100.111                                 | 29512.                               | -2594820.                      | -2341985.               | 244.665                                | -8067.                                 | -3836.                      | 0.401                                  |                             |
| (2 sigma)           | $\pm 0.174$              | $\pm 0.436$            | $\pm 0.437$                              | $\pm 31.$                            | $\pm 32.$                      | $\pm 382.$              | $\pm 0.040$                            | $\pm 432.$                             | $\pm 382.$                  | $\pm 0.040$                            |                             |
| 550.                | 170.145                  | 175.066                | -106.208                                 | 37871.                               | -2594282.                      | -2316726.               | 220.024                                | -8120.                                 | -3410.                      | 0.324                                  |                             |
| 600.                | 175.305                  | 190.098                | -112.79                                  | 46611.                               | -2594599.                      | -221522.                | 221.98                                 | -8159.                                 | -3249.                      | 0.259                                  |                             |
| 650.                | 179.705                  | 204.308                | -119.093                                 | 55389.                               | -2592813.                      | -2226381.               | 182.128                                | -8234.                                 | -2541.                      | 0.204                                  |                             |
| 700.                | 183.483                  | 217.767                | -125.665                                 | 64471.                               | -2591958.                      | -2241302.               | 167.248                                | -8407.                                 | -2095.                      | 0.156                                  |                             |
| 750.                | 186.744                  | 230.540                | -132.335                                 | 73/29.                               | -2591064.                      | -2216286.               | 154.356                                | -8563.                                 | -1639.                      | 0.114                                  |                             |
| (2 sigma)           | $\pm 0.160$              | $\pm 0.440$            | $\pm 0.435$                              | $\pm 66.$                            | $\pm 432.$                     | $\pm 402.$              | $\pm 0.028$                            | $\pm 432.$                             | $\pm 402.$                  | $\pm 0.028$                            |                             |
| 800.                | 189.571                  | 242.685                | -138.761                                 | 83139.                               | -2590157.                      | -2191331.               | 143.079                                | -8757.                                 | -1171.                      | 0.076                                  |                             |
| 850.                | 192.028                  | 254.253                | -145.117                                 | 92680.                               | -2589261.                      | -2166432.               | 133.133                                | -9710.                                 | -685.                       | 0.042                                  |                             |
| 900.                | 194.168                  | 265.291                | -151.584                                 | 102336.                              | -2588396.                      | -2141585.               | 124.294                                | -9569.                                 | -158.                       | 0.009                                  |                             |
| 950.                | 196.033                  | 275.840                | -157.848                                 | 112092.                              | -2609345.                      | -216392.                | 116.367                                | -9412.                                 | -361.                       | -0.020                                 |                             |
| 1000.               | 197.657                  | 285.937                | -164.002                                 | 121935.                              | -2608075.                      | -2030485.               | 109.196                                | -9245.                                 | -871.                       | -0.046                                 |                             |
| (2 sigma)           | $\pm 0.306$              | $\pm 0.442$            | $\pm 0.434$                              | $\pm 91.$                            | $\pm 432.$                     | $\pm 449.$              | $\pm 0.023$                            | $\pm 432.$                             | $\pm 449.$                  | $\pm 0.023$                            |                             |
| 1050.               | 199.070                  | 295.616                | -170.041                                 | 131854.                              | -2607020.                      | -2064632.               | 102.710                                | -9075.                                 | -1373.                      | -0.068                                 |                             |
| 1100.               | 200.296                  | 304.903                | -175.661                                 | 141839.                              | -2605931.                      | -2038830.               | 91.816                                 | -8955.                                 | -1866.                      | -0.089                                 |                             |
| 1150.               | 201.356                  | 313.833                | -181.763                                 | 151881.                              | -2604832.                      | -2013077.               | 91.437                                 | -8743.                                 | -2352.                      | -0.107                                 |                             |
| 1200.               | 202.267                  | 322.423                | -187.446                                 | 161972.                              | -2603711.                      | -1987372.               | 86.508                                 | -8591.                                 | -2831.                      | -0.123                                 |                             |
| 1250.               | 203.044                  | 330.696                | -193.011                                 | 172106.                              | -2602578.                      | -1981715.               | 81.976                                 | -8456.                                 | -3304.                      | -0.138                                 |                             |
| (2 sigma)           | $\pm 0.564$              | $\pm 0.453$            | $\pm 0.434$                              | $\pm 160.$                           | $\pm 447.$                     | $\pm 516.$              | $\pm 0.022$                            | $\pm 447.$                             | $\pm 516.$                  | $\pm 0.022$                            |                             |
| 1300.               | 203.700                  | 338.672                | -198.461                                 | 182275.                              | -2601438.                      | -1936103.               | 77.794                                 | -8340.                                 | -3773.                      | -0.152                                 |                             |
| 1350.               | 204.246                  | 346.371                | -203.98                                  | 192474.                              | -2600294.                      | -1910535.               | 73.923                                 | -8249.                                 | -4237.                      | -0.164                                 |                             |
| 1400.               | 204.693                  | 353.807                | -209.023                                 | 202698.                              | -2599150.                      | -1885009.               | 70.330                                 | -8186.                                 | -4698.                      | -0.175                                 |                             |
| 1450.               | 205.043                  | 360.996                | -214.140                                 | 212942.                              | -2598008.                      | -1889524.               | 66.987                                 | -8155.                                 | -5157.                      | -0.186                                 |                             |
| 1500.               | 205.321                  | 367.953                | -219.552                                 | 233201.                              | -2596871.                      | -1834078.               | 63.868                                 | -8160.                                 | -5616.                      | -0.196                                 |                             |
| (2 sigma)           | $\pm 0.865$              | $\pm 0.493$            | $\pm 0.435$                              | $\pm 314.$                           | $\pm 519.$                     | $\pm 598.$              | $\pm 0.021$                            | $\pm 519.$                             | $\pm 598.$                  | $\pm 0.021$                            |                             |
| 1550.               | 205.516                  | 374.689                | -224.061                                 | 233472.                              | -2595142.                      | -1808671.               | 60.952                                 | -8204.                                 | -6076.                      | -0.205                                 |                             |
| 1600.               | 205.641                  | 381.216                | -228.871                                 | 243752.                              | -2594621.                      | -1783299.               | 58.219                                 | -8292.                                 | -6538.                      | -0.213                                 |                             |

$\text{Al}_2\text{O}_5\text{Si}$  $\text{Al}_2\text{SiO}_5$ 

Kyanite

Formula weight = 162.046 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\%$ )

$S^\circ = 84.47 \pm 0.44 \text{ J/(mol}\cdot\text{K)}$

$\Delta H_f^\circ = -2594.27 \pm 0.43 \text{ kJ/mol}$

$V^\circ = 44.22 \pm 0.02 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -2444.11 \pm 0.39 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1600 K)

$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$

$S(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$

$[\text{H}^\circ(T) - \text{H}^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

$a_1 = 0.0$

$a_4 = -2.23489 \times 10^3$

$a_6 = -1.29800 \times 10^{-2}$

$a_2 = 2.37951 \times 10^4$

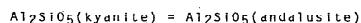
$a_5 = 3.36114 \times 10^2$

$a_7 = 0.0$

$a_3 = -3.55746 \times 10^3$

Critical Reactions

Inversion:



$T_i = 430.46 \text{ (calculated)}$

$\Delta S_i^\circ = 9.20 \pm 1.80 \text{ J/(mol}\cdot\text{K)}$

$\Delta H_i^\circ = 3.96 \pm 0.77 \text{ kJ/mol}$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of kyanite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                                  | Data Type         | Method                 | No. of Points | Range        |
|---|-------------------|------------------------|---------------|--------------|
| Todd (1950) <sup>a</sup>                | heat capacity     | isothermal calorimetry | 10            | 206 - 296 K  |
| Pankratz and Kelley (1964) <sup>a</sup> | relative enthalpy | drop calorimetry       | 12            | 390 - 1503 K |
| Todd (1950) <sup>a</sup>                | entropy           | isothermal calorimetry | 1             | 298.15 K     |

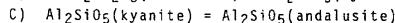
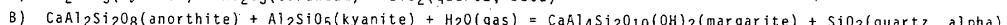
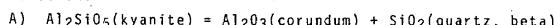
a The measurements were made on an impure natural sample of kyanite. The observed heat-capacity and entropy values were assumed to equal the molar sum of the heat capacities and entropies, respectively, of the components. The stoichiometry used in calculation: kyanite, 0.9928; corundum, 0.0091; hematite, 0.001; lime, 0.0014.

The standard error of estimate of the fitted heat capacity of Todd (1950) is 0.62 J/(mol·K). The standard error of estimate of the fitted relative enthalpy measurements of Pankratz and Kelley (1964) is 263 J/mol, or approximately 0.2 percent of the observed value. The fitted entropy of 298.15 K is  $84.47 \pm 0.44 \text{ J/(mol}\cdot\text{K)}$ , or a departure of 0.7 J/mol from the experimental value of  $83.77 \pm 0.33$  calculated from Todd (1950).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                  | Method                                | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---|---------------------------------------|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Anderson and Kleppa (1969) <sup>b</sup> | solution calorimetry<br>(borate salt) | A                     | 974       | 1             | $6.135 \pm 0.450$                    | -2595.993                            |
| Storre and Nitsch (1974)                | gas-medium pressure apparatus         | B                     | 803-933   | 6             | $-81.952 \pm 1.121$                  | -2593.649                            |
| Newton (1966a)                          | gas-medium pressure apparatus         | C                     | 973-1123  | 7             | $4.021 \pm 0.218$                    | -2594.313                            |
| Holdaway (1971)                         | gas-medium pressure apparatus         | C                     | 650-858   | 6             | $4.215 \pm 0.179$                    | -2594.507                            |

a Reactions:



b Anderson and Kleppa (1969) measured the enthalpy of solution of kyanite in lead borate salt melt at 974.15 K. To complete the thermodynamic cycle, their data were evaluated in combination with the enthalpies of solution of quartz and corundum (Charlu and others, 1978) and the changes in enthalpy of solution with temperature (Shearer and Kleppa, 1973) in the salt melt. Corrections were not made for the enthalpies of dilution and of mixing of the product melts.

Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for  $\text{H}_2\text{O}(\text{gas})$  from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for kyanite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-2594.269 \pm 0.433 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of kyanite and presents the data in their poorest perspective.

Most of the phase-equilibrium data cited above bracket the regression fit in free-energy space. However, the phase-equilibrium studies lack sufficient precision to constrain the fit tightly, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate.

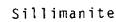
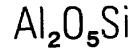
The molar volume of kyanite was obtained from the work of Winter and Ghose (1979).

Al<sub>2</sub>O<sub>5</sub>Si

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| Temperature<br>(K)  | C <sub>p</sub><br>J/(mol·K) | S <sup>e</sup><br>J/(mol·K) | (G <sub>T</sub> <sup>o</sup> -H <sub>T</sub> <sup>o</sup> ) <sub>r</sub> /T<br>J/(mol·K) | H <sub>T</sub> <sup>o</sup> -H <sub>T</sub> <sup>o</sup> <sub>r</sub><br>J/mol | Formation from the Elements               |   |                                     | Formation from the Oxides                  |  |                                      |
|---------------------|-----------------------------|-----------------------------|--|--|---|---|-------------------------------------|--|--|--------------------------------------|
|                     |                             |                             |  |  | ΔH <sub>f</sub> <sup>o</sup> , e<br>J/mol | ΔG <sub>f</sub> <sup>o</sup> , e<br>J/mol | log K <sub>f</sub> <sup>o</sup> , e | ΔH <sub>f</sub> <sup>o</sup> , ox<br>J/mol | ΔG <sub>f</sub> <sup>o</sup> , ox<br>J/mol | log K <sub>f</sub> <sup>o</sup> , ox |
| 273.15              | 116.803                     | 85.519                      | -96.572  | -3019.   | -2587269.                                 | -2453363.                                 | 469.158                             | -1378.                                     | -2378.                                     | 0.455                                |
| 298.15<br>(2 sigma) | 124.533<br>±0.159           | 96.090<br>±0.550            | -96.090<br>±0.550  | 0.<br>±0.  | -2587774.<br>±537.                        | -2441083.<br>±443.                        | 427.667<br>±0.078                   | -1363.<br>±537.                            | -2471.<br>±443.                            | 0.433<br>±0.078                      |
| 300.                | 125.064                     | 96.862                      | -96.092  | 231.   | -2587306.                                 | -2440173.                                 | 424.872                             | -1363.                                     | -2477.                                     | 0.431                                |
| 350.                | 137.672                     | 97.664                      | -97.664  | 6812.  | -2588428.                                 | -241512.                                  | 360.995                             | -1363.                                     | -2664.                                     | 0.398                                |
| 400.                | 147.650                     | 136.127                     | -101.300   | 13954.   | -2588365.                                 | -2390790.                                 | 312.05                              | -1399.                                     | -2848.                                     | 0.372                                |
| 450.                | 155.753                     | 154.061                     | -106.180   | 21546.   | -2588509.                                 | -2366056.                                 | 274.644                             | -1470.                                     | -3025.                                     | 0.351                                |
| 500.                | 162.463                     | 170.829                     | -111.816   | 2507.  | -2588330.                                 | -2341341.                                 | 244.998                             | -1577.                                     | -3192.                                     | 0.333                                |
| (2 sigma)           | ±0.176                      | ±0.548                      | ±0.548   | ±32.   | ±537.                                     | ±406.                                     | ±0.042                              | ±537.                                      | ±406.                                      | ±0.042                               |
| 550.                | 168.102                     | 186.585                     | -117.904   | 37775.   | -2587383.                                 | -2316663.                                 | 220.018                             | -1721.                                     | -3347.                                     | 0.318                                |
| 600.                | 172.900                     | 201.423                     | -124.252   | 46103.   | -2587312.                                 | -2292031.                                 | 199.539                             | -1903.                                     | -3487.                                     | 0.304                                |
| 650.                | 177.022                     | 215.430                     | -130.732   | 55054.   | -2586653.                                 | -2267450.                                 | 182.214                             | -2124.                                     | -3610.                                     | 0.290                                |
| 700.                | 180.591                     | 228.682                     | -137.259   | 63996.   | -2585937.                                 | -222922.                                  | 167.369                             | -2386.                                     | -3715.                                     | 0.277                                |
| 750.                | 183.700                     | 241.250                     | -143.777   | 73105.   | -2555192.                                 | -221847.                                  | 154.906                             | -2691.                                     | -3799.                                     | 0.265                                |
| (2 sigma)           | ±0.161                      | ±0.551                      | ±0.551   | ±66.   | ±538.                                     | ±399.                                     | ±0.028                              | ±538.                                      | ±399.                                      | ±0.028                               |
| 800.                | 186.422                     | 253.194                     | -150.245   | 82359.   | -2584441.                                 | -2194022.                                 | 143.255                             | -1040.                                     | -3862.                                     | 0.252                                |
| 850.                | 188.816                     | 264.570                     | -156.938   | 91742.   | -2587084.                                 | -2165644.                                 | 133.30                              | -1153.                                     | -3896.                                     | 0.239                                |
| 900.                | 190.927                     | 275.423                     | -162.938   | 101236.  | -2583300.                                 | -2143308.                                 | 124.510                             | -1173.                                     | -3881.                                     | 0.225                                |
| 950.                | 192.794                     | 285.97                      | -169.133   | 110830.  | -2603361.                                 | -2120617.                                 | 116.600                             | -1178.                                     | -3864.                                     | 0.212                                |
| (2 sigma)           | ±0.309                      | ±0.552                      | ±0.552   | ±92.   | ±539.                                     | ±438.                                     | ±0.023                              | ±539.                                      | ±438.                                      | ±0.023                               |
| 1000.               | 194.447                     | 295.729                     | -175.217   | 120512.  | -2603003.                                 | -209205.                                  | 109.042                             | -1173.                                     | -3848.                                     | 0.201                                |
| (2 sigma)           | ±0.309                      | ±0.552                      | ±0.552   | ±92.   | ±539.                                     | ±438.                                     | ±0.023                              | ±539.                                      | ±438.                                      | ±0.023                               |
| 1050.               | 195.912                     | 305.252                     | -181.184   | 130672.  | -2602107.                                 | -2069837.                                 | 102.969                             | -1161.                                     | -3832.                                     | 0.191                                |
| 1100.               | 197.210                     | 314.937                     | -187.032   | 140101.  | -2601180.                                 | -2045112.                                 | 97.086                              | -1161.                                     | -3816.                                     | 0.181                                |
| 1150.               | 198.361                     | 323.189                     | -192.762   | 149990.  | -2600227.                                 | -2019231.                                 | 91.716                              | -1138.                                     | -3802.                                     | 0.173                                |
| 1200.               | 199.379                     | 331.653                     | -198.374   | 159335.  | -2599253.                                 | -199391.                                  | 86.976                              | -1139.                                     | -3787.                                     | 0.165                                |
| 1250.               | 200.278                     | 339.811                     | -203.869   | 169926.  | -2598262.                                 | -196792.                                  | 82.771                              | -1139.                                     | -3773.                                     | 0.158                                |
| (2 sigma)           | ±0.572                      | ±0.562                      | ±0.562   | ±161.  | ±531.                                     | ±513.                                     | ±0.021                              | ±551.                                      | ±513.                                      | ±0.021                               |
| 1300.               | 201.069                     | 347.681                     | -209.250   | 179960.  | -2597256.                                 | -1943633.                                 | 78.096                              | -1159.                                     | -3758.                                     | 0.151                                |
| 1350.               | 201.763                     | 355.283                     | -214.519   | 190032.  | -2596240.                                 | -1938513.                                 | 74.232                              | -1159.                                     | -3742.                                     | 0.145                                |
| 1400.               | 202.368                     | 362.632                     | -219.578   | 200335.  | -2595216.                                 | -193430.                                  | 70.545                              | -1153.                                     | -3729.                                     | 0.139                                |
| 1450.               | 202.892                     | 369.743                     | -224.331   | 21067.   | -2594187.                                 | -1883835.                                 | 67.306                              | -1154.                                     | -3734.                                     | 0.133                                |
| 1500.               | 203.342                     | 376.629                     | -229.660   | 220423.  | -2593154.                                 | -1843375.                                 | 64.192                              | -1152.                                     | -3680.                                     | 0.128                                |
| (2 sigma)           | ±0.879                      | ±0.595                      | ±0.595   | ±318.  | ±612.                                     | ±611.                                     | ±0.021                              | ±612.                                      | ±611.                                      | ±0.021                               |
| 1550.               | 203.723                     | 383.303                     | -234.528   | 23000.   | -2592118.                                 | -183399.                                  | 61.280                              | -1159.                                     | -3652.                                     | 0.123                                |
| 1600.               | 204.042                     | 389.776                     | -239.229   | 240794.  | -2591083.                                 | -1794547.                                 | 58.550                              | -1153.                                     | -3620.                                     | 0.118                                |
| 1650.               | 204.303                     | 396.059                     | -243.935   | 25103.   | -2590048.                                 | -176547.                                  | 55.987                              | -1152.                                     | -3581.                                     | 0.113                                |
| 1700.               | 204.510                     | 402.161                     | -248.500   | 26124.   | -263925.                                  | -173219.                                  | 53.563                              | -1151.                                     | -3536.                                     | 0.109                                |
| 1750.               | 204.658                     | 408.992                     | -252.975   | 271454.  | -2638354.                                 | -176874.                                  | 51.246                              | -1150.                                     | -3482.                                     | 0.104                                |
| (2 sigma)           | ±1.208                      | ±0.668                      | ±0.668   | ±564.  | ±617.                                     | ±730.                                     | ±0.022                              | ±617.                                      | ±730.                                      | ±0.022                               |
| 1800.               | 204.779                     | 413.859                     | -257.364   | 281690.  | -2637182.                                 | -1690563.                                 | 49.059                              | -1811.                                     | -3420.                                     | 0.099                                |
| (2 sigma)           | ±1.276                      | ±0.688                      | ±0.688   | ±624.  | ±311.                                     | ±756.                                     | ±0.022                              | ±811.                                      | ±756.                                      | ±0.022                               |

HAAS, ROBINSON, AND HEMINGWAY



Formula weight = 162.046 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 96.090 \pm 0.550 \text{ J/(mol}\cdot\text{K)} \quad \Delta H_f^\circ = -2587.774 \pm 0.537 \text{ kJ/mol}$$

$$V^\circ = 50.049 \pm 0.014 \text{ cm}^3/\text{mol} \quad \Delta G_f^\circ = -2441.083 \pm 0.443 \text{ kJ/mol}$$

Equations at Reference Pressure, 101,325 kPa (Temperature range 200 to 1800 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T)-H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

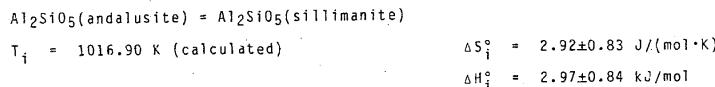
$$a_1 = 0.0 \quad a_4 = -2.050871 \times 10^3 \quad a_6 = -9.470810 \times 10^{-3}$$

$$a_2 = 1.66762 \times 10^4 \quad a_5 = 3.134705 \times 10^2 \quad a_7 = 0.0$$

$$a_3 = -3.164868 \times 10^3$$

Critical Reactions

## Inversion:

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of sillimanite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                                  | Data Type         | Method                 | No. of Points | Range        |
|---|-------------------|------------------------|---------------|--------------|
| Todd (1950) <sup>a</sup>                | heat capacity     | isothermal calorimetry | 10            | 206 - 297 K  |
| Pankratz and Kelley (1964) <sup>a</sup> | relative enthalpy | drop calorimetry       | 13            | 401 - 1496 K |
| Todd (1950) <sup>a</sup>                | entropy           | isothermal calorimetry | 1             | 298.15 K     |

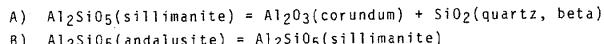
a The measurements were made on an impure natural sample of sillimanite. The observed heat-capacity and entropy values were assumed to equal the molar sum of the heat capacities and entropies, respectively, of the components. The stoichiometry used was: sillimanite, 0.9821; hematite, 0.0068; magnetite, 0.0032; Mg<sub>3</sub>(PO<sub>4</sub>), 0.0027; Mg<sub>2</sub>, 0.0017; MnO, 0.0009; quartz, 0.0008; whitlockite, 0.0007; P<sub>2</sub>O<sub>5</sub>(crystal), 0.0004.

The heat capacity measured by Todd (1950) was fit with a standard error of estimate of 0.61 J/(mol·K). The relative enthalpy measurements of Pankratz and Kelley (1964) were fit with a standard error of estimate of 2675 J/mol or approximately 1.3 percent of the observed value. The fitted entropy at 298.15 K is 96.09 ± 0.55 J/(mol·K), or a departure of 0.02 J/mol from the experimental value, corrected for composition, of 96.11 ± 0.42 calculated from the data of Todd (1950).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                                | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---------------------------------------|---------------------------------------|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Charlu and others (1978) <sup>b</sup> | solution calorimetry<br>(borate salt) | A                     | 970       | 1             | -0.432 ± 0.583                       | -2585.979                            |
| Holdaway (1971)                       | gas-medium pressure apparatus         | B                     | 764-917   | 2 pair        | 2.483 ± 0.063                        | -2587.799                            |

## a Reactions:



b Charlu and others (1978) measured the enthalpy of solution of sillimanite in lead borate salt melt at 970 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of quartz and corundum in the salt melt; corrections were not made for the enthalpies of dilution and of mixing of the product melts.

The phase-equilibrium study of Holdaway (1971) was evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for H<sub>2</sub>O(gas) from Fisher and Zen (1971) were used in the conversion. The study cited in Table 2 complies with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for sillimanite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of -2587.774 ± 0.537 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of sillimanite and presents the data in their poorest perspective.

The phase-equilibria data cited above bracket the regression fit in free-energy space.

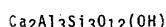
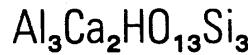
The molar volume of sillimanite was obtained from the work of Winter and Ghose (1979).

