



### **Abstract**

We present a three-dimensional, time-dependent simulation of a laboratory-scale rod-stabilized premixed turbulent V-flame. The simulations are performed using an adaptive time-dependent low Mach number model with detailed chemical kinetics and a mixture model for differential species diffusion. The algorithm is based on a second-order projection formulation and does not require an explicit subgrid model for turbulence or turbulence chemistry interaction. Adaptive mesh refinement is used to dynamically resolve the flame and turbulent structures. Here, we briefly discuss the numerical procedure and present detailed comparisons with experimental measurements showing that the computation is able to accurately capture the basic flame morphology and associated mean velocity field. Finally, we discuss key issues that arise in performing these types of simulations and the implications of these issues for using computation to form a bridge between turbulent flame experiments and basic combustion chemistry.

## Introduction

Premixed turbulent flames are of increasing practical importance and remain a significant research challenge in the combustion community. To investigate experimentally the interaction of turbulence with the flame front, a variety of simplified flame configurations have been studied and they can be categorized by the flame stabilization mechanism. Recent examples include studies by Sattler et al. [17] of a turbulent V-flame, Shepherd et al. [18] of a swirl-stabilized flame, Most et al. [10] of a bluff-body stabilized flame, Chen et al. [4] of Bunsen and stagnation flames, and Filatyev et al. [6] of slot Bunsen flames. Modern experimental diagnostics as well as theory (see, for example, Peters [15]) have made substantial progress in understanding basic flame physics and developing models that can be used for engineering design. However, the inability of theory to deal with the complexity of realistic chemical kinetics in a turbulent flow field, and the present limitations in experimental diagnostics to resolve 3D flame properties, represent major obstacles to continued progress.

Numerical simulation offers the potential to augment theory and experiment and overcome the limitations of standard approaches in analyzing laboratory-scale flames. The excessive computation costs of incorporating detailed transport and chemical kinetics have necessitated compromises in the fidelity or scope of simulations for premixed turbulent combustion. Simulation of laboratory-scale systems typically involves models for subgrid-scale turbulent fluctuations. Approaches based on large eddy simulation (LES) or Reynolds-averaged Navier Stokes (RANS) fall into this class. In addition to the turbulence model these approaches also require a model for the speed of flame propagation in a turbulent field or some other model for turbulence chemistry interaction.

The goal of the present work is to simulate a laboratory-scale,  $\mathcal{O}(10)$  cm flame without requiring a turbulence model, a burning velocity model or the introduction of some other type of turbulence closure hypothesis. Standard computational tools for this type of simulation are based on high-order explicit integration methods for the compressible Navier Stokes equations and are typically referred to as direct numerical simulations (DNS). The computational requirements of DNS have limited most simulations to small-scale two-dimensional models. Recent work by Vervisch et al. [23] presents the simulation of a laboratory-scale “turbulent” premixed V-flame in two dimensions and represents the current state-of-the-art in two-dimensional DNS. Tanahashi et al. [20, 21] performed compressible DNS of turbulent, premixed hydrogen flames in three dimensions with detailed hydrogen chemistry. Their simulations, performed in a domain less than 1 cm in each linear dimension, are the first three-dimensional simulations of premixed hydrogen combustion with detailed chemistry.

Low Mach number models, which analytically remove acoustic waves, provide an alternative formulation for simulation of premixed flames with detailed chemistry. The low Mach number approach was originally formulated by Rehm and Baum [16]. Najm et al. [11–13], and Bell et al. [2] have used low Mach number models for simulation of vortex flame interaction with detailed chemistry. Bell et al. [3] used an adaptive low Mach number model to simulate a turbulent premixed methane flame in three dimensions with detailed chemistry in an idealized  $\mathcal{O}(1)$  cm<sup>3</sup> domain.

In this paper, we scale up the the simulation of Bell et al. [3] to a laboratory-scale

turbulent rod-stabilized premixed methane V-flame. This simulation, which models a domain more than three orders of magnitude larger than that of any previous efforts, represents a major increment in simulation complexity, and the first simulation of a full laboratory-scale flame of this type using detailed chemistry and transport. We discuss the computational algorithm, techniques used to gather flame statistics, details of the simulation setup and grid resolution requirements for the adaptive low Mach number implementation. We then present detailed comparisons with experimental data. Although there are no explicit subgrid models in the simulation, there are a number of issues that must be addressed in performing this type of computation such as the fidelity of the chemical kinetics and transport model and characterization of boundary conditions. These issues are discussed in the context of the comparison of experiment and computation.

## Experimental Configuration and Diagnostics

A photograph of the laboratory V-flame experiment appears as an inset in Figure 1. A methane/air mixture at equivalence ratio  $\phi = 0.7$  exits a 5 cm diameter circular nozzle with a mean axial velocity of 3 m/s. Turbulence is introduced by a perforated plate mounted 9 cm upstream of the nozzle exit. The integral length scale,  $\ell_t$  of the turbulence measured by PIV (Particle Imaging Velocimetry) at the nozzle exit is approximately 3.5 mm. The fluctuation intensity is anisotropic at 7.0% and 5.5% in the axial and radial directions respectively, relative to the mean axial velocity. The flame is stabilized by a 2 mm diameter rod spanning the nozzle at its exit. The visible flame extends 15 cm or more downstream from the rod.

