KPP – A Software Environment for the Simulation of Chemical Kinetics

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Related Work

CHEMKIN (http://www.reactiondesign.com/lobby/open)

Translates symbolic chemical system in a data file that is then used by internal libraries for simulation. Gas-phase kinetics, surface kinetics, reversible equations, transport, mixing, deposition for different types of reactors, direct sensitivity analysis (Senkin). Database of reaction data, graphical postprocessor for results.

KINALC (http://www.chem.leeds.ac.uk/Combustion/kinalc.htm)

Postprocessor to CHEMKIN for sensitivity and uncertainty analysis, parameter estimation, and mechanism reduction; etc.

KINTECUS (http://www.kintecus.com)

Compiler/ chemical modeling software. Can run heterogeneous and equilibrium chemistry, generates analytical Jacobians, fit/optimize rate constants, initial concentrations, etc. from data; sensitivity analysis; Excel interface. Can use Chemkin models and databases.

CANTERA (http://rayleigh.cds.caltech.edu/~goodwin/cantera)

Object-oriented package for chemically-reacting flows. C++ kernel, STL, standard numerical libraries, Interfaces for MATLAB, Python, C++, and Fortran. Capabilities: homogeneous and heterogeneous kinetics, equilibria, reactor modeling, multicomponent transport.

LARKIN/LIMKIN (http://www.zib.de/nowak/codes/limkin_1.0/full)

Simulation of LARge systems of chemical reaktion KINetics and parameter identification. Parser generates Fortran code for function and Jacobian, or internal data arrays.

DYNAFIT (http://www.biokin.com/dynafit)

Performs nonlinear least-squares regression of chemical kinetic, enzyme kinetic, or ligand-receptor binding data using experimental data. Parses symbolic equations.

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KPP in a Nutshell

- The Kinetic PreProcessor
- <u>Purpose</u>: automatically implement building blocks for large-scale simulations
- Parses chemical mechanisms
- Generates Fortran and C code for simulation, and direct and adjoint sensitivity analysis
- Function, Jacobian, Hessian, Stoichiometric matrix, derivatives of function&Jacobian w.r.t. rate coefficients
- Treatment of sparsity
- Comprehensive library of numerical integrators
- Used in several countries by academia/research/industry
- Free! http://www.cs.vt.edu/~asandu/Software/KPP





KPP Architecture







KPP Example

#INCLUDE atoms

#DEFVAR O = O; O1D = O; O3 = O + O + O; NO = N + O; NO2 = N + O + O;

#DEFFIX O2 = O + O; M = ignore;

#EQUATIONS { Small Stratospheric }						
O2 + hv = 20	:	2.6E-10*SUN**3;				
O + O2 = O3	:	8.0E-17;				
O3 + hv = O + O2	:	6.1E-04*SUN;				
0 + 03 = 202	:	1.5E-15;				
O3 + hv = O1D + O2	:	1.0E-03*SUN**2;				
O1D + M = O + M	:	7.1E-11;				
O1D + O3 = 2O2	:	1.2E-10;				
NO + O3 = NO2 + O2	:	6.0E-15;				
NO2 + O = NO + O2	:	1.0E-11;				
NO2 + hv = NO + O	:	1.2E-02*SUN;				

SUBROUTINE FunVar (V, R, F, RCT, A_VAR) INCLUDE 'small.h' REAL*8 V(NVAR), R(NRAD), F(NFIX) REAL*8 RCT(NREACT), A_VAR(NVAR) C A - rate for each equation REAL*8 A(NREACT) C Computation of equation rates A(1) = RCT(1)*F(2)A(2) = RCT(2)*V(2)*F(2)A(3) = RCT(3)*V(3) A(4) = RCT(4)*V(2)*V(3)A(5) = RCT(5)*V(3) A(6) = RCT(6)*V(1)*F(1)A(7) = RCT(7)*V(1)*V(3)A(8) = RCT(8)*V(3)*V(4)A(9) = RCT(9)*V(2)*V(5)A(10) = RCT(10)*V(5)C Aggregate function $A_VAR(1) = A(5)-A(6)-A(7)$ $A_VAR(2) = 2*A(1)-A(2)+A(3)-A(4)+A(6)-$ &A(9)+A(10) $A_VAR(3) = A(2)-A(3)-A(4)-A(5)-A(7)-A(8)$ $A_VAR(4) = -A(8)+A(9)+A(10)$ $A_VAR(5) = A(8)-A(9)-A(10)$ RETURN END





Sparse Jacobians

IDEAS:

- Chem. interactions: sparsity pattern (off-line)
- Min. fill-in reordering
- Expand sparsity structure
- Row compressed form
- Doolitle LU factorization
- Loop-free substitution

