

Multilayer Laue Lenses: a Path towards Nanofocusing of Hard X-rays

National Synchrotron Light Source

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Jörg Maser

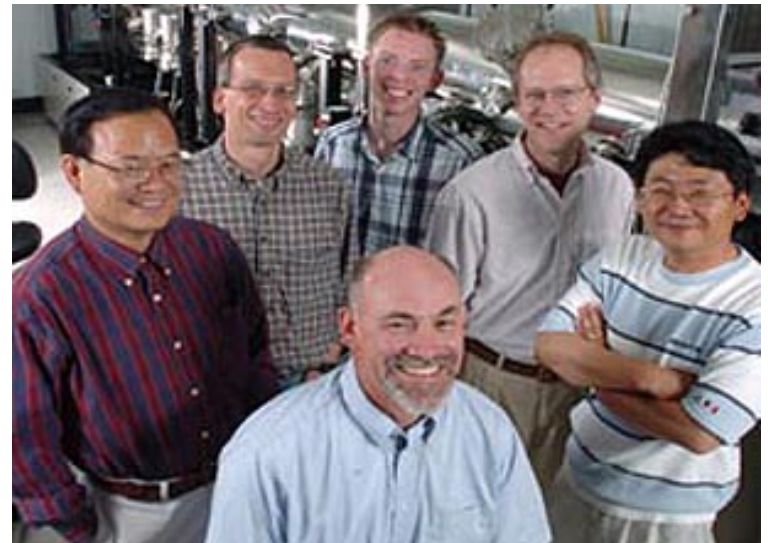
X-ray Science Division
Center for Nanoscale Materials
Argonne National Laboratory



*Argonne National Laboratory is managed by
The University of Chicago for the U.S. Department of Energy*

Collaborators

- Hyon Chol Kang: X-ray characterization of MLL; Polishing of MLL
- Brian Stephenson: X-ray characterization of MLL
- Al Macrander, Chian Liu, Ray Conley: Deposition of MLL
- Stefan Vogt, Fourier Optics
- Hanfei Yan



Outline

- I) Introduction: Why do we care about focusing of X-rays?
- II) Properties of X-ray optics - Overview
- III) Nanometer Focusing of X-rays - Volume Diffractive Optics
- IV) Technical Approach to Nanofocusing - Multilayer Laue Lenses
- V) Summary/Outlook: where does the MLL approach lead? How does the ultimate x-ray optic look?
- VI) Acknowledgments

Thrust: Towards Ultimate Resolution Limits for X-rays

1) Why do we care about X-ray Focusing?

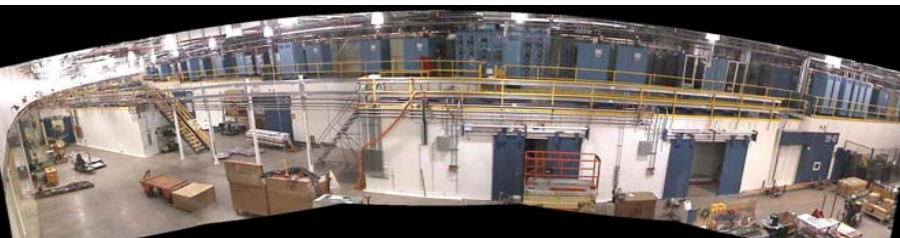
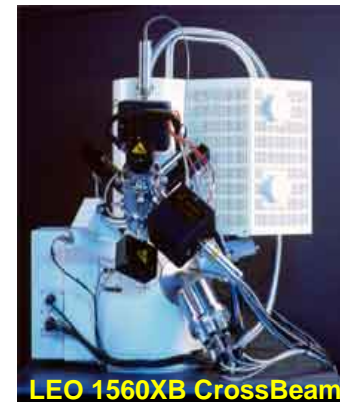
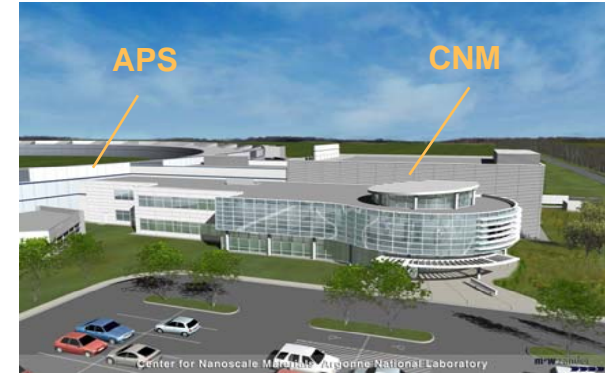
Argonne's Center for Nanoscale Materials

■ Mission:

- “Explore and develop new approaches to fabrication, characterization and understanding of nanoscale confined materials with new properties”

■ Major fabrication/characterization tools:

- E-beam lithography (25 kV, 100 kV systems)
- FIB/SEM
- Near-Field Scanning Optical Microscope
- Hard X-ray Nanoprobe Beamline (30 nm initial resolution, instrument design for < 10 nm)



Nanoprobe Beamline Layout:

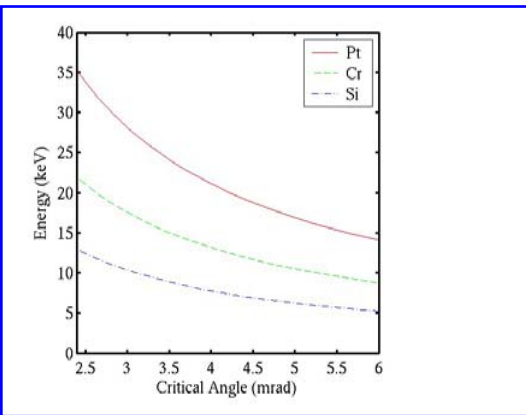
Double mirror system:

M1a: fully illuminated, horizontally bent

M1b: flat

PD = 0.5 - 4 W/mm²

P_{tot} = 70 - 730 W



Twin undulators:

PD = 905 W/mm² @ 25.5 m

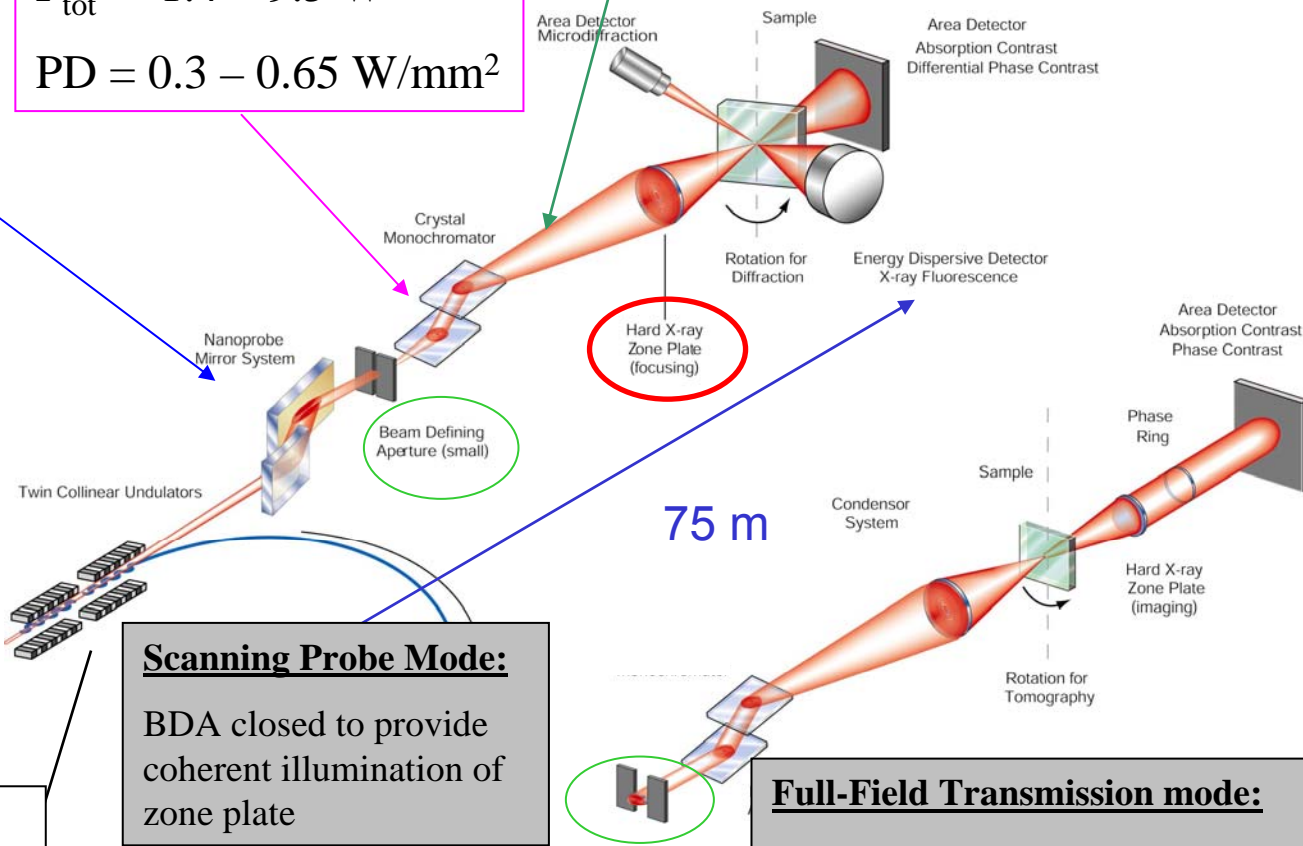
P_{tot} = 20.7 W @ I = 180 mA

Crystal monochromator

P_{tot} = 1.4 - 9.5 W

PD = 0.3 - 0.65 W/mm²

Polarizer, beam chopper



Scanning Probe Mode:

BDA closed to provide coherent illumination of zone plate

Full-Field Transmission mode:

BDA open to provide coherent illumination of zone plate

II) What we would like from High-Resolution X-ray Optics

■ Requirements:

- Highest spatial resolution
 - Ideally: *wavelength limited* (1 \AA) $NA \rightarrow 1$.
- High focusing/imaging efficiency
 - Ideally *100%*
- Large acceptance (focusing: accept full coherent fraction of beam)
- Full-field imaging capability
 - Example: *500 x 500 pixels*

■ Desired:

- Energy tunability
- Broad bandpass
- (Easy alignment)

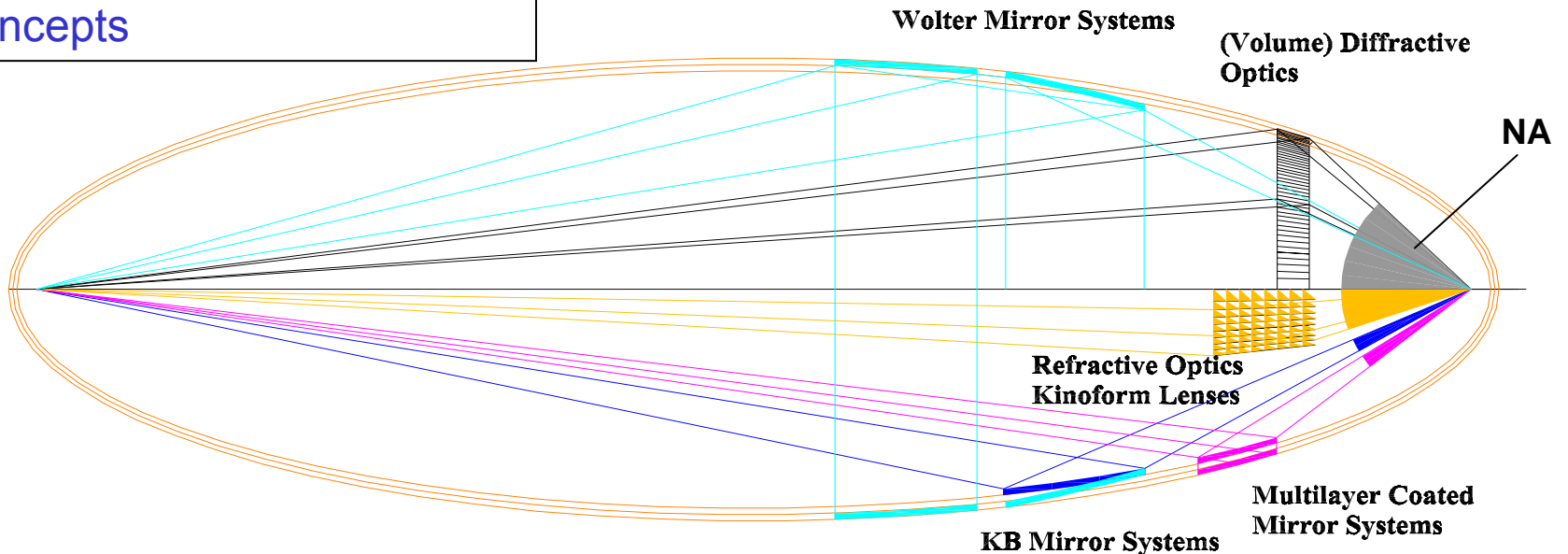
Far-Field Focusing of X-rays – Conceptual Approaches

Interaction of x-rays with matter:

$$n = 1 - \delta - i\beta, \quad 0 < \delta, \beta \ll 1 \quad (\delta \sim 10^{-5}, \beta \sim 10^{-6}, W, 20 \text{ keV})$$

- $\delta > 0 \rightarrow$ Total external reflection for $\theta < \theta_c$
- $\beta > 0$: Absorption
- $\delta \ll 1$ Weak interaction \rightarrow Good focusing efficiency challenging for high numerical aperture