**$\text{Al}_3\text{Ca}_2\text{HO}_{13}\text{Si}_3$**   
**Zoisite (orthorhombic, dimorphous with Clinzoisite, member of Epidote Group)**  
 Issued September, 1979

| Temperature<br>( $\text{K}$ ) | $C_p^{\circ}$<br>$\text{J}/(\text{mol} \cdot \text{K})$ | $S^{\circ}$<br>$\text{J}/(\text{mol} \cdot \text{K})$ | $(G_f^{\circ} - H_f^{\circ})/T$<br>$\text{J}/\text{mol}$ | $H_f^{\circ} - H_T^{\circ}$<br>$\text{J}/\text{mol}$ | Formation from the Elements                      |                         |  | Formation from the Oxides     |  |                               |
|-------------------------------|---|---|--|--|--|-------------------------|--|-------------------------------|--|-------------------------------|
|                               |   |   |  |  | $\Delta G_f^{\circ}, e$<br>$\text{J}/\text{mol}$ | $\log K_f^{\circ}, e$   | $\Delta G_f^{\circ}, \text{ox}$<br>$\text{J}/\text{mol}$ | $\log K_f^{\circ}, \text{ox}$ | $\Delta G_f^{\circ}, \text{ox}$<br>$\text{J}/\text{mol}$ | $\log K_f^{\circ}, \text{ox}$ |
| 273.15                        | 330.732   | 266.032   | -297.244   | -8526.   | -6889989.  | -6528649.               | 1248.477   | -231737.                      | -221957.   | 43.592                        |
| 293.15<br>(2 sigma)           | 350.863<br>$\pm 0.563$                                  | 295.885<br>$\pm 0.662$                                | -295.885<br>$\pm 0.$                                     | 0.<br>$\pm 0.662$                                    | -6891117.<br>$\pm 877.$                          | -6495524.<br>$\pm 745.$ | 1137.988<br>$\pm 0.130$                                  | -232353.<br>$\pm 87.$         | -227583.<br>$\pm 745.$                                   | 39.872<br>$\pm 0.130$         |
| 300.                          | 352.247   | 298.059   | -295.891   | 650.   | -6891186.  | -6493069.               | 1130.543   | -224083.<br>$\pm 87.$         | -224083.<br>$\pm 87.$                                    | 39.621<br>$\pm 0.130$         |
| 350.                          | 385.162   | 357.934   | -300.320   | 19119.   | -6892422.  | -6426603.               | 1159.117   | -235583.<br>$\pm 87.$         | -226650.<br>$\pm 87.$                                    | 33.822<br>$\pm 0.130$         |
| 400.                          | 411.309   | 408.134   | -310.498   | 39054.   | -6892647.  | -6360031.               | 830.534  | -254578.<br>$\pm 87.$         | -221132.<br>$\pm 87.$                                    | 29.269<br>$\pm 0.130$         |
| 450.                          | 432.626   | 457.851   | -324.140   | 60170.   | -6892114.  | -6263479.               | 730.528  | -254640.<br>$\pm 87.$         | -220323.<br>$\pm 87.$                                    | 25.574<br>$\pm 0.130$         |
| 500.                          | 450.554   | 504.377   | -339.863   | 82257.   | -6891015.  | -6227019.               | 650.532  | -25705.<br>$\pm 97.$          | -21656.<br>$\pm 97.$                                     | 22.618<br>$\pm 0.068$         |
| (2 sigma)                     | $\pm 1.382$   | $\pm 0.852$   | $\pm 0.669$  | $\pm 220.$   | $\pm 977.$                                       | $\pm 654.$              | $\pm 0.068$  | $\pm 97.$                     | $\pm 654.$   | $\pm 0.068$                   |
| 550.                          | 465.329   | 548.022   | -356.823   | 105160.  | -6889496.  | -6160690.               | 585.093  | -254795.<br>$\pm 87.$         | -21682.<br>$\pm 87.$                                     | 20.199<br>$\pm 0.130$         |
| 600.                          | 478.137   | 589.074   | -374.484   | 128754.  | -6887679.  | -6034513.               | 530.574  | -251931.<br>$\pm 87.$         | -208848.<br>$\pm 87.$                                    | 18.182<br>$\pm 0.130$         |
| 650.                          | 489.204   | 627.793   | -392.494   | 152944.  | -6885661.  | -6028497.               | 484.456  | -25128.<br>$\pm 87.$          | -205001.<br>$\pm 87.$                                    | 16.474<br>$\pm 0.130$         |
| 700.                          | 498.846   | 664.408   | -410.621   | 177651.  | -6883526.  | -5966640.               | 444.937  | -255402.<br>$\pm 87.$         | -201135.<br>$\pm 87.$                                    | 15.009<br>$\pm 0.130$         |
| 750.                          | 507.05  | 699.119   | -428.707   | 202809.  | -6883014.  | -5898666.               | 410.694  | -25765.<br>$\pm 87.$          | -19747.<br>$\pm 87.$                                     | 13.737<br>$\pm 0.130$         |
| (2 sigma)                     | $\pm 2.438$   | $\pm 1.066$   | $\pm 0.728$  | $\pm 431.$   | $\pm 1135.$                                      | $\pm 520.$              | $\pm 0.036$  | $\pm 1135.$                   | $\pm 520.$   | $\pm 0.036$                   |
| 800.                          | 514.769   | 732.103   | -446.647   | 228365.  | -6880626.  | -5831201.               | 380.738  | -255231.<br>$\pm 87.$         | -193331.<br>$\pm 87.$                                    | 12.623<br>$\pm 0.130$         |
| 850.                          | 521.386   | 763.53  | -464.370   | 254272.  | -6878374.  | -5755682.               | 354.315  | -25859.<br>$\pm 87.$          | -189367.<br>$\pm 87.$                                    | 11.637<br>$\pm 0.130$         |
| 900.                          | 527.277   | 794.485   | -481.828   | 280491.  | -6876236.  | -5700290.               | 330.836  | -258388.<br>$\pm 87.$         | -185289.<br>$\pm 87.$                                    | 10.754<br>$\pm 0.130$         |
| 950.                          | 532.337   | 822.117   | -498.990   | 306989.  | -6906700.  | -5634420.               | 309.302  | -257511.<br>$\pm 87.$         | -181245.<br>$\pm 87.$                                    | 9.966<br>$\pm 0.130$          |
| 1000.                         | 537.247   | 849.575   | -515.839   | 333736.  | -6904672.  | -5567510.               | 290.817  | -257056.<br>$\pm 87.$         | -177236.<br>$\pm 87.$                                    | 9.258<br>$\pm 0.130$          |
| (2 sigma)                     | $\pm 6.928$   | $\pm 1.564$   | $\pm 0.77$   | $\pm 1237.$  | $\pm 1614.$                                      | $\pm 441.$              | $\pm 0.023$  | $\pm 1614.$                   | $\pm 441.$   | $\pm 0.023$                   |
| 1050.                         | 541.472   | 875.891   | -532.362   | 360706.  | -6902739.  | -5500700.               | 273.645  | -256345.<br>$\pm 87.$         | -171263.<br>$\pm 87.$                                    | 8.619<br>$\pm 0.130$          |
| 1100.                         | 545.270   | 901.170   | -548.555   | 387876.  | -6900917.  | -5433980.               | 258.038  | -255605.<br>$\pm 87.$         | -169324.<br>$\pm 87.$                                    | 8.040<br>$\pm 0.130$          |
| 1150.                         | 548.886   | 925.484   | -564.418   | 415226.  | -6914966.  | -53366779.              | 243.167  | -25859.<br>$\pm 87.$          | -16518.<br>$\pm 87.$                                     | 7.514<br>$\pm 0.130$          |
| 1200.                         | 551.761   | 948.902   | -579.953   | 442739.  | -69111523.                                       | -5293540.               | 230.683  | -25119.<br>$\pm 87.$          | -161546.<br>$\pm 87.$                                    | 7.032<br>$\pm 0.130$          |
| 1250.                         | 554.529   | 971.483   | -595.166   | 470397.  | -6908021.  | -5222445.               | 218.652  | -233325.<br>$\pm 87.$         | -157703.<br>$\pm 87.$                                    | 6.590<br>$\pm 0.130$          |
| (2 sigma)                     | $\pm 12.441$  | $\pm 3.342$   | $\pm 0.907$  | $\pm 3531.$  | $\pm 3630.$                                      | $\pm 736.$              | $\pm 0.031$  | $\pm 3630.$                   | $\pm 736.$   | $\pm 0.031$                   |

## THERMODYNAMIC DATA FOR MINERALS

627



Zoisite

Formula weight = 454.361 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 295.885 \pm 0.662 \text{ J}/(\text{mol}\cdot\text{K}) \quad \Delta H_f^\circ = -6891.117 \pm 0.877 \text{ kJ/mol}$$

$$V^\circ = 136.520 \pm 0.400 \text{ cm}^3/\text{mol} \quad \Delta G_f^\circ = -6495.524 \pm 0.745 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1250 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^{2/2}$$

$$[H^\circ(T)-H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^{3/3}$$

$$a_1 = 0.0 \quad a_4 = 5.391475 \times 10^3 \quad a_6 = -1.984469 \times 10^{-2}$$

$$a_2 = 1.225488 \times 10^5 \quad a_5 = 8.346223 \times 10^2 \quad a_7 = 0.0$$

$$a_3 = -8.148754 \times 10^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of zoisite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

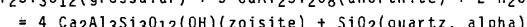
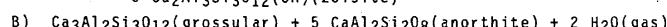
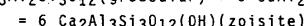
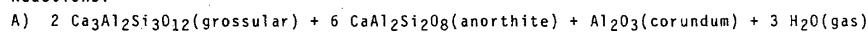
| Source                    | Data Type     | Method                | No. of Points | Range       |
|---------------------------|---------------|-----------------------|---------------|-------------|
| Perkins and others (1980) | heat capacity | adiabatic calorimetry | 8             | 200 - 298 K |
| Perkins and others (1980) | heat capacity | differential scanning | 11            | 298 - 730 K |
| Perkins and others (1980) | entropy       | adiabatic calorimetry | 1             | 298.15 K    |

The compositionally adjusted heat capacities that were obtained on a natural zoisite by Perkins and others (1980) using an adiabatic calorimeter and differential scanning calorimeter were fit with a standard error of estimate of 1.5 and 1.7  $\text{J}/(\text{mol}\cdot\text{K})$ , respectively. The fitted entropy at 298.15 K is  $295.885 \pm 0.662 \text{ J}/(\text{mol}\cdot\text{K})$  or a departure of 0.03  $\text{J}/\text{mol}$  from the compositionally adjusted value of  $295.85 \pm 0.29$  reported by Perkins and others.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source           | Method                                   | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|------------------|--|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Newton (1965)    | gas- and solid-medium pressure apparatus | A                     | 843-1113  | 6 pair        | -306.468 $\pm 2.790$                 | -6891.532                            |
| Boettcher (1970) | gas-medium pressure apparatus            | A                     | 898-928   | 1 pair        | -308.308 $\pm 4.088$                 | -6891.225                            |
| Strens (1968)    | gas-medium pressure apparatus            | B                     | 770-823   | 1 pair        | -220.561 $\pm 5.976$                 | -6892.258                            |
| Boettcher (1970) | gas-medium pressure apparatus            | B                     | 853-933   | 2 pair        | -213.025 $\pm 2.944$                 | -6890.374                            |

a Reactions:



Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for  $\text{H}_2\text{O}(\text{gas})$  from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

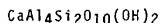
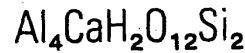
After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for zoisite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-6891.117 \pm 0.877 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of zoisite and presents the data in their poorest perspective. Most of the phase-equilibria data cited above bracket the regression fit in free-energy space.

The molar volume of zoisite was obtained from the compilation of Robie and others (1967).

$\text{CaAl}_4\text{Si}_2\text{O}_{10}(\text{OH})_2$   
Margarite (monoclinic, Mica Group)

Issued September, 1979  
Al<sub>4</sub>CaH<sub>2</sub>O<sub>12</sub>Si<sub>2</sub>

| Temperature<br>(K) | $C_p^o$<br>$\text{J}/(\text{mol}\cdot\text{K})$ | $S^o$<br>$\text{J}/(\text{mol}\cdot\text{K})$ | $(G_T^o - H_{\text{Tr}}^o)/T$<br>$\text{J}/(\text{mol}\cdot\text{K})$ | Formation from the Elements                |  |  | Formation from the Oxides |  |  |
|--------------------|---|---|---|--|--|--|---------------------------|--|--|
|                    |   |   |   | $H_{\text{Tr}}^o$<br>$\text{J}/\text{mol}$ | $\Delta H_f^o, e$<br>$\text{J}/\text{mol}$ | $\Delta G_f^o, e$<br>$\text{J}/\text{mol}$ | $\log K_f^o, e$           | $\Delta H_f^o, \text{ox}$<br>$\text{J}/\text{mol}$ | $\Delta G_f^o, \text{ox}$<br>$\text{J}/\text{mol}$ |
| 273.15             | 302.855   | 236.210                                       | -264.893  | -7835.                                     | -6238317.                                  | -5887259.                                  | 1125.823                  | -144791.   | -137885.   |
| (2 sigma)          | 323.444<br>±0.515                               | 263.642<br>±0.594                             | -263.642<br>±0.594  | 0.<br>±0.                                  | -6239610.<br>±1023.                        | -5855068.<br>±949.                         | 1025.783<br>±0.166        | -145889.<br>±1023.                                 | -137203.<br>±909.                                  |
| 300.               | 324.858   | 265.647                                       | -263.648  | 600.                                       | -6239691.                                  | -5852682.                                  | 1010.042                  | -145967.<br>-147949.                               | -137119.<br>-135520.                               |
| 350.               | 358.437   | 318.353                                       | -267.734  | 17717.                                     | -6241190.                                  | -5788045.                                  | 86.818                    | -147949.<br>-189497.                               | -20.225.<br>-130718.                               |
| 400.               | 385.016   | 368.016                                       | -277.197  | 36327.                                     | -6241660.                                  | -5723271.                                  | 747.382                   | -189092.<br>-188597.                               | 17.010.<br>14.323.                                 |
| 450.               | 406.600   | 414.652                                       | -283.906  | 56136.                                     | -6241181.                                  | -5638497.                                  | 65.821                    | -123394.<br>-116120.                               | 12.131.<br>±0.095.                                 |
| 500.               | 424.472   | 458.445                                       | -304.593  | 76926.                                     | -6240332.                                  | -5593806.                                  | 58.380                    | -188597.<br>±1075.                                 | ±0.095.<br>±901.                                   |
| (2 sigma)          | ±1.136  | ±0.710  | ±0.598  | ±160.                                      | ±1015.                                     | ±905.                                      | ±0.095                    | ±1075.   | ±0.095.  |
| 550.               | 439.997   | 499.626                                       | -322.471  | 98535.                                     | -6238618.                                  | -5529243.                                  | 525.123                   | -188046.<br>-187466.                               | -101749.<br>-187466.                               |
| 600.               | 452.281   | 538.410                                       | -337.033  | 120338.                                    | -6236732.                                  | -5464836.                                  | 475.756                   | -186380.<br>-186380.                               | 8.856.<br>7.603.                                   |
| 650.               | 463.563   | 575.076                                       | -353.947  | 143733.                                    | -6234508.                                  | -5400596.                                  | 433.997                   | -186307.<br>-186307.                               | 6.532.<br>6.532.                                   |
| 700.               | 472.773   | 609.764                                       | -370.992  | 167140.                                    | -6232923.                                  | -5336526.                                  | 399.216                   | -185766.<br>-185766.                               | 5.606.<br>5.606.                                   |
| 750.               | 481.059   | 642.671                                       | -388.017  | 190990.                                    | -6230788.                                  | -5272587.                                  | 367.215                   | -80494.<br>±1191.                                  | -80494.<br>±856.                                   |
| (2 sigma)          | ±0.978  | ±0.980  | ±0.644  | ±404.                                      | ±1191.                                     | ±856.                                      | ±0.060                    | ±1191.   | ±0.060.  |
| 800.               | 488.316   | 673.954                                       | -404.918  | 215229.                                    | -6228287.                                  | -5208789.                                  | 340.099                   | -185270.<br>-186669.                               | -73494.<br>-66511.                                 |
| 850.               | 494.698   | 703.754                                       | -421.627  | 239807.                                    | -6225835.                                  | -5145145.                                  | 316.182                   | -185057.<br>-185057.                               | 4.087.<br>3.453.                                   |
| 900.               | 500.327   | 732.193                                       | -438.097  | 264886.                                    | -6223561.                                  | -5081641.                                  | 294.931                   | -183197.<br>-183197.                               | 5.2560.<br>5.2560.                                 |
| 950.               | 505.005   | 759.380                                       | -451.296  | 289829.                                    | -6264413.                                  | -5017477.                                  | 275.880                   | -182504.<br>-182504.                               | 2.3845.<br>2.3845.                                 |
| 1000.              | 509.714   | 785.413                                       | -470.206  | 315207.                                    | -6261914.                                  | -4951913.                                  | 255.661                   | ±1253.<br>±866.                                    | ±0.045.<br>±0.045.                                 |
| (2 sigma)          | ±1.983  | ±1.019  | ±0.711  | ±55.                                       | ±123.                                      | ±866.                                      | ±0.045                    | ±1253.   | ±0.045.  |
| 1050.              | 513.622   | 810.379                                       | -485.814  | 340792.                                    | -6259413.                                  | -4886475.                                  | 241.089                   | -181192.<br>-17975.                                | 1.934.<br>1.526.                                   |
| 1100.              | 517.087   | 834.34  | -501.116  | 366662.                                    | -6256926.                                  | -4821155.                                  | 226.937                   | -32132.<br>-178666.                                | 1.526.<br>1.156.                                   |
| 1150.              | 520.158   | 857.408                                       | -516.109  | 39295.                                     | -626232.                                   | -4756667.                                  | 216.009                   | -25445.<br>-177275.                                | 0.819.<br>0.511.                                   |
| 1200.              | 522.875   | 879.605                                       | -530.795  | 418512.                                    | -6258988.                                  | -4610231.                                  | 204.160                   | -18811.<br>-176014.                                | 0.819.<br>0.511.                                   |
| 1250.              | 525.276   | 900.999                                       | -545.178  | 44477.                                     | -625556.                                   | -4634936.                                  | 194.265                   | -12239.<br>±1447.                                  | -12239.<br>±1447.                                  |
| (2 sigma)          | ±3.932  | ±1.243  | ±0.762  | ±1007.                                     | ±1447.                                     | ±955.                                      | ±0.040                    | ±1447.   | ±0.040.  |



Margarite

Formula weight = 398.186 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 263.642 \pm 0.594 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -6239.610 \pm 1.023 \text{ kJ/mol}$$

$$V^\circ = 133.800 \pm 0.100 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -5855.068 \pm 0.949 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1250 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 0.0 \quad a_4 = -5.406581 \times 10^3 \quad a_6 = -2.514555 \times 10^{-2}$$

$$a_2 = 1.254512 \times 10^5 \quad a_5 = 8.265040 \times 10^2 \quad a_7 = 0.0$$

$$a_3 = -8.42743810^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of margarite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

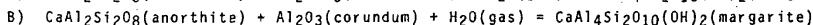
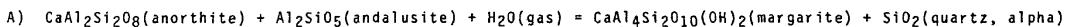
| Source                    | Data Type     | Method                            | No. of Points | Range        |
|---------------------------|---------------|-----------------------------------|---------------|--------------|
| Perkins and others (1980) | heat capacity | differential scanning calorimetry | 16            | 298 - 1000 K |
| Perkins and others (1980) | entropy       | adiabatic calorimetry             | 1             | 298.15 K     |

The compositionally adjusted heat capacities of Perkins and others (1980), obtained from measurements on a natural margarite sample, were fit with a standard error of estimate of 1.6 J/(mol·K). The fitted entropy value at 298.15 K is  $263.642 \pm 0.594 \text{ J/(mol}\cdot\text{K)}$  or a departure of 0.01 J/mol from the compositionally adjusted value of  $263.63 \pm 0.26 \text{ J/(mol}\cdot\text{K)}$  reported by Perkins and others.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                 | Method                                   | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|------------------------|--|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Storre & Nitsch (1974) | gas- and solid-medium pressure apparatus | A                     | 763-833   | 2 pair        | -89.818 ± 1.710                      | -6239.055                            |
| Chatterjee (1974)      | gas-medium pressure apparatus            | B                     | 763-893   | 5 pair        | -94.087 ± 0.931                      | -6239.467                            |

a Reactions:



Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for  $\text{H}_2\text{O(gas)}$  from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for margarite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-6239.610 \pm 1.023 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of margarite and presents the data in their poorest perspective. Most of the phase-equilibria data cited above bracket the regression fit in free-energy space.

The molar volume of margarite was obtained from the compilation of Hobie and others (1967).

## Ca

Issued September, 1979  
 Reference state:  
 alpha crystals (face-centered cubic) 273.15 K to 720 K  
 beta crystals (body-centered cubic) 720 K to 1112 K  
 liquid 1112 K to 1755 K  
 ideal monatomic gas 1755 K to 1800 K

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_f^o - H_f^o)/T$<br>J/mol | $H_f^o - H_{f,r}^o$<br>J/mol | Formation from the Elements |                            |                        | Formation from the Oxides   |                             |                        |
|--------------------|----------------------|--------------------|------------------------------|------------------------------|-----------------------------|----------------------------|------------------------|-----------------------------|-----------------------------|------------------------|
|                    |                      |                    |                              |                              | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, \alpha_x$ | $\Delta H_f^o, ox$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, \alpha_x$ |
| 273.15             | 25.180               | 39.404             | -41.716                      | -631.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 298.15             | 25.341               | 41.616             | -41.616                      | 0.                           | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 300.               | 25.354               | 41.773             | -41.617                      | 47.                          | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 350.               | 25.743               | 45.709             | -41.927                      | 1324.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 400.               | 26.255               | 49.178             | -42.620                      | 2623.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 450.               | 26.900               | 52.307             | -43.525                      | 3952.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 500.               | 27.671               | 55.180             | -44.549                      | 5315.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 550.               | 28.560               | 57.858             | -45.639                      | 6721.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 600.               | 29.558               | 60.385             | -46.763                      | 8173.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 650.               | 30.657               | 62.194             | -47.904                      | 9678.                        | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 700.               | 31.849               | 65.109             | -49.051                      | 11240.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 720.               | 32.351               | 66.013             | -49.510                      | 11882.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 720.               | 29.341               | 67.389             | -49.510                      | 12801.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 750.               | 30.581               | 68.512             | -50.245                      | 13700.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 800.               | 32.647               | 70.552             | -51.451                      | 15281.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 850.               | 34.712               | 72.593             | -52.634                      | 16965.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 900.               | 36.776               | 74.635             | -53.800                      | 18752.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 950.               | 38.840               | 76.679             | -54.950                      | 20642.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1000.              | 40.903               | 78.724             | -56.088                      | 22636.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1050.              | 42.966               | 80.769             | -57.214                      | 24733.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1100.              | 45.029               | 82.816             | -58.331                      | 26933.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1112.              | 45.524               | 83.307             | -58.538                      | 27476.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1112.              | 29.275               | 90.968             | -58.598                      | 35995.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1150.              | 29.275               | 91.952             | -59.684                      | 37108.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1150.              | 29.275               | 93.98              | -61.055                      | 38571.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1200.              | 29.275               | 94.393             | -62.365                      | 40035.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1250.              | 29.275               | 94.393             | -62.365                      | 40035.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1300.              | 29.275               | 95.541             | -63.619                      | 41499.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1350.              | 29.275               | 96.446             | -64.822                      | 42963.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1400.              | 29.275               | 97.711             | -65.977                      | 44427.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1450.              | 29.275               | 98.738             | -67.089                      | 45890.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1500.              | 29.275               | 99.730             | -68.161                      | 47354.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1550.              | 29.275               | 100.690            | -69.195                      | 48818.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1600.              | 29.275               | 101.620            | -70.194                      | 50282.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1650.              | 29.275               | 102.521            | -71.160                      | 51745.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1700.              | 29.275               | 103.395            | -72.095                      | 53209.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1750.              | 29.275               | 104.243            | -73.002                      | 54673.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1755.              | 29.275               | 104.327            | -73.091                      | 54819.                       | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1755.              | 20.851               | 191.628            | -73.091                      | 208032.                      | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |
| 1800.              | 20.862               | 192.156            | -76.081                      | 208971.                      | 0.                          | 0.                         | 0.                     | -                           | -                           | -                      |

## Ca

Ca (reference state) Calcium, alpha; Calcium, beta; Formula weight = 40.080 g/mol  
 Calcium, liquid; Calcium, ideal monatomic gas

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s) (calcium, alpha)

$$\begin{aligned} S^\circ &= 41.616 \text{ J/(mol}\cdot\text{K)} & \Delta H_f^\circ &= 0.0 \text{ kJ/mol} \\ V^\circ &= 26.190 \pm 0.04 \text{ cm}^3/\text{mol} & \Delta G_f^\circ &= 0.0 \text{ kJ/mol} \end{aligned}$$

Equations at Reference Pressure, 101.325 kPa

$$\begin{aligned} C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] &= a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2 \\ S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] &= -a_1/(2 T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2 \\ [H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) &= -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3 \end{aligned}$$

## Calcium, alpha (temperature range 200 to 720 K)

$$\begin{aligned} a_1 &= -2.20152 \times 10^5 & a_4 &= 7.62562 \times 10^1 & a_6 &= 9.83620 \times 10^{-3} \\ a_2 &= -1.42730 \times 10^4 & a_5 &= 0.0 & a_7 &= 9.72458 \times 10^{-6} \\ a_3 &= 3.64127 \times 10^2 & & & & \end{aligned}$$

## Calcium, beta (temperature range 720 to 1112 K)

$$\begin{aligned} a_1 &= 0.0 & a_4 &= 3.71052 \times 10^1 & a_6 &= 2.05709 \times 10^{-2} \\ a_2 &= -1.56800 \times 10^3 & a_5 &= 0.0 & a_7 &= 0.0 \\ a_3 &= -7.53816 & & & & \end{aligned}$$

## Calcium, liquid (temperature range 1112 to 1755 K)

$$\begin{aligned} a_1 &= 0.0 & a_4 &= -1.14367 \times 10^2 & a_6 &= 0.0 \\ a_2 &= -8.728 \times 10^3 & a_5 &= 2.92754 \times 10^1 & a_7 &= 0.0 \\ a_3 &= 0.0 & & & & \end{aligned}$$

## Calcium, ideal monatomic gas (temperature range 1755 to 1800 K)

$$\begin{aligned} a_1 &= 0.0 & a_4 &= 3.19488 \times 10^1 & a_6 &= -3.02477 \times 10^{-4} \\ a_2 &= -6.07200 \times 10^3 & a_5 &= 2.14177 \times 10^1 & a_7 &= 2.25282 \times 10^{-7} \\ a_3 &= -8.35017 \times 10^0 & & & & \end{aligned}$$

Critical Reactions

## Inversion:

$$\begin{aligned} \text{Ca(calcium, alpha)} &= \text{Ca(calcium, beta)} \\ T_i &= 720 \text{ K (observed)} & \Delta S_i^\circ &= 1.2276 \text{ J/(mol}\cdot\text{K)} \\ & & \Delta H_i^\circ &= 0.919 \text{ kJ/mol} \end{aligned}$$

## Melting:

$$\begin{aligned} \text{Ca(calcium, beta)} &= \text{Ca(calcium, liquid)} \\ T_m &= 1112 \text{ K (observed)} & \Delta S_m^\circ &= 7.661 \text{ J/(mol}\cdot\text{K)} \\ & & \Delta H_m^\circ &= 8.519 \text{ kJ/mol} \end{aligned}$$

## Vaporization:

$$\begin{aligned} \text{Ca(calcium, liquid)} &= \text{Ca(calcium, ideal monatomic gas)} \\ T_v &= 1755 \text{ K (observed)} & \Delta S_v^\circ &= 87.301 \text{ J/(mol}\cdot\text{K)} \\ & & \Delta H_v^\circ &= 153.213 \text{ kJ/mol} \end{aligned}$$

Sources for Thermodynamic Properties

The thermodynamic properties for calcium were taken from the following sources:

| <u>Property</u>          | <u>Source</u>              |
|--------------------------|----------------------------|
| Heat capacity            | Hultgren and others (1973) |
| Entropy                  | CODATA Task Group (1978)   |
| Enthalpy of inversion    | Hultgren and others (1973) |
| Enthalpy of melting      | Hultgren and others (1973) |
| Enthalpy of vaporization | Hultgren and others (1973) |

## CaO

Issued September, 1979

CaO  
Lime (cubic)

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_T^o - H_{Tr}^o)/T$<br>J/(mol·K) | Formation from the Oxides |                            |                 |                  |
|--------------------|----------------------|--------------------|-------------------------------------|---------------------------|----------------------------|-----------------|------------------|
|                    |                      |                    |                                     | $\Delta H_f^o$<br>J/mol   | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$ | $\log K_f^o, ox$ |
| 273.15             | 40.605               | 34.475             | -38.265                             | -1035.                    | -635131.                   | -606133.        | 115.911          |
| 298.15             | 42.153               | 38.100             | -38.100                             | 0.                        | -635094.                   | -603480.        | 105.727          |
| 300.               | 42.256               | 38.361             | -38.101                             | 78.                       | -635090.                   | -603284.        | 105.041          |
| 350.               | 44.624               | 45.063             | -38.625                             | 2253.                     | -634931.                   | -593994.        | 89.246           |
| 400.               | 46.380               | 51.142             | -39.815                             | 453.                      | -634706.                   | -592732.        | 77.403           |
| 450.               | 47.738               | 56.686             | -41.387                             | 6885.                     | -634444.                   | -583501.        | 68.195           |
| 500.               | 48.821               | 61.774             | -43.174                             | 9300.                     | -634169.                   | -582300.        | 60.832           |
| 550.               | 49.707               | 66.470             | -45.081                             | 11764.                    | -633838.                   | -577126.        | 54.811           |
| 600.               | 50.446               | 70.827             | -47.048                             | 14268.                    | -633644.                   | -571977.        | 49.795           |
| 650.               | 51.075               | 74.891             | -49.035                             | 16806.                    | -633419.                   | -565847.        | 45.552           |
| 700.               | 51.617               | 78.696             | -51.019                             | 19374.                    | -633232.                   | -561333.        | 41.917           |
| 750.               | 52.092               | 82.274             | -52.985                             | 21967.                    | -633927.                   | -556595.        | 38.765           |
| 800.               | 52.513               | 85.649             | -54.922                             | 24582.                    | -633728.                   | -551447.        | 36.006           |
| 850.               | 52.891               | 88.845             | -56.824                             | 27228.                    | -633621.                   | -546308.        | 33.572           |
| 900.               | 53.235               | 91.878             | -58.688                             | 29871.                    | -633516.                   | -541173.        | 31.409           |
| 950.               | 53.550               | 94.764             | -60.511                             | 32501.                    | -633466.                   | -535036.        | 29.443           |
| 1000.              | 53.842               | 97.519             | -62.293                             | 35225.                    | -633380.                   | -530892.        | 27.731           |
| 1050.              | 54.117               | 100.152            | -64.034                             | 37921.                    | -634129.                   | -525737.        | 26.154           |
| 1100.              | 54.376               | 102.676            | -65.733                             | 40637.                    | -634494.                   | -520568.        | 24.720           |
| 1150.              | 54.624               | 105.99             | -67.393                             | 43365.                    | -642827.                   | -51099.         | 23.397           |
| 1200.              | 54.863               | 107.428            | -69.012                             | 46039.                    | -642442.                   | -505554.        | 22.180           |
| 1250.              | 55.095               | 109.673            | -70.594                             | 48848.                    | -642049.                   | -504025.        | 21.062           |
| 1300.              | 55.321               | 111.838            | -72.139                             | 51608.                    | -641649.                   | -498512.        | 20.030           |
| 1350.              | 55.545               | 113.930            | -73.648                             | 54380.                    | -641242.                   | -493014.        | 19.076           |
| 1400.              | 55.766               | 115.954            | -75.123                             | 57163.                    | -640838.                   | -487532.        | 18.190           |
| 1450.              | 55.986               | 117.915            | -76.565                             | 59957.                    | -640406.                   | -482664.        | 17.366           |
| 1500.              | 56.207               | 119.817            | -77.976                             | 62762.                    | -639976.                   | -476612.        | 16.597           |
| 1550.              | 56.429               | 121.663            | -79.355                             | 65577.                    | -639537.                   | -471173.        | 15.878           |
| 1600.              | 56.652               | 123.458            | -80.705                             | 68404.                    | -639050.                   | -465449.        | 15.205           |
| 1650.              | 56.879               | 125.205            | -82.028                             | 71243.                    | -638633.                   | -460339.        | 14.573           |
| 1700.              | 57.109               | 126.306            | -83.323                             | 74092.                    | -638167.                   | -455944.        | 13.919           |
| 1750.              | 57.342               | 128.565            | -84.592                             | 76954.                    | -637631.                   | -443562.        | 13.419           |
| 1800.              | 57.580               | 130.184            | 0.                                  | 0.                        | -790039.                   | -440270.        | 0.               |
|                    |                      |                    |                                     |                           |                            | 12.776          | 0.               |

## CaO

CaO

Lime

Formula weight = 56.079 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 38.100 \text{ J}/(\text{mol}\cdot\text{K}) \quad \Delta H_f^\circ = -635.094 \text{ kJ/mol}$$

$$V^\circ = 16.764 \pm 0.005 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -603.480 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (temperature range 200 to 1800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = -2.55577 \times 10^5 \quad a_4 = -4.20068 \times 10^2 \quad a_6 = -3.08248 \times 10^{-3}$$

$$a_2 = -7.05800 \times 10^3 \quad a_5 = 7.16851 \times 10^1 \quad a_7 = 2.23862 \times 10^{-6}$$

$$a_3 = -4.31990 \times 10^2$$

Sources for Thermodynamic Properties

The thermodynamic properties for lime were taken from the following sources:

| <u>Property</u>                         | <u>Source</u>  |
|---|--|
| Heat capacity                           | Stull and Prophet (1971) and Chase and others (1974, 1975) |
| Entropy                                 | CODATA Task Group (1978)                                   |
| Enthalpy of formation from the elements | CODATA Task Group (1978)                                   |

The molar volume of lime was obtained from the compilation of Robie and others (1967).