The PIV system consists of a double-pulse New Wave Solo PIV laser (120 mJ) at 532 nm and a Kodak/Red Lake ES 4.0 digital camera with 2048 by 2048 pixel resolution. The field of view was approximately 12 cm by 12 cm and the pixel resolution was 0.065 mm/pixel. A cyclone type particle seeder was used to seed the reactant stream with 0.4–0.6 mm (Sumitomo AKP-15)  $\text{Al}_2\text{O}_3$  particles. Data acquisition and analysis were performed on 448 image pairs using software developed by Wernet [24]. The two-pass, adaptive cross-correlation interrogation regions of  $32 \times 32$  pixels with final 50% overlapping gave a velocity field spatial resolution of approximately 1 mm.

## Computational Model

A schematic of the computational domain is shown in Figure 1. Our strategy is to characterize independently the turbulence generation in the nozzle using nonreacting simulations to provide time-dependent boundary conditions for the reacting flow simulation. The reacting component of the calculation is based on a low Mach number formulation obtained by expanding the reacting Navier-Stokes equations in powers of the Mach number (see ([8] for details). In this formalism, the pressure  $p = p_0 + \pi$  consists of a spatially uniform component,  $p_0$ , and the perturbation,  $\pi \sim p \cdot M^2$ , where  $M$  is the local Mach number. The methodology treats the fluid as a mixture of perfect gases, and uses a mixture-averaged model for differential species diffusion, ignoring

Soret, Dufour and radiation effects. To second order in the small parameter  $M$ , the low Mach number equations for flow in an unconfined domain at atmospheric pressure are given by

$$\frac{\partial \rho U}{\partial t} + \nabla \cdot \rho U U = -\nabla \pi + \nabla \cdot \tau + \rho g \hat{z}, \quad (1)$$

$$\frac{\partial \rho Y_m}{\partial t} + \nabla \cdot U \rho Y_m = \nabla \cdot \rho D_m \nabla Y_m - \dot{\omega}_m, \quad (2)$$

$$\frac{\partial \rho h}{\partial t} + \nabla \cdot U \rho h = \nabla \cdot \frac{\lambda}{c_p} \nabla h + \quad (3)$$

$$\sum_m \nabla \cdot h_m \left( \rho D_m - \frac{\lambda}{c_p} \right) \nabla Y_m,$$

where  $\rho$  is the density,  $U$  is the velocity,  $Y_m$  is the mass fraction of species  $m$ ,  $h$  is the mass-weighted enthalpy of the gas mixture,  $T$  is the temperature, and  $\dot{\omega}_m$  is the net destruction rate for specie  $m$  due to chemical reactions. Also,  $\lambda$  is the thermal conductivity,  $\tau$  is the stress tensor,  $c_p$  is the specific heat of the mixture,  $h_m(T)$  and  $D_m$  are the enthalpy and species mixture-averaged diffusion coefficients of species  $m$ , respectively, and  $g \hat{z}$  is the gravitational acceleration. These evolution equations are supplemented by an equation of state for a perfect gas mixture:

$$p_0 = \rho R_{mix} T = \rho \mathcal{R} T \sum_m \frac{Y_m}{W_m} \quad (4)$$

where  $W_m$  is the molecular weight of species  $m$ , and  $\mathcal{R}$  is the universal gas constant.

Note that the system (1-3) does not admit acoustic waves since the thermodynamic pressure field is essentially constant. Differentiating the equation of state (4) in the frame of the fluid, and using the conservation equations to replace advective derivatives, we obtain an elliptic constraint on the evolving velocity field:

$$\begin{aligned} \nabla \cdot U &= \frac{1}{\rho c_p T} \left( \nabla \cdot \lambda \nabla T + \sum_m \rho D_m \nabla Y_m \cdot \nabla h_m \right) \\ &+ \frac{1}{\rho} \sum_m \frac{W}{W_m} \nabla \cdot \rho D_m \nabla Y_m + \frac{1}{\rho} \sum_m \left( \frac{h_m(T)}{c_p T} - \frac{W}{W_m} \right) \dot{\omega}_m \end{aligned} \quad (5)$$

where  $W$  is the mean molecular weight.