#JACOBIAN [ON | OFF | SPARSE]

JacVar(...), JacVar_SP(...), JacVar_SP_Vec(...), JacVarTR_SP_Vec(...) KppDecomp(...) KppSolve(...), KppSolveTR(...) E.g. SAPRC-99 74+5 spc./211 react. NZ=839, NZLU=920







Computational Efficiency

Linear Algebra

(1/Lapack)	Dec	Sol	Dec+7Sol
Harwell	0.61	0.21	0.35
KPP	0.23	0.06	0.12







Sparse Hessians

E.g. SAPRC99. NZ = 848x2 (0.2%)



- 3-tensor
- sparse coordinate format
- account for symmetry

#HESSIAN [ON | OFF]

HessVar(...) HessVar_Vec(...) HessVarTR_Vec(...)





Stoichiometric Form

#STOICMAT [ON | OFF]

STOICM (column compressed) ReactantProd(...) JacVarReactantProd(...)

dFunVar_dRcoeff(...) dJacVar_dRcoeff(...)







Requirements for Numerics

- Numerical stability (stiff chemistry)
- Accuracy: medium-low (relerr~10⁻⁶-10⁻²)
- Low Computational Time
- Mass Balance
- Positivity



Stiff Integration Methods

BDF

$$\sum_{i=0}^{k} \alpha_{i}^{[n]} y^{n-i} = h_{n} \sum_{i=0}^{k} \beta_{i}^{[n]} f(y^{n-i})$$

Implicit Runge-Kutta

$$y^{n+1} = y^{n} + \sum_{j=1}^{s} b_{j} f(Y_{j}),$$
$$Y_{i} = y^{n} + \sum_{j=1}^{s} a_{i,j} f(Y_{j})$$



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Rosenbrock Methods

$$y^{n+1} = y^{n} + \sum_{j=1}^{s} m_{j} k_{j}$$

$$Y_{i} = y^{n} + \sum_{j=1}^{i-1} a_{i,j} k_{j}$$

$$\left(\frac{1}{h\gamma} I - J^{n}\right) \cdot k_{i} = f(Y_{i}) + \sum_{j=1}^{i-1} \frac{1}{h} c_{i,j} k_{j}$$

- No Newton Iterations
- Suitable for Stiff Systems
- Mass Conservative
- Efficient: Low/Med Accuracy





Direct Decoupled Sensitivity

Problem $\begin{cases} y' = f(t, y, p) & S_{\ell} = \partial y / \partial p_{\ell} \\ S_{\ell}' = J(t, y, p) \cdot S_{\ell} + f_{p_{\ell}}(t, y, p) & 1 \le \ell \le m \end{cases}$

$$I - h\gamma J = P^{T}LU \implies$$

$$I - h\gamma \mathfrak{T} = \begin{bmatrix} P^{T}L & 0 & \cdots & 0 \\ -h\gamma [(JS_{1})_{y} + J_{p_{1}}]U^{-1} & P^{T}L & \cdots & 0 \\ \vdots & 0 & \ddots & \vdots \\ -h\gamma [(JS_{m})_{y} + J_{p_{m}}]U^{-1} & 0 & \cdots & P^{T}L \end{bmatrix} \cdot \begin{bmatrix} U & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & U \end{bmatrix}$$











Adjoint Sensitivity Analysis

Problem: Stiff ODE, scalar functional.

$$y' = f(t, y), \quad t^0 \le t \le t^f, \quad \psi(y(t)) \implies \nabla_{y^0} \psi(y(t^f))$$

Continuous: Take adjoint of problem, then discretize.

$$\lambda' = -J^T(t, y) \cdot \lambda, \quad t^f \ge t \ge t^0, \quad \lambda(t^f) = (\nabla_y \psi)(y(t^f)) \implies \nabla_{y^0} \psi = \lambda(t^0)$$

Discrete: Discretize the problem, then take adjoint:

$$y^{k+1} = F^k(y^k), \quad k = 0, 1, \cdots, N-1$$

$$\lambda^k = (\nabla_y F^k)^T(y^k), \quad \lambda^N = (\nabla_y \psi)(y^N) \implies \nabla_{y^0} \psi(y^N) = \lambda^0$$

Note: In both approaches the forward solution needs to be precomputed and stored.