**CaO<sub>3</sub>Si**

Issued September, 1979

Reference state: Wollastonite 273.15 K to 1398 K  
 Cyclowollastite 1398 K to 1800 K



| Temperature<br>(K) | Formation from the Elements  |                 |  | Formation from the Oxides                             |                               |                                  |
|--------------------|------------------------------|-----------------|--|---|-------------------------------|----------------------------------|
|                    | C° <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K) | (G° <sub>T</sub> -G° <sub>T<sub>r</sub></sub> )/T<br>J/(mol·K) | H° <sub>f</sub> -H° <sub>f<sub>r</sub></sub><br>J/mol | ΔG° <sub>f</sub> , e<br>J/mol | log K° <sub>f, ox</sub><br>J/mol |
| 273.15             | 83.472                       | 73.538          | -81.369  | -2139.  | -1634686.<br>±0.028           | -1556383.<br>±0.106              |
| (2 s gma)          | ±0.552                       | ±0.552          | ±0.678   | 0.<br>±0.678  | ±702.<br>±608.                | ±106.<br>±608.                   |
| 300.               | 87.843                       | 81.571          | -81.030  | 162.<br>4727.   | -1634769.<br>-1634733.        | 297.628.<br>259.549              |
| 350.               | 94.482                       | 95.632          | -82.125  | 9587.<br>-1634514.                                    | -1634682.<br>-1634004.        | -88974.<br>-88943.               |
| 400.               | 99.707                       | 108.633         | -84.635  | 14682.<br>-1634166.                                   | -1634734.<br>-1634710.        | -89414.<br>-89490.               |
| 450.               | 103.929                      | 120.539         | -87.973  | 19968.<br>-1633731.                                   | -1634166.<br>-1491460.        | -89570.<br>-88954.               |
| (2 s gma)          | ±0.346                       | ±0.622          | ±0.622   | ±77.<br>±0.677  | ±710.<br>±575.                | ±0.060.<br>±0.060                |
| 550.               | 110.331                      | 142.113         | -95.907  | 25413.<br>-1633240.                                   | -1633240.<br>-1477256.        | 140.298.<br>-89013.              |
| 600.               | 112.813                      | 151.832         | -100.166   | 30994.<br>-1632277.                                   | -1632277.<br>-1433099.        | -89056.<br>-89013.               |
| 650.               | 115.948                      | 160.938         | -104.494   | 36688.<br>-1632882.                                   | -1632882.<br>-1448986.        | -89124.<br>-89124.               |
| 700.               | 116.802                      | 169.536         | -108.835   | 42484.<br>-1631651.                                   | -1631651.<br>-1439194.        | -89144.<br>-89144.               |
| (2 s gma)          | ±0.624                       | ±0.624          | ±0.624   | ±132.<br>±0.675                                       | ±715.<br>±576.                | ±0.040.<br>±0.040                |
| 800.               | 119.863                      | 185.331         | -117.427   | 54323.<br>-1631382.                                   | -1631382.<br>-1406787.        | 91.854.<br>-89823.               |
| 850.               | 121.141                      | 192.637         | -121.638   | 60341.<br>-1630851.                                   | -1630851.<br>-1429766.        | -89873.<br>-89923.               |
| 900.               | 122.287                      | 199.534         | -125.777   | 66435.<br>-1630418.                                   | -1630418.<br>-1338773.        | -89931.<br>-89931.               |
| 950.               | 123.322                      | 206.234         | -129.839   | 72576.<br>-1630035.                                   | -1630035.<br>-1344803.        | -89974.<br>-89974.               |
| 1000.              | 124.262                      | 212.534         | -133.818   | 78765.<br>-1629716.                                   | -1629716.<br>-1350850.        | -90009.<br>-89650.               |
| (2 s gma)          | ±0.509                       | ±0.509          | ±0.705   | ±224.<br>±0.673                                       | ±32.<br>±624.                 | ±0.033.<br>±715.                 |
| 1050.              | 125.121                      | 218.668         | -137.715   | 85001.<br>-1629594.                                   | -1629594.<br>-1336909.        | 56.508.<br>-90710.               |
| 1100.              | 125.911                      | 224.507         | -141.528   | 91277.<br>-1629479.                                   | -1629479.<br>-1322979.        | -90631.<br>-89962.               |
| 1150.              | 126.642                      | 230.120         | -145.259   | 97591.<br>-1637335.                                   | -1637335.<br>-1308763.        | -90533.<br>-90533.               |
| 1200.              | 127.323                      | 235.524         | -148.308   | 103941.<br>-1636488.                                  | -1636488.<br>-1294946.        | -90476.<br>-90476.               |
| 1250.              | 127.961                      | 240.262         | -152.477   | 110322.<br>-1633589.                                  | -1633589.<br>-1280265.        | -90433.<br>-89676.               |
| (2 s gma)          | ±1.512                       | ±1.512          | ±0.700   | ±225.<br>±0.673                                       | ±731.<br>±713.                | ±0.030.<br>±713.                 |
| 1300.              | 128.562                      | 245.766         | -155.969   | 116735.<br>-1634699.                                  | -1634699.<br>-1266070.        | 50.871.<br>-90336.               |
| 1350.              | 129.132                      | 255.639         | -162.596   | 123178.<br>-1632923.                                  | -1632923.<br>-1253346.        | -90439.<br>-90226.               |
| 1398.              | 129.654                      | 255.119         | -162.596   | 129389.<br>-163293.                                   | -163293.<br>-1238346.         | -90439.<br>-90439.               |
| 1400.              | 129.533                      | 259.267         | -162.596   | 135177.<br>-1627138.                                  | -1627138.<br>-1238346.        | -90439.<br>-90439.               |
| 1450.              | 129.558                      | 259.412         | -162.735   | 135433.<br>-1627101.                                  | -1627101.<br>-1237790.        | -90439.<br>-90439.               |
| 1500.              | 130.160                      | 264.059         | -166.149   | 141926.<br>-1626183.                                  | -1626183.<br>-123902.         | -90439.<br>-90439.               |
| (2 s gma)          | ±6.721                       | ±6.721          | ±1.488   | ±0.658<br>±1.488                                      | ±2099.<br>±2087.              | ±0.029.<br>±2037.                |
| 1550.              | 131.270                      | 272.747         | -172.748   | 154998.<br>-1624302.                                  | -1624302.<br>-1196222.        | -84347.<br>-90167.               |
| 1600.              | 131.783                      | 276.933         | -175.939   | 161576.<br>-1623341.                                  | -1623341.<br>-1192428.        | -84347.<br>-90334.               |
| 1650.              | 132.271                      | 280.956         | -179.061   | 168176.<br>-1622366.                                  | -1622366.<br>-1186665.        | -84347.<br>-90334.               |
| 1700.              | 132.735                      | 284.911         | -182.117   | 174802.<br>-1671886.                                  | -1671886.<br>-1154481.        | -84347.<br>-90732.               |
| 1750.              | 133.178                      | 288.755         | -185.110   | 181449.<br>-1670742.                                  | -1670742.<br>-1139280.        | -84347.<br>-90919.               |
| (2 s gma)          | ±10.183                      | ±10.183         | ±2.612   | ±0.693<br>±4011.                                      | ±3988.<br>±1067.              | ±0.032.<br>±0.032                |
| 1800.              | 133.601                      | 292.533         | -188.043   | 188110.<br>-1822415.                                  | -1822415.<br>-1120188.        | -84478.<br>-91106.               |
| (2 s gma)          | ±10.918                      | ±10.918         | ±2.875   | ±0.718<br>±4512.                                      | ±1155.<br>±1155.              | ±0.034.<br>±0.034                |

$\text{CaO}_3\text{Si}$  $\text{CaSiO}_3$  (reference state)

Wollastonite, Cyclowollastonite

Formula weight = 116.164 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s) (wollastonite)

$$S^\circ = 81.028 \pm 0.678 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -1634.766 \pm 0.702 \text{ kJ/mol}$$

$$V^\circ = 39.930 \pm 0.200 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -1549.213 \pm 0.608 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

Wollastonite (temperature range 200 to 1398 K)

$$a_1 = 0.0$$

$$a_4 = -1.212413 \times 10^3$$

$$a_6 = -9.115107 \times 10^{-3}$$

$$a_2 = 3.0259 \times 10^3$$

$$a_5 = 1.927733 \times 10^2$$

$$a_7 = 4.413189 \times 10^{-6}$$

$$a_3 = -1.7296 \times 10^3$$

Cyclowollastonite (temperature range 1398 to 1800 K)

$$a_1 = -9.739076 \times 10^3$$

$$a_4 = -1.024504 \times 10^3$$

$$a_6 = -3.621589 \times 10^{-4}$$

$$a_2 = -2.474400 \times 10^3$$

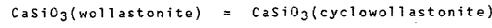
$$a_5 = 1.672547 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -1.372368 \times 10^3$$

Critical Reaction

Inversion:



$$T_i = 1398 \text{ K (observed)}$$

$$\Delta S_i^\circ = 4.138 \pm 1.42 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_i^\circ = 5.785 \pm 1.76 \text{ kJ/mol}$$

For detailed information on  $\text{CaSiO}_3$ , refer to the appropriate tables on the individual phases.

**CaO<sub>3</sub>Si**

Cassiopeia (=Pseudowollastonite, triclinic, dimorphous with Wollastonite)

Issued September, 1979

| Temperature<br>(K) | C° <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K)   | (G° <sub>f</sub> -H° <sub>r</sub> )/T<br>J/(mol·K) | Formation from the Elements   |                               |                         |                               | Formation from the Oxides |                               |                         |                               |
|--------------------|------------------------------|-------------------|--|-------------------------------|-------------------------------|-------------------------|-------------------------------|---------------------------|-------------------------------|-------------------------|-------------------------------|
|                    |                              |                   |  | ΔH° <sub>f</sub> , e<br>J/mol | ΔG° <sub>f</sub> , e<br>J/mol | log K° <sub>f, ox</sub> | ΔG° <sub>f, ox</sub><br>J/mol | log K° <sub>f, ox</sub>   | ΔH° <sub>f, ox</sub><br>J/mol | log K° <sub>f, ox</sub> | ΔG° <sub>f, ox</sub><br>J/mol |
| 273.15             | 83.890                       | 79.740            | -87.504  | -2143.                        | -1627538.                     | -1550929.               | 296.585                       | -81842.                   | -83921.                       | 16.048                  |                               |
| (2 sigma)          | 87.450<br>±1.553             | 87.244<br>±0.915  | -87.244<br>±0.915                                  | 0.<br>±0.                     | -1627614.<br>±932.            | -1543914.<br>±784.      | 270.487<br>±0.137             | -81822.<br>±932.          | -84113.<br>±784.              | 14.736<br>±0.137        | HAAS, ROBINSON, AND HEMINGWAY |
| 300.               | 87.696                       | 87.785            | -87.255  | 162.                          | -1627617.                     | -154395.                | 268.729                       | -81821.                   | -84127.                       | 14.648                  |                               |
| 350.               | 93.566                       | 101.762           | -88.336  | 469.9.                        | -1627610.                     | -1529356.               | 228.244                       | -81819.                   | -84512.                       | 12.613                  |                               |
| 400.               | 98.286                       | 114.575           | -90.816  | 950.0.                        | -1627450.                     | -1513229.               | 197.881                       | -81861.                   | -84894.                       | 11.086                  |                               |
| 450.               | 102.187                      | 126.383           | -94.129  | 1451.4.                       | -1627182.                     | -1501329.               | 174.270                       | -81942.                   | -85269.                       | 9.898                   |                               |
| 500.               | 105.479                      | 137.325           | -97.909  | 1970.8.                       | -1626839.                     | -1483636.               | 155.384                       | -82062.                   | -85633.                       | 8.946                   |                               |
| (2 sigma)          | 111.284<br>±1.284            | 110.890<br>±0.890 | -97.905<br>±0.890                                  | 1970.8.<br>±228.              | -1626839.<br>±952.            | -1483636.<br>±713.      | 155.384<br>±0.074             | -82062.<br>±952.          | -85633.<br>±713.              | 8.946<br>±0.074         |                               |
| 550.               | 108.306                      | 147.514           | -101.960   | 25054.                        | -1626447.                     | -1473434.               | 139.935                       | -82220.                   | -85982.                       | 8.166                   |                               |
| 600.               | 110.766                      | 157.046           | -106.158   | 30533.                        | -1626026.                     | -1459542.               | 127.064                       | -82418.                   | -86316.                       | 7.514                   |                               |
| 650.               | 112.932                      | 165.999           | -110.610   | 36126.                        | -1625593.                     | -1456886.               | 116.177                       | -8256.                    | -86631.                       | 6.962                   |                               |
| 700.               | 114.857                      | 174.440           | -114.694   | 41822.                        | -1625161.                     | -1431863.               | 106.347                       | -82934.                   | -86927.                       | 6.487                   |                               |
| 750.               | 116.582                      | 182.424           | -118.946   | 47609.                        | -1625579.                     | -1418034.               | 98.761                        | -83255.                   | -87201.                       | 6.073                   |                               |
| (2 sigma)          | 118.140<br>±1.586            | 189.999<br>±0.966 | -123.152<br>±0.810                                 | 53477.<br>±488.               | -1626447.<br>±926.            | -1473434.<br>±672.      | 91.686<br>±0.047              | -83618.<br>±926.          | -87453.<br>±672.              | 5.710<br>±0.047         |                               |
| 800.               | 119.554                      | 197.044           | -127.298   | 59420.                        | -1624638.                     | -1390425.               | 85.445                        | -84741.                   | -87475.                       | 5.388                   |                               |
| 850.               | 120.845                      | 204.075           | -131.344   | 64341.                        | -1624271.                     | -1376658.               | 79.999                        | -84469.                   | -87847.                       | 5.098                   |                               |
| 900.               | 122.030                      | 210.641           | -135.374   | 71503.                        | -1623977.                     | -1362911.               | 74.938                        | -8476.                    | -8817.                        | 4.840                   |                               |
| 950.               | 123.123                      | 216.328           | -139.728   | 77632.                        | -1623756.                     | -134176.                | 70.774                        | -84767.                   | -88186.                       | 4.606                   |                               |
| 1000.              | 124.133<br>±1.833            | 222.960<br>±0.806 | -143.137<br>±0.728                                 | 83814.<br>±718.               | -1623619.<br>±966.            | -1335451.<br>±686.      | 66.435<br>±0.036              | -84745.<br>±963.          | -88360.<br>±686.              | 4.396<br>±0.036         |                               |
| (2 sigma)          | 125.072<br>±3.771            | 228.157<br>±0.908 | -146.838<br>±0.676                                 | 90044.<br>±981.               | -1623559.<br>±1173.           | -1321130.<br>±735.      | 62.664<br>±0.331              | -84745.<br>±1173.         | -88360.<br>±735.              | 4.396<br>±0.031         |                               |
| 1050.              | 124.133                      | 222.960           | -143.137   | 83814.                        | -1623619.                     | -1335451.               | 66.435                        | -84745.                   | -88360.                       | 4.396                   |                               |
| 1100.              | 125.072                      | 228.157           | -146.838   | 90044.                        | -1623559.                     | -1321130.               | 62.664                        | -84745.                   | -88360.                       | 4.396                   |                               |
| 1150.              | 125.945                      | 234.336           | -150.579   | 96320.                        | -1631454.                     | -1307730.               | 59.199                        | -84745.                   | -88360.                       | 4.204                   |                               |
| 1200.              | 126.762                      | 239.713           | -154.122   | 102338.                       | -1630618.                     | -1295673.               | 56.312                        | -84672.                   | -88533.                       | 4.029                   |                               |
| 1250.              | 127.527                      | 244.304           | -157.708   | 108959.                       | -1630618.                     | -1295673.               | 53.474                        | -84672.                   | -88533.                       | 3.722                   |                               |
| (2 sigma)          | 128.245<br>±6.721            | 249.920<br>±1.438 | -161.158<br>±0.663                                 | 115390.<br>±1903.             | -1628893.<br>±2087.           | -1265664.<br>±822.      | 50.855<br>±0.029              | -84745.<br>±2087.         | -88360.<br>±822.              | 3.586<br>±0.029         |                               |
| 1300.              | 128.920                      | 254.772           | -164.836   | 12819.                        | -1628005.                     | -125110.                | 48.332                        | -84745.                   | -89242.                       | 3.586                   |                               |
| 1350.              | 129.558                      | 259.472           | -167.843   | 128381.                       | -1627101.                     | -1237790.               | 46.182                        | -84745.                   | -89242.                       | 3.460                   |                               |
| 1400.              | 130.160                      | 264.029           | -171.082   | 134774.                       | -1626183.                     | -1222902.               | 44.090                        | -84402.                   | -89608.                       | 3.343                   |                               |
| 1450.              | 130.730                      | 268.152           | -174.234   | 141297.                       | -1625250.                     | -1210046.               | 42.138                        | -84402.                   | -89793.                       | 3.235                   |                               |
| (2 sigma)          | 131.270<br>±6.721            | 272.747<br>±1.438 | -177.362<br>±0.663                                 | 147847.<br>±1903.             | -1624302.<br>±2087.           | -1196222.<br>±822.      | 40.312                        | -84347.<br>±2087.         | -89167.                       | 3.039                   |                               |
| 1550.              | 131.783                      | 276.923           | -180.469   | 154423.                       | -1628341.                     | -1182128.               | 38.602                        | -84483.                   | -89334.                       | 2.950                   |                               |
| 1600.              | 132.271                      | 280.936           | -183.395   | 161025.                       | -1622366.                     | -1163665.               | 36.397                        | -84483.                   | -89334.                       | 2.866                   |                               |
| 1650.              | 132.735                      | 284.041           | -186.324   | 167650.                       | -161886.                      | -1154481.               | 35.473                        | -84483.                   | -89732.                       | 2.788                   |                               |
| 1700.              | 133.178                      | 288.795           | -189.197   | 174298.                       | -1670742.                     | -113980.                | 34.006                        | -84483.                   | -901919.                      | 2.714                   |                               |
| (2 sigma)          | 133.601<br>±10.183           | 292.533<br>±2.875 | -192.016<br>±0.773                                 | 180967.<br>±4300.             | -16282415.<br>±4487.          | -1120188.<br>±1155.     | 32.507<br>±0.034              | -84483.<br>±4487.         | -91106.<br>±1155.             | 2.644<br>±0.034         |                               |

$\text{CaO}_3\text{Si}$  $\text{CaSiO}_3$ 

Cyclowollastonite

Formula weight = 116.164 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 87.244 \pm 0.915 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -1627.614 \pm 0.932 \text{ kJ/mol}$$

$$V^\circ = 40.080 \pm 0.280 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -1543.914 \pm 0.784 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = -9.739076 \times 10^3$$

$$a_4 = -1.024504 \times 10^3$$

$$a_6 = -3.621589 \times 10^{-4}$$

$$a_2 = -2.474400 \times 10^3$$

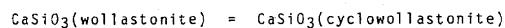
$$a_5 = 1.672547 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -1.372368 \times 10^3$$

Critical Reactions

## Inversion:



$$T_i = 1398 \text{ K (observed)}$$

$$\Delta S_i^\circ = 4.138 \pm 1.42 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 5.785 \pm 1.76 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of cyclowollastonite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                  | Data Type         | Method                      | No. of Points | Range        |
|-------------------------|-------------------|-----------------------------|---------------|--------------|
| Wagner (1932)           | heat capacity     | low-temperature calorimetry | 7             | 201 - 295 K  |
| Wagner (1932)           | relative enthalpy | drop calorimetry            | 12            | 576 - 1558 K |
| White (1919)            | relative enthalpy | drop calorimetry            | 28            | 373 - 1673 K |
| Parks and Kelley (1926) | specific heat     | aneroid calorimetry         | 6             | 195 - 298 K  |
| Robie and others (1979) | entropy           |                             | 1             | 298.15       |

The heat-capacity measurements of Wagner (1932) were fit with a standard error of estimate of 0.70 J/(mol·K). The relative enthalpy measurements of Wagner (1932) and White (1919) were fit with standard error of estimate of 666 J/mol (0.97 percent of observed value) and 265 J/mol (0.35 percent of observed value), respectively. The specific heat measurements of Parks and Kelley (1926) were fit with a standard error of estimate of 1.1 J/(mol·K) or 1.3 percent of the observed value. The fitted entropy at 298.15 K is  $87.244 \pm 0.915 \text{ J}/(\text{mol}\cdot\text{K})$  or a departure of 0.21 from the value of  $87.45 \pm 0.42$  reported by Robie and others (1979).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                             | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---------------------------------------|------------------------------------|-----------------------|-----------|---------------|------------------------------------|--------------------------------------|
| Charlu and others (1978) <sup>b</sup> | solution calorimetry (borate salt) | A                     | 970       | 1             | -80.389 $\pm$ 1.273                | -1626.181                            |
| Kracek and others (1953) <sup>c</sup> | solution calorimetry (HF)          | B                     | 347.85    | 1             | -6.526 $\pm$ 4.183                 | -1628.240                            |
| Nacken (1930) <sup>d</sup>            | solution calorimetry (HCl-HF)      | B                     | 314.85    | 4             | -8.171 $\pm$ 5.916                 | -1626.595                            |
| Kay and Taylor (1960) <sup>e</sup>    | silica activity                    | C                     | 1773      | 1             | -86.058 $\pm$ 2.771                | -1626.253                            |
| Kay and Taylor (1960) <sup>e</sup>    | silica activity                    | D                     | 1543      | 1             | 59.386 $\pm$ 2.412                 | -1623.448                            |
| Benz and Wagner (1961)                | Emf                                | E                     | 943-1003  | 10            | -41.441 $\pm$ 0.186                | -1629.791                            |

$\text{CaO}_3\text{Si}$ 

## a Reactions:

- A)  $\text{CaO}(\text{lime}) + \text{SiO}_2(\text{quartz, beta}) = \text{CaSiO}_3(\text{cyclowollastonite})$   
 B)  $\text{CaSiO}_3(\text{cyclowollastonite}) = \text{CaSiO}_3(\text{wollastonite})$   
 C)  $\text{CaO}(\text{lime}) + \text{SiO}_2(\text{cristobalite, beta}) = \text{CaSiO}_3(\text{cyclowollastonite})$   
 D)  $\text{CaSiO}_3(\text{cyclowollastonite}) + \text{CaAl}_2\text{Si}_2\text{O}_8(\text{anorthite}) = \text{Ca}_2\text{Al}_2\text{Si}_2\text{O}_7(\text{gehlenite}) + 2 \text{SiO}_2(\text{cristobalite, beta})$   
 E)  $1/2 \text{CaO}(\text{lime}) + \text{CaSiO}_3(\text{cyclowollastonite}) = 1/2 \text{Ca}_3\text{Si}_2\text{O}_7(\text{rankinite})$

b Charlu and others (1978) measured the enthalpy of solution of cyclowollastonite in lead borate salt melt at 970 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of lime and quartz in the salt melt; corrections were not made for the enthalpies of dilution and of mixing of the product melts.

c Kracek and others (1953) measured the enthalpy of solution of cyclowollastonite in HF acid solution at 347.85 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpy of solution of wollastonite.

d Nacken (1930) measured the enthalpy of solution of cyclowollastonite in HCl-HF acid solution at 314.85 K. To complete the thermodynamic cycle, the data were evaluated in combination with his enthalpy of solution of wollastonite.

e Kay and Taylor (1960) determined the activity of silica in the silicate liquid for the lime-alumina-silica system. Using the silica activity from their study and the measured temperature and composition of the silicate melt in equilibrium with anorthite, cyclowollastonite, and gehlenite, we obtained the equilibrium constants for reactions C and D at the melt temperature and 101.325 kPa.

Phase-equilibrium studies were evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature. After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for cyclo-wollastonite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-1627.614 \pm 0.932 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of cyclowollastonite and presents the data in their poorest perspective. The phase-equilibria studies lack the precision to discriminate among the experimental enthalpies of solution.

The temperature of the experimentally observed inversion of wollastonite to cyclowollastonite at 101.325 kPa was entered as a fixed value in the regression and supplies an additional constraint on the free energy of cyclowollastonite and its dimorph. This inversion temperature is listed as "observed" in the section on critical reactions.

The molar volume of cyclowollastonite was obtained from the compilation of Robie and others (1967).