The chemical kinetics are modeled using the DRM-19 subset of the GRI-Mech 1.2 methane mechanism [7]. DRM-19 is a detailed mechanism containing 20 chemical species and 84 fundamental reactions. Transport and thermodynamic properties are from the GRI-1.2 databases. Our basic discretization algorithm combines a symmetric operator-split coupling of chemistry and diffusion processes with a density-weighted approximate projection method for incorporating the velocity divergence constraint arising from the low Mach number formulation. This basic integration scheme is embedded in a parallel adaptive mesh refinement (AMR) algorithm. Our approach to adaptive refinement is based on a block-structured hierarchical grid system composed of nested rectangular grid patches. The adaptive algorithm is second-order accurate

in space and time, and discretely conserves species mass and enthalpy. The reader is referred to [5] for details of the low Mach number model and its numerical implementation and to [3] for previous applications of this methodology to the simulation of premixed turbulent flames.

## Nozzle Characterization

The experimental characterization of the turbulent fluctuations consists of measures for the integral scale length and intensity, and does not include sufficient information to completely specify the inlet flow. In order to generate realistic inlet turbulence, we performed two auxiliary nonreacting simulations. The first incorporated the curved boundary of the nozzle walls, the inlet jets and turbulence generation plate using an embedded boundary algorithm for 3D time-dependent compressible gas dynamics (see [14]). The integration procedure in this code is time-explicit and, in the present case, is severely constrained by CFL stability limits due to acoustic waves. In spite of this limitation, the solution was evolved to a statistically steady state. Statistics were then collected on the time-dependent fluctuation profiles at the nozzle exit. In the boundary layer region approximately 1.25 mm from the nozzle wall, the rms fluctuation level in the axial velocity increased to 100% over its mean value. The radial fluctuations exhibited a corresponding 80% decrease. Away from the nozzle walls, the turbulent intensities of the resulting flow matched the experimental data taken from the central region of the nozzle exit plane, including the observed anisotropy. Using this procedure to generate the time-dependent boundary data for the reacting flow simulation would require running the two codes simultaneously, and managing the coupling of the resulting datasets for the duration of the reacting flow simulation.

Alternatively, we may assume that the fluid in the nozzle is an isothermal homogeneous gas, and that the turbulence generation in the central region of the nozzle is not strongly influenced by the side walls of the nozzle. Under these conditions the flow through the nozzle may then be approximated in a Lagrangian frame using an temporal evolution of an array of perturbed jets. The diameter and spacing of the jets corresponds to those of the turbulence generation plate used in the experiment. This second model was carried out over a triply-periodic domain, 5 cm on a side using the incompressible flow algorithm discussed in [1]. The flowfield was initialized with a hexagonal array of 3.2 mm jets spaced 4.8 mm apart, and the initial velocity magnitudes were chosen so that they average over the domain to the experimentally measured mean flow rate. The simulation was performed on a  $256^3$  grid using a kinematic viscosity of  $1.6 \cdot 10^{-5}$  m<sup>2</sup>/s, corresponding to a methane-air mixture at  $\phi=0.7$  and  $T=300$  K, and the flow was evolved for 0.03 seconds (i.e., the mean residence time of the flow in the nozzle). At  $t = 0.03$  s, the integral length scale, turbulence intensity and anisotropy of the resulting simulated flow agreed with the limited experimental data measured in the central region of the exit plane. This periodic model for the nozzle flow has a distinct practical advantage over the first approach, namely, we can cycle through the fluctuation data as often as necessary. To properly reflect the presence of the nozzle wall, the periodic data was shaped using radial fits of the axial and radial fluctuations from the flowfield computed using the embedded boundary algorithm.

## Reacting Flow Simulation Setup

The computational domain for the reacting flow simulation is a cube, 12 cm on a side, with the nozzle exit centered on the lower face. The top and sides of this domain are approximated as outflow boundary conditions that express hydrostatic balance with the vertical gravitational force. The reactant stream inflow profile is formed by superimposing a top-hat velocity profile with thin boundary layers at the nozzle wall on the shaped turbulent fluctuations obtained from the nonreacting computations discussed above. The flame stabilization rod is modeled as a 2 mm wide no-flow strip at the nozzle exit with smooth increase to mean conditions away from the rod. The mean velocity is scale to match the experimental mean of 3 m/s. We specify an air coflow of 1.5 m/s into the bottom of the domain outside the nozzle to control the early-time transient vortex ring that forms between the ambient gas and the outer layer of the reactant flow downstream of the inflow. This coflow provides a relatively crude approximation to the laboratory environment of the flame. The solution in the reacting flow region is initialized with room-temperature stagnant air throughout the domain, and a small hot region just above the rod. As the flow evolves, the heated air ignites a flame near the inlet, and the flame surface propagates downstream. The initial evolution was carried out with a 2-level adaptive grid hierarchy, where a factor of two refinement from the base grid of  $96^3$  dynamically tracks regions of high vorticity and chemical activity (the flame front) until the flame is fully established. Then an additional factor of two refinement was placed at the flame surface and high vorticity regions for an effective fine-grid resolution of  $\Delta x = 312.5 \mu\text{m}$ . The refinement strategy resulted in approximately 12% of the  $1728 \text{ cm}^3$  domain being refined to the highest level. The resulting flame was evolved until it reached statistical equilibrium.