Far-field Focusing/Imaging Concepts



Properties of Far-Field X-ray Optics

X-ray optic	Diffractive Optics	Reflective Optics	Refractive Optics
Numerical aperture	<ul style="list-style-type: none"> • High NA possible Limits: Volume diffraction? Fabrication	<ul style="list-style-type: none"> • Limited NA (θ_c) – KB: $NA \cong \frac{1}{2} (2 \cdot \theta_c)$ – Wolter: $NA \cong 4 \theta_c$ – Multilayer: $NA \sim m \cdot \theta_c$ 	<ul style="list-style-type: none"> • Limited aperture: $\beta > 0 \rightarrow D_{eff} < D$
Resolution limit	< 1 nm?	<ul style="list-style-type: none"> – KB: $\sim 16 \text{ nm}/m$ – Wolter: $\sim 3 \text{ nm}/m$ 	CRL: $\sim 20 \text{ nm}$ A-CRL: $\beta = 0$: $\sim 2 \text{ nm}$ \rightarrow Fresnel lens: CFL?
Efficiency	20% - 30% (60%-80%)	70% - 90%	20% - 30%
Chromaticity	$f \sim 1/\lambda$	Non-chromatic ($m = 1$)	$f \sim 1/\lambda^2$
Field of view	Y ($\delta > 10 \text{ nm}$) N ($\delta \ll 10 \text{ nm}$)	<ul style="list-style-type: none"> • Kirkpatrick/Baez: N • Wolter: Y 	Y
Other	<ul style="list-style-type: none"> • Monochromatic beam • On-axis geometry • Any x-ray energy 	<ul style="list-style-type: none"> • White (pink) beam (non-ML) • Grazing inc. geometry. • Any x-ray energy • KB: working distance! 	<ul style="list-style-type: none"> • Monochromatic beam • On-axis geometry • Limited energy range • Long lenses
Limitations	<ul style="list-style-type: none"> • (High aspect ratio/tilt) • Positioning/alignment 	<ul style="list-style-type: none"> • Figure errors 	<ul style="list-style-type: none"> • Small working distance at high resolution

X-ray Focusing and Imaging – Current State of the Art

■ State of the art in x-ray imaging and focusing (2D focus):

- Refractive Optics: $\delta \sim 50 \text{ nm}$ ($E = 21 \text{ keV}$) (*Schroer, APL, 2005*)
- Reflective Optics: $\delta \sim 40 \text{ nm}$ ($E \sim 15 \text{ keV}$) (*Mimura, JJAP 2005*)
- Diffractive Optics: $\delta \sim 15 \text{ nm}$, ($E = 0.8 \text{ keV}$) (*Chao, Nature, 2005*)

■ Spatial Resolution limit of optics: $\delta = c \cdot \lambda / \text{NA}$, $c = 0.5 \text{ (1D)} - 0.6 \text{ (2D)}$

- $\text{NA} = 1 \rightarrow \delta \approx \lambda$ ($\lambda = 0.6 \text{ \AA}$, $E = 20 \text{ keV}$)

■ What is the ultimate resolution limit for x-ray focusing?

- Diffractive optics: $\sim 1 \text{ nm}$ (*Kang, 2006*); \AA feasible?
- Reflective Optics: $\sim 16 \text{ nm}$ (KB). 3 nm (Wolter) (non-ML)
- Refractive Optics: $\sim 2 \text{ nm}$ ($\beta = 0$, *Schroer, 2005*)

III) Nanometer focusing using Diffractive Optics:

→ Volume Diffractive Optics

Section III: What is the physics of volume diffraction?

- Change of d-spacing
- Weak interaction: t large ($t > \text{DOF}$ for high NA)
- Dynamic Effects

- Energy tunability
- Full-field imaging

Section IV: How to fabricate volume diffractive optics with large NA?

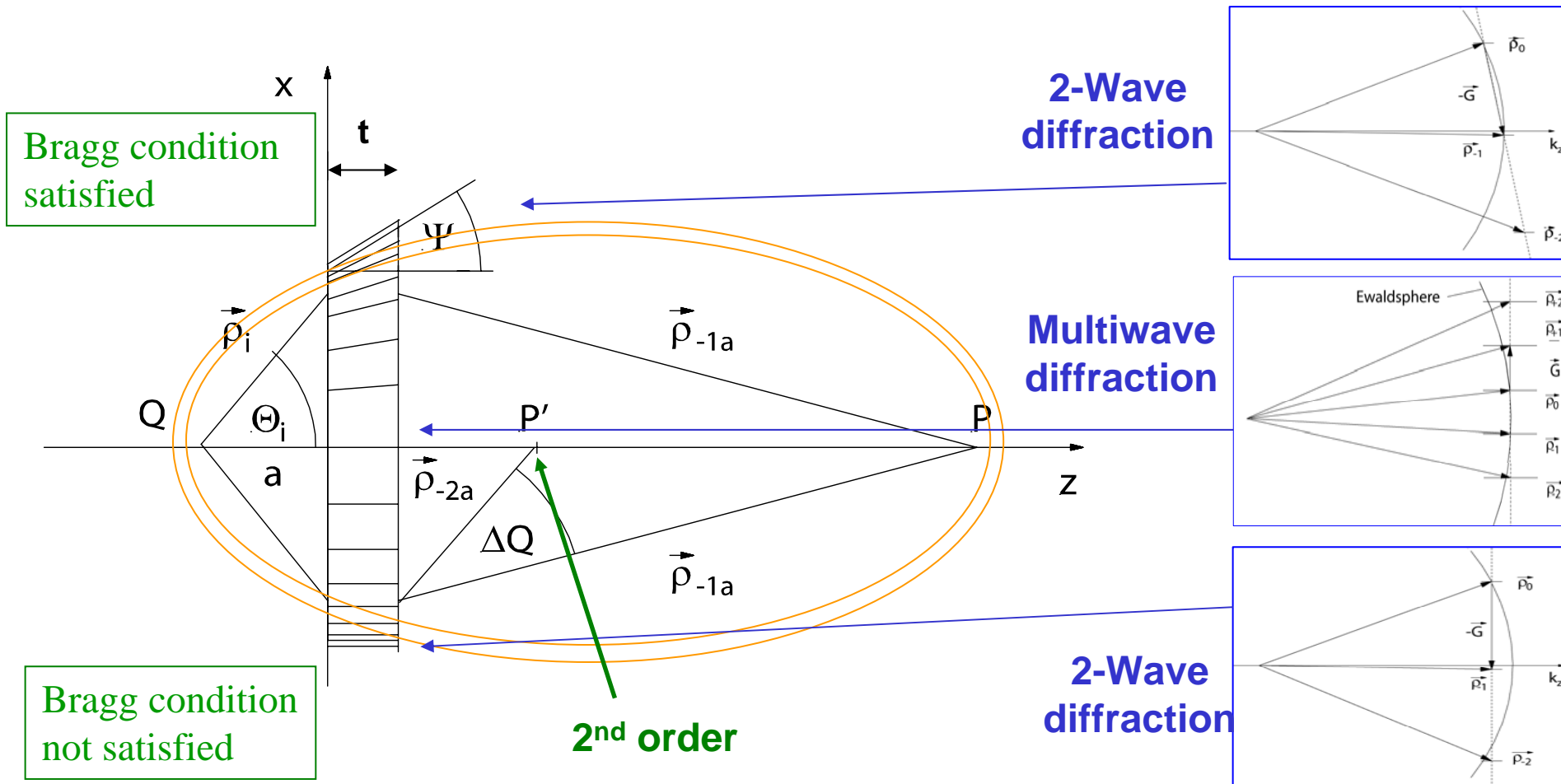
→ Multilayer Laue Lens

How does the “ideal” Diffractive Optic look like?