## THERMODYNAMIC DATA FOR MINERALS

| Temperature<br>(K)  | $C_p^o$<br>J/(mol·K)  | $S^o$<br>J/(mol·K)    | $(G_f^o - H_f^o)/T$<br>J/mol | Formation from the Elements |                            | Formation from the Oxides |                             |
|---------------------|-----------------------|-----------------------|------------------------------|-----------------------------|----------------------------|---------------------------|-----------------------------|
|                     |                       |                       |                              | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$<br>J/mol  | $\Delta H_f^o, ox$<br>J/mol |
| 273.15              | 83.472                | 73.538                | -81.369                      | -2139.                      | -1634686.                  | -1556383.                 | 297.628                     |
| 298.15<br>(2 sigma) | 87.562<br>$\pm 0.552$ | 81.028<br>$\pm 0.678$ | -81.028<br>$\pm 0.678$       | 0.<br>$\pm 0$               | -1634766.<br>$\pm 702.$    | -1549213.<br>$\pm 608.$   | 271.415<br>$\pm 106$        |
| 300.                | 87.843                | 81.571                | -81.030                      | 162.                        | -1634769.                  | -1548682.                 | 269.449                     |
| 350.                | 94.482                | 95.632                | -82.125                      | 4727.                       | -1634733.                  | -1544334.                 | 228.987                     |
| 400.                | 99.07                 | 108.603               | -84.035                      | 9587.                       | -1634514.                  | -150004.                  | 198.492                     |
| 450.                | 103.129               | 120.592               | -87.73                       | 14682.                      | -1634166.                  | -1505710.                 | 174.778                     |
| 500.                | 107.411               | 131.735               | -91.799                      | 19968.                      | -1633731.                  | -1491460.                 | 155.812                     |
| (2 sigma)           | $\pm 0.346$           | $\pm 0.692$           | $\pm 0.677$                  | $\pm 77.$                   | $\pm 710.$                 | $\pm 575.$                | $\pm 710.$                  |
| 550.                | 110.331               | 142.113               | -95.907                      | 25413.                      | -1633240.                  | -1477256.                 | 140.298                     |
| 600.                | 112.813               | 151.822               | -100.166                     | 30994.                      | -1632717.                  | -143099.                  | 127.374                     |
| 650.                | 114.348               | 160.938               | -104.194                     | 36689.                      | -1632182.                  | -148986.                  | 116.442                     |
| 700.                | 116.802               | 169.526               | -108.335                     | 42484.                      | -1631651.                  | -1434914.                 | 107.074                     |
| 750.                | 118.427               | 177.641               | -113.154                     | 48365.                      | -1631974.                  | -1420842.                 | 98.956                      |
| (2 sigma)           | $\pm 0.324$           | $\pm 0.690$           | $\pm 0.675$                  | $\pm 132.$                  | $\pm 715.$                 | $\pm 576.$                | $\pm 715.$                  |
| 800.                | 119.863               | 185.331               | -117.427                     | 54323.                      | -1631382.                  | -1406787.                 | 91.854                      |
| 850.                | 121.141               | 192.637               | -121.538                     | 60349.                      | -1630861.                  | -1392766.                 | 85.589                      |
| 900.                | 122.287               | 199.594               | -125.638                     | 66435.                      | -1630418.                  | -138773.                  | 80.022                      |
| 950.                | 123.322               | 206.234               | -129.839                     | 72576.                      | -1630055.                  | -1344803.                 | 75.042                      |
| 1000.               | 124.662               | 212.584               | -133.518                     | 78766.                      | -1629776.                  | -1305850.                 | 70.561                      |
| (2 sigma)           | $\pm 0.509$           | $\pm 0.705$           | $\pm 0.673$                  | $\pm 224.$                  | $\pm 732.$                 | $\pm 624.$                | $\pm 732.$                  |
| 1050.               | 125.121               | 218.668               | -137.715                     | 85001.                      | -1629584.                  | -1326909.                 | 66.508                      |
| 1100.               | 125.911               | 224.507               | -141.528                     | 91277.                      | -1629459.                  | -1322975.                 | 62.023                      |
| 1150.               | 126.642               | 230.120               | -145.259                     | 97591.                      | -1637335.                  | -138763.                  | 59.446                      |
| 1200.               | 127.323               | 235.525               | -148.308                     | 103940.                     | -1636468.                  | -129496.                  | 56.348                      |
| 1250.               | 127.961               | 240.735               | -152.477                     | 110322.                     | -1635589.                  | -1280265.                 | 53.199                      |
| (2 sigma)           | $\pm 1.512$           | $\pm 0.700$           | $\pm 0.673$                  | $\pm 225.$                  | $\pm 731.$                 | $\pm 0.033$               | $\pm 731.$                  |
| 1300.               | 128.562               | 245.766               | -155.969                     | 116735.                     | -1634693.                  | -1266070.                 | 50.871                      |
| 1350.               | 129.132               | 250.625               | -159.386                     | 123178.                     | -1633738.                  | -1237782.                 | 48.339                      |
| 1400.               | 129.675               | 255.335               | -162.729                     | 129648.                     | -1632886.                  | -122687.                  | 46.182                      |
| 1450.               | 130.197               | 259.894               | -166.001                     | 136145.                     | -1631964.                  | -122687.                  | 44.082                      |
| 1500.               | 130.700               | 264.317               | -169.205                     | 142668.                     | -1631030.                  | -1239624.                 | 42.123                      |
| (2 sigma)           | $\pm 4.272$           | $\pm 0.845$           | $\pm 0.675$                  | $\pm 711.$                  | $\pm 1007.$                | $\pm 828.$                | $\pm 1007.$                 |
| 1550.               | 131.187               | 268.610               | -172.443                     | 149215.                     | -1630086.                  | -119593.                  | 40.291                      |
| 1600.               | 131.663               | 272.783               | -175.417                     | 155786.                     | -1629130.                  | -1181592.                 | 38.575                      |
| 1650.               | 132.129               | 276.841               | -178.429                     | 163381.                     | -1628161.                  | -1161622.                 | 36.964                      |
| 1700.               | 132.587               | 280.793               | -181.382                     | 169999.                     | -1677689.                  | -115331.                  | 35.134                      |
| 1750.               | 133.040               | 284.643               | -184.277                     | 175640.                     | -1676552.                  | -1133782.                 | 33.962                      |
| (2 sigma)           | $\pm 8.450$           | $\pm 1.576$           | $\pm 0.692$                  | $\pm 223.$                  | $\pm 2349.$                | $\pm 991.$                | $\pm 2349.$                 |
| 1800.               | 133.491               | 288.397               | -187.117                     | 182303.                     | -1828231.                  | -1118523.                 | 32.459                      |
| (2 sigma)           | $\pm 9.455$           | $\pm 1.803$           | $\pm 0.702$                  | $\pm 2664.$                 | $\pm 2774.$                | $\pm 1039.$               | $\pm 1039.$                 |

CaSiO<sub>3</sub>

Wollastonite

Formula weight = 116.164 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 81.028 \pm 0.678 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -1634.766 \pm 0.702 \text{ kJ/mol}$$

$$V^\circ = 39.930 \pm 0.200 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -1549.213 \pm 0.608 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 0.0$$

$$a_4 = -1.212413 \times 10^3$$

$$a_6 = -9.115107 \times 10^{-3}$$

$$a_2 = 3.025900 \times 10^3$$

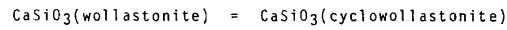
$$a_5 = 1.927733 \times 10^2$$

$$a_7 = 4.413189 \times 10^{-6}$$

$$a_3 = -1.729600 \times 10^3$$

Critical Reactions

## Inversion:



$$T_i = 1398 \text{ K (observed)}$$

$$\Delta S_i^\circ = 4.138 \pm 1.42 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 5.785 \pm 1.76 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of wollastonite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                            | Data Type         | Method                      | No. of Points | Range        |
|-----------------------------------|-------------------|-----------------------------|---------------|--------------|
| Cristescu and Simon (1934)        | heat capacity     | low-temperature calorimetry | 2             | 200 - 210 K  |
| Cristescu (cited in Wagner, 1932) | heat capacity     | low-temperature calorimetry | 7             | 200 - 304 K  |
| Gronow and Schwiete (1933)        | relative enthalpy | drop calorimetry            | 5             | 573 - 1373 K |
| Southard (1941)                   | relative enthalpy | drop calorimetry            | 13            | 485 - 1423 K |
| Roth and Bertram (1929)           | relative enthalpy | drop calorimetry            | 7             | 323 - 1157 K |
| White (1919)                      | relative enthalpy | drop calorimetry            | 18            | 373 - 1573 K |
| Wagner (1932)                     | relative enthalpy | drop calorimetry            | 11            | 566 - 1383 K |
| Hemingway and Robie (1977)        | entropy           | drop calorimetry            | 1             | 298.15 K     |

The heat capacities measured by Cristescu and Simon (1934) and Cristescu (cited in Wagner, 1932) were fit with a standard error of estimate of 0.07 and 1.0  $\text{J}/(\text{mol}\cdot\text{K})$ , respectively. The relative enthalpy measurements of Gronow and Schwiete (1933) were fit with a standard error of estimate of 761  $\text{J}/\text{mol}$  or approximately 0.64 percent of the observed value. The relative enthalpy measurements of Southard (1941) were fit with a standard error of estimate of 147  $\text{J}/\text{mol}$  or approximately 0.16 percent of the observed value. The relative enthalpy measurements of Roth and Bertram (1929) were fit with a standard error of estimate of 658  $\text{J}/\text{mol}$  or approximately 1.5 percent of the observed value. The relative enthalpy measurements of White (1919) were fit with a standard error of estimate of 1033  $\text{J}/\text{mol}$  or approximately 1.2 percent of the observed value. The relative enthalpy measurements of Wagner (1932) were fit with a standard error of estimate of 752  $\text{J}/\text{mol}$  or approximately 0.65 percent of the observed value. The fitted entropy value at 298.15 K is  $81.028 \pm 0.678 \text{ J}/(\text{mol}\cdot\text{K})$ , or a departure of 0.97 J from the experimental value of  $82.00 \pm 0.40 \text{ J}/(\text{mol}\cdot\text{K})$  given by Hemingway and Robie (1977).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                | Method                                | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---------------------------------------|---------------------------------------|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Charlu and others (1978) <sup>b</sup> | solution calorimetry<br>(borate salt) | A                     | 970       | 1             | $87.754 \pm 1.551$                   | -1633.556                            |
| Benz and Wagner (1961)                | Emf                                   | A                     | 898-1148  | 12            | $87.606 \pm 0.384$                   | -1636.310                            |
| Barany (1966) <sup>c</sup>            | solution calorimetry (HF)             | B                     | 346.85    | 6             | $89.762 \pm 0.979$                   | -1635.564                            |
| Kracek and others (1953) <sup>d</sup> | solution calorimetry (HF)             | C                     | 347.85    | 1             | $-6.526 \pm 4.183$                   | -1634.150                            |
| Nacken (1930) <sup>e</sup>            | solution calorimetry<br>(HCl-HF)      | C                     | 314.85    | 6             | $-8.171 \pm 5.916$                   | -1635.795                            |
| Newton (1966b)                        | gas-medium pressure apparatus         | D                     | 803-923   | 4             | $-51.708 \pm 0.304$                  | -1633.747                            |
| Huckenholz (1974)                     | unspecified                           | D                     | 848-858   | 2             | $-49.366 \pm 0.328$                  | -1634.918                            |
| Newton (1966b)                        | gas-medium pressure apparatus         | E                     | 973-1023  | 4             | $-49.102 \pm 1.847$                  | -1635.334                            |
| Huckenholz (1974)                     | unspecified                           | E                     | 888-958   | 4             | $-50.100 \pm 0.499$                  | -1634.835                            |
| Boettcher (1970)                      | gas-medium pressure apparatus         | E                     | 893-1053  | 4             | $-50.329 \pm 1.454$                  | -1634.721                            |
| Liou (1971)                           | gas-medium pressure apparatus         | F                     | 708-828   | 10            | $-89.180 \pm 0.496$                  | -1634.781                            |
| Hays (1965)                           | solid-medium pressure apparatus       | G                     | 1473-1523 | 4             | $-156.099 \pm 6.608$                 | -1635.678                            |
| Huckenholz (1974)                     | unspecified                           | G                     | 1125-1423 | 12            | $-158.750 \pm 2.236$                 | -1634.794                            |
| Shmulovich (1974)                     | gas-medium pressure apparatus         | G                     | 1133-1153 | 2             | $-159.942 \pm 1.763$                 | -1634.397                            |

$\text{CaO}_3\text{Si}$ 

## a Reactions:

- A)  $\text{CaSiO}_3(\text{wollastonite}) = \text{SiO}_2(\text{quartz, beta}) + \text{CaO}(\text{lime})$   
 B)  $\text{CaSiO}_3(\text{wollastonite}) = \text{SiO}_2(\text{quartz, alpha}) + \text{CaO}(\text{lime})$   
 C)  $\text{CaSiO}_3(\text{cyclowollastonite}) = \text{CaSiO}_3(\text{wollastonite})$   
 D)  $\text{CaAl}_2\text{Si}_2\text{O}_8(\text{anorthite}) + 2 \text{CaSiO}_3(\text{wollastonite}) = \text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12(\text{grossular}) + \text{SiO}_2(\text{quartz, alpha})$   
 E)  $\text{CaAl}_2\text{Si}_2\text{O}_8(\text{anorthite}) + 2 \text{CaSiO}_3(\text{wollastonite}) = \text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12(\text{grossular}) + \text{SiO}_2(\text{quartz, beta})$   
 F)  $\text{CaAl}_2\text{Si}_2\text{O}_8(\text{anorthite}) + \text{CaSiO}_3(\text{wollastonite}) + \text{H}_2\text{O}(\text{gas}) = \text{Ca}_2\text{Al}_2\text{Si}_3\text{O}_{10}(\text{OH})_2(\text{prehnite})$   
 G)  $\text{CaAl}_2\text{Si}_2\text{O}_8(\text{anorthite}) + \text{Ca}_2\text{Al}_2\text{Si}_3\text{O}_7(\text{gehlenite}) + 3 \text{CaSiO}_3(\text{wollastonite}) = 2 \text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_12(\text{grossular})$

- b Charlu and others (1978) measured the enthalpy of solution of wollastonite in lead borate salt melt at 970 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpies of solution of lime and quartz in the salt melt; corrections were not made for the enthalpies of dilution and of mixing of the product melts.
- c Barany (1966) measured the enthalpy of solution of wollastonite in HF acid solution at 346.85 K. To complete the thermodynamic cycle, the data were evaluated in combination with the enthalpies of solution of lime (Barany, 1963) and of quartz (Hemingway and Robie, 1977; Bennington and others, 1978) in similar solutions.
- d Kracek and others (1953) measured the enthalpy of solution of wollastonite in HF acid solution at 347.85 K. To complete the thermodynamic cycle, their data were evaluated in combination with their enthalpy of solution of cyclowollastonite.
- e Nacken (1930) measured the enthalpy of solution of wollastonite in HCl-HF acid solution at 314.85 K. To complete the thermodynamic cycle, the data were evaluated in combination with his enthalpy of solution of cyclowollastonite.

Phase-equilibrium studies (utilizing gas- and solid-medium pressure apparatus) were evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. Molar volumes of the phases and free-energy data for  $\text{H}_2\text{O}(\text{gas})$  from Fisher and Zen (1971) were used in the conversion. The studies cited in Table 2 comply with the following criteria: 1) starting materials and reaction products were characterized, and 2) chemical equilibrium was demonstrated.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for wollastonite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-1634.766 \pm 0.702$  kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of wollastonite and presents the data in their poorest perspective.

Most of the phase-equilibria data cited above bracket the regression fit in free-energy space. However, the phase-equilibria studies also lack sufficient precision to constrain the fit tightly, as the scatter in the calculated enthalpies of reaction and enthalpies of formation listed in Table 2 demonstrate. The phase-equilibria studies lack the precision to discriminate among the experimental enthalpies of solution.

The temperature of the experimentally observed inversion of wollastonite to cyclowollastonite was entered as a fixed value in the regression and supplies an additional constraint on the free energy of wollastonite and its dimorph. This inversion temperature is listed as "observed" in the section on critical reactions.

The molar volume of wollastonite was obtained from the compilation of Robie and others (1967) and the work of Evans (1977).

$\text{Ca}_2\text{O}_4\text{Si}$ 

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$\text{Ca}_2\text{SiO}_4$   
 Reference state: Ca Olivine  
 Alpha prime  
 (crystal)

273.15 K to 1120 K  
 1120 K to 1710 K  
 1710 K to 1800 K

| Temperature<br>(K)  | $C_p^\circ$<br>J/(mol·K) | $S^\circ$<br>J/(mol·K) | $(G_f^\circ - H_f^\circ)/T$<br>J/mol | $H_f^\circ - H_f^\circ_{\text{yr}}$<br>J/mol | Formation from the Elements           |                                       |                              |                              | $\Delta G_f^\circ, \text{e}$<br>J/mol | $\Delta H_f^\circ, \text{o}$<br>J/mol | $\log K_f^{\circ, \text{x}}$ |
|---------------------|--------------------------|------------------------|--------------------------------------|--|---------------------------------------|---------------------------------------|------------------------------|------------------------------|---------------------------------------|---------------------------------------|------------------------------|
|                     |                          |                        |                                      |  | $\Delta H_f^\circ, \text{e}$<br>J/mol | $\Delta G_f^\circ, \text{e}$<br>J/mol | $\log K_f^{\circ, \text{e}}$ | $\log K_f^{\circ, \text{o}}$ |                                       |                                       |                              |
| 273.15              | 120.737                  | 109.706                | -120.939                             | -3082.                                       | -231.6400.                            | -220.9561.                            | 422.535                      | 385.391                      | -135573.                              | -136420.                              | 26.088                       |
| 298.15<br>(2 sigma) | 125.690<br>$\pm 0.387$   | 120.499<br>$\pm 2.045$ | -120.499<br>$\pm 2.045$              | 0  | -231.6534.<br>$\pm 2441.$             | -219.9776.<br>$\pm 1881.$             | 422.535<br>$\pm 0.330$       | 385.391<br>$\pm 2441.$       | -135648.<br>$\pm 2441.$               | -136494.<br>$\pm 1881.$               | 23.913<br>$\pm 0.330$        |
| 300.                | 126.025                  | 121.278                | -120.552                             | 233.   | -231.6540.                            | -219.9051.                            | 382.889                      | 325.267                      | -135654.                              | -136500.                              | 23.767                       |
| 350.                | 133.898                  | 141.321                | -122.057                             | 6739.  | -231.6540.                            | -219.9463.                            | 382.889                      | 325.267                      | -135654.                              | -136500.                              | 23.767                       |
| 400.                | 140.297                  | 159.630                | -125.634                             | 13598.                                       | -231.6543.                            | -219.9884.                            | 282.052                      | -136118.                     | -136625.                              | -136625.                              | 20.380                       |
| 450.                | 145.551                  | 176.482                | -130.350                             | 20755.                                       | -231.6566.                            | -219.0336.                            | 248.444                      | -136412.                     | -136775.                              | -136775.                              | 17.853                       |
| 500.                | 150.846                  | 192.112                | -135.653                             | 28174.                                       | -231.6567.                            | -219.0289.                            | 221.561                      | -136721.                     | -136799.                              | -136799.                              | 15.816                       |
| (2 sigma)           | $\pm 0.500$              | $\pm 2.055$            | $\pm 2.046$                          | $\pm 78.$                                    | $\pm 2448.$                           | $\pm 1522.$                           | $\pm 0.159$                  | $\pm 2448.$                  | $\pm 1522.$                           | $\pm 1522.$                           | $\pm 0.159$                  |
| 550.                | 155.417                  | 206.706                | -141.556                             | 35833.                                       | -231.5156.                            | -210.1369.                            | 199.571                      | -137032.                     | -136792.                              | -136792.                              | 12.991                       |
| 600.                | 159.629                  | 220.413                | -147.562                             | 43710.                                       | -231.4486.                            | -201.9569.                            | 181.251                      | -137335.                     | -136756.                              | -136756.                              | 11.962                       |
| 650.                | 163.510                  | 233.345                | -153.658                             | 51790.                                       | -231.3981.                            | -202.598.                             | 165.752                      | -137625.                     | -136696.                              | -136696.                              | 10.985                       |
| 700.                | 167.074                  | 245.595                | -159.501                             | 60056.                                       | -231.3580.                            | -203.5284.                            | 162.472                      | -137900.                     | -136514.                              | -136514.                              | 10.194                       |
| (2 sigma)           | $\pm 0.411$              | $\pm 170.322$          | $\pm 257.234$                        | $\pm 165.912$                                | $\pm 2460.$                           | $\pm 1124.$                           | $\pm 0.078$                  | $\pm 2460.$                  | $\pm 1124.$                           | $\pm 1124.$                           | $\pm 0.078$                  |
| 750.                | 173.251                  | 268.322                | -171.958                             | 77083.                                       | -231.3607.                            | -204.603.                             | 130.887                      | -138421.                     | -136395.                              | -136395.                              | 8.906                        |
| 800.                | 175.859                  | 278.905                | -177.950                             | 85812.                                       | -231.2911.                            | -198.5313.                            | 122.002                      | -139393.                     | -136755.                              | -136755.                              | 8.373                        |
| 850.                | 178.138                  | 289.023                | -183.842                             | 95812.                                       | -231.2442.                            | -196.0559.                            | 114.107                      | -139233.                     | -136075.                              | -136075.                              | 7.886                        |
| 900.                | 180.084                  | 298.708                | -189.634                             | 103620.                                      | -231.1912.                            | -196.834.                             | 107.044                      | -139026.                     | -135205.                              | -135205.                              | 7.473                        |
| 950.                | 181.690                  | 307.987                | -195.322                             | 112666.                                      | -231.1636.                            | -197.627.                             | 100.689                      | -138785.                     | -135747.                              | -135747.                              | 7.091                        |
| (2 sigma)           | $\pm 1.256$              | $\pm 2.064$            | $\pm 2.052$                          | $\pm 150.$                                   | $\pm 2453.$                           | $\pm 860.$                            | $\pm 0.045$                  | $\pm 2453.$                  | $\pm 860.$                            | $\pm 860.$                            | $\pm 0.045$                  |
| 1000.               | 182.952                  | 316.884                | -200.900                             | 121783.                                      | -231.1529.                            | -190.8430.                            | 94.939                       | -138526.                     | -135601.                              | -135601.                              | 6.746                        |
| 1050.               | 183.864                  | 325.417                | -206.357                             | 130955.                                      | -231.106.                             | -189.233.                             | 89.712                       | -138162.                     | -135468.                              | -135468.                              | 6.433                        |
| 1100.               | 184.130                  | 328.733                | -208.223                             | 134635.                                      | -232.8167.                            | -188.1432.                            | 87.746                       | -138162.                     | -135118.                              | -135118.                              | 6.316                        |
| 1120.               | 185.325                  | 340.954                | -208.523                             | 148334.                                      | -231.4468.                            | -188.1432.                            | 87.746                       | -124463.                     | -134118.                              | -134118.                              | 6.316                        |
| 1150.               | 186.612                  | 345.879                | -212.142                             | 15391.                                       | -231.3877.                            | -186.9836.                            | 84.931                       | -139026.                     | -135114.                              | -135114.                              | 6.164                        |
| 1200.               | 188.832                  | 353.868                | -217.736                             | 163298.                                      | -231.2225.                            | -185.0563.                            | 80.553                       | -123899.                     | -136220.                              | -136220.                              | 5.959                        |
| 1250.               | 191.147                  | 361.623                | -223.335                             | 172798.                                      | -231.0985.                            | -183.1356.                            | 76.528                       | -123450.                     | -136742.                              | -136742.                              | 5.714                        |
| (2 sigma)           | $\pm 2.130$              | $\pm 1.479$            | $\pm 1.845$                          | $\pm 2837.$                                  | $\pm 1559.$                           | $\pm 912.$                            | $\pm 0.038$                  | $\pm 1559.$                  | $\pm 912.$                            | $\pm 912.$                            | $\pm 0.038$                  |
| 1300.               | 193.556                  | 369.167                | -228.848                             | 182415.                                      | -230.8952.                            | -181.2217.                            | 72.816                       | -122354.                     | -132346.                              | -132346.                              | 5.516                        |
| 1350.               | 196.060                  | 376.518                | -234.131                             | 192155.                                      | -230.7118.                            | -179.3146.                            | 69.381                       | -121688.                     | -138446.                              | -138446.                              | 5.334                        |
| 1400.               | 198.558                  | 383.695                | -239.193                             | 202022.                                      | -230.6177.                            | -177.4145.                            | 66.194                       | -120937.                     | -138332.                              | -138332.                              | 5.185                        |
| 1450.               | 201.351                  | 390.713                | -244.431                             | 212022.                                      | -230.5224.                            | -175.5216.                            | 63.230                       | -120935.                     | -139043.                              | -139043.                              | 5.009                        |
| 1500.               | 204.139                  | 397.586                | -249.430                             | 222159.                                      | -230.0951.                            | -173.6359.                            | 60.465                       | -120095.                     | -139681.                              | -139681.                              | 4.864                        |
| (2 sigma)           | $\pm 5.194$              | $\pm 1.476$            | $\pm 1.576$                          | $\pm 2853.$                                  | $\pm 1396.$                           | $\pm 1153.$                           | $\pm 0.040$                  | $\pm 1396.$                  | $\pm 1153.$                           | $\pm 1153.$                           | $\pm 0.040$                  |
| 1550.               | 207.020                  | 404.326                | -254.356                             | 232438.                                      | -2298652.                             | -171.7577.                            | 57.882                       | -119160.                     | -140349.                              | -140349.                              | 4.730                        |
| 1600.               | 209.997                  | 410.946                | -259.156                             | 242863.                                      | -229622.                              | -1698871.                             | 55.462                       | -118125.                     | -141049.                              | -141049.                              | 4.605                        |
| 1650.               | 213.067                  | 417.454                | -263.355                             | 253439.                                      | -229364.                              | -168024.                              | 53.192                       | -116987.                     | -142711.                              | -142711.                              | 4.339                        |
| 1700.               | 216.877                  | 425.132                | -269.330                             | 266336.                                      | -234063.                              | -1657246.                             | 50.623                       | -101085.                     | -143689.                              | -143689.                              | 4.339                        |
| 1710.               | 199.600                  | 433.547                | -273.135                             | 288702.                                      | -232463.                              | -1641611.                             | 48.999                       | -100735.                     | -141783.                              | -141783.                              | 4.488                        |
| (2 sigma)           | $\pm 34.005$             | $\pm 1.490$            | $\pm 1.499$                          | $\pm 2981.$                                  | $\pm 1818.$                           | $\pm 1429.$                           | $\pm 0.043$                  | $\pm 1818.$                  | $\pm 1429.$                           | $\pm 1429.$                           | $\pm 0.043$                  |
| 1800.               | 199.600                  | 443.785                | -277.846                             | 298690.                                      | -2628383.                             | -1614273.                             | 46.845                       | -100338.                     | -144922.                              | -144922.                              | 4.206                        |
| (2 sigma)           | $\pm 34.005$             | $\pm 1.700$            | $\pm 1.333$                          | $\pm 3329.$                                  | $\pm 2346.$                           | $\pm 1484.$                           | $\pm 0.043$                  | $\pm 2346.$                  | $\pm 1484.$                           | $\pm 1484.$                           | $\pm 0.043$                  |

$\text{Ca}_2\text{O}_4\text{Si}$ 

$\text{Ca}_2\text{SiO}_4$  (reference state)      Ca-Olivine;  $\text{Ca}_2\text{SiO}_4$ , alpha prime;  
 $\text{Ca}_2\text{SiO}_4$ , alpha      Formula weight = 132.163 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 120.499 \pm 2.045 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -2316.534 \pm 2.441 \text{ kJ/mol}$$

$$V^\circ = 59.110 \pm 0.360 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -2199.776 \pm 1.881 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

## Ca-Olivine (temperature range 200 to 1120 K)

$$a_1 = -2.360066 \times 10^6$$

$$a_4 = 2.391441 \times 10^2$$

$$a_6 = 1.065862 \times 10^{-1}$$

$$a_2 = -7.387180 \times 10^4$$

$$a_5 = 0.0$$

$$a_7 = -8.150119 \times 10^{-5}$$

$$a_3 = 1.656378 \times 10^3$$

Ca<sub>2</sub>SiO<sub>4</sub>, alpha prime (temperature range 1120 to 1710 K)

$$a_1 = 0.0$$

$$a_4 = -8.056381 \times 10^2$$

$$a_6 = 0.0$$

$$a_2 = -4.835440 \times 10^4$$

$$a_5 = 1.616203 \times 10^2$$

$$a_7 = 1.889700 \times 10^{-5}$$

$$a_3 = 0.0$$

Ca<sub>2</sub>SiO<sub>4</sub>, alpha (temperature range 1710 to 1800 K)

$$a_1 = 0.0$$

$$a_4 = -1.052325 \times 10^3$$

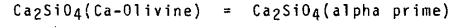
$$a_6 = 0.0$$

$$a_2 = -5.951 \times 10^4$$

$$a_5 = 1.996000 \times 10^2$$

$$a_7 = 0.0$$

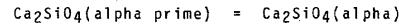
$$a_3 = 0.0$$

Critical ReactionsInversions:

$$T_i = 1120 \text{ K (observed)}$$

$$\Delta S_i^\circ = 12.231 \pm 2.51 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 13.699 \pm 2.46 \text{ kJ/mol}$$



$$T_i = 1710 \text{ K}$$

$$\Delta S_i^\circ = 8.415 \pm 2.49 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 14.390 \pm 3.39 \text{ kJ/mol}$$

For detailed information on Ca<sub>2</sub>SiO<sub>4</sub>, refer to the appropriate tables on the individual phases.