It is not feasible to fully resolve to high accuracy all of the scales of a laboratory-scale flame of the size considered here with currently available computer hardware. The relevant question, however, is whether the resolution we can obtain is sufficient to capture the interaction between the flame and turbulence as manifested in the basic flame morphology and mean velocity fields. The two significant ingredients needed to meet this requirement are that we accurately represent the burning velocity and accurately represent turbulent inflow conditions. For a premixed methane flame at a fuel equivalence ratio of  $\phi=0.7$ , the thermal thickness is approximately  $600 \mu\text{m}$ . High-resolution one-dimensional simulations using GRI-MECH 3.0 [7], the best available chemical mechanism for methane combustion, predict a laminar burning velocity of 19.00 cm/sec. In general, a numerical burning velocity is a function of not only spatial and temporal resolution but also depends on the chemical mechanism and transport properties and details of the numerical algorithm. At a spatial resolution of  $312.5 \mu\text{m}$  and a temporal resolution of  $19 \mu\text{s}$ , our methodology predicts a burning velocity based on DRM-19 of approximately 19.04 cm/sec, representing an error of  $< 0.25\%$ . We note that at this resolution, there are errors of as much as 10% in some of the details of the chemical pathways; nevertheless, the burning velocity is accurately predicted.

The other key scale that must be resolved is the inflowing turbulence. Standard estimates show that the Kolmogorov scale of the inflowing turbulent reactants is approximately  $220 \mu\text{m}$ . Although resolution of the Kolmogorov scale is often quoted as the smallest scale that needs to be resolved, Moin and Mahesh [9] note that this

requirement is probably too stringent and suggest that multiples of 4-8 are adequate to obtain good statistical matches using spectral discretizations. This suggests that the  $\Delta x = 312.5 \mu\text{m}$  needed to accurately predict the burning velocity is sufficient to resolve the inflow turbulence. To further test the resolution, we performed a limited evolution at an additional factor-of-two refinement ( $156.25 \mu\text{m}$ ). Although we were not able to run long enough at this resolution to compute reasonable statistics, the data suggested that  $\Delta x = 312.5 \mu\text{m}$  provided adequate resolution of the flow.

Once the flow reached statistical equilibrium at  $\Delta x = 312.5 \mu\text{m}$ , we evolved the flame for a total of 43.3 ms, and the analysis was based on simulation data at 0.44 ms intervals. CPU requirements depended on the refinement strategy, but the computation progressed approximately  $38 \mu\text{s}$  per hour on 256 processors of a parallel computer (IBM SP RS/6000 with 375 MHz processors). The total run, including the refinement study, generated approximately 6 TB of data for analysis. An image of the instantaneous flame surface at  $312.5 \mu\text{m}$  resolution appears in Figure 2.

## Experimental Comparisons

Whether the simulation provides an adequate representation of the flame physics depends on the adequacy of the models for chemistry, transport and thermodynamics and the characterization of the boundary conditions needed for the simulation. To evaluate the overall accuracy of the simulation, we compare the simulated results with experimental data. In particular, we consider both the flame structure and the mean velocity fields using measurements typical of those used in the analysis of the corresponding experimental data.

### Scalar Flame Structure

A number of markers for the position of the flame surface have been suggested in the combustion literature, including specific isopleths of fuel or product mass fractions, temperature or density. On the scale of the 12 cm viewing window for the experimental data and the 1 mm resolution of the PIV imaging technique, all of these measures are identical. A typical centerline slice of the methane concentration obtained from the simulation is shown on the left in Figure 3. Experimentally, the instantaneous flame location is determined using the large differences in Mie scattering intensities from the reactants and products to clearly outline the flame (Figure 3 right). Comparing the figures we see that the wrinkling of the flame in the experiment and the computation is of similar size and structure. To characterize the flame brush, which represents the mean flame location, the position of the flame fronts were obtained from 100 PIV images (such Figure 3) by an edge finding algorithm for rendering binarized images. Their average produces a map of the mean reaction progress,  $\bar{c}$ , where  $\bar{c} = 0$  in reactants, and  $\bar{c} = 1$  in the products. Contours of  $\bar{c}$  for the simulation data were computed by extracting centerline slices of the fluid density and using the same imaging processing software used to analyze the experimental data to binarize and average the computational data.



Contours of  $\bar{c}$  are depicted in Figure 4a. The data shows excellent agreement in the mean flame structure on the left and reasonably good agreement on the right. The asymmetries in the computational data suggests that the sample size is somewhat too small to obtain fully converged statistics. To characterize the flame spreading angle more precisely we averaged the left and right  $\bar{c}$  curves, and fit them to a line. The angle between those fits and the vertical is plotted in Figure 4b as a function of  $\bar{c}$ . For  $\bar{c} = 0.5$  the simulation predicts a flame angle of  $13.4^\circ$  compared to  $12.2^\circ$  for the experiment representing a 10% overestimate of the flame angle. For the central range of  $\bar{c}$ , the simulation and experiment data exhibit similar spreading trends. To provide a more detailed comparison of the flame brush growth, in Figure 4c we plot the thickness of the flame brush for the experiment and the simulation as a function of height. The data shows that computation underpredicts the growth of the flame brush thickness by approximately 25%.