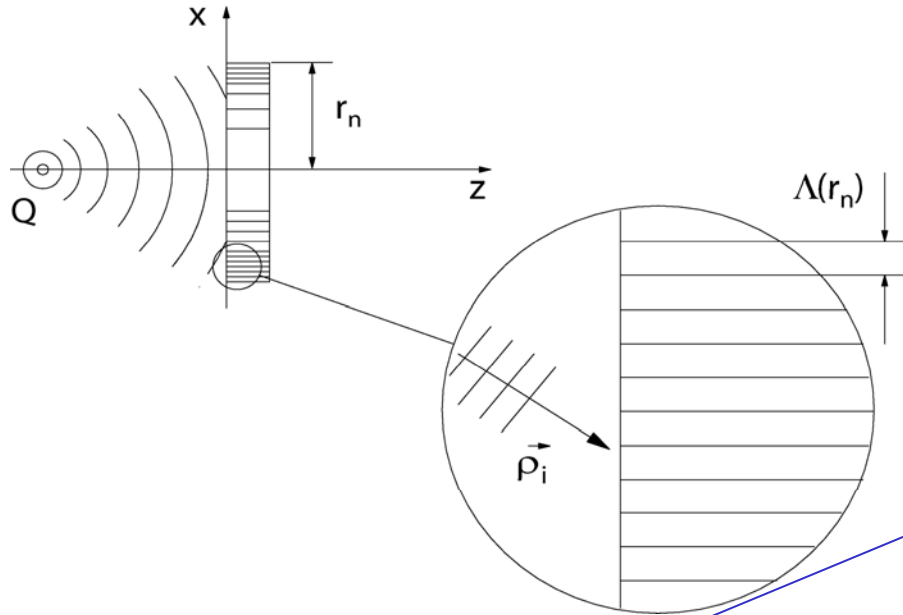
→ Volume Diffractive Optics (VDO)

Large Aspect ratio: $t/dr_n = 15,000$ (WSi₂-Si, 20 keV, $t = 15 \mu\text{m}$, $dr_n = 1 \text{ nm}$)

A “ray” interacts with **420 zones** \Rightarrow Dynamic diffraction theory



Theoretical Description of Diffraction by VDO:



1) Dynamic Diffraction Theory (N-wave CWT):

- i) Decompose ZP into “locally 1D gratings”
- ii) Calculate complex amplitude $A(r_n, z)$ at rear interface of ZP (e.g. N-wave Coupled Wave Theory)
- iii) Reconstruct wavefront on exit pupil

2) Fourier Optics

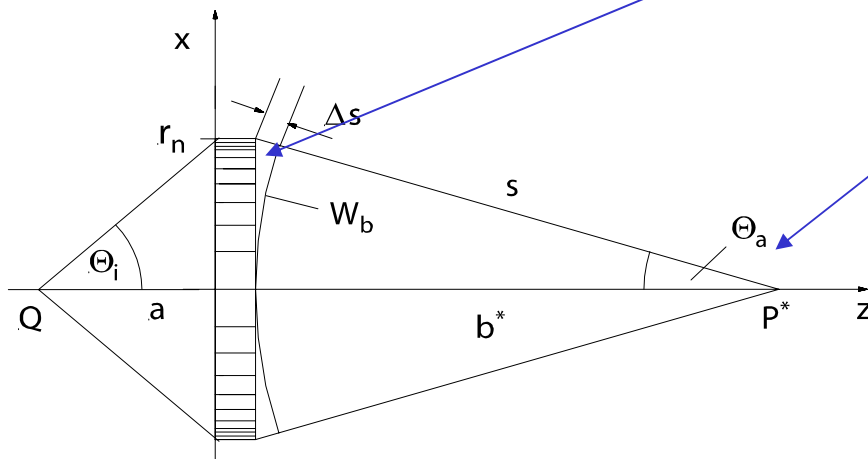
Calculate PSF, MTF

Current limitations of approach

$$t \ll f:$$

20 keV, $D = 20 \mu\text{m}$, $dr_N = 1 \text{ nm}$:
 $t = 13.5 \mu\text{m}$, $f = 0.5 \text{ mm}$, $t/f \approx 0.03$

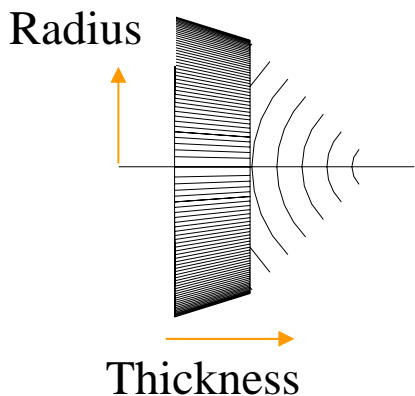
Borrmann effect? Straight zones?



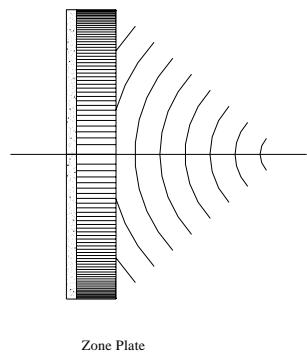
Diffraction Properties of VDO: Local Diffraction Efficiency

$r_N = 15 \text{ } \mu\text{m}$
 $\text{WSi}_2\text{-Si}$
 $E = 19.5 \text{ keV}$