Ca<sub>2</sub>O<sub>4</sub>Si

$\text{Al}_2\text{Si}_1\text{O}_4$  reference state: Larnite prime (crystall.) 273.15 K to 970 K  
Alpha prime (crystall.) 970 K to 1710 K  
1710 K to 1800 K

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| Reference state:       |                                  | Larnite                     |             | 273.15 K to 970 K  |                               | Alpha prime<br>(crystal)            |                             | 370 K to 1710 K                      |                              | 1710 K to 1800 K |  |
|------------------------|----------------------------------|-----------------------------|-------------|--|-------------------------------|-------------------------------------|-----------------------------|--------------------------------------|------------------------------|------------------|--|
| $\alpha_2\text{SiO}_4$ | $\text{Ca}_2\text{O}_4\text{Si}$ | $\text{C}^\circ_{\text{p}}$ | $S^\circ$   | $(\text{G}^\circ_{\text{f}} - \text{H}^\circ_{\text{f,r}})/\text{T}$ | $\text{H}^\circ_{\text{f,r}}$ | $\Delta\text{H}^\circ_{\text{f,e}}$ | $\log K^\circ_{\text{f,e}}$ | $\Delta\text{G}^\circ_{\text{f,ox}}$ | $\log K^\circ_{\text{f,ox}}$ |                  |  |
| (K)                    | J/(mol · K)                      | J/(mol · K)                 | J/(mol · K) | J/mol  | J/mol                         | J/mol                               | J/mol                       | J/mol                                | J/mol                        |                  |  |
| 273.15                 | 122.972                          | 115.710                     | -127.219    | -3144.   | -2306625.                     | -2201426.                           | 420.980                     | -125798.                             | -128285.                     |                  |  |
|                        | 128.401                          | 126.719                     | -126.719    | 0.   | -2306697.                     | -2191794.                           | 385.993                     | -125811.                             | -128512.                     |                  |  |
| (2 sigma)              | ±0.238                           | ±1.286                      | ±1.286      | ±0.  | ±1328.                        | ±1039.                              | ±0.182                      | ±328.                                | ±1039.                       |                  |  |
|                        | 300.                             | 128.775                     | 127.514     | -126.721   | 238.                          | -2306699.                           | -2191081.                   | 381.501                              | -125815.                     |                  |  |
| 350.                   | 137.745                          | 148.065                     | -128.224    | 6110.  | -2306574.                     | -2171816.                           | 324.126                     | -126352.                             | -128979.                     |                  |  |
|                        | 400.                             | 144.975                     | 166.946     | 13984.   | -2306191.                     | -2152589.                           | 281.099                     | -126597.                             | -129860.                     |                  |  |
| 450.                   | 150.963                          | 184.378                     | -136.853    | 21386.   | -2305628.                     | -2133421.                           | 247.641                     | -125644.                             | -130741.                     |                  |  |
|                        | 500.                             | 156.030                     | 200.553     | -142.224   | 29065.                        | -2304940.                           | -2114323.                   | 220.882                              | -130293.                     |                  |  |
| (2 sigma)              | ±0.464                           | ±1.283                      | ±1.284      | ±68.   | ±1333.                        | ±883.                               | ±0.092                      | ±1333.                               | ±0.092                       |                  |  |
|                        | 550.                             | 160.388                     | 215.634     | -148.402   | 36078.                        | -2095174.                           | 198.995                     | -126050.                             | -130702.                     |                  |  |
| 600.                   | 161.190                          | 229.756                     | -154.599    | 45094.   | -2303366.                     | -2076344.                           | 180.762                     | -126114.                             | -131142.                     |                  |  |
|                        | 650.                             | 167.544                     | 243.033     | -160.836   | 5389.                         | -2305456.                           | -2057450.                   | 165.339                              | -126185.                     | -131558.         |  |
| 700.                   | 170.532                          | 255.561                     | -167.215    | 61842.   | -2307136.                     | -2038631.                           | 152.677.                    | -126118.                             | -131967.                     |                  |  |
|                        | 750.                             | 173.216                     | 267.420     | -173.503   | 70137.                        | -2302633.                           | -201978.                    | 140.671                              | -126382.                     | -132370.         |  |
| (2 sigma)              | ±0.665                           | ±1.311                      | ±1.281      | ±09.   | ±1355.                        | ±768.                               | ±0.053                      | ±1355.                               | ±0.053                       |                  |  |
|                        | 800.                             | 175.645                     | 278.677     | -179.728   | 79160.                        | -2301693.                           | -2000974.                   | 130.650                              | -126507.                     | -132765.         |  |
| 850.                   | 177.856                          | 289.393                     | -185.866    | 87198.   | -2300888.                     | -1992204.                           | 121.811                     | -123707.                             | -133147.                     |                  |  |
|                        | 900.                             | 179.879                     | 299.617     | -191.904   | 90942.                        | -2300226.                           | -1963448.                   | 113.957                              | -121118.                     | -133494.         |  |
| 950.                   | 181.841                          | 309.393                     | -197.832    | 10983.   | -22299712.                    | -1944785.                           | 106.932                     | -126826.                             | -133856.                     |                  |  |
|                        | 970.                             | 184.445                     | 313.187     | -200.171   | 109125.                       | -2229549.                           | -1937314.                   | 104.325                              | -126695.                     | -134005.         |  |
| (2 sigma)              | 970.                             | 179.400                     | 314.763     | -200.171   | 111153.                       | -22298013.                          | -1937311.                   | 104.325                              | -125171.                     | -132765.         |  |
|                        | 1000.                            | 180.510                     | 320.244     | -203.692   | 116552.                       | -22291913.                          | -1926160.                   | 100.612                              | -125062.                     | -134280.         |  |
| (2 sigma)              | ±0.830                           | ±1.359                      | ±1.284      | ±68.   | ±1402.                        | ±772.                               | ±0.040                      | ±1402.                               | ±772.                        |                  |  |
|                        | 1050.                            | 182.454                     | 329.098     | -209.454   | 125626.                       | -22297850.                          | -1907575.                   | 94.897                               | -124846.                     | -134746.         |  |
| 1100.                  | 184.486                          | 337.632                     | -215.087    | 134199.  | -22297925.                    | -1888989.                           | 85.701                      | -124583.                             | -135224.                     |                  |  |
|                        | 1150.                            | 186.612                     | 345.879     | -220.996   | 144076.                       | -2313237.                           | -1869836.                   | 80.934                               | -124667.                     | -135714.         |  |
| 1200.                  | 188.832                          | 353.868                     | -225.983    | 153162.  | -2313230.                     | -1850563.                           | 80.553                      | -122118.                             | -136220.                     |                  |  |
|                        | 1250.                            | 191.147                     | 361.623     | -231.254   | 162961.                       | -2310685.                           | -1831355.                   | 76.528                               | -123450.                     | -136742.         |  |
| (2 sigma)              | ±2.130                           | ±1.479                      | ±1.285      | ±847.  | ±1559.                        | ±910.                               | ±0.038                      | ±1559.                               | ±910.                        |                  |  |
|                        | 1300.                            | 193.556                     | 369.167     | -236.114   | 17278.                        | -2308952.                           | -1812217.                   | 78.816                               | -122940.                     | -137284.         |  |
| 1350.                  | 196.060                          | 376.518                     | -241.468    | 182118.  | -2301118.                     | -1793146.                           | 69.381                      | -122354.                             | -137846.                     |                  |  |
|                        | 1400.                            | 198.658                     | 383.695     | -246.120   | 192186.                       | -2305177.                           | -1774115.                   | 66.194                               | -121688.                     | -138432.         |  |
| 1450.                  | 201.351                          | 390.713                     | -251.775    | 202186.  | -2301124.                     | -1755216.                           | 65.230                      | -120937.                             | -139043.                     |                  |  |
|                        | 1500.                            | 204.139                     | 397.586     | -256.038   | 21322.                        | -2300951.                           | -1736359.                   | 60.465                               | -120095.                     | -139681.         |  |
| (2 sigma)              | ±5.794                           | ±1.476                      | ±1.294      | ±903.  | ±1596.                        | ±1153.                              | ±0.040                      | ±1596.                               | ±1153.                       |                  |  |
|                        | 1550.                            | 207.020                     | 404.326     | -260.713   | 222301.                       | -2298652.                           | -1717577.                   | 57.882                               | -119160.                     | -140349.         |  |
| 1600.                  | 209.967                          | 410.946                     | -265.304    | 23326.   | -2296222.                     | -169881.                            | 55.622                      | -118125.                             | -141049.                     |                  |  |
|                        | 1650.                            | 213.067                     | 417.454     | -269.817   | 243302.                       | -2293654.                           | -1680243.                   | 53.192                               | -116887.                     | -141783.         |  |
| 1700.                  | 216.233                          | 423.862                     | -274.553    | 254334.  | -2341451.                     | -1661216.                           | 51.044                      | -115741.                             | -142553.                     |                  |  |
|                        | 1710.                            | 216.877                     | 425.132     | -275.132   | 256500.                       | -2304863.                           | -1657246.                   | 50.623                               | -115478.                     | -142711.         |  |
| (2 sigma)              | 1710.                            | 199.600                     | 433.547     | -275.132   | 27090.                        | -2326473.                           | -1657246.                   | 50.623                               | -10035.                      | -142711.         |  |
|                        | 1750.                            | 199.600                     | 438.162     | -278.006   | 278874.                       | -2324801.                           | -1641611.                   | 48.999                               | -10035.                      | -143689.         |  |
| (2 sigma)              | ±34.005                          | ±1.490                      | ±1.300      | ±242.  | ±1818.                        | ±1429.                              | ±0.043                      | ±1816.                               | ±1429.                       |                  |  |
|                        | 1800.                            | 199.600                     | 443.785     | -283.311   | 28854.                        | -2628383.                           | -1612043.                   | 46.845                               | -10035.                      | -144922.         |  |
| (2 sigma)              | ±34.005                          | ±1.780                      | ±1.301      | ±2346.   | ±2346.                        | ±14423.                             | ±0.043                      | ±1816.                               | ±14484.                      |                  |  |

$\text{Ca}_2\text{O}_4\text{Si}$ 

$\text{Ca}_2\text{SiO}_4$  (reference state) Larnite;  $\text{Ca}_2\text{SiO}_4$ , alpha prime;  $\text{Ca}_2\text{SiO}_4$ , alpha Formula weight = 132.163 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 126.719 \pm 1.286 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -2306.697 \pm 1.328 \text{ kJ/mol}$$

$$V^\circ = 51.600 \pm 0.540 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -2191.794 \pm 1.039 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

## Larnite (temperature range 200 to 970 K)

$$a_1 = 0.0$$

$$a_4 = -1.538485 \times 10^3$$

$$a_6 = 0.0$$

$$a_2 = -2.120900 \times 10^3$$

$$a_5 = 2.496890 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -2.094286 \times 10^3$$

 $\text{Ca}_2\text{SiO}_4$ , alpha prime (temperature range 970 to 1710 K)

$$a_1 = 0.0$$

$$a_4 = -8.056381 \times 10^2$$

$$a_6 = 0.0$$

$$a_2 = -4.835440 \times 10^4$$

$$a_5 = 1.616203 \times 10^2$$

$$a_7 = 1.889700 \times 10^{-5}$$

$$a_3 = 0.0$$

 $\text{Ca}_2\text{SiO}_4$ , alpha (temperature range 1710 to 1800 K)

$$a_1 = 0.0$$

$$a_4 = -1.052325 \times 10^3$$

$$a_6 = 0.0$$

$$a_2 = -5.951000 \times 10^4$$

$$a_5 = 1.996000 \times 10^2$$

$$a_7 = 0.0$$

Critical Reactions

## Inversions:



$$T_i = 970 \text{ K (calculated)}$$

$$\Delta S_i^\circ = 1.576 \pm 1.93 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 1.528 \pm 0.61 \text{ kJ/mol}$$



$$T_i = 1710 \text{ K}$$

$$\Delta S_i^\circ = 8.415 \pm 2.49 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 14.390 \pm 3.39 \text{ kJ/mol}$$

For detailed information on  $\text{Ca}_2\text{SiO}_4$ , refer to the appropriate tables on the individual phases.

$\text{Ca}_2\text{SiO}_4$   
Alpha

$\text{Ca}_2\text{O}_4\text{Si}$

Issued September, 1979

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K)    | $S^o$<br>J/(mol·K)     | $(G_f^o - H_f^o)/T$<br>J/(mol·K) | $H_f^o - H_{Tr}^o$<br>J/mol | Formation from the Elements |                            |                          | Formation from the Oxides   |                             |                           |
|--------------------|-------------------------|------------------------|----------------------------------|-----------------------------|-----------------------------|----------------------------|--------------------------|-----------------------------|-----------------------------|---------------------------|
|                    |                         |                        |                                  |                             | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$<br>J/mol | $\Delta H_f^o, ox$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, ox$<br>J/mol |
| 1650.              | 199.600                 | 426.418                | --                               | --                          | -2278342.                   | -1619721.                  | 53.176                   | -101675.                    | -141261.                    | 4.472                     |
| 1700.              | 199.600                 | 432.376                | --                               | --                          | -2326392.                   | -1661161.                  | 51.041                   | -101181.                    | -142468.                    | 4.378                     |
| 1750.<br>(2 sigma) | 199.600<br>$\pm 34.005$ | 438.162<br>$\pm 1.490$ | --<br>$\pm 1.490$                | --<br>$\pm 1.490$           | -2324801.<br>$\pm 1618.$    | -1641611.<br>$\pm 1429.$   | 48.999<br>$\pm 0.043$    | -100735.<br>$\pm 18.8.$     | -14389.<br>$\pm 1429.$      | 4.289<br>$\pm 0.043$      |
| 1800.<br>(2 sigma) | 199.600<br>$\pm 34.005$ | 443.385<br>$\pm 1.700$ | --<br>$\pm 1.700$                | --<br>$\pm 1.700$           | -2628383.<br>$\pm 2346.$    | -1614273.<br>$\pm 1484.$   | 46.845<br>$\pm 0.043$    | -100338.<br>$\pm 2346.$     | -141922.<br>$\pm 1484.$     | 4.206<br>$\pm 0.043$      |

 $\text{Ca}_2\text{SiO}_4$ , alpha

Formula weight = 132.163 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = \pm J/(mol \cdot K)$$

$$\Delta H_f^\circ = \pm \text{kJ/mol}$$

$$\gamma^\circ = \pm \text{cm}^3/\text{mol}$$

$$\Delta G_f^\circ = \pm \text{kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 1650 to 1800 K)

$$C_p^\circ(T)/[J/(mol \cdot K)] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[J/(mol \cdot K)] = -a_1/(2 T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15K)]/(J/mol) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 0.0$$

$$a_4 = -1.052325 \times 10^3$$

$$a_6 = 0.0$$

$$a_2 = -5.95100 \times 10^4$$

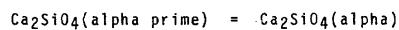
$$a_5 = 1.996000 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = 0.0$$

Critical Reactions

## Inversion:



$$T_i = 1710 \text{ K (observed)}$$

$$\Delta S_i^\circ = 8.415 \pm 2.49 \text{ J/(mol \cdot K)}$$

$$\Delta H_i^\circ = 14.390 \pm 3.387 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Table 1 provides the sources for the primary data used in evaluating the thermodynamic properties of  $\text{Ca}_2\text{SiO}_4$ , alpha.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                      | Data Type         | Method           | No. of Points | Range         |
|-----------------------------|-------------------|------------------|---------------|---------------|
| Coughlin and O'Brien (1957) | relative enthalpy | drop calorimetry | 5             | 1715 - 1816 K |

The relative enthalpy measurements of Coughlin and O'Brien (1957) were fit with a standard error of estimate of 287 J/mol or approximately 0.1 percent of the observed value.

The temperature of the experimentally observed inversion of alpha prime- $\text{Ca}_2\text{SiO}_4$  to alpha- $\text{Ca}_2\text{SiO}_4$  was entered as a fixed value in the regression and supplies constraint on the free energy of  $\text{Ca}_2\text{SiO}_4$ , alpha. This inversion temperature is listed as "observed" in the section on critical reactions.

$\text{Ca}_2\text{SiO}_4$   
Alpha prime      (orthorhombic, pseudohexagonal, dimorphous with Larnite)

Issued September, 1979  
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| Temperature<br>(K) | $C_p^{\circ}$<br>J/(mol·K) | $S^{\circ}$<br>J/(mol·K) | $(G_f^{\circ} - H_{f,r}^{\circ})T$<br>J/mol | $H_f^{\circ} - H_{f,r}^{\circ}$<br>J/mol | Formation from the Elements          |                                       |                                   |  | Formation from the Oxides                |                                  |  |  |
|--------------------|----------------------------|--------------------------|---|--|--------------------------------------|---------------------------------------|-----------------------------------|--|--|----------------------------------|--|--|
|                    |                            |                          |   |  | $\Delta H_f^{\circ}, e$<br>J/mol     | $\Delta G_f^{\circ}, e$<br>J/mol      | $\log K_f^{\circ}, e$             | $\Delta H_f^{\circ}, \text{ox}$<br>J/mol | $\Delta G_f^{\circ}, \text{ox}$<br>J/mol | $\log K_f^{\circ}, \text{ox}$    |  |  |
| 950.<br>(2 sigma)  | 178.675<br>$\pm 5.830$     | 311.033<br>$\pm 1.359$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2298123.<br>-2297913.<br>$\pm 772.$ | -1944753.<br>-1926160.<br>$\pm 0.040$ | 106.930<br>100.612<br>$\pm 1402.$ | -125237.<br>-125062.<br>$\pm 772.$       | -133824.<br>-13480.<br>$\pm 0.040$       | 7.358<br>7.014<br>$\pm 0.040$    |  |  |
| 1050.<br>(2 sigma) | 182.454<br>$\pm 5.866$     | 329.098<br>$\pm 1.359$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2297850.<br>-2307925.<br>$\pm 772.$ | -1907575.<br>-1888889.<br>$\pm 0.040$ | 94.897<br>89.701<br>$\pm 1402.$   | -124846.<br>-124583.<br>$\pm 772.$       | -134746.<br>-135224.<br>$\pm 0.040$      | 6.703<br>6.421<br>$\pm 0.040$    |  |  |
| 1100.<br>(2 sigma) | 186.612<br>$\pm 5.932$     | 337.032<br>$\pm 1.379$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2313877.<br>-2312325.<br>$\pm 772.$ | -1869836.<br>-1850563.<br>$\pm 0.040$ | 84.331<br>80.553<br>$\pm 1402.$   | -124267.<br>-124267.<br>$\pm 772.$       | -135714.<br>-136220.<br>$\pm 0.040$      | 6.164<br>5.929<br>$\pm 0.040$    |  |  |
| 1150.<br>(2 sigma) | 188.832<br>$\pm 6.147$     | 345.879<br>$\pm 1.423$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2310685.<br>-2310685.<br>$\pm 772.$ | -1831356.<br>-1831356.<br>$\pm 0.040$ | 76.528<br>76.528<br>$\pm 1402.$   | -123891.<br>-123450.<br>$\pm 772.$       | -136742.<br>-136742.<br>$\pm 0.040$      | 5.714<br>5.714<br>$\pm 0.040$    |  |  |
| 1200.<br>(2 sigma) | 191.147<br>$\pm 6.130$     | 361.023<br>$\pm 1.479$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2308952.<br>-2308952.<br>$\pm 772.$ | -1812217.<br>-1812217.<br>$\pm 0.040$ | 72.816<br>72.816<br>$\pm 1402.$   | -122940.<br>-122354.<br>$\pm 772.$       | -137284.<br>-137866.<br>$\pm 0.040$      | 5.516<br>5.334<br>$\pm 0.040$    |  |  |
| 1250.<br>(2 sigma) | 193.556<br>$\pm 6.060$     | 369.167<br>$\pm 1.518$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2307118.<br>-2307118.<br>$\pm 772.$ | -193146.<br>-1774145.<br>$\pm 0.040$  | 69.381<br>66.194<br>$\pm 1402.$   | -122354.<br>-121688.<br>$\pm 772.$       | -137866.<br>-138432.<br>$\pm 0.040$      | 5.334<br>5.165<br>$\pm 0.040$    |  |  |
| 1300.<br>(2 sigma) | 196.060<br>$\pm 6.658$     | 376.518<br>$\pm 1.595$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2305177.<br>-2303124.<br>$\pm 772.$ | -1774145.<br>-1755216.<br>$\pm 0.040$ | 66.194<br>63.230<br>$\pm 1402.$   | -121688.<br>-120937.<br>$\pm 772.$       | -137866.<br>-139033.<br>$\pm 0.040$      | 5.165<br>5.009<br>$\pm 0.040$    |  |  |
| 1350.<br>(2 sigma) | 198.658<br>$\pm 6.351$     | 383.595<br>$\pm 1.595$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2303124.<br>-2300951.<br>$\pm 772.$ | -1755216.<br>-1736559.<br>$\pm 0.040$ | 60.465<br>59.1153.<br>$\pm 1402.$ | -120937.<br>-120095.<br>$\pm 772.$       | -139033.<br>-139681.<br>$\pm 0.040$      | 4.864<br>4.864<br>$\pm 0.040$    |  |  |
| 1400.<br>(2 sigma) | 201.351<br>$\pm 6.139$     | 390.713<br>$\pm 1.476$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2298652.<br>-2298652.<br>$\pm 772.$ | -1717577.<br>-1698871.<br>$\pm 0.040$ | 57.882<br>55.662<br>$\pm 1402.$   | -119160.<br>-118125.<br>$\pm 772.$       | -140349.<br>-141049.<br>$\pm 0.040$      | 4.730<br>4.605<br>$\pm 0.040$    |  |  |
| 1450.<br>(2 sigma) | 204.139<br>$\pm 5.794$     | 397.386<br>$\pm 1.476$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2293654.<br>-231451.<br>$\pm 772.$  | -1680243.<br>-1661246.<br>$\pm 0.040$ | 53.192<br>51.044<br>$\pm 1402.$   | -116987.<br>-115741.<br>$\pm 772.$       | -141783.<br>-142533.<br>$\pm 0.040$      | 4.488<br>4.380<br>$\pm 0.040$    |  |  |
| 1500.<br>(2 sigma) | 207.020<br>$\pm 5.794$     | 404.326<br>$\pm 1.476$   | --<br>--                                    | --<br>$\pm 1402.$                        | -231451.<br>-2318447.<br>$\pm 772.$  | -1661246.<br>-1641283.<br>$\pm 0.043$ | 48.990<br>47.279<br>$\pm 1402.$   | -115741.<br>-11382.<br>$\pm 772.$        | -142533.<br>-143361.<br>$\pm 0.043$      | 4.380<br>4.279<br>$\pm 0.043$    |  |  |
| 1550.<br>(2 sigma) | 209.997<br>$\pm 5.653$     | 410.946<br>$\pm 1.496$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2318447.<br>-231858.<br>$\pm 772.$  | -1641283.<br>-1621432.<br>$\pm 0.043$ | 48.990<br>47.279<br>$\pm 1402.$   | -11382.<br>-112858.<br>$\pm 772.$        | -143361.<br>-14432.<br>$\pm 0.043$       | 4.279<br>4.1432.<br>$\pm 0.043$  |  |  |
| 1600.<br>(2 sigma) | 213.067<br>$\pm 5.233$     | 417.454<br>$\pm 1.386$   | --<br>--                                    | --<br>$\pm 1402.$                        | -231858.<br>-2318447.<br>$\pm 772.$  | -1621432.<br>-1611432.<br>$\pm 0.043$ | 48.990<br>47.279<br>$\pm 1402.$   | -112858.<br>-111382.<br>$\pm 772.$       | -14432.<br>-143361.<br>$\pm 0.043$       | 4.1432.<br>4.043.<br>$\pm 0.043$ |  |  |
| 1650.<br>(2 sigma) | 216.233<br>$\pm 5.492$     | 423.862<br>$\pm 1.177$   | --<br>--                                    | --<br>$\pm 1402.$                        | -2318447.<br>-231858.<br>$\pm 772.$  | -1611432.<br>-1601432.<br>$\pm 0.043$ | 48.990<br>47.279<br>$\pm 1402.$   | -111382.<br>-1101432.<br>$\pm 772.$      | -143361.<br>-14232.<br>$\pm 0.043$       | 4.043.<br>3.980.<br>$\pm 0.043$  |  |  |
| 1700.<br>(2 sigma) | 219.492<br>$\pm 5.653$     | 430.177<br>$\pm 1.996$   | --<br>--                                    | --<br>$\pm 1402.$                        | -231858.<br>-2318653.<br>$\pm 772.$  | -1601432.<br>-1591432.<br>$\pm 0.043$ | 48.990<br>47.279<br>$\pm 1402.$   | -1101432.<br>-1081432.<br>$\pm 772.$     | -14232.<br>-1411432.<br>$\pm 0.043$      | 3.980.<br>3.920.<br>$\pm 0.043$  |  |  |

$\text{Ca}_2\text{O}_4\text{Si}$  $\text{Ca}_2\text{SiO}_4$ , alpha prime

Formula weight = 132.163 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\%$ )

$$S^\circ = 116.049 \pm 13.62 \text{ J}/(\text{mol}\cdot\text{K}) \quad \Delta H_f^\circ = -2198.074 \pm 7.537 \text{ kJ/mol}$$

$$V^\circ = 52.298 \text{ cm}^3/\text{mol}^a \quad \Delta G_f^\circ = -2079.989 \pm 3.536 \text{ kJ/mol}$$

a Molar volume measured at 1023 K.