Figures 5 and 6 show, respectively, the mean axial ( $\langle W \rangle$ ) and transverse ( $\langle U \rangle$ ) velocity components in a vertical plane centered on the circular nozzle for the simulation and the experiment. Below each of the color plates, horizontal cuts of the averaged data show direct comparisons between the simulated and measured data at height intervals of 20 mm. Profiles are shown only where experimentally meaningful values were available; in the outer shear layer the PIV diagnostic detects only intermittent seeding due to mixing with the unseeded laboratory air. Data from the simulation was averaged over approximately 43.3 ms. The  $\bar{c} = 0.1$  and  $\bar{c} = 0.9$  contours (dashed lines) are superimposed on the 2D images to indicate the mean flame zone location. The computed and experimental velocity data shows good qualitative agreement. The simulation captures with remarkable fidelity the major features of the experimental data, i.e. flame generated outward deflection in the unburned gases, inward flow convergence and a centerline flow acceleration in the burned gases.

A notable difference in the velocity fields is that the experimental measurements just above the nozzle exhibit a depression in axial velocity at the centerline not apparent in the simulation data, which conversely shows a localized acceleration there. In the experiment, the flow near the rod involves complex vortex shedding leading to a turbulent wake which is not represented accurately by the simplistic treatment of the rod boundary condition we have used in the computation. As a result, the simulated flame is anchored to the top of the rod, whereas in the experiment the flame is stabilized in the shear layer between the recirculation zone behind the rod and the reactant flow [19]. The rod remains at a temperature well below that of the combustion products. We speculate that this effect leads to an enhanced centerline acceleration in the simulated results relative to the experiment where the flame structure is delayed somewhat downstream. Nevertheless, the bulk of flame is entirely outside the wake so that its dynamics are determined predominantly by its interaction with the reactant flow turbulence.

Another notable difference is apparent near the top of the simulation domain, where both the  $W$  and  $U$  data show substantial deviation at the left and right edges of the plot. One possibility is that these differences arise as a result of the imposed coflow and the imposition of outflow boundary conditions. It is difficult to draw definitive conclusions here because the experimental technique for measuring velocity based on seed particles in the inflow yields poor data in regions where significant ambient air is entrained into the shear layer by turbulent mixing.

## Discussion

The discrepancies between the computation and the experiment underscore the nonnumerical issues that arise in performing these types of simulations. One issue concerns the characterization of boundary conditions. The importance of properly characterizing the inflow turbulence is obvious. Also, the flame stabilization region has not been simulated here in detail and this appears affect the growth of the flame brush close to the rod. Finally, our simple approximation of the complex rod stabilization process has generated an anomalous jet in the center of the simulated flow. While dramatic improvements are likely achievable by extending the geometrical complexity of simulation algorithm to allow modeling of the stabilization process in detail, an alternative approach would involve modifying the experiment directly in an attempt to simplify the flame stabilization mechanism itself. Initial experiments have been performed using a thin heated wire as a flame stabilizer. The results from this configuration will provide a better basis of comparison with simulations by effectively eliminating the recirculation zone and hence the need to model it. Another more subtle issue arises because the experiment we considered was an open flame in a large laboratory. It is neither possible nor desirable to simulate the entire laboratory and it is impossible to have anything but a simplistic guess of boundary conditions to represent the laboratory's effect. As with flame stabilization, the best approach to address this problem may instead be to modify the experiment so that the flame is more completely isolated from the laboratory. Thus, one element to improving the comparison between experiment and computation is to design the experiment to minimize uncertainties associated with its characterization.

The other major issue that arises in these type of simulations is the ability of the chemical kinetics and transport to accurately predict the flame properties. For the simulation presented here, we observe that in the computation, the flame angle is too large and the flame brush is too narrow. This discrepancy can potentially be attributed to numerics or boundary conditions; however, chemistry and transport are also possible causes. We have demonstrated that at the resolution discussed, we match the laminar burning velocity of the best available mechanisms for methane combustion. However, comparison with experimental data (see [22]) shows that at the lean conditions considered here, the computed burning velocity overestimates experimentally measured values by 15-20%. The observed errors in the flame angle and flame brush thickness are all consistent with a numerical burning velocity that is too high.