**Ideal
Volume
Optics**



**“Flat”
Volume
Optics**



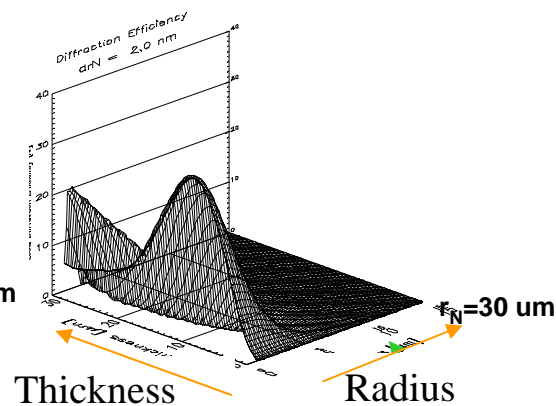
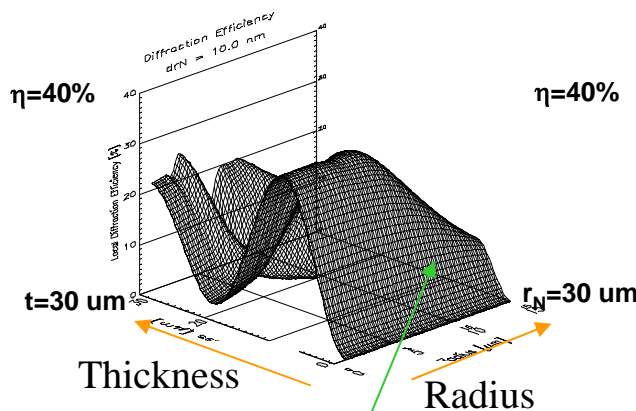
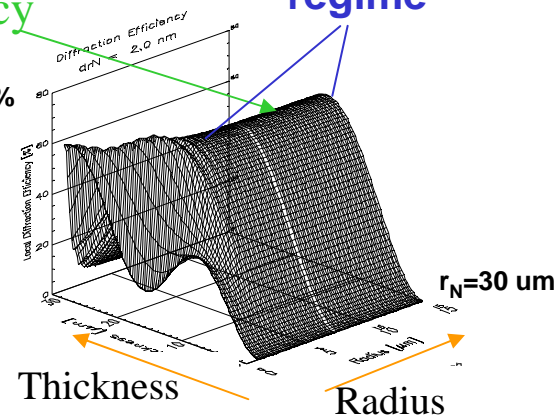
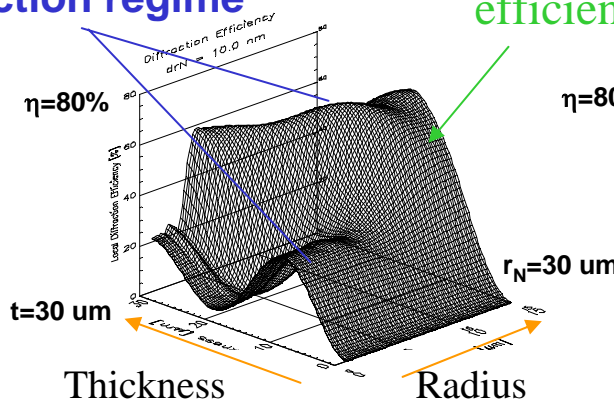
$dr_N = 10 \text{ nm}$

$dr_N = 2 \text{ nm}$

**Multiwave
diffraction regime**

**Increased
efficiency**

**2-Wave diffraction
regime**

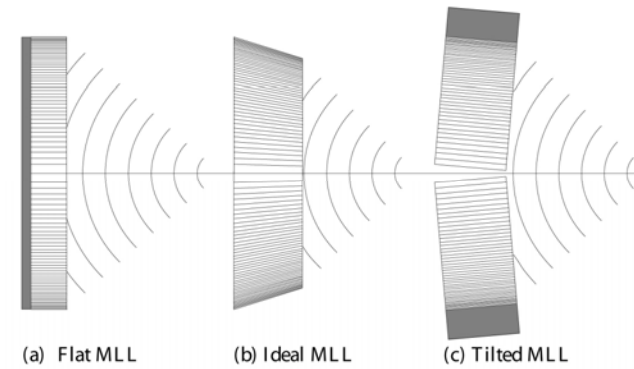
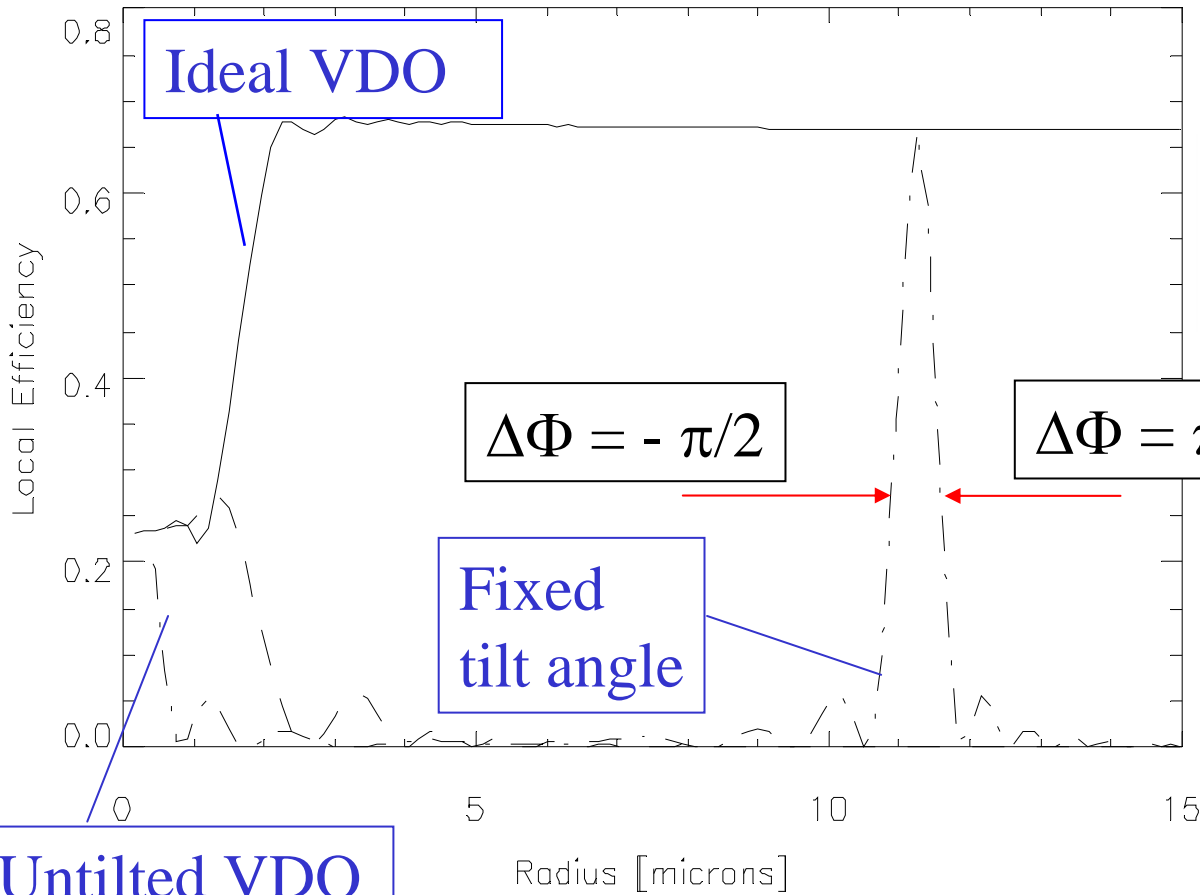


Reduced efficiency

“No” efficiency

What about the phase?