Equations at Reference Pressure, 101.325 kPa (Temperature range 950 to 1750 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[\Delta H^\circ(T) - \Delta H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

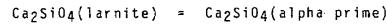
$$a_1 = 0.0 \quad a_4 = -8.056381 \times 10^2 \quad a_6 = 0.0$$

$$a_2 = 14.835440 \times 10^4 \quad a_5 = 1.616203 \times 10^2 \quad a_7 = 1.889700 \times 10^{-5}$$

$$a_3 = 0.0$$

Critical Reactions

## Inversion:



$$T_i = 970 \text{ K (observed)} \quad \Delta S_i^\circ = 1.576 \pm 1.93 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 1.528 \pm 0.61 \text{ kJ/mol}$$

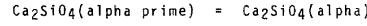
## Inversion:



$$T_i = 1120 \text{ K (observed)} \quad \Delta S_i^\circ = 12.231 \pm 2.51 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 13.699 \pm 2.46 \text{ kJ/mol}$$

## Inversion:



$$T_i = 1710 \text{ K (observed)} \quad \Delta S_i^\circ = 8.415 \pm 2.49 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 14.390 \pm 3.387 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of  $\text{Ca}_2\text{SiO}_4$  (alpha prime).

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

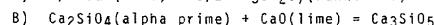
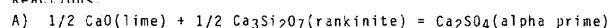
| Source                      | Data Type         | Method           | No. of Points | Range        |
|-----------------------------|-------------------|------------------|---------------|--------------|
| Coughlin and O'Brien (1957) | relative enthalpy | drop calorimetry | 12            | 974 - 1690 K |

The relative enthalpy measurements of Coughlin and O'Brien (1957) were fit with a standard error of estimate of 274 J/(mol·K) or approximately 0.14 percent of the observed value.

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                   | Method                  | Reaction <sup>a</sup> | Range T/K        | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|--|-------------------------|-----------------------|------------------|---------------|--------------------------------------|--------------------------------------|
| Benz and Wagner (1961)<br>Carlson (1931) | Emf<br>phase equilibria | A<br>B                | 971-1143<br>1523 | 10<br>1       | -5.517 ± 0.379<br>11.669 ± 0.145     | -2198.122<br>-2197.975               |

a Reactions:



Phase-equilibrium studies were evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. The temperatures of the experimentally observed polymorphic transitions of larnite to alpha prime- $\text{Ca}_2\text{SiO}_4$ , Ca-olivine to alpha prime- $\text{Ca}_2\text{SiO}_4$ , and alpha prime- $\text{Ca}_2\text{SiO}_4$  to alpha- $\text{Ca}_2\text{SiO}_4$  were entered as fixed values in the regression and supply additional constraints on the free energy of alpha prime- $\text{Ca}_2\text{SiO}_4$  and its polymorphs. These inversion temperatures are listed as "observed" in the section on critical reactions.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each reaction. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for alpha prime- $\text{Ca}_2\text{SiO}_4$  (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-2198.074 \pm 7.537 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of alpha prime- $\text{Ca}_2\text{SiO}_4$  and presents the data in their poorest perspective.

The molar volume measured at 1023 K was taken from the work of Douglas (1952).

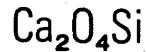
**Ca<sub>2</sub>SiO<sub>4</sub>**  
**Ca Olivine (gamma Ca<sub>2</sub>SiO<sub>4</sub>, orthorhombic, polymorphous with Bredigite and Larnite)**

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| Temperature<br>(K) | C <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K) | (G <sub>T</sub> <sup>°</sup> -H <sub>T,r</sub> <sup>°</sup> )/T<br>J/mol | Formation from the Elements                 |   |                               | Formation from the Oxides   |                             |                                |                |
|--------------------|-----------------------------|-----------------|--|---|---|-------------------------------|-----------------------------|-----------------------------|--------------------------------|----------------|
|                    |                             |                 |  | ΔH <sub>f,r</sub> <sup>°</sup> , e<br>J/mol | ΔG <sub>f,r</sub> <sup>°</sup> , e<br>J/mol | log K <sub>f,e</sub><br>J/mol | ΔH <sub>f,ox</sub><br>J/mol | ΔG <sub>f,ox</sub><br>J/mol | log K <sub>f,ox</sub><br>J/mol |                |
| 273.15             | 120.737                     | 109.706         | -120.989   | -3082.                                      | -2316400.                                   | -2209561.                     | 422.535                     | -135573.                    | -136420.                       | 26.088         |
| (2 sigma)          | 125.690 ± 0.387             | 120.439 ± 2.045 | -120.499 ± 0.45  | -3082.                                      | -2316534. ± 2441.                           | -2199776. ± 881.              | 385.391 ± 0.330             | -135648. ± 2441.            | -136494. ± 1881.               | 23.913 ± 0.330 |
| 300.               | 126.025                     | 121.278         | -120.502   | 233.  | -2316540.                                   | -2199051.                     | 382.889                     | -135654.                    | -136500.                       | 23.767         |
| (2 sigma)          | 133.898 ± 0.297             | 141.321 ± 2.045 | -122.067 ± 0.45  | 233.  | -2316561. ± 16413.                          | -2179963. ± 5984.             | 325.267                     | -135659.                    | -136625.                       | 20.390         |
| 400.               | 145.851                     | 176.432         | -125.634   | 1358.                                       | -2316413.                                   | -215984.                      | 282.052                     | -136118.                    | -136718.                       | 17.853         |
| (2 sigma)          | 150.846 ± 0.500             | 192.112 ± 2.055 | -130.360 ± 0.46  | 2075.                                       | -2316096. ± 140336.                         | -2140336.                     | 248.444                     | -136412.                    | -136725.                       | 15.876         |
| 550.               | 155.417                     | 206.706         | -141.556   | 35833.                                      | -2315667. ± 1522.                           | -2120829. ± 152.              | 221.561                     | -136721.                    | -136799.                       | 14.291         |
| (2 sigma)          | 159.629 ± 0.411             | 220.413 ± 2.053 | -147.562 ± 0.46  | 35833.                                      | -2315156. ± 152.                            | -2101369. ± 152.              | 199.571                     | -137032.                    | -136792.                       | 12.991         |
| 600.               | 163.510                     | 233.345         | -153.668   | 43710.                                      | -2314586.                                   | -2081959.                     | 181.251                     | -13735.                     | -136756.                       | 11.906         |
| (2 sigma)          | 167.074 ± 0.411             | 245.595 ± 2.053 | -159.801 ± 0.46  | 43710.                                      | -2313981. ± 2062598.                        | -2062598.                     | 165.752                     | -137625.                    | -136696.                       | 10.985         |
| 700.               | 170.322                     | 257.234         | -165.912   | 68492.                                      | -2313360. ± 234415.                         | -2043284. ± 234415.           | 152.472                     | -137500.                    | -136614.                       | 10.194         |
| (2 sigma)          | 170.322 ± 0.411             | 268.322 ± 2.053 | -162.084 ± 0.46  | 68492.                                      | -2313360. ± 234415.                         | -2043284. ± 234415.           | 140.960                     | -138154.                    | -136513.                       | 9.508          |
| 800.               | 173.251                     | 268.322         | -171.968   | 77083.                                      | -2313607.                                   | -2004603.                     | 130.887                     | -138421.                    | -136395.                       | 8.906          |
| (2 sigma)          | 175.859 ± 0.411             | 278.305 ± 2.053 | -177.950 ± 0.46  | 77083.                                      | -2312911.                                   | -1985313.                     | 122.002                     | -139393.                    | -136255.                       | 8.373          |
| 900.               | 178.138                     | 289.023         | -183.842   | 94663.                                      | -2312342.                                   | -1966059.                     | 114.007                     | -139233.                    | -136075.                       | 7.898          |
| (2 sigma)          | 180.084 ± 0.411             | 298.708 ± 2.053 | -189.634 ± 0.46  | 94663.                                      | -2311912.                                   | -1949834.                     | 107.044                     | -139026.                    | -135905.                       | 7.473          |
| 1000.              | 181.690                     | 307.937         | -195.322   | 11266.                                      | -2311636.                                   | -1927627.                     | 100.689                     | -138135.                    | -135747.                       | 7.091          |
| (2 sigma)          | 182.952 ± 0.411             | 316.834 ± 2.053 | -200.900 ± 0.46  | 112783.                                     | -2311529.                                   | -1908430.                     | 94.939                      | -138526.                    | -135601.                       | 6.746          |
| 1100.              | 183.864                     | 325.417         | -206.367   | 13055.                                      | -2311605.                                   | -188933.                      | 89.112                      | -138254.                    | -135468.                       | 6.433          |
| (2 sigma)          | 184.422 ± 0.411             | 333.604 ± 2.053 | -211.723 ± 0.46  | 140164.                                     | -2327625.                                   | -1863469.                     | 84.914                      | -138016.                    | -135347.                       | 6.148          |
| 1150.              | 184.422 ± 0.411             | 325.417 ± 2.053 | -211.723 ± 0.46  | 140164.                                     | -2327625.                                   | -1863469.                     | 82.038                      | -1245.                      | -1826.                         | ± 0.038        |

## THERMODYNAMIC DATA FOR MINERALS

6

 $\text{Ca}_2\text{SiO}_4$ , gamma

Calcium Olivine

Formula weight = 132.163 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 120.499 \pm 2.045 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = -2316.534 \pm 2.441 \text{ kJ/mol}$$

$$V^\circ = 59.110 \pm 0.360 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -2199.776 \pm 1.881 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1150 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = -2.360066 \times 10^6$$

$$a_4 = 2.391441 \times 10^2$$

$$a_6 = 1.065862 \times 10^{-1}$$

$$a_2 = 7.387180 \times 10^4$$

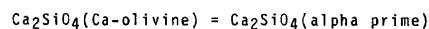
$$a_5 = 0.0$$

$$a_7 = -8.150119 \times 10^{-5}$$

$$a_3 = 1.656378 \times 10^3$$

Critical Reactions

## Inversion:



$$T_i = 1120 \text{ K (observed)}$$

$$\Delta S_i^\circ = 12.231 \pm 2.51 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_i^\circ = 13.699 \pm 2.46 \text{ kJ/mol}$$

Primary Experimental Data Used in the Analysis

Table 1 provides the sources for the primary data used in evaluating the thermodynamic properties of Ca-olivine.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                      | Data Type         | Method                 | No. of Points | Range        |
|-----------------------------|-------------------|------------------------|---------------|--------------|
| King (1957)                 | heat capacity     | isothermal calorimetry | 10            | 206 - 296 K  |
| Coughlin and O'Brien (1957) | relative enthalpy | drop calorimetry       | 18            | 405 - 1113 K |
| King (1957)                 | entropy           | isothermal calorimetry | 1             | 298.15 K     |

The heat-capacity values of King (1957) were fit with a standard error of estimate of 0.56 J/(mol·K). The relative enthalpy measurements of Coughlin and O'Brien (1957) were fit with a standard error of estimate of 232 J/mol or approximately 0.93 percent of the observed value. The fitted entropy at 298.15 K is  $120.499 \pm 2.045 \text{ J}/(\text{mol}\cdot\text{K})$ , or a departure of 0.001 from the experimental value of  $120.50 \pm 0.84$  reported by King (1957).

The temperatures of the experimentally observed inversion of Ca-olivine to alpha prime- $\text{Ca}_2\text{SiO}_4$  was entered as a fixed value in the regression and supplies a constraint on the free energy of Ca-olivine and its polymorphs. This inversion temperature is listed as "observed" in the section on critical reactions.

The molar volume of Ca olivine was obtained from the compilation of Robie and others (1967).

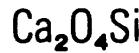
Ca<sub>2</sub>SiO<sub>4</sub>

Issued September 1981

| Temperature<br>(K) | C <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K) | (G <sub>T</sub> <sup>°</sup> -H <sub>Tf</sub> <sup>°</sup> )/T<br>J/mol | Formation from the Elements  |   |   | Formation from the Oxide            |  |  |
|--------------------|-----------------------------|-----------------|---|--|---|---|-------------------------------------|--|--|
|                    |                             |                 |   | H <sub>T</sub> <sup>°</sup> -H <sub>Tf</sub> <sup>°</sup><br>J/mol | ΔH <sub>f</sub> <sup>°</sup> , e<br>J/mol | ΔG <sub>f</sub> <sup>°</sup> , e<br>J/mol | log K <sub>f</sub> <sup>°</sup> , e | ΔH <sub>f</sub> <sup>°</sup> , OX<br>J/mol | ΔG <sub>f</sub> <sup>°</sup> , OX<br>J/mol |
| 273.15             | 122.972                     | 115.710         | -127.219  | -3144.   | -2306625.                                 | -2201426.                                 | 420.980                             | -125798.                                   | -128285.                                   |
| (2 sigma)          | 298.15                      | 128.401         | 126.719   | -126.119<br>±1.286   | 0.<br>±0.                                 | -2306697.<br>±1328.                       | -2191794.<br>±0.182                 | -125811.<br>±1128.                         | -128512.<br>±1039.                         |
| 300.               | 128.775                     | 127.514         | -126.721  | 238.   | -2306699.                                 | -2191031.                                 | 381.501                             | -125813.                                   | -128529.                                   |
| 350.               | 137.745                     | 148.016         | -128.324  | 6910.  | -2306574.                                 | -2171816.                                 | 324.126                             | -125812.                                   | -128979.                                   |
| 400.               | 144.975                     | 166.916         | -131.988  | 13984.   | -2306191.                                 | -2152589.                                 | 281.099                             | -125897.                                   | -129422.                                   |
| 450.               | 156.363                     | 184.318         | -136.953  | 21396.   | -2305628.                                 | -2133421.                                 | 247.641                             | -125944.                                   | -129860.                                   |
| 500.               | 156.330                     | 200.533         | -142.424  | 29066.   | -2301940.                                 | -2114323.                                 | 230.882                             | -125955.                                   | -132939.                                   |
| (2 sigma)          |                             | ±0.464          | ±1.243  | ±1.284   | ±65.                                      | ±1333.                                    | ±883.                               | ±1133.                                     | ±883.                                      |
| 550.               | 160.388                     | 215.634         | -148.402  | 36978.   | -2304174.                                 | -2095288.                                 | 188.995                             | -126050.                                   | -130720.                                   |
| 600.               | 164.190                     | 229.756         | -154.599  | 45098.   | -2303366.                                 | -207634.                                  | 180.762                             | -126114.                                   | -131142.                                   |
| 650.               | 167.544                     | 243.033         | -160.896  | 53389.   | -2302245.                                 | -2057459.                                 | 155.339                             | -126189.                                   | -131558.                                   |
| 700.               | 170.532                     | 255.561         | -167.215  | 61842.   | -2301736.                                 | -2038637.                                 | 152.125                             | -126227.                                   | -131967.                                   |
| 750.               | 173.216                     | 267.410         | -173.503  | 7043.  | -2301633.                                 | -2019798.                                 | 140.671                             | -126382.                                   | -132370.                                   |
| (2 sigma)          |                             | ±0.665          | ±1.311  | ±1.281   | ±209.                                     | ±1355.                                    | ±764.                               | ±1355.                                     | ±764.                                      |
| 800.               | 175.845                     | 278.677         | -179.728  | 79160.   | -2301693.                                 | -2000974.                                 | 130.650                             | -126607.                                   | -132765.                                   |
| 850.               | 177.856                     | 289.393         | -185.866  | 87998.   | -2300888.                                 | -1982204.                                 | 121.811                             | -127370.                                   | -133147.                                   |
| 900.               | 179.879                     | 299.617         | -191.904  | 96942.   | -2300226.                                 | -1963478.                                 | 113.957                             | -127118.                                   | -133494.                                   |
| 950.               | 181.741                     | 309.393         | -197.832  | 105987.  | -2299112.                                 | -1944785.                                 | 116.932                             | -126826.                                   | -133856.                                   |
| 1000.              | 183.462                     | 318.760         | -203.646  | 115116.  | -2292351.                                 | -1926114.                                 | 110.610                             | -126500.                                   | -134234.                                   |
| (2 sigma)          |                             | ±0.791          | ±1.370  | ±1.285   | ±390.                                     | ±1403.                                    | ±773.                               | ±1403.                                     | ±773.                                      |

## THERMODYNAMIC DATA FOR MINERALS

653

 $\text{Ca}_2\text{SiO}_4$ , beta

Larnite

Formula weight = 132.163 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$S^\circ = 126.719 \pm 1.286 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_f^\circ = -2306.697 \pm 1.328 \text{ kJ/mol}$

$V^\circ = 51.600 \pm 0.540 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -2191.794 \pm 1.039 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1000 K)

$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$

$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

$a_1 = 0.0$

$a_4 = -1.538485 \times 10^3$

$a_6 = 0.0$

$a_2 = -2.120900 \times 10^3$

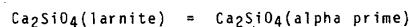
$a_5 = 2.496890 \times 10^2$

$a_7 = 0.0$

$a_3 = -2.094286 \times 10^3$

Critical Reactions

## Inversion:



$T_i = 970 \text{ K (observed)}$

$\Delta S_i^\circ = 1.576 \pm 1.93 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_i^\circ = 1.528 \pm 0.61 \text{ kJ/mol}$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of larnite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                      | Data Type         | Method                 | No. of Points | Range       |
|-----------------------------|-------------------|------------------------|---------------|-------------|
| Todd (1951)                 | heat capacity     | isothermal calorimetry | 10            | 206 - 296 K |
| Coughlin and O'Brien (1957) | relative enthalpy | drop calorimetry       | 10            | 406 - 965 K |
| Hemingway and Robie (1977)  | entropy           |                        | 1             | 298.15 K    |

The heat capacity measured by Todd (1951) was fit with a standard error of estimate of 0.13 J/(mol·K). The relative enthalpy measurements of Coughlin and O'Brien (1957) were fit with a standard error of estimate of 102 J/mol or approximately 0.16 percent of the observed value. The fitted entropy at 298.15 K is  $126.719 \pm 1.286 \text{ J}/(\text{mol}\cdot\text{K})$  which agrees with the experimental value of  $126.7 \pm 0.8 \text{ J}/(\text{mol}\cdot\text{K})$  reported by Hemingway and Robie (1977).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                  | Method   | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_r^\circ(298.15 \text{ K})$<br>kJ | $\Delta H_f^\circ(298.15 \text{ K})$<br>kJ/mol |
|---|--|-----------------------|-----------|---------------|--|--|
| Brunauer and others (1956) <sup>b</sup> | solution calorimetry<br>(HF-HNO <sub>3</sub> ) | A                     | 296.15    | 1             | -8.637 ± 0.831                             | -2306.681                                      |
| King (1951) <sup>c</sup>                | solution calorimetry (HF) <sup>c</sup>         | B                     | 346.85    | 6             | 126.069 ± 1.971                            | -2306.954                                      |
| Benz and Wagner (1961)                  | Emf  | C                     | 943-963   | 3             | -2.678 ± 0.088                             | -2312.720                                      |

## a Reactions:

- A)  $\text{Ca}_3\text{SiO}_5 = \text{Ca}_2\text{SiO}_4(\text{larnite}) + \text{CaO}(\text{lime})$
- B)  $\text{Ca}_2\text{SiO}_4(\text{larnite}) = \text{SiO}_2(\text{quartz, alpha}) + 2 \text{CaO}(\text{lime})$
- C)  $1/2 \text{CaO}(\text{lime}) + 1/2 \text{Ca}_3\text{Si}_2\text{O}_7(\text{rankinite}) = \text{Ca}_2\text{SiO}_4(\text{larnite})$

b Brunauer and others (1956) measured the difference in the heat of solution of  $\text{Ca}_3\text{SiO}_5$  and a 1:1 molar mixture of larnite and lime.

c King (1951) measured the heat of solution of larnite in HF acid at 346.85 K. To complete the thermodynamic cycle, his data were evaluated in combination with the more recent data for the enthalpies of solution of lime (Barany, 1963) and of quartz (Hemingway and Robie, 1977; Bennington and others, 1978) in similar solutions.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for larnite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-2306.697 \pm 1.320 \text{ kJ/mol}$  obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of larnite and presents the data in their poorest perspective.

The temperatures of well-defined experimentally observed polymorphic transitions were entered as fixed values in the regression and supply additional constraints on the free energy of larnite and its polymorphs. These inversion temperatures are listed as "observed" in the section on critical reactions.

The molar volume of larnite was obtained from the compilation of Robie and others (1967).

**Ca<sub>3</sub>SiO<sub>5</sub>**  
(crystal)  
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| Temperature<br>( $\kappa$ ) | $C_p^o$<br>J/(mol·K)   | $S^o$<br>J/(mol·K)     | $(G_T^o - H_{Tr}^o)/T$<br>J/mol | Formation from the Elements |                             |                           | Formation from the Oxides    |                              |                         |              |
|-----------------------------|------------------------|------------------------|---------------------------------|-----------------------------|-----------------------------|---------------------------|------------------------------|------------------------------|-------------------------|--------------|
|                             |                        |                        |                                 | $\Delta H_f^o$ , e<br>J/mol | $\Delta S_f^o$ , e<br>J/mol | $\log K_f^o$ , e<br>J/mol | $\Delta H_f^o$ , ox<br>J/mol | $\Delta S_f^o$ , ox<br>J/mol | $\log K_f^o$ , ox       |              |
| - 273.15                    | 164.410                | 153.834                | -169.268                        | -4202.                      | -2933125.                   | -2799938.                 | 535.434                      | -117167.                     | -120665.                |              |
| (2 sigma)                   | 171.604<br>$\pm 0.853$ | 168.600<br>$\pm 0.311$ | -168.600<br>$\pm 0.311$         | 0.<br>$\pm 0.$              | -2933137.<br>$\pm 1700.$    | -2787747.<br>$\pm 1659.$  | 488.401<br>$\pm 0.298$       | -117157.<br>$\pm 1700.$      | -120985.<br>$\pm 1699.$ |              |
| 300.                        | 172.099                | 169.653                | -168.603                        | 318.                        | -2933132.                   | -2786845.                 | 485.232                      | -117157.                     | -121009.                |              |
| 350.                        | 183.906                | 197.115                | -170.744                        | 9230.                       | -2932784.                   | -2762485.                 | 412.278                      | -117131.                     | -12153.                 |              |
| 400.                        | 193.347                | 222.310                | -175.637                        | 18659.                      | -2932088.                   | -273201.                  | 357.572                      | -117087.                     | -12202.                 |              |
| 450.                        | 201.110                | 245.546                | -182.131                        | 2837.                       | -2931152.                   | -2714019.                 | 315.035                      | -117024.                     | -12257.                 |              |
| 500.                        | 207.650                | 267.032                | -189.562                        | 38760.                      | -2930059.                   | -2689951.                 | 281.017                      | -116945.                     | -12321.                 |              |
| (2 sigma)                   | $\pm 3.398$            | $\pm 1.120$            | $\pm 0.352$                     | $\pm 456.$                  | $\pm 1956.$                 | $\pm 1662.$               | $\pm 0.174$                  | $\pm 1956.$                  | $\pm 1662.$             |              |
| 550.                        | 213.200                | 287.139                | -197.532                        | 49284.                      | -2928875.                   | -2665997.                 | 253.195                      | -116854.                     | -12493.                 |              |
| 600.                        | 218.023                | 305.901                | -205.789                        | 50067.                      | -2927651.                   | -2642153.                 | 230.020                      | $\pm 116755.$                | $\pm 12473.$            |              |
| 650.                        | 222.248                | 323.523                | -224.175                        | 71076.                      | -2926429.                   | -268411.                  | 210.418                      | $\pm 116654.$                | $\pm 12562.$            |              |
| 700.                        | 225.903                | 340.133                | -222.584                        | 32284.                      | -2925247.                   | -2694762.                 | 193.623                      | $\pm 116556.$                | $\pm 12635.$            |              |
| (2 sigma)                   | 750.                   | 229.313                | -230.949                        | 9368.                       | -2926442.                   | -271095.                  | 179.066                      | $\pm 116465.$                | $\pm 12645.$            |              |
| 800.                        | 232.301                | 370.736                | -239.224                        | 105209.                     | -2925300.                   | -2547427.                 | 166.330                      | $\pm 116385.$                | $\pm 127711.$           |              |
| 850.                        | 235.000                | 384.902                | -247.380                        | 116593.                     | -2924178.                   | -2232845.                 | 155.097                      | $\pm 117039.$                | $\pm 128480.$           |              |
| 900.                        | 237.451                | 398.414                | -255.398                        | 128705.                     | -2923286.                   | -2400323.                 | 145.115                      | $\pm 116751.$                | $\pm 12473.$            |              |
| 950.                        | 241.733                | 423.630                | -263.267                        | 140655.                     | -2922633.                   | -27684.                   | 136.186                      | $\pm 116661.$                | $\pm 12966.$            |              |
| (2 sigma)                   | $\pm 6.077$            | $\pm 2.573$            | $\pm 1.167$                     | $\pm 1574.$                 | $\pm 292226.$               | $\pm 2453313.$            | $\pm 1343.$                  | $\pm 115515.$                | $\pm 12979.$            |              |
| 1000.                       | 243.614                | 435.191                | -278.533                        | 154805.                     | -2922070.                   | -2429956.                 | 128.152                      | $\pm 116511.$                | $\pm 13021.$            |              |
| (2 sigma)                   | 1050.                  | 245.349                | 446.854                         | -285.928                    | 177030.                     | -2922172.                 | -2406521.                    | $\pm 116461.$                | $\pm 1343.$             |              |
| 1100.                       | 246.955                | 457.806                | -293.165                        | 139338.                     | -294150.                    | -2382224.                 | 118.276                      | $\pm 116451.$                | $\pm 1343.$             |              |
| 1200.                       | 248.444                | 468.348                | -300.246                        | 201723.                     | -293950.                    | -257763.                  | 108.204                      | $\pm 11713.$                 | $\pm 1328.$             |              |
| 1250.                       | 249.828                | 478.519                | -307.174                        | 214181.                     | -2941709.                   | -233334.                  | 102.631                      | $\pm 117075.$                | $\pm 13366.$            |              |
| (2 sigma)                   | 1300.                  | 251.118                | 488.343                         | -313.955                    | 226705.                     | -2940659.                 | 97.507                       | $\pm 117021.$                | $\pm 13425.$            |              |
| 1350.                       | 252.322                | 497.813                | -320.590                        | 239291.                     | -293114.                    | -2382224.                 | 108.204                      | $\pm 117021.$                | $\pm 13313.$            |              |
| 1400.                       | 253.449                | 507.040                | -327.086                        | 251916.                     | -293464.                    | -2220783.                 | 84.351                       | $\pm 117075.$                | $\pm 13366.$            |              |
| 1450.                       | 254.504                | 515.952                | -333.446                        | 264435.                     | -2936734.                   | -2236734.                 | 80.577                       | $\pm 117090.$                | $\pm 13471.$            |              |
| 1500.                       | 255.495                | 524.597                | -339.674                        | 277185.                     | -2929971.                   | -2212808.                 | 77.057                       | $\pm 109141.$                | $\pm 13919.$            |              |
| (2 sigma)                   | 1550.                  | 256.425                | 532.990                         | -345.775                    | 230183.                     | -2927531.                 | -2188943.                    | 73.767                       | $\pm 117051.$           | $\pm 13190.$ |
| 1600.                       | 257.301                | 541.145                | -351.754                        | 303026.                     | -293114.                    | -2284896.                 | 88.408                       | $\pm 111107.$                | $\pm 136582.$           |              |
| 1650.                       | 258.126                | 549.076                | -357.614                        | 315912.                     | -293464.                    | -2220783.                 | 84.351                       | $\pm 110447.$                | $\pm 13738.$            |              |
| 1700.                       | 258.904                | 556.793                | -363.359                        | 328838.                     | -2936734.                   | -2236734.                 | 80.577                       | $\pm 109790.$                | $\pm 14317.$            |              |
| 1750.                       | 259.638                | 564.309                | -368.993                        | 341802.                     | -296863.                    | -2092311.                 | 62.452                       | $\pm 106107.$                | $\pm 144828.$           |              |
| (2 sigma)                   | 1800.                  | 260.331                | 571.633                         | -374.521                    | 354801.                     | -293732.                  | $\pm 0.067$                  | $\pm 13732.$                 | $\pm 231.$              |              |
| (2 sigma)                   | $\pm 34.435$           | $\pm 9.712$            | $\pm 1.934$                     | $\pm 15153.$                | $\pm 3423647.$              | $\pm 2055533.$            | $\pm 0.076$                  | $\pm 15328.$                 | $\pm 214.$              |              |

$\text{Ca}_3\text{O}_5\text{Si}$ 

$\text{Ca}_3\text{SiO}_5$  (reference)       $\text{Ca}_3\text{SiO}_5$       Formula weight = 228.323 g/mol  
 (Hatrurite and others polymorphs, undifferentiated)<sup>a</sup>

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 168.600 \pm 0.311 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -2933.13 \pm 1.700 \text{ kJ/mol}$$

$$V^\circ = 72.742 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -2787.747 \pm 1.699 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1800 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = -6.525972 \times 10^4$$

$$a_4 = -2.053310 \times 10^3$$

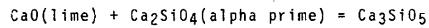
$$a_6 = -2.325287 \times 10^{-3}$$

$$a_2 = -4.046000 \times 10^3$$

$$a_5 = 3.339197 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -2.766085 \times 10^3$$

Critical ReactionsDecomposition:

$$T_d = 1622.76 \text{ K (calculated)}$$

$$\Delta S_d^\circ = 7.114 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_d^\circ = 10.834 \text{ kJ/mol}$$

<sup>a</sup> Data insufficient to evaluate properties of individual polymorphs. Equation constants and tabular data represent averaged properties of all polymorphs in temperature range of stability at 101.325 kPa.