## Conclusion

The simulations presented here demonstrate that it is possible to simulate a laboratory scale flame in three dimensions without having to sacrifice a realistic representation of chemical and transport processes. Indeed, within the limitations imposed by the difficulties of matching the exact boundary conditions of the experiments and simulations, the predictions obtained are remarkably successful. These results indicate that further, more detailed comparisons are now appropriate. These will include such parameters as flame front curvature and the flame surface density, which is often used to quantify the combustion intensity in low Mach number premixed flames. In both cases two

dimensional comparisons between simulations and experiments are relatively straightforward but it will be possible from the simulation data to extend the investigation to three dimensions and obtain a complete description of flame front curvature and surface density, both of which are very difficult to achieve experimentally. It should be noted that the theoretical basis for the analysis of the experimental data often derives from thin-flame models and that the simulations have no such limitation. Similarly, analysis of the velocity field can go beyond comparisons with two dimensional PIV data, to obtain, within the context of a laboratory sized flow field, a detailed understanding of the interaction of the flame front with the three dimensional strain field.

The computation documented here represents a major advance in the tools available for studying reacting flow. The ability to perform these types of computations has the potential to have a substantive impact on the study of turbulent combustion. In particular, by designing experiments that are well-characterized and specifically designed as companions to such simulations, we can not only provide a much more comprehensive view of a turbulent flame; we can also establish fundamental linkages between turbulent flame experiments and basic combustion chemistry.

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## References

- [1] A. S. Almgren, J. B. Bell, P. Colella, L. H. Howell, and M. L. Welcome. *J. Comput. Phys.*, 142:1–46, May 1998.
- [2] J. B. Bell, N. J. Brown, M. S. Day, M. Frenklach, J. F. Grcar, and S. R. Tonse. *Proc. Combust. Inst.*, 28:1933–1939, 2000.
- [3] J. B. Bell, M. S. Day, and J. F. Grcar. *Proc. Combust. Inst.*, 29:1987–1993, 2002.
- [4] Y.-C. Chen, P. A. M. Kalt, R. W. Bilger, and N. Swaminathan. *Proc. Combust. Inst.*, pages 1863–1871, 2002.
- [5] M. S. Day and J. B. Bell. *Combust. Theory Modelling*, 4:535–556, 2000.
- [6] S. A. Filatyev, J. F. Driscoll, C. D. Carter, and J. M. Donbar. *Combust. Flame*, 2005. in press.

- [7] M. Frenklach, H. Wang, M. Goldenberg, G. P. Smith, D. M. Golden, C. T. Bowman, R. K. Hanson, W. C. Gardiner, and V. Lissianski. GRI-Mech—an optimized detailed chemical reaction mechanism for methane combustion. Technical Report GRI-95/0058, Gas Research Institute, 1995. [http://www.me.berkeley.edu/gri\\_mech/](http://www.me.berkeley.edu/gri_mech/).
- [8] A. Majda and J. A. Sethian. *Combust. Sci. Technol.*, 42:185–205, 1985.
- [9] P. Moin and K. Mahesh. *Annu. Rev. Fluid Mech.*, 30:539–578, 1998.
- [10] D. Most, F. Dinkelacker, and A. Leipertz. *Proc. Combust. Inst.*, 29:1801–1806, 2002.
- [11] H. N. Najm, O. M. Knio, P. H. Paul, and P. S. Wyckoff. *Combust. Sci. Technol.*, 140:369–403, 1998.
- [12] H. N. Najm, P. H. Paul, C. J. Mueller, and P. S. Wyckoff. *Combust. Flame*, 113(3):312–332, 1998.
- [13] H. N. Najm and P. S. Wyckoff. *Combust. Flame*, 110(1–2):92–112, 1997.
- [14] R. B. Pember, J. B. Bell, P. Colella, W. Y. Crutchfield, and M. W. Welcome. *J. Comp. Phys.*, 120:278–304, 1995.
- [15] N. Peters. *Turbulent Combustion*. Cambridge University Press, Cambridge, 2000.
- [16] R.G. Rehm and H.R. Baum. *N. B. S. J. Res.*, 83:297–308, 1978.
- [17] S. S. Sattler, D. A. Knaus, and F. C. Gouldin. *Proc. Combust. Inst.*, 29:1785–1795, 2002.
- [18] I. G. Shepherd, R. K. Cheng, T. Plessing, C. Kortschik, and N. Peters. *Proc. Combust. Inst.*, 29:1833–1840, 2002.
- [19] I. G. Shepherd, Hertzberg, J. R., and L. Talbot. In M. Y. Hussaini, A. Kumar, and R. G. Voigt, editors, *Major Research Topics in Combustion*. Springer-Verlag, New York, 1992.
- [20] M. Tanahashi, M. Fujimura, and T. Miyauchi. *Proc. Combust. Inst.*, 28:529–535, 2000.
- [21] M. Tanahashi, Y. Nada, Y. Ito, and T. Miyauchi. *Proc. Combust. Inst.*, 29:2041–2049, 2002.
- [22] C.M. Vagelopoulos, F.N. Egolfopoulos, and C.K. Law. *Proc. Combust. Inst.*, 25:1341, 1994.
- [23] L. Vervisch, R. Hauguel, P. Domingo, and M. Rullaud. *J. Turbulence*, 5:1–36, 2004.
- [24] M. P. Wernet. In *Proceedings of the 18th International Congress on Instrumentation for Aerospace Simulation Facilities*, 1999. Toulouse, France.