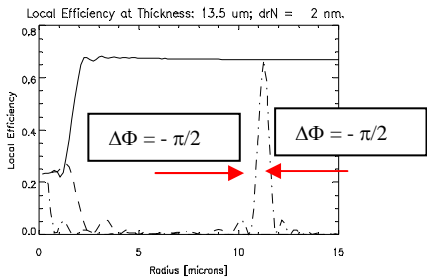
Local Efficiency at Thickness: 13.5 μm; drN = 2 nm



→ Phase changes on the order of π over small range of the aperture

Phase Effects in Volume Diffractive Optics: Local Phase Shift

$r_N = 15 \text{ } \mu\text{m}$
 $\text{WSi}_2\text{-Si}$
 $E = 19.5 \text{ keV}$



$dr_N = 10 \text{ nm}$

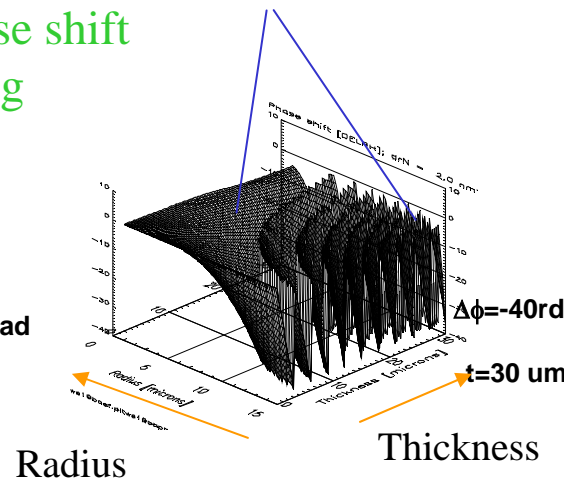
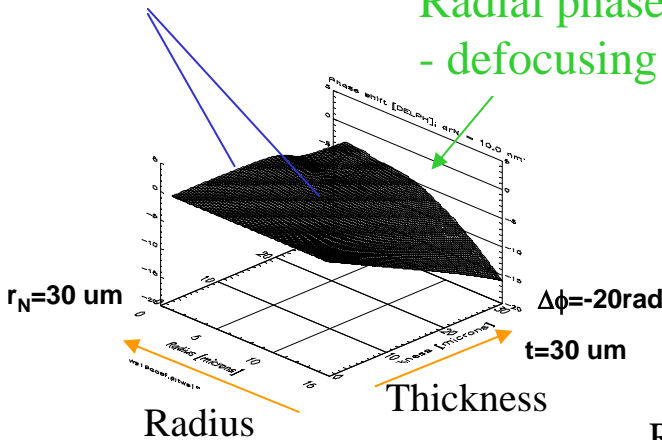
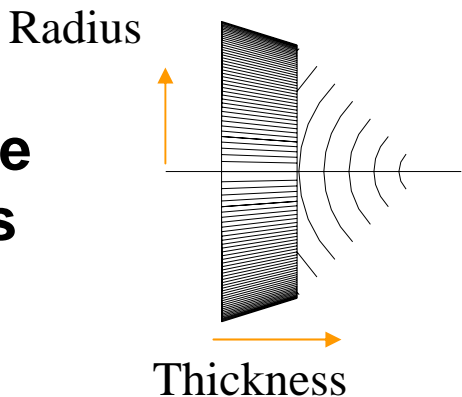
$dr_N = 2 \text{ nm}$

**Multiwave
diffraction regime**

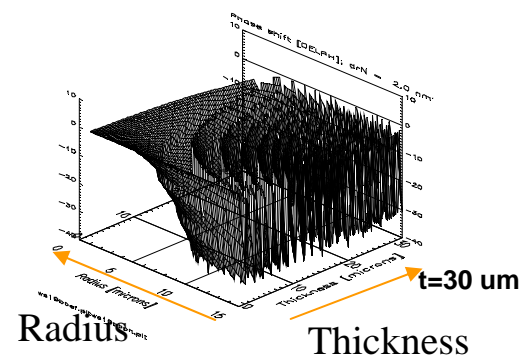
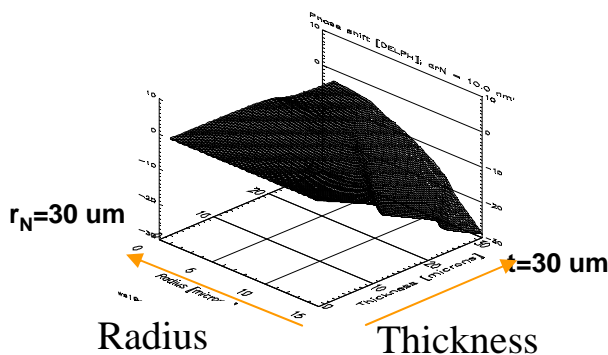
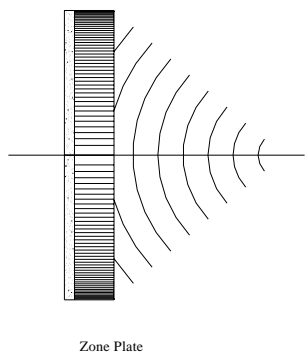
**2-Wave diffraction
regime**