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of  $\text{Ca}_3\text{SiO}_5$ .

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                     | Data Type         | Method                 | No. of Points | Range        |
|----------------------------|-------------------|------------------------|---------------|--------------|
| Todd (1951)                | heat capacity     | isothermal calorimetry | 9             | 206 - 297 K  |
| Gronow and Schwiete (1933) | relative enthalpy | drop calorimetry       | 12            | 576 - 1558 K |
| Todd (1951)                | entropy           | isothermal calorimetry | 1             | 298.15 K     |

The heat-capacity values of Todd (1951) were fit with a standard error of estimate of 0.19 J/(mol·K). The relative enthalpy measurements of Gronow and Schwiete (1933) were fit with a standard error of estimate of 1021 J/mol or approximately 0.46 percent of the observed value. The fitted entropy value at 298.15 K is  $168.600 \pm 0.311 \text{ J/(mol}\cdot\text{K)}$  or a departure of 0.003 from the experimental value of  $168.6 \pm 1.25$  reported by Todd (1951).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                                  | Method                                       | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H^\circ(298.15 \text{ K})$ | $\Delta H_f^\circ(298.15 \text{ K})$ |
|---|--|-----------------------|-----------|---------------|------------------------------------|--------------------------------------|
| Brunauer and others (1956) <sup>b</sup> | solution calorimetry (HCl-HNO <sub>3</sub> ) | A                     | 296.15    | 1             | -8.637 ± 0.831                     | -2933.153                            |
| Carlson (1931)                          | phase equilibria                             | B                     | 1523      | 1             | 11.669 ± 0.145                     | -2933.136                            |

a Reactions:

- A)  $\text{Ca}_3\text{SiO}_5 = \text{Ca}_2\text{SiO}_4(\text{larnite}) + \text{CaO(lime)}$
- B)  $\text{Ca}_2\text{SiO}_4(\text{alpha prime}) + \text{CaO(lime)} = \text{Ca}_3\text{SiO}_5$

<sup>b</sup> Brunauer and others (1956) measured the difference in the heat of solution of  $\text{Ca}_3\text{SiO}_5$  and a 1:1 molar mixture of larnite and lime.

The phase-equilibrium study of Carlson (1931) was evaluated after converting the data to free energies of reaction at 101.325 kPa and temperature. After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated and is shown in column 6 of Table 2. From this enthalpy of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for  $\text{Ca}_3\text{SiO}_5$  (column 7 of Table 2) was calculated and can be compared with the enthalpy of formation of -2933.137 ± 1.70 kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of  $\text{Ca}_3\text{SiO}_5$  and presents the data in their poorest perspective.

The molar volume was taken from the work of Yamaguchi and Miyabe (1960).

$\text{Ca}_3\text{Si}_2\text{O}_7$   
Rankinite (monoclinic)

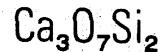
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$\text{Ca}_3\text{O}_7\text{Si}_2$

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| Temperature<br>(K)  | $C_p^o$<br>$\text{J}/(\text{mol} \cdot \text{K})$ | $S^o$<br>$\text{J}/(\text{mol} \cdot \text{K})$ | $(G_f^o - H_{f,r}^o)/T$ | $H_f^o - H_{f,r}^o$<br>$\text{J}/\text{mol}$ | Formation from the Elements                |  |                   | Formation from the Oxides                   |   |                  |
|---------------------|---|---|-------------------------|--|--|--|-------------------|---|---|------------------|
|                     |   |   |                         |  | $\Delta H_f^o, e$<br>$\text{J}/\text{mol}$ | $\Delta S_f^o, e$<br>$\text{J}/\text{mol}$ | $\log K_f^o, e$   | $\Delta H_f^o, ox$<br>$\text{J}/\text{mol}$ | $\Delta S_f^o, ox$<br>$\text{J}/\text{mol}$ | $\log K_f^o, ox$ |
| 273.15              | 204.957   | 192.235   | -211.434                | -5244.                                       | -3973011.                                  | -3790325.                                  | 724.826           | -246438.                                    | -250177.                                    | 47.841           |
| 298.15<br>(2 sigma) | 214.369<br>±0.714                                 | 210.600<br>±2.938                               | -210.600<br>±0.         | -3973202.<br>±3200.                          | -3773595.<br>±4466.                        | ±0.432                                     | 661.118           | -246524.<br>±3200.                          | -250513.<br>±2466.                          | 43.889<br>±0.432 |
| 300.                | 215.016   | 211.928   | -210.604                | 397.   | -3973210.                                  | -3773257.                                  | 656.325           | -246527.                                    | -250537.                                    | 43.622           |
| 350.                | 230.468   | 246.277   | -213.281                | 115.9.                                       | -3973134.                                  | -3731880.                                  | 557.997           | -246621.                                    | -251195.                                    | 37.489           |
| 400.                | 242.564   | 277.868   | -219.407                | 233.04.                                      | -3972631.                                  | -3704446.                                  | 483.881           | -246717.                                    | -251845.                                    | 32.888           |
| 450.                | 252.365   | 307.024   | -227.544                | 357.66.                                      | -3971835.                                  | -3670933.                                  | 426.245           | -246911.                                    | -25472.                                     | 29.306           |
| 500.<br>(2 sigma)   | 260.380<br>±1.088                                 | 334.049<br>±2.959                               | -236.859<br>±2.937      | 485.91.<br>±180.                             | -3970851.<br>±3224.                        | -3633840.<br>±2027.                        | 380.147<br>±0.212 | -24718.<br>±3224.                           | -25079.<br>±3224.                           | 20.439<br>±0.212 |
| 550.                | 267.039   | 350.181   | -246.850                | 617.82.                                      | -3969762.                                  | -3606691.                                  | 342.440           | -24741.                                     | -251661.                                    | 24.091           |
| 600.                | 272.596   | 382.662   | -257.200                | 752.77.                                      | -3966632.                                  | -3576643.                                  | 311.026           | -24773.                                     | -25214.                                     | 22.131           |
| 650.                | 277.270   | 404.671   | -267.706                | 890.27.                                      | -3966516.                                  | -3536689.                                  | 284.453           | -24823.                                     | -25423.                                     | 20.471           |
| 700.                | 281.217   | 424.367   | -278.236                | 1029.2.                                      | -3966461.                                  | -3506820.                                  | 261.682           | -24874.                                     | -255214.                                    | 19.044           |
| 750.<br>(2 sigma)   | 284.560<br>±1.207                                 | 444.887<br>±3.038                               | -288.702<br>±2.943      | 1171.9.<br>±452.                             | -3968011.<br>±3277.                        | -3471913.<br>±1607.                        | 241.945<br>±0.112 | -24945.<br>±3277.                           | -251652.<br>±3277.                          | 17.805<br>±0.112 |
| 800.                | 287.391   | 463.345   | -299.045                | 1314.9.                                      | -3966857.                                  | -3441012.                                  | 224.675           | -250213.                                    | -250401.                                    | 16.718           |
| 850.                | 289.785   | 480.841   | -309.229                | 1458.0.                                      | -3965965.                                  | -340175.                                   | 209.441           | -252556.                                    | -25368.                                     | 15.754           |
| 900.                | 291.905   | 497.464   | -319.229                | 1604.2.                                      | -3965349.                                  | -3375383.                                  | 195.902           | -25278.                                     | -256587.                                    | 14.892           |
| 950.                | 293.498   | 511.288   | -329.029                | 1750.5.                                      | -3955020.                                  | -3345618.                                  | 183.790           | -25294.                                     | -257795.                                    | 14.120           |
| 1000.<br>(2 sigma)  | 294.905<br>±0.930                                 | 528.379<br>±3.157                               | -338.622<br>±2.959      | 1897.5.<br>±677.                             | -3964990.<br>±3339.                        | -330862.<br>±1474.                         | 172.889<br>±0.077 | -253147.<br>±3339.                          | -25994.<br>±1474.                           | 13.424<br>±0.077 |
| 1050.               | 296.062   | 542.797   | -348.004                | 2045.2.                                      | -3955267.                                  | -3271100.                                  | 163.027           | -253330.                                    | -251180.                                    | 12.794           |
| 1100.               | 296.995   | 556.592   | -357.174                | 2193.9.                                      | -3965859.                                  | -324317.                                   | 154.060           | -253670.                                    | -251354.                                    | 12.221           |
| 1150.               | 297.730   | 569.811   | -366.134                | 2342.8.                                      | -3960389.                                  | -3210660.                                  | 145.833           | -253997.                                    | -257515.                                    | 11.697           |
| 1200.               | 298.287   | 582.494   | -374.887                | 2491.9.                                      | -3988004.                                  | -3176793.                                  | 138.282           | -254318.                                    | -256660.                                    | 11.216           |
| 1250.               | 298.684   | 599.679   | -383.436                | 2640.4.                                      | -398212.                                   | -3144991.                                  | 131.338           | -254822.                                    | -257787.                                    | 10.772           |
| (2 sigma)           | 299.038<br>±0.930                                 | 613.157<br>±3.157                               | -397.980<br>±2.980      | 2844.<br>±844.                               | -3339.                                     | -31725.                                    | ±0.072            | ±3339.                                      | ±1725.                                      | ±0.072           |
| 1300.               | 298.936   | 606.399   | -391.788                | 2789.5.                                      | -3985708.                                  | -3105251.                                  | 124.931           | -255333.                                    | -25896.                                     | 10.362           |
| 1350.               | 299.057   | 611.684   | -399.947                | 2939.5.                                      | -3944215.                                  | -307570.                                   | 119.001           | -25599.                                     | -25984.                                     | 9.982            |
| 1400.               | 299.058   | 628.560   | -407.918                | 30889.                                       | -3988237.                                  | -3041944.                                  | 113.496           | -256586.                                    | -258048.                                    | 9.628            |

 $\text{Ca}_3\text{Si}_2\text{O}_7$ 

Rankinite

Formula weight = 288.407 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$$S^\circ = 210.600 \pm 2.938 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -3973.202 \pm 3.20 \text{ kJ/mol}$$

$$V^\circ = 96.506 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -3773.595 \pm 2.466 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (Temperature range 200 to 1400 K)

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = 3.397203 \times 10^5$$

$$a_4 = -2.971338 \times 10^3$$

$$a_6 = -2.103545 \times 10^{-2}$$

$$a_2 = 1.106750 \times 10^4$$

$$a_5 = 4.732091 \times 10^2$$

$$a_7 = 0.0$$

$$a_3 = -4.318802 \times 10^3$$

Primary Experimental Data Used in the Analysis

Tables 1 and 2 provide the sources for the primary data used in evaluating the thermodynamic properties of rankinite.

Table 1. Sources for Heat Capacity, Relative Enthalpy, Entropy, and Related Data

| Source                          | Data Type     | Method                 | No. of Points | Range        |
|---------------------------------|---------------|------------------------|---------------|--------------|
| King (1957)<br>Estimated values | heat capacity | isothermal calorimetry | 10            | 206 - 296 K  |
| King (1957)                     | heat capacity | component summation    | 12            | 400 - 1500 K |
| King (1957)                     | entropy       | isothermal calorimetry | 1             | 298.15 K     |

The heat capacity measured by King (1957) was fit with a standard error of estimate of 0.28 J/(mol·K). The estimated heat-capacity values were fit with a standard error of estimate of 5.33 J/(mol·K). The fitted entropy at 298.15 K is  $210.600 \pm 2.938 \text{ J/(mol}\cdot\text{K)}$ , or a departure of 0.27 J/mol from the experimental value of  $210.87 \pm 1.26$  reported by King (1957).

Table 2. Sources for the Enthalpy and Free Energy of Reaction and Related Data, and Enthalpies Calculated After Fitting

| Source                 | Method | Reaction <sup>a</sup> | Range T/K | No. of Points | $\Delta H_f^\circ(298.15 \text{ K})$ | $\Delta G_f^\circ(298.15 \text{ K})$ |
|------------------------|--------|-----------------------|-----------|---------------|--------------------------------------|--------------------------------------|
| Benz and Wagner (1961) | Emf    | A                     | 943-963   | 3             | -2.678 $\pm$ 0.088                   | -3961.156                            |
| Benz and Wagner (1961) | Emf    | B                     | 971-1143  | 10            | -5.517 $\pm$ 0.379                   | -3973.106                            |
| Benz and Wagner (1961) | Emf    | C                     | 943-1003  | 10            | -41.441 $\pm$ 0.186                  | -3968.856                            |

a Reactions:

- A)  $\frac{1}{2} \text{CaO(lime)} + \frac{1}{2} \text{Ca}_3\text{Si}_2\text{O}_7(\text{rankinite}) = \text{Ca}_2\text{Si}_4\text{O}_9(\text{larnite})$
- B)  $\frac{1}{2} \text{CaO(lime)} + \frac{1}{2} \text{Ca}_3\text{Si}_2\text{O}_7(\text{rankinite}) = \text{Ca}_2\text{Si}_4\text{O}_9(\text{alpha prime})$
- C)  $\frac{1}{2} \text{CaO(lime)} + \text{Ca}_3\text{Al}_2\text{Si}_3\text{O}_{10}(\text{cyclo wollastonite}) = \frac{1}{2} \text{Ca}_3\text{Si}_2\text{O}_7(\text{rankinite})$

Phase-equilibrium studies of Benz and Wagner (1961) were evaluated after the data were converted to free energies of reaction at 101.325 kPa and temperature.

After fitting, as a test of consistency, the average enthalpy of reaction at 298.15 K and 101.325 kPa was calculated for each source. These enthalpies are shown in column 6 of Table 2. From these enthalpies of reaction and the calculated enthalpies of formation of other phases in the reactions, the enthalpy of formation for rankinite (column 7 of Table 2) was calculated for each source and can be compared with the enthalpy of formation of  $-3973.202 \pm 3.20$  kJ/mol obtained from the fit. This calculation assigns the error of fit entirely to the heat of formation of rankinite and presents the data in their poorest perspective.

The molar volume was taken from the work of Saburi and others (1976).

**H<sub>2</sub>**

H<sub>2</sub>  
Reference Table: Ideal diatomic gas 273.15 K to 1800 K

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| Temperature<br>(K) | C <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K) | (G <sub>T</sub> <sup>°</sup> -H <sub>T,r</sub> <sup>°</sup> )/T<br>J/(mol·K) | H <sub>T</sub> <sup>°</sup> -H <sub>T,r</sub> <sup>°</sup><br>J/mol | Formation from the Elements |                            |                               | Formation from the Oxides   |                             |                                |
|--------------------|-----------------------------|-----------------|--|---|-----------------------------|----------------------------|-------------------------------|-----------------------------|-----------------------------|--------------------------------|
|                    |                             |                 |  |   | ΔH <sub>f,e</sub><br>J/mol  | ΔG <sub>f,e</sub><br>J/mol | log K <sub>f,e</sub><br>J/mol | ΔH <sub>f,ox</sub><br>J/mol | ΔG <sub>f,ox</sub><br>J/mol | log K <sub>f,ox</sub><br>J/mol |
| 273.15             | 28.513                      | 128.058         | -130.683   | -717.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 298.15             | 28.822                      | 130.570         | -130.570   | 0.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 300.               | 28.839                      | 130.748         | -130.570   | 53.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 350.               | 29.127                      | 135.219         | -130.923   | 1504.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 400.               | 29.221                      | 139.116         | -131.709   | 2963.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 450.               | 29.244                      | 142.559         | -132.727   | 4425.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 500.               | 29.250                      | 145.641         | -133.667   | 5887.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 550.               | 29.263                      | 148.429         | -135.066   | 7350.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 600.               | 29.293                      | 150.977         | -136.387   | 8814.   | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 650.               | 29.345                      | 153.323         | -137.509   | 10280.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 700.               | 29.417                      | 155.500         | -138.717   | 11748.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 750.               | 29.511                      | 157.533         | -139.304   | 13222.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 800.               | 29.623                      | 159.441         | -141.066   | 14700.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 850.               | 29.751                      | 161.241         | -142.201   | 16184.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 900.               | 29.995                      | 162.945         | -143.306   | 17675.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 950.               | 30.052                      | 164.566         | -144.383   | 19174.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1000.              | 30.220                      | 166.112         | -145.431   | 20681.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1050.              | 30.397                      | 167.590         | -146.451   | 22196.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1100.              | 30.584                      | 169.009         | -147.445   | 23720.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1150.              | 30.777                      | 170.372         | -148.112   | 25254.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1200.              | 30.975                      | 171.686         | -149.354   | 26798.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1250.              | 31.179                      | 172.955         | -150.273   | 28352.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1300.              | 31.387                      | 174.182         | -151.169   | 29916.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1350.              | 31.597                      | 175.370         | -152.044   | 31491.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1400.              | 31.810                      | 176.523         | -152.898   | 33076.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1450.              | 32.024                      | 177.643         | -153.332   | 34672.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1500.              | 32.239                      | 178.733         | -154.547   | 36278.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1550.              | 32.455                      | 179.793         | -155.344   | 37896.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1600.              | 32.670                      | 180.827         | -156.125   | 39524.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1650.              | 32.885                      | 181.836         | -156.888   | 41163.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1700.              | 33.099                      | 182.820         | -157.337   | 42812.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1750.              | 33.311                      | 183.783         | -158.370   | 44473.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |
| 1800.              | 33.522                      | 184.724         | -159.089   | 46143.  | 0.                          | 0.                         | 0.                            | --                          | --                          | --                             |

## THERMODYNAMIC DATA FOR MINERALS

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 $\text{H}_2$ , ideal gas

Hydrogen, ideal diatomic gas

Formula weight = 2.016 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$$S^\circ = 130.570 \text{ J}/(\text{mol}\cdot\text{K})$$

$$\Delta H_f^\circ = 0.0 \text{ kJ/mol}$$

$$V^\circ = 24789.200 \pm 3.4 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = 0.0 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa (temperature range 200 to 1800 K)

$$C_p(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T)-H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

$$a_1 = -5.1040600 \times 10^5$$

$$a_4 = 1.29375 \times 10^2$$

$$a_6 = 5.85357 \times 10^{-3}$$

$$a_2 = -1.8603165 \times 10^4$$

$$a_5 = 7.44240$$

$$a_7 = -1.38995 \times 10^{-6}$$

$$a_3 = 4.1016500 \times 10^2$$

Sources for Thermodynamic Properties

The thermodynamic properties for hydrogen were taken from the following sources:

| <u>Property</u> | <u>Source</u>              |
|-----------------|----------------------------|
| Heat capacity   | Hultgren and others (1973) |
| Entropy         | CODATA Task Group (1978)   |

$H_2O$   
Reference state: liquid 273.15 K to 373.15 K  
ideal gas 373.15 K to 1800 K

Issued September, 1979

# $H_2O$

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K) | $S^o$<br>( $\frac{J}{mol}$ · $K$ ) | $(\frac{\partial^o H_f^o}{\partial T} + H_f^o)_{Tr}$ /T<br>J/mol | Formation from the Elements   |                            |                 |                                    | Formation from the Oxides          |                         |                                    |                         |
|--------------------|----------------------|------------------------------------|--|-------------------------------|----------------------------|-----------------|------------------------------------|------------------------------------|-------------------------|------------------------------------|-------------------------|
|                    |                      |                                    |  | $H_f^o - H_f^o_{Tr}$<br>J/mol | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$ | $\Delta H_f^o, \text{ox}$<br>J/mol | $\Delta G_f^o, \text{ox}$<br>J/mol | $\log K_f^o, \text{ox}$ | $\Delta G_f^o, \text{ox}$<br>J/mol | $\log K_f^o, \text{ox}$ |
| 273.15             | 75.884               | 63.307                             | -70.218  | -1888.                        | -286613.                   | -241274.        | 46.139                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 298.15             | 75.254               | 69.921                             | -69.921  | 0.                            | -285808.                   | -237160.        | 41.549                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 300                | 75.230               | 70.386                             | -69.922  | 139.                          | -285749.                   | -236858.        | 41.241                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 350                | 75.469               | 81.881                             | -70.837  | 3900.                         | -28178.                    | -228854.        | 34.152                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 373.15             | 76.003               | 86.831                             | -71.681  | 5633.                         | -28447.                    | -225197.        | 31.524                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 373.15             | 34.048               | 196.318                            | -71.681  | 46509.                        | -242592.                   | -225197.        | 31.524                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 400                | 34.245               | 198.601                            | -80.127  | 47435.                        | -242865.                   | -223956.        | 29.243                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 450                | 34.669               | 202.448                            | -93.530  | 49148.                        | -243368.                   | -221539.        | 25.716                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 500                | 35.154               | 206.426                            | -104.639   | 50833.                        | -243861.                   | -219088.        | 22.883                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 550                | 35.686               | 209.801                            | -114.048   | 52664.                        | -244340.                   | -216557.        | 20.570                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 600                | 36.253               | 212.330                            | -122.159   | 54453.                        | -244804.                   | -214033.        | 18.634                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 650                | 36.846               | 215.855                            | -129.255   | 56220.                        | -245251.                   | -211422.        | 16.993                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 700                | 37.458               | 218.608                            | -135.540   | 58147.                        | -245681.                   | -208864.        | 15.584                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 750                | 38.082               | 221.213                            | -141.165   | 60046.                        | -246093.                   | -206201.        | 14.361                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 800                | 38.715               | 223.691                            | -146.247   | 61956.                        | -246488.                   | -203538.        | 13.289                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 850                | 39.352               | 226.057                            | -151.872   | 63907.                        | -246864.                   | -202612.        | 12.342                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 900                | 39.989               | 228.325                            | -155.113   | 65891.                        | -247224.                   | -198113.        | 11.498                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 950                | 40.624               | 230.504                            | -159.024   | 67916.                        | -247566.                   | -195375.        | 10.742                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1000               | 41.254               | 232.604                            | -165.650   | 69933.                        | -24891.                    | -192660.        | 10.061                             | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1050               | 41.878               | 234.632                            | -166.030   | 72032.                        | -248200.                   | -189849.        | 9.444                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1100               | 42.494               | 236.594                            | -168.193   | 74141.                        | -244920.                   | -18703.         | 8.883                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1150               | 43.100               | 238.596                            | -172.165   | 76251.                        | -248169.                   | -184265.        | 8.370                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1200               | 43.695               | 240.343                            | -174.968   | 78451.                        | -249031.                   | -181155.        | 7.899                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1250               | 44.278               | 242.139                            | -177.619   | 80650.                        | -249278.                   | -178634.        | 7.465                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1300               | 44.848               | 243.887                            | -180.134   | 82878.                        | -248511.                   | -175803.        | 7.064                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1350               | 45.404               | 245.590                            | -182.527   | 85151.                        | -249730.                   | -17294.         | 6.692                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1400               | 45.945               | 247.251                            | -184.809   | 87448.                        | -24936.                    | -17017.         | 6.347                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1450               | 46.472               | 248.872                            | -186.990   | 89729.                        | -250310.                   | -16723.         | 6.025                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1500               | 46.982               | 250.456                            | -189.079   | 92065.                        | -250310.                   | -164403.        | 5.725                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1550               | 47.477               | 252.005                            | -191.084   | 94427.                        | -250480.                   | -161536.        | 5.444                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1600               | 47.954               | 253.520                            | -193.012   | 96833.                        | -250638.                   | -158635.        | 5.180                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1650               | 48.415               | 255.003                            | -194.868   | 99222.                        | -250786.                   | -155738.        | 4.932                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1700               | 48.858               | 256.555                            | -195.658   | 101654.                       | -251923.                   | -152907.        | 4.698                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1750               | 49.283               | 257.877                            | -198.387   | 104108.                       | -251051.                   | -15003.         | 4.478                              | 0.                                 | 0.                      | 0.                                 | 0.                      |
| 1800               | 49.689               | 259.271                            | -200.059   | 106582.                       | -251170.                   | -147134.        | 4.270                              | 0.                                 | 0.                      | 0.                                 | 0.                      |

**H<sub>2</sub>O**H<sub>2</sub>O (reference state)H<sub>2</sub>O, water; H<sub>2</sub>O, ideal gas

Formula weight = 18.015 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$S^\circ = 69.921 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_f^\circ = -285.808 \text{ kJ/mol}$

$V^\circ = 18.069 \pm 0.003 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -237.160 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa

$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$

$[\Delta H^\circ(T) - \Delta H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

H<sub>2</sub>O, water (temperature range 200 to 373.15 K)

$a_1 = 6.6170441 \times 10^5$

$a_4 = -1.5130719 \times 10^3$

$a_6 = 3.0064551 \times 10^{-2}$

$a_2 = -1.1932000 \times 10^4$

$a_5 = 2.2085094 \times 10^2$

$a_7 = 0.0$

$a_3 = -2.6676397 \times 10^3$

H<sub>2</sub>O, ideal gas (temperature range 373.15 to 1800 K)

$a_1 = -1.310770 \times 10^5$

$a_4 = 1.55636 \times 10^2$

$a_6 = 1.29775 \times 10^{-2}$

$a_2 = -1.499822 \times 10^4$

$a_5 = 1.04381 \times 10^1$

$a_7 = -4.46885 \times 10^{-6}$

$a_3 = 2.99100 \times 10^2$

Critical Reaction

## Inversion:

H<sub>2</sub>O, water = H<sub>2</sub>O, ideal gas

$T_i = 373.15 \text{ K (observed)}$

$\Delta S_i^\circ = 109.487 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_i^\circ = 40.856 \text{ kJ/mol}$

Sources for Thermodynamic Properties

The thermodynamic properties for water and the ideal gas were taken from the following sources:

| <u>Property</u>                         | <u>Source</u>  |
|---|--|
| Heat capacity                           | Stull and Prophet (1971) and Chase and others (1974, 1975) |
| Entropy                                 | CODATA Task Group (1978)                                   |
| Enthalpy of formation from the elements | CODATA Task Group (1978)                                   |