Linear Multistep Methods $\sum_{i=0}^{k} \alpha_{i}^{[n]} y^{n-i} = h_{n} \sum_{i=0}^{k} \beta_{i}^{[n]} f(y^{n-i})$ **Method** $\sum_{i=1}^{\kappa} \alpha_{i}^{[m]} \lambda^{m+i} = h_{m} \sum_{i=1}^{\kappa} \beta_{i}^{[m]} J^{T} \left(y^{m+i} \right) \cdot \lambda^{m+i}$ **Continuous Adjoint** $\sum_{i=0}^{\kappa} \alpha_i^{[m+i]} \lambda^{m+i} = J^T (y^m) \cdot \sum_{i=0}^{k} h_{m+i} \beta_i^{[m+i]} \lambda^{m+i}$ **Discrete Adjoint**

Consistency: ~one-leg method, in general not consistent with continuous adj. eqn. **Implementation**: with KPP





Runge Kutta Methods

Method
$$y^{n+1} = y^n + h \sum_{i=1}^s b_i f(Y^i), \quad Y^i = y^n + h \sum_{i=1}^s a_{i,j} f(Y^j)$$

Continuous Adjoint

$$\lambda^{n} = \lambda^{n+1} + h \sum_{i=1}^{s} b_{i} J^{T} \Big(y(t^{n+1} - c_{i}h) \Big) \cdot \Lambda^{i}, \quad \Lambda^{i} = \lambda^{n+1} + h \sum_{j=1}^{s} a_{i,j} J^{T} \Big(y(t^{n+1} - c_{i}h) \Big) \cdot \Lambda^{j}$$

$$Discrete Adjoint$$
(Hager, 2000)
$$\lambda^{n} = \lambda^{n+1} + \sum_{i=1}^{s} \theta^{i}, \quad \theta^{i} = h J^{T} \Big(Y^{i} \Big) \cdot \left[b_{i} \lambda^{n+1} + \sum_{j=1}^{s} a_{j,i} \theta^{j} \right]$$

Consistency (Sandu, 2003) Consider a Runge-Kutta method of order p.
 Its discrete adjoint is an order p numerical discretization of the continuous adjoint equation. (Proof: use elementary differentials of transfer fcns).
 Implementation: with KPP





Singular Perturbation

Test problem relevant for stiff systems:

$$y' = f(y, z), \quad \varepsilon z' = g(y, z), \quad t^0 \le t \le t^f$$

Distinguish between derivatives w.r.t. stiff/non-stiff variables

$$\lambda(t) = \nabla_{y(t)} \psi(y(t^f), z(t^f)), \quad \mu(t) = \nabla_{z(t)} \psi(y(t^f), z(t^f))$$

(Sandu, 2003)

 If RK with invertible coefficient matrix A and R(∞) = 0; and the cost function depends only on the non-stiff variable y
 Then μ= 0 and λ are solved with the same accuracy as the original method, within O(ε).
 A similar conclusion holds for continuous RK adjoints.





Rosenbrock Methods

Continuous
Adjoint
$$\Lambda^{i} = \lambda^{n+1} + \sum_{j=1}^{i-1} a_{i,j} z_{j}, \quad Y^{i} = y(t^{n+1} - h\alpha_{i}), \quad \lambda^{n} = \lambda^{n+1} + \sum_{j=1}^{s} m_{j} z_{j}$$

$$\begin{bmatrix} \frac{1}{h\gamma} I - (J^{n+1})^{T} \end{bmatrix} \cdot z_{i} = J^{T} (Y^{i}) \cdot \Lambda^{i} + \sum_{j=1}^{i-1} \frac{1}{h} c_{i,j} z_{j}, \quad 1 \le i \le s$$

$$\begin{bmatrix} \frac{1}{h\gamma} I - (J^{n})^{T} \end{bmatrix} \cdot u_{i} = m_{i} \lambda^{n+1} + \sum_{j=i+1}^{s} \left(a_{j,i} v_{j} + \frac{1}{h} c_{j,i} u_{j} \right)$$
Discrete
Adjoint
$$v_{i} = J^{T} (Y_{i}) \cdot u_{i} \qquad s \ge i \ge 1$$

$$\lambda^{n} = \lambda^{n+1} + \sum_{i=1}^{s} \left(H^{n} \times k_{i} \right)^{T} \cdot u_{i} + \sum_{i=1}^{s} v_{i}$$

Consistency *(Sandu, 2003)* Similar to Runge-Kutta **Implementation**: with KPP





- $T_{discrete adjoint} \le 5 T_{forward}$ (Griewank, 2000)
- KPP/Rodas-3 on SAPRC-99:

T _{cont-adj}	T _{cont-grad}	T _{discr-adj}	T _{discr-grad}
/T _{fwd}	/T _{fwd}	/T _{fwd}	/T _{fwd}
1.2	3.3	2.3	4.4





KPP Numerical Library

Simulation

Sparse: BDF (VODE, LSODES), Runge-Kutta (Radau5), Rosenbrock (Ros-{1,2,3,4},Rodas-{3,5}. QSSA. Drivers

Direct Decoupled Sensitivity

Sparse: ODESSA, Rosenbrock, I.C. and R.C.