Radial phase shift
- defocusing

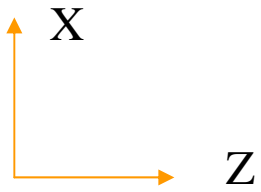
**Ideal
Volume
Optics**



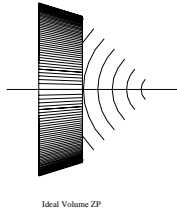
**“Flat”
Volume
Optics**



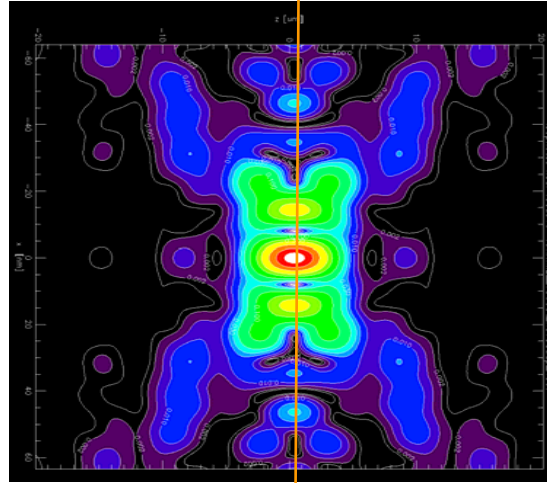
Focusing properties of VDO



**Ideal
Volume
Optics**

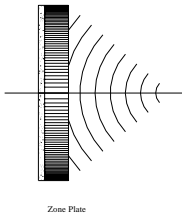


$dr_N = 10 \text{ nm}, t = 15 \mu\text{m}$

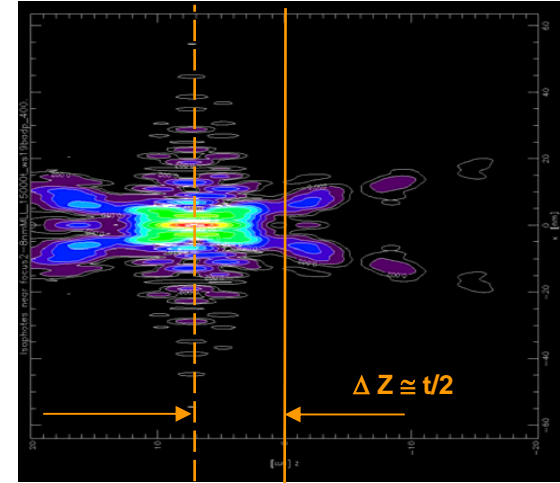


Thin-lens Focal plane

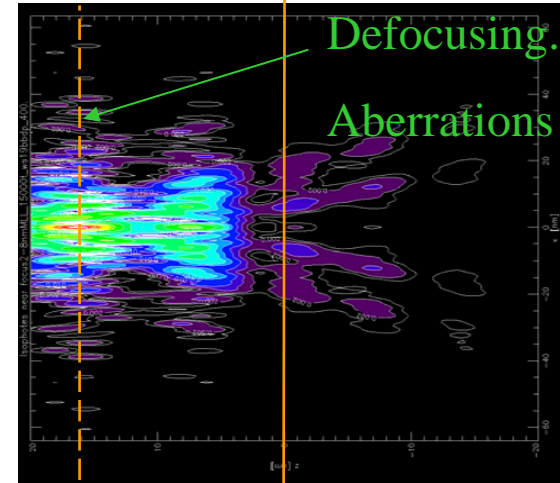
**Flat
Volume
Optics**



$dr_N = 2 \text{ nm}, t = 15 \mu\text{m}$



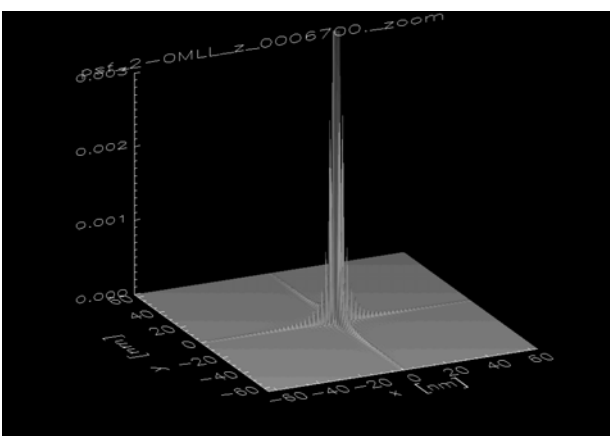
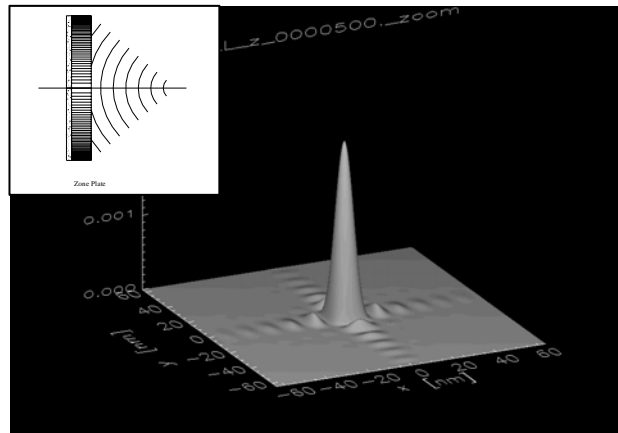
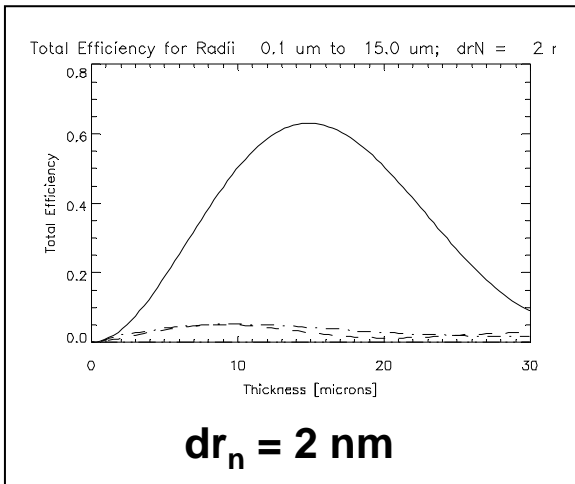
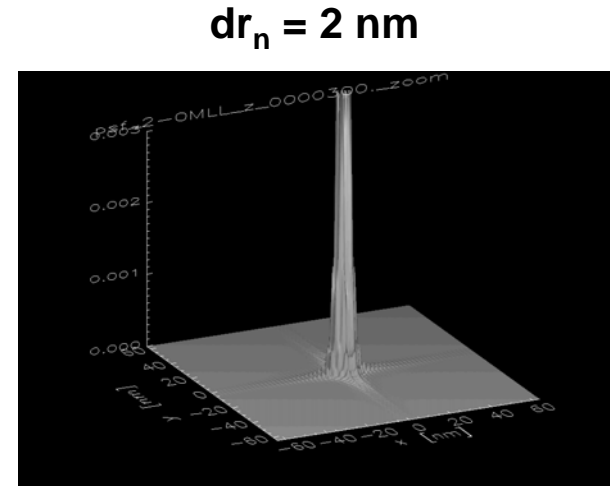
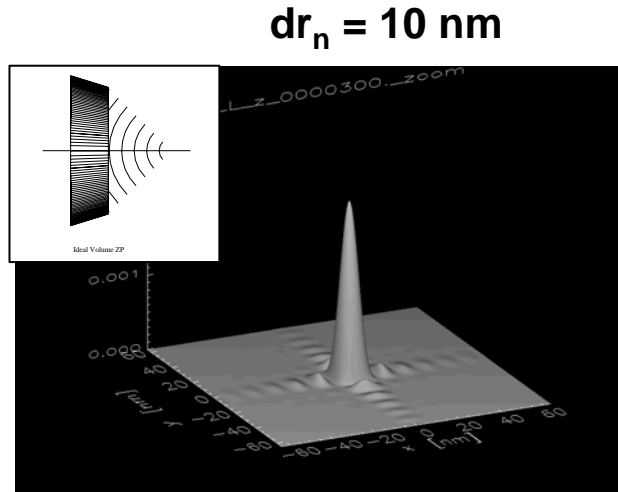
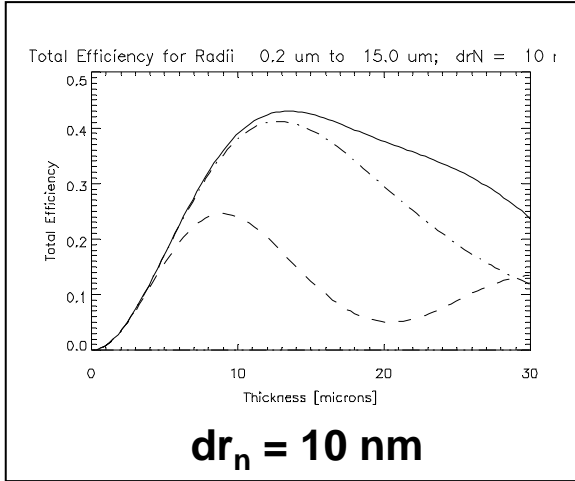
Plane of best focus