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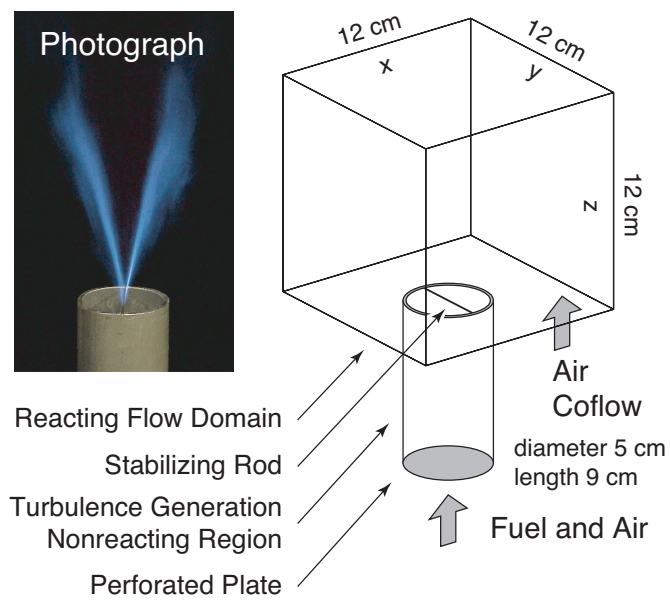


Figure 1: Schematic of the computation domain showing the division into the turbulence generation and reacting flow regions. A photograph of the laboratory experiment appears as an inset.

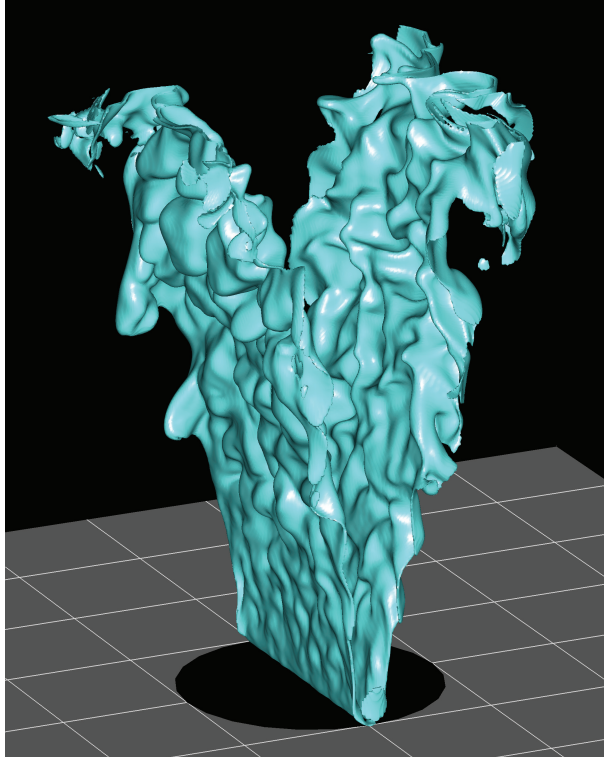


Figure 2: *Simulated instantaneous flame surface, depicted here as an isosurface of the local temperature gradient,  $\|\nabla T\| = 10^3$  (K/mm).*

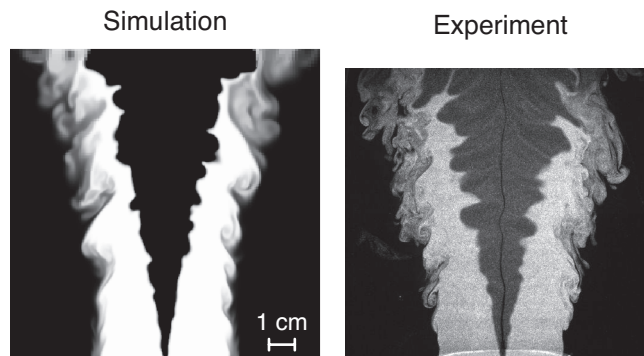


Figure 3: *Computed  $\text{CH}_4$  mole fraction and typical Mie scattering image used for PIV.*