Adjoint Sensitivity

Continuous Adj. with any simulation method Discrete Adj. Rosenbrock. Drivers.





Swedish Meteo & Hydro Inst.

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MATCH 3D transport/chemistry/deposition model





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Max Planck Institute







MISTRA-MPIC, U. Heidelberg

"Chemical reactions in the gas phase are considered in all model layers, aerosol chemistry only in layers where the relative humidity is greater than the crystallization humidity. [...] The set of chemical reactions is solved using <u>KPP</u>."

(http://www.iup.uni-heidelberg.de/institut/forschung/groups/atmosphere/modell/glasow)







User Contributions to KPP

	menu	Home	The Company	Our e
	Kppcons			
rtenum .com	<mark>z (3K)</mark> 01_06_01.pdf.gz (17	<u>0K)</u> or		

Artenum SARL ParisCyberVillage 101-103 Bld Mac Donald 75019 Paris 19ème France <u>www.artenum.com</u> (Consulting company)

Our news

Scientifc Computing News on Artenum.org

Online conference registration on Artenum.net KPP(Kinetic PreProcessor) is a software dedicated to a quick and development of computation code for numerical simulation of chemical reaction systems. Applications fields are aerosols and modeling, combustion of hydrocarbons, atmospheric chemistry, It allows the definition of large set of chemical reaction systems i types of species defined by the user. But KPP doesn't take into the mass conservation law. From a mathematical point of view, it a singular jacobian matrix, restricting the use of KPP for seeking o state using Newton-Raphson algorithm.

The **Kppcons** module and the patch vanish this singularity to seifixed points by iterative Newton-Raphson method. It is used for exainterstelar chemistry.

Kppcons is written in Ansi C and is usable for all plateforms abl KPP. it is available under GPL licence.





Example: Modeling Air Pollution









The Forward Model

Mass Balance Equations. *C* = mole fraction. ρ = air density.

$$\frac{dC_{i}}{dt} = -\vec{u} \cdot \nabla C_{i} + \frac{1}{\rho} \nabla (\rho K \cdot \nabla C_{i}) + \frac{1}{\rho} f_{i}(\rho C) + E_{i}$$

$$C_{i}(t^{0}, x) = C_{i}^{0}(x), \qquad t^{0} \leq t \leq t^{F}$$

$$C_{i}(t, x) = C_{i}^{IN}(t, x) \quad on \quad \Gamma^{IN}$$

$$K \frac{\partial C_{i}}{\partial n} = 0 \quad on \quad \Gamma^{OUT}$$

$$K \frac{\partial C_{i}}{\partial n} = V_{i}^{DEP} C_{i} - Q_{i} \quad on \quad \Gamma^{GROUND}$$





Discrete Forward Model

Operator Splitting:

- Conservative Methods for Transport
- Stiff Methods for Chemistry (KPP),
- Specific Methods for Aerosols,
- Different Time Steps.

 $C^{k+1} = N_{[t,t+\Delta t]} \circ C^k$

 $N_{[t,t+\Delta t]} = T_{HOR}^{\Delta t} \circ T_{VERT}^{\Delta t} \circ R_{CHEM}^{\Delta t} \circ T_{VERT}^{\Delta t} \circ T_{HOR}^{\Delta t}$





Chemical Data Assimilation







4D-Var Data Assimilation

$$\min \psi(p) = \frac{1}{2} \sum_{k=1}^{N} \left(H^{k} y^{k} - o^{k} \right)^{T} R_{k}^{-1} \left(H^{k} y^{k} - o^{k} \right) + \frac{1}{2} \left(p - p^{b} \right)^{T} B^{-1} \left(p - p^{b} \right)$$

(Note: Need the gradient of J)





Continuous Adjoint Model

$$\begin{aligned} \frac{d\lambda_i}{dt} &= -\nabla \cdot \left(\vec{u}\lambda_i \right) - \nabla \cdot \left(\rho K \cdot \nabla \frac{\lambda_i}{\rho} \right) - \left(F^T (\rho C) \cdot \lambda \right)_i - \phi_i \\ \lambda_i \left(t^F, x \right) &= \lambda_i^F (x), \qquad t^F \ge t \ge t^o \\ \lambda_i (t, x) &= 0 \quad on \quad \Gamma^{IN} \\ \vec{u}\lambda_i + \rho K \frac{\partial (\lambda_i / \rho)}{\partial n} &= 0 \quad on \quad \Gamma^{OUT} \\ \rho K \frac{\partial (\lambda_i / \rho)}{\partial n} &= V_i^{DEP} \lambda_i \quad on \quad \Gamma^{GROUND} \end{aligned}$$

Note: Linearized chemistry generated by KPP.