$H_2O$   
Ideal Gas

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$H_2O$

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| Temperature<br>(K) | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_f^o - H_f^o)/T$<br>J/mol | Formation from the Elements |                            |                 | Formation from the Oxides   |                             |                  |
|--------------------|----------------------|--------------------|------------------------------|-----------------------------|----------------------------|-----------------|-----------------------------|-----------------------------|------------------|
|                    |                      |                    |                              | $H_f^o - H_{Tr}^o$<br>J/mol | $\Delta H_f^o, e$<br>J/mol | $\log K_f^o, e$ | $\Delta H_f^o, ox$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, ox$ |
| 273.15             | 33.540               | 185.790            | -188.864                     | -840.                       | -241592.                   | -229710.        | 43.927                      | 0.                          | 0.               |
| 298.15             | 33.632               | 188.731            | -188.731                     | 0.                          | -241836.                   | -228611.        | 40.052                      | 0.                          | 0.               |
| 300.               | 33.640               | 188.939            | -188.732                     | 62.                         | -241854.                   | -228529.        | 39.790                      | 0.                          | 0.               |
| 350.               | 33.897               | 194.143            | -189.142                     | 1750.                       | -242357.                   | -226229.        | 33.769                      | 0.                          | 0.               |
| 373.15             | 34.048               | 196.318            | -189.520                     | 2537.                       | -242592.                   | -225197.        | 31.524                      | 0.                          | 0.               |
| 400.               | 34.245               | 198.691            | -190.057                     | 3453.                       | -242865.                   | -223936.        | 29.243                      | 0.                          | 0.               |
| 450.               | 34.669               | 202.748            | -191.246                     | 5176.                       | -243366.                   | -221599.        | 25.716                      | 0.                          | 0.               |
| 500.               | 35.154               | 206.426            | -192.583                     | 6921.                       | -243861.                   | -219088.        | 22.888                      | 0.                          | 0.               |
| 550.               | 35.686               | 209.801            | -193.997                     | 8692.                       | -244340.                   | -216587.        | 20.570                      | 0.                          | 0.               |
| 600.               | 36.553               | 212.930            | -195.146                     | 10491.                      | -244804.                   | -214643.        | 18.634                      | 0.                          | 0.               |
| 650.               | 36.846               | 215.855            | -196.304                     | 12318.                      | -245251.                   | -211452.        | 16.993                      | 0.                          | 0.               |
| 700.               | 37.458               | 218.608            | -198.357                     | 14175.                      | -245681.                   | -208546.        | 15.584                      | 0.                          | 0.               |
| 750.               | 38.082               | 221.213            | -199.95                      | 16664.                      | -246093.                   | -206201.        | 14.361                      | 0.                          | 0.               |
| 800.               | 38.715               | 223.691            | -201.211                     | 17984.                      | -246486.                   | -20328.         | 13.289                      | 0.                          | 0.               |
| 850.               | 39.352               | 226.057            | -202.604                     | 19935.                      | -246864.                   | -200632.        | 12.342                      | 0.                          | 0.               |
| 900.               | 39.989               | 228.325            | -203.910                     | 21911.                      | -247224.                   | -198113.        | 11.498                      | 0.                          | 0.               |
| 950.               | 40.624               | 230.504            | -205.310                     | 23934.                      | -247566.                   | -195315.        | 10.742                      | 0.                          | 0.               |
| 1000.              | 41.254               | 232.604            | -206.622                     | 23981.                      | -247891.                   | -192620.        | 10.061                      | 0.                          | 0.               |
| 1050.              | 41.878               | 234.632            | -207.908                     | 28060.                      | -248200.                   | -189849.        | 9.444                       | 0.                          | 0.               |
| 1100.              | 42.494               | 236.594            | -209.168                     | 30169.                      | -248492.                   | -187033.        | 8.883                       | 0.                          | 0.               |
| 1150.              | 43.100               | 240.343            | -211.611                     | 32309.                      | -248769.                   | -18370.         | 8.370                       | 0.                          | 0.               |
| 1200.              | 43.695               | 240.343            | -211.611                     | 34479.                      | -249031.                   | -181455.        | 7.899                       | 0.                          | 0.               |
| 1250.              | 44.278               | 242.139            | -212.796                     | 36678.                      | -249276.                   | -178634.        | 7.465                       | 0.                          | 0.               |
| 1300.              | 44.848               | 243.887            | -213.959                     | 38906.                      | -249511.                   | -175803.        | 7.064                       | 0.                          | 0.               |
| 1350.              | 45.404               | 245.590            | -215.099                     | 41163.                      | -249730.                   | -172564.        | 6.692                       | 0.                          | 0.               |
| 1400.              | 45.445               | 247.251            | -216.217                     | 43446.                      | -249936.                   | -170117.        | 6.347                       | 0.                          | 0.               |
| 1450.              | 46.472               | 248.872            | -217.316                     | 45757.                      | -250126.                   | -167233.        | 6.025                       | 0.                          | 0.               |
| 1500.              | 46.982               | 250.456            | -218.394                     | 48093.                      | -250310.                   | -164403.        | 5.725                       | 0.                          | 0.               |
| 1550.              | 47.477               | 252.005            | -219.453                     | 50455.                      | -250480.                   | -161536.        | 5.444                       | 0.                          | 0.               |
| 1600.              | 47.954               | 253.520            | -220.494                     | 52841.                      | -250638.                   | -158665.        | 5.180                       | 0.                          | 0.               |
| 1650.              | 48.115               | 255.003            | -221.518                     | 55250.                      | -250786.                   | -155708.        | 4.932                       | 0.                          | 0.               |
| 1700.              | 48.858               | 256.455            | -222.524                     | 57682.                      | -250923.                   | -152907.        | 4.698                       | 0.                          | 0.               |
| 1750.              | 49.283               | 257.877            | -223.514                     | 60136.                      | -251051.                   | -15023.         | 4.478                       | 0.                          | 0.               |
| 1800.              | 49.689               | 259.271            | -224.488                     | 62610.                      | -251170.                   | -147134.        | 4.270                       | 0.                          | 0.               |

 $\text{H}_2\text{O}$  $\text{H}_2\text{O}$ , ideal gas

Formula weight = 18.015 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2\text{s}$ )

$S^\circ = 188.731 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_f^\circ = -241.836 \text{ kJ/mol}$

$V^\circ = 24789.200 \pm 3.4 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = -228.611 \text{ kJ/mol}$

Equations at Reference Pressure, 101.325 kPa (temperature range 200 to 1800 K)

$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$

$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

$a_1 = -1.310770 \times 10^5$

$a_4 = 1.55636 \times 10^2$

$a_6 = 1.29775 \times 10^{-2}$

$a_2 = -1.499812 \times 10^4$

$a_5 = 1.04381 \times 10^1$

$a_7 = -4.46885 \times 10^{-6}$

$a_3 = 2.99188 \times 10^2$

Critical Reaction

Inversion:

 $\text{H}_2\text{O}$ , water =  $\text{H}_2\text{O}$ , ideal gas

$T_i = 373.15 \text{ K (observed)}$

$\Delta S_i^\circ = 109.487 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_i^\circ = 40.856 \text{ kJ/mol}$

Sources for Thermodynamic Properties

The thermodynamic properties for the ideal gas were taken from the following sources:

| <u>Property</u>                         | <u>Source</u>  |
|---|--|
| Heat capacity                           | Stull and Prophet (1971) and Chase and others (1974, 1975) |
| Entropy                                 | CODATA Task Group (1978)                                   |
| Enthalpy of formation from the elements | CODATA Task Group (1978)                                   |

$O_2$ 

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Reference Table: Ideal diatomic gas 273.15 K to 1800 K

| Temperature<br>(K) | Formation from the Elements |                    |                              | Formation from the Oxides          |                          |                             |
|--------------------|-----------------------------|--------------------|------------------------------|------------------------------------|--------------------------|-----------------------------|
|                    | $C_p^o$<br>J/(mol·K)        | $S^o$<br>J/(mol·K) | $(G_f^o - H_f^o)/T$<br>J/mol | $\Delta H_f^o - H_f^o, e$<br>J/mol | $\log K_f^o, e$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol |
| 273.15             | 29.199                      | 202.468            | -205.148                     | -732.                              | 0.                       | 0.                          |
| 293.15             | 29.377                      | 205.033            | -205.033                     | 0.                                 | 0.                       | 0.                          |
| 300.               | 29.391                      | 205.214            | -205.033                     | 54.                                | 0.                       | 0.                          |
| 350.               | 29.336                      | 209.718            | -205.393                     | 1535.                              | 0.                       | 0.                          |
| 400.               | 30.320                      | 213.733            | -206.197                     | 3039.                              | 0.                       | 0.                          |
| 450.               | 30.805                      | 217.392            | -207.244                     | 4567.                              | 0.                       | 0.                          |
| 500.               | 31.274                      | 220.662            | -208.125                     | 6119.                              | 0.                       | 0.                          |
| 550.               | 31.722                      | 223.614            | -209.676                     | 7694.                              | 0.                       | 0.                          |
| 600.               | 32.145                      | 226.443            | -210.959                     | 9291.                              | 0.                       | 0.                          |
| 650.               | 32.545                      | 229.032            | -212.250                     | 10908.                             | 0.                       | 0.                          |
| 700.               | 32.921                      | 231.457            | -213.537                     | 12545.                             | 0.                       | 0.                          |
| 750.               | 33.275                      | 233.741            | -214.808                     | 14200.                             | 0.                       | 0.                          |
| 800.               | 33.607                      | 235.819            | -216.059                     | 15872.                             | 0.                       | 0.                          |
| 850.               | 33.919                      | 237.916            | -217.287                     | 17560.                             | 0.                       | 0.                          |
| 900.               | 34.212                      | 239.893            | -218.489                     | 19263.                             | 0.                       | 0.                          |
| 950.               | 34.487                      | 241.750            | -219.666                     | 20981.                             | 0.                       | 0.                          |
| 1000.              | 34.744                      | 243.526            | -220.814                     | 22712.                             | 0.                       | 0.                          |
| 1050.              | 34.985                      | 245.227            | -221.936                     | 24455.                             | 0.                       | 0.                          |
| 1100.              | 35.209                      | 246.810            | -223.032                     | 26210.                             | 0.                       | 0.                          |
| 1150.              | 35.419                      | 248.419            | -224.103                     | 27976.                             | 0.                       | 0.                          |
| 1200.              | 35.613                      | 249.941            | -225.148                     | 29752.                             | 0.                       | 0.                          |
| 1250.              | 35.793                      | 251.399            | -226.169                     | 31537.                             | 0.                       | 0.                          |
| 1300.              | 35.960                      | 252.806            | -227.167                     | 33331.                             | 0.                       | 0.                          |
| 1350.              | 36.112                      | 254.166            | -228.142                     | 35133.                             | 0.                       | 0.                          |
| 1400.              | 36.252                      | 255.412            | -229.095                     | 36942.                             | 0.                       | 0.                          |
| 1450.              | 36.378                      | 256.716            | -230.027                     | 38757.                             | 0.                       | 0.                          |
| 1500.              | 36.492                      | 257.911            | -230.938                     | 40579.                             | 0.                       | 0.                          |
| 1550.              | 36.594                      | 259.189            | -231.830                     | 42406.                             | 0.                       | 0.                          |
| 1600.              | 36.683                      | 260.353            | -232.704                     | 44238.                             | 0.                       | 0.                          |
| 1650.              | 36.760                      | 261.483            | -233.559                     | 46075.                             | 0.                       | 0.                          |
| 1700.              | 36.826                      | 262.581            | -234.396                     | 47914.                             | 0.                       | 0.                          |
| 1750.              | 36.880                      | 263.619            | -235.217                     | 49757.                             | 0.                       | 0.                          |
| 1800.              | 36.922                      | 264.689            | -236.021                     | 51602.                             | 0.                       | 0.                          |

$O_2$  $O_2$ , ideal gas

Oxygen, ideal diatomic gas

Formula weight = 31.999 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$S^\circ = 205.033 \text{ J}/(\text{mol}\cdot\text{K})$

$\Delta H_f^\circ = 0.0 \text{ kJ/mol}$

$V^\circ = 24789.200 \pm 3.4 \text{ cm}^3/\text{mol}$

$\Delta G_f^\circ = 0.0 \text{ kJ/mol}$

Equations at Reference Pressure, 101,325 kPa (Temperature range 200 to 1800 K)

$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$

$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$

$[H^\circ(T)-H^\circ(298.15\text{K})]/(\text{J}/\text{mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$

$a_1 = 1.84663 \times 10^5$

$a_4 = -3.75052 \times 10^1$

$a_6 = 3.17977 \times 10^{-3}$

$a_2 = -6.32300 \times 10^3$

$a_5 = 3.54525 \times 10^1$

$a_7 = -1.85549 \times 10^{-6}$

$a_3 = -1.70675 \times 10^2$

Sources for Thermodynamic Properties

The thermodynamic properties for oxygen were taken from the following sources:

| <u>Property</u> | <u>Source</u>              |
|-----------------|----------------------------|
| Heat capacity   | Hultgren and others (1973) |
| Entropy         | CODATA Task Group (1978)   |

**O<sub>2</sub>Si**

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| Temperature<br>(K) | C <sub>p</sub><br>J/(mol·K) | S°<br>J/(mol·K) | (G <sub>T</sub> <sup>o</sup> -H <sub>T</sub> <sup>o</sup> ) <sub>T</sub><br>J/(mol·K) | H <sub>T</sub> <sup>o</sup> -H <sub>T'</sub> <sup>o</sup><br>J/mol | Formation from the Elements               |   |  | Formation from the Oxides                 |   |  |
|--------------------|-----------------------------|-----------------|---|--|---|---|--|---|---|--|
|                    |                             |                 |   |  | ΔH <sub>f</sub> <sup>o</sup> , e<br>J/mol | ΔG <sub>f</sub> <sup>o</sup> , e<br>J/mol | log K <sub>f</sub> <sup>o</sup> ,<br>J/mol | ΔH <sub>f</sub> <sup>o</sup> , X<br>J/mol | ΔG <sub>f</sub> <sup>o</sup> , X<br>J/mol | log K <sub>f</sub> <sup>o</sup> ,<br>J/mol |
| 273.15             | 42.184                      | 37.653          | -41.633   | -1087.   | -910565.                                  | -860875.                                  | 164.626                                    | 0.  | 0.  | 0.   |
| 298.15             | 44.748                      | 41.460          | -41.460   | 0.   | -910693.                                  | -856321.                                  | 150.024                                    | 0.  | 0.  | 0.   |
| 300.               | 44.928                      | 41.737          | -41.461   | 83.  | -910707.                                  | -855984.                                  | 149.040                                    | 0.  | 0.  | 0.   |
| 350.               | 49.357                      | 49.005          | -42.05  | 2443.  | -910859.                                  | -846449.                                  | 126.385                                    | 0.  | 0.  | 0.   |
| 400.               | 53.140                      | 55.849          | -43.329   | 5008.  | -910884.                                  | -837702.                                  | 109.393                                    | 0.  | 0.  | 0.   |
| 450.               | 56.463                      | 62.304          | -45.082   | 7750.  | -910796.                                  | -825559.                                  | 96.177                                     | 0.  | 0.  | 0.   |
| 500.               | 59.443                      | 68.410          | -47.113   | 10649.   | -910603.                                  | -819430.                                  | 85.605                                     | 0.  | 0.  | 0.   |
| 550.               | 62.160                      | 74.204          | -49.314   | 13690.   | -910329.                                  | -810325.                                  | 76.958                                     | 0.  | 0.  | 0.   |
| 600.               | 64.671                      | 79.722          | -51.620   | 16861.   | -909963.                                  | -801249.                                  | 69.755                                     | 0.  | 0.  | 0.   |
| 650.               | 67.015                      | 83.992          | -53.96  | 18054.   | -908957.                                  | -792207.                                  | 63.663                                     | 0.  | 0.  | 0.   |
| 700.               | 69.224                      | 90.040          | -56.382   | 23560.   | -908995.                                  | -783203.                                  | 58.443                                     | 0.  | 0.  | 0.   |
| 750.               | 71.320                      | 94.888          | -58.789   | 27074.   | -908398.                                  | -772338.                                  | 53.923                                     | 0.  | 0.  | 0.   |
| 800.               | 73.321                      | 99.555          | -61.192   | 30691.   | -907730.                                  | -765315.                                  | 49.370                                     | 0.  | 0.  | 0.   |
| 844.               | 75.015                      | 103.526         | -63.296   | 33954.   | -907085.                                  | -757500.                                  | 46.881                                     | 0.  | 0.  | 0.   |
| 844.               | 67.386                      | 104.430         | -63.396   | 34718.   | -906322.                                  | -757500.                                  | 46.881                                     | 0.  | 0.  | 0.   |
| 850.               | 67.446                      | 104.908         | -63.568   | 35122.   | -906226.                                  | -756442.                                  | 46.885                                     | 0.  | 0.  | 0.   |
| 900.               | 67.948                      | 108.777         | -65.392   | 38507.   | -905895.                                  | -737639.                                  | 43.392                                     | 0.  | 0.  | 0.   |
| 950.               | 68.450                      | 112.464         | -68.341   | 41917.   | -905514.                                  | -738858.                                  | 40.625                                     | 0.  | 0.  | 0.   |
| 1000.              | 68.952                      | 115.988         | -70.636   | 45352.   | -905131.                                  | -73096.                                   | 38.136                                     | 0.  | 0.  | 0.   |
| 1050.              | 69.454                      | 119.366         | -72.877   | 48812.   | -904745.                                  | -721354.                                  | 35.885                                     | 0.  | 0.  | 0.   |
| 1100.              | 69.956                      | 122.607         | -75.064   | 52297.   | -904353.                                  | -712630.                                  | 33.840                                     | 0.  | 0.  | 0.   |
| 1150.              | 70.459                      | 125.228         | -77.199   | 55808.   | -903924.                                  | -703550.                                  | 31.373                                     | 0.  | 0.  | 0.   |
| 1200.              | 70.961                      | 128.737         | -79.285   | 59343.   | -903550.                                  | -692326.                                  | 30.263                                     | 0.  | 0.  | 0.   |
| 1250.              | 71.463                      | 131.644         | -81.321   | 62904.   | -903137.                                  | -686565.                                  | 28.690                                     | 0.  | 0.  | 0.   |
| 1300.              | 71.965                      | 134.457         | -83.311   | 66490.   | -902713.                                  | -677910.                                  | 27.239                                     | 0.  | 0.  | 0.   |
| 1350.              | 72.467                      | 137.182         | -85.256   | 70100.   | -902279.                                  | -662272.                                  | 25.896                                     | 0.  | 0.  | 0.   |
| 1400.              | 72.969                      | 139.827         | -87.158   | 73736.   | -901834.                                  | -660650.                                  | 24.649                                     | 0.  | 0.  | 0.   |
| 1450.              | 73.471                      | 142.396         | -89.019   | 77397.   | -901375.                                  | -651044.                                  | 23.89                                      | 0.  | 0.  | 0.   |
| 1500.              | 73.973                      | 144.895         | -90.840   | 81083.   | -900904.                                  | -643455.                                  | 22.407                                     | 0.  | 0.  | 0.   |
| 1550.              | 74.475                      | 147.329         | -92.623   | 84795.   | -900418.                                  | -634881.                                  | 21.395                                     | 0.  | 0.  | 0.   |
| 1600.              | 74.977                      | 149.702         | -94.370   | 88531.   | -899917.                                  | -623323.                                  | 20.447                                     | 0.  | 0.  | 0.   |
| 1650.              | 75.479                      | 152.016         | -96.082   | 92292.   | -899400.                                  | -617782.                                  | 19.557                                     | 0.  | 0.  | 0.   |
| 1700.              | 75.981                      | 154.277         | -97.760   | 96079.   | -949316.                                  | -608806.                                  | 18.706                                     | 0.  | 0.  | 0.   |
| 1750.              | 76.483                      | 156.487         | -99.407   | 99890.   | -948633.                                  | -588799.                                  | 17.873                                     | 0.  | 0.  | 0.   |
| 1800.              | 76.986                      | 158.649         | -101.022  | 103727.  | -947967.                                  | -588813.                                  | 17.087                                     | 0.  | 0.  | 0.   |

O<sub>2</sub>SiSiO<sub>2</sub> (reference state)

Quartz, alpha; Quartz, beta

Formula weight = 60.085 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K (123) (quartz, alpha)

$$S^\circ = 41.460 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = -910.699 \text{ kJ/mol}$$

$$V^\circ = 22.688 \pm 0.001 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = -856.321 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p(T)/[J/(mol\cdot K)] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2 a_6 T + a_7 T^2$$

$$S^\circ(T)/[J/(mol\cdot K)] = -a_1/(2 T^2) - 2 a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2 a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2 a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

Quartz, alpha (temperature range 200 to 844 K)

$$a_1 = 0.0$$

$$a_4 = -5.29232 \times 10^2$$

$$a_6 = 1.09962 \times 10^{-2}$$

$$a_2 = 1.05800 \times 10^3$$

$$a_5 = 8.32101 \times 10^1$$

$$a_7 = 0.0$$

$$a_3 = -7.77338 \times 10^2$$

Quartz, beta (temperature range 844 to 1800 K)

$$a_1 = 0.0$$

$$a_4 = -3.00994 \times 10^2$$

$$a_6 = 5.0208 \times 10^{-3}$$

$$a_2 = -1.801085 \times 10^4$$

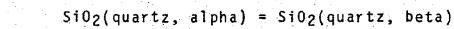
$$a_5 = 5.89107 \times 10^1$$

$$a_7 = 0.0$$

$$a_3 = 0.0$$

Critical Reaction

Inversion:



$$T_i = 844 \text{ K}$$

$$\Delta S_i^\circ = 0.904 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_i^\circ = -0.764 \text{ kJ/mol}$$

Sources for Thermodynamic Properties

The thermodynamic properties for quartz were taken from the following sources:

| Property                                | Source   |
|---|--|
| Heat capacity                           | Stull and Prophet (1971) and Chase and others (1974, 1975) |
| Entropy                                 | CODATA Task Group (1978)                                   |
| Enthalpy of formation from the elements | CODATA Task Group (1978)                                   |

The molar volume of quartz was obtained from the compilation of Robie and others (1967).

## Si

Reference state: crystals 273.15 K to 1685 K  
liquid 1685 K to 1800 K

Issued September, 1979

| Temperature<br>(K) | $C_p^o$<br>J/(mol·K) | $S^o$<br>J/(mol·K) | $(G_f^o - H_f^o)_{Tr}^o$ / $T$<br>J/mol | $H_f^o - H_{Tr}^o$<br>J/mol | Formation from the Elements |                            |                 | Formation from the Oxides   |                             |                  |
|--------------------|----------------------|--------------------|---|-----------------------------|-----------------------------|----------------------------|-----------------|-----------------------------|-----------------------------|------------------|
|                    |                      |                    |   |                             | $\Delta H_f^o, e$<br>J/mol  | $\Delta G_f^o, e$<br>J/mol | $\log K_f^o, e$ | $\Delta H_f^o, ox$<br>J/mol | $\Delta G_f^o, ox$<br>J/mol | $\log K_f^o, ox$ |
| 273.15             | 19.154               | 17.097             | -18.888                                 | -489.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 298.15             | 19.946               | 18.810             | -18.810                                 | 0.                          | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 300.               | 19.999               | 18.934             | -18.810                                 | 37.                         | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 350.               | 21.222               | 22.113             | -19.559                                 | 1069.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 400.               | 22.146               | 25.010             | -19.624                                 | 2154.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 450.               | 22.875               | 27.662             | -20.372                                 | 3280.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 500.               | 23.470               | 30.104             | -21.225                                 | 4439.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 550.               | 23.970               | 32.365             | -22.136                                 | 5626.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 600.               | 24.398               | 34.459             | -23.077                                 | 6835.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 650.               | 24.771               | 36.437             | -24.030                                 | 8055.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 700.               | 25.100               | 38.285             | -25.928                                 | 9312.                       | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 750.               | 25.394               | 40.027             | -25.928                                 | 10574.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 800.               | 25.659               | 41.675             | -26.861                                 | 11851.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 850.               | 25.901               | 43.238             | -27.779                                 | 13140.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 900.               | 26.122               | 44.724             | -28.680                                 | 14440.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 950.               | 26.517               | 46.142             | -29.562                                 | 15752.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1000.              | 26.517               | 47.498             | -30.426                                 | 17073.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1050.              | 26.693               | 48.796             | -31.269                                 | 18403.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1100.              | 26.859               | 50.041             | -32.094                                 | 19742.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1150.              | 27.015               | 51.239             | -32.901                                 | 21089.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1200.              | 27.162               | 52.322             | -33.689                                 | 22443.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1250.              | 27.302               | 53.503             | -34.459                                 | 23805.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1300.              | 27.435               | 54.577             | -35.213                                 | 25173.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1350.              | 27.561               | 55.614             | -35.949                                 | 26548.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1400.              | 27.682               | 56.619             | -36.669                                 | 27929.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1450.              | 27.797               | 57.592             | -37.374                                 | 29316.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1500.              | 27.908               | 58.537             | -38.064                                 | 30709.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1550.              | 28.015               | 59.454             | -38.739                                 | 32107.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1600.              | 28.118               | 60.345             | -39.401                                 | 33510.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1650.              | 28.217               | 61.211             | -40.048                                 | 34919.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1685.              | 28.285               | 61.804             | -40.494                                 | 35908.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1685.              | 25.522               | 91.805             | -40.494                                 | 86459.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1700.              | 25.522               | 92.031             | -40.948                                 | 86811.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1750.              | 25.522               | 92.771             | -42.418                                 | 88117.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |
| 1800.              | 25.522               | 93.490             | -43.827                                 | 89394.                      | 0.                          | 0.                         | 0.              | --                          | --                          | --               |

Si (reference state)

Silicon, crystal; Silicon, liquid

Formula weight = 28.086 g/mol

Summary of Critical DataData at Reference Temperature, 298.15 K ( $\pm 2$ s)

$$S^\circ = 18.810 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_f^\circ = 0.0 \text{ kJ/mol}$$

$$V^\circ = 12.056 \pm 0.002 \text{ cm}^3/\text{mol}$$

$$\Delta G_f^\circ = 0.0 \text{ kJ/mol}$$

Equations at Reference Pressure, 101.325 kPa

$$C_p^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = a_1/T^2 + a_3/T^{0.5} + a_5 + 2a_6 T + a_7 T^2$$

$$S^\circ(T)/[\text{J}/(\text{mol}\cdot\text{K})] = -a_1/(2T^2) - 2a_3/T^{0.5} + a_4 + a_5 \ln(T) + 2a_6 T + a_7 T^2/2$$

$$[H^\circ(T) - H^\circ(298.15\text{K})]/(\text{J/mol}) = -a_1/T + a_2 + 2a_3 T^{0.5} + a_5 T + a_6 T^2 + a_7 T^3/3$$

Silicon, crystal (temperature range 200 to 1685 K)

$$a_1 = -4.48020 \times 10^5 \quad a_4 = -4.82356 \times 10^2 \quad a_6 = 2.81373 \times 10^{-4}$$

$$a_2 = -3.83500 \times 10^3 \quad a_5 = 3.17050 \times 10^1 \quad a_7 = 0.0$$

$$a_3 = -1.77189 \times 10^2$$

Silicon, liquid (temperature range 1685 to 1800 K)

$$a_1 = 0.0 \quad a_4 = -9.78143 \times 10^1 \quad a_6 = 0.0$$

$$a_2 = -7.610 \times 10^3 \quad a_5 = 2.55224 \times 10^1 \quad a_7 = 0.0$$

$$a_3 = 0.0$$

Critical ReactionMelting:

$$T_m = 1685 \text{ K} \quad \Delta S_m^\circ = 30.001 \text{ J/(mol}\cdot\text{K)}$$

$$\Delta H_m^\circ = 50.551 \text{ kJ/mol}$$

Sources for Thermodynamic Properties

The thermodynamic properties for silicon were taken from the following sources:

| Property            | Source                     |
|---------------------|----------------------------|
| Heat capacity       | Hultgren and others (1973) |
| Entropy             | CODATA Task Group (1978)   |
| Enthalpy of melting | Hultgren and others (1973) |