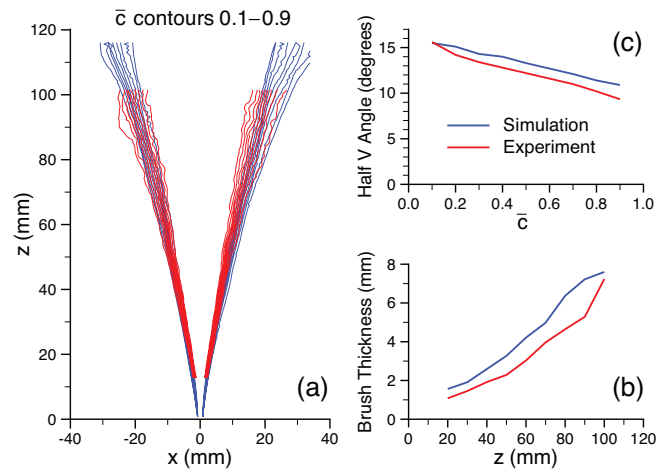


Figure 4: Comparison of  $\bar{c}$  contours: (a) spatial contours; (b) flame angle as a function of  $\bar{c}$ ; (c) flame brush thickness as a function of height. Thickness,  $\delta_t$ , is computed by fitting to  $\bar{c}$  profiles the function  $\bar{c} = 1 / (1 + \exp(-4(x - x_{0.5})/\delta_t))$  where  $x_{0.5}$  is the position of  $\bar{c} = 0.5$ .



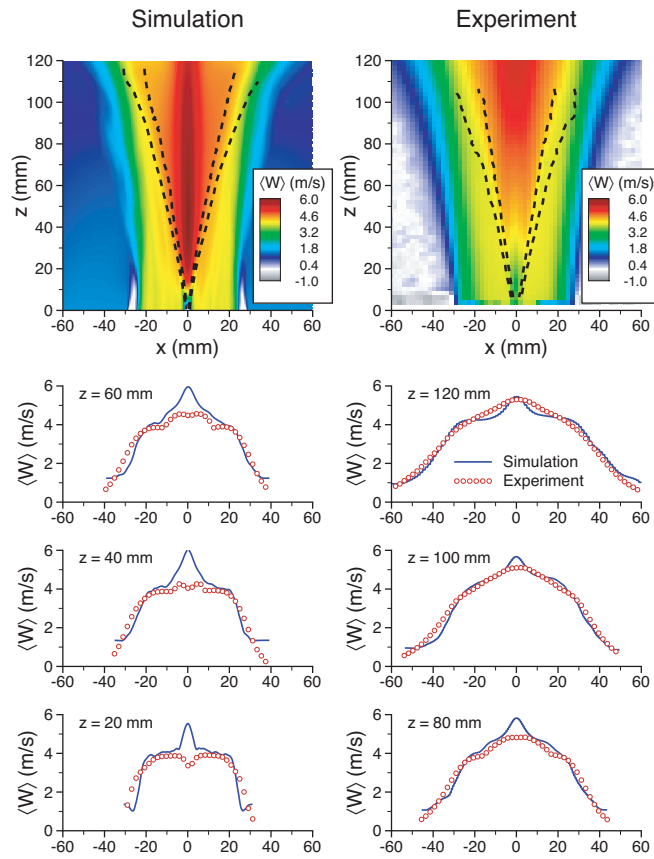


Figure 5: Mean axial velocity in the simulation and the experiment with profiles of both at 6 elevations. Regions with no signal appear speckled and are omitted from the profiles.

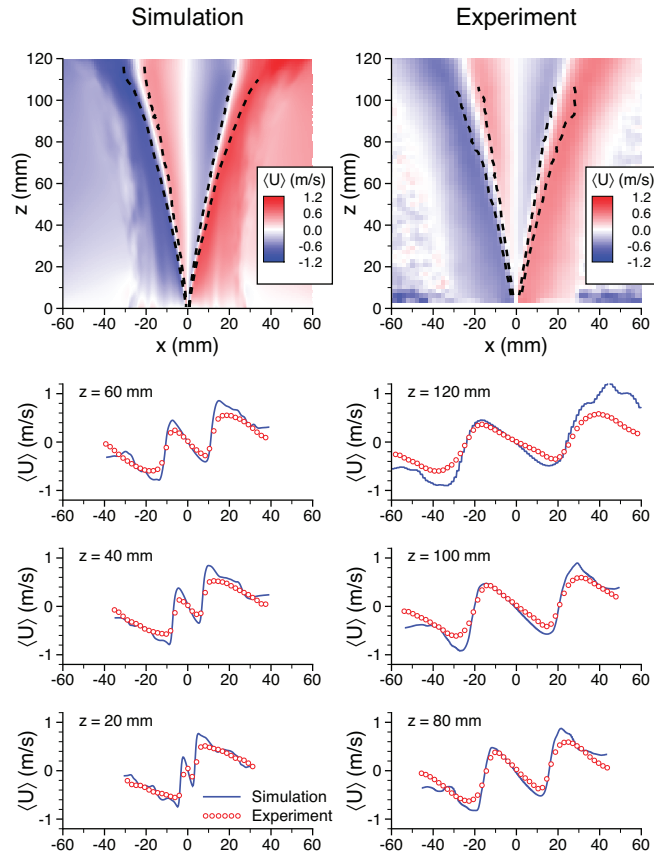


Figure 6: Mean transverse velocity in the simulation and the experiment with profiles of both at 6 elevations. Regions with no signal appear speckled and are omitted from the profiles.