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Discrete Adjoint Model

Operator Split Tangent Linear and Adjoint Discrete Models

$$\begin{split} \delta C^{k+1} &= N'_{[t,t+\Delta t]} \circ \delta C^{k} \\ N'_{[t,t+\Delta t]} &= \left(T^{\Delta t}_{HOR}\right)' \circ \left(T^{\Delta t}_{VERT}\right)' \circ \left(R^{\Delta t}_{CHEM}\right)' \circ \left(T^{\Delta t}_{VERT}\right)' \circ \left(T^{\Delta t}_{HOR}\right)' \\ \lambda^{k} &= N^{'*}_{[t,t+\Delta t]} \circ \lambda^{k+1} \\ N^{'*}_{[t,t+\Delta t]} &= \left(T^{\Delta t}_{HOR}\right)'^{*} \circ \left(T^{\Delta t}_{VERT}\right)'^{*} \circ \left(R^{\Delta t}_{CHEM}\right)'^{*} \circ \left(T^{\Delta t}_{VERT}\right)'^{*} \circ \left(T^{\Delta t}_{HOR}\right)'^{*} \end{split}$$

Note: Chemical Model Discrete/Continuous Adjoints automatically generated by KPP





Adjoint STEM-III



- Measurement info used to adjust initial fields and improve predictions;
- East Asia. Grid: 80 x 80Km. Time: [0,6] GMT, 03/01/01.
- SAPRC 99 (Ros-2); 3rd order upwind FD; LBFGS;
- Parallelization with PAQMSG
- Distributed Level-2 Checkpointing Scheme





NASA Trace-P Experiment

Nominal Flight Tracks for the NASA Aircraft During the TRACE-P Mission



- Transport and Chemical Evolution over the Pacific
- ➤March-April 2001
- ➢Quantify Asian transport
- Understand chemistry over West Pacific



Computational Setting



Model Size ~ 8,000,000 variables

Computational domain:

- Area: 7.200 x 4.800 km
- Horizontal grid: 80 x 80 Km
- Vertical grid: 18 layers,10 km.







Trace-P Simulation 00:00:00 2001070 1 of 72 Sunday March 01-04, 2001 O_3 NO_2 SO_2 H3E.58 154.366 Vis5D





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Model vs. Observations



- Cost functional = model-observation gap.
- The analysis produces an optimal state of the atmosphere using:
 - Model information consistent with physics/chemistry
 - Measurement information consistent with reality



More Observations

NO: Observation vs. Model

SO₂: Observation vs. Model







Target: O₃ at Cheju Island

55N









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Areas of Influence

>Ψ = Ozone at Cheju, 0GMT, 03/04/2001
 >Influence areas (adjoint isosurfaces) depend on meteo, but cannot be determined solely by them (nonlinear chemistry).
 >Boundary condition uncertainties 3 days before.







Flights on March 07, 2001







Assimilation of DC-8 O₃







Assimilation of P3-B O₃

O₃ along DC-8 flight

Control = Initial O_3 Assim. Window [0,12] GMT

O₃ along P3-B flight





Assimilation of Multiple Species

P3-B Obs: O₃(8%); NO, NO₂(20%); HNO₃, PAN, RNO₃(100%)





Sensitivity Analysis

 $\psi = NO_Y$ (P3-B) Averaged gradients help with choice of control variables





Assimilation of DC-8 CO

<u>Control:</u> Initial CO Conc.

<u>Control:</u> <u>Initial Conc. of 50 spc</u>.

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Assimilation of DC-8 CO



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Different Control Sets

Observed: NO_Y (P3-B)

 $NO_{Y} = NO + NO_{2} + NO_{3} + 2*N_{2}O_{5} + HONO + HNO_{3} + HNO_{4} + RNO_{3} + PAN + PAN_{2} + PBZN + MA_PAN$









Conclusions

- KPP software tool for the simulation of chemical kinetics
- Code generation
- > Useful (and widely used!) to build blocks for large-scale simulations
- Examples of chemical data assimilation which allows enhanced chemical weather forecasts





Quote of the Day

"Persons pretending to forecast the future shall be considered disorderly under subdivision 3, section 901 of the criminal code and liable to a fine of \$250 and/or 6 months in prison."

Section 889, New York State Code of Criminal Procedure (after M.D. Webster)













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