Thin-lens Focal plane

Focusing properties – PSF near focal plane

WSi₂-Si, E = 19.5 keV



Total Diffraction Efficiency

Point spread function of 2D MLL, full aperture utilized

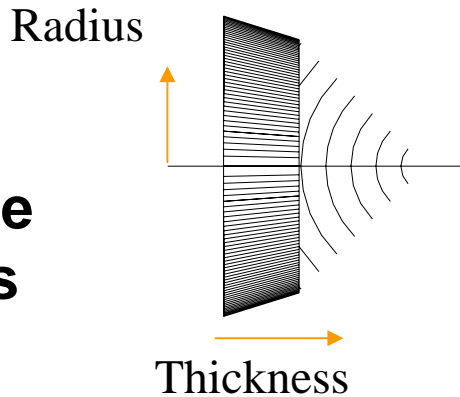
Energy Tunability of VDO

Slanting angle ψ_B : VDO optimized for energy E_0 , $2d \sin \theta_B = hc/E_0$

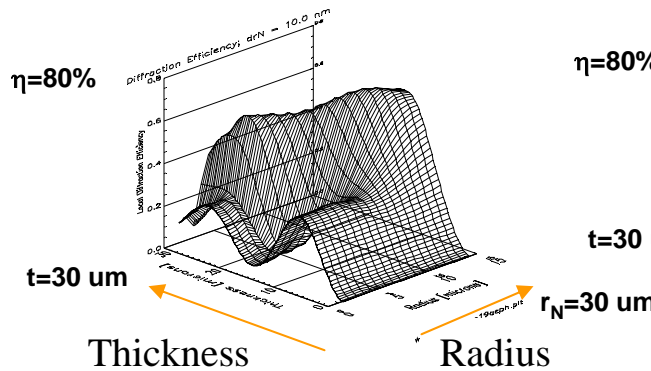
Use at different energy E' leads to deviations from the Bragg condition

$r_N = 15 \text{ um}$
 $\text{WSi}_2\text{-Si}$
 $E = 19.5 \text{ keV}$

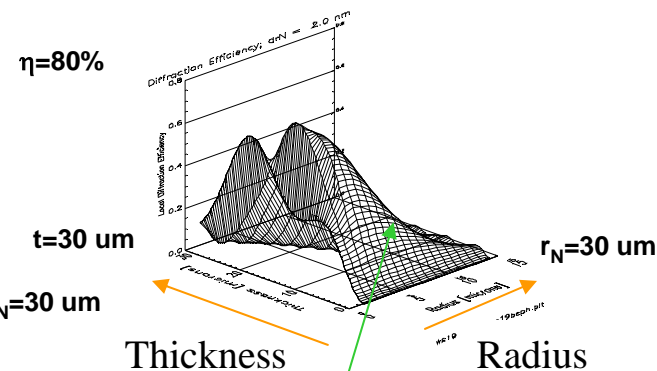
**Ideal
Volume
Optics**



$dr_N = 10 \text{ nm}$



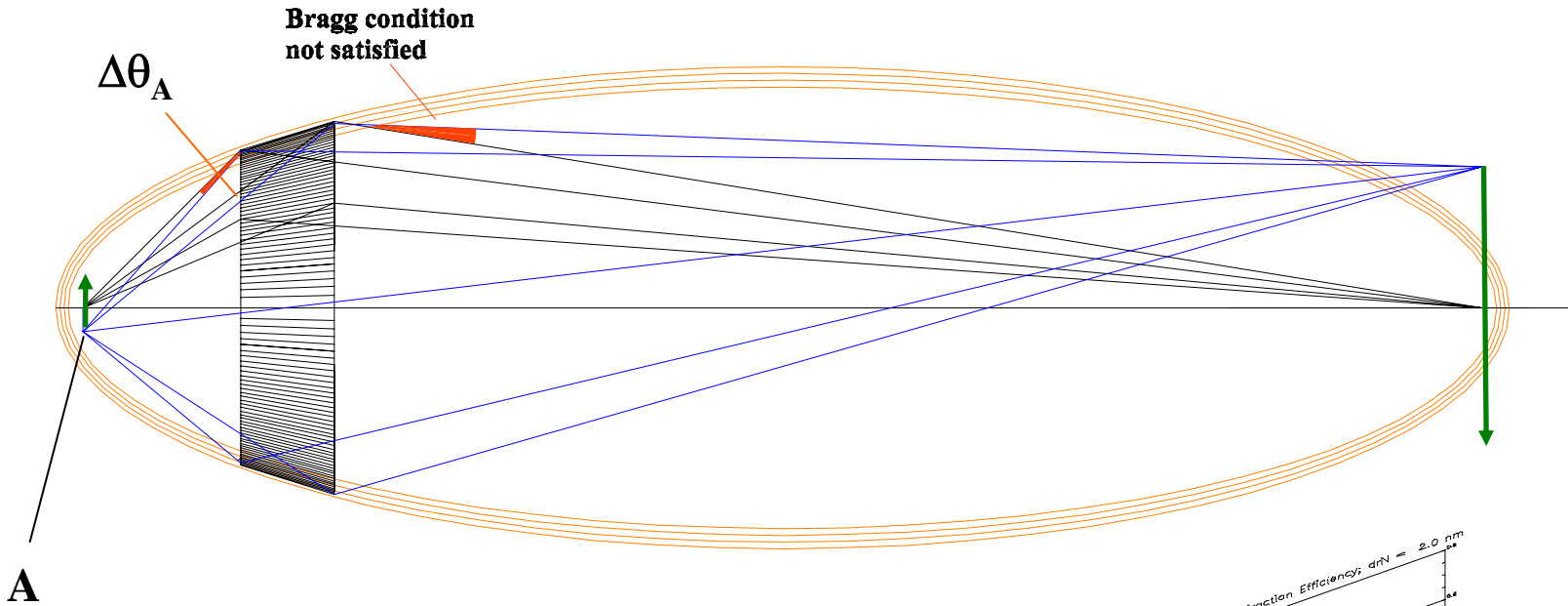
$dr_N = 2 \text{ nm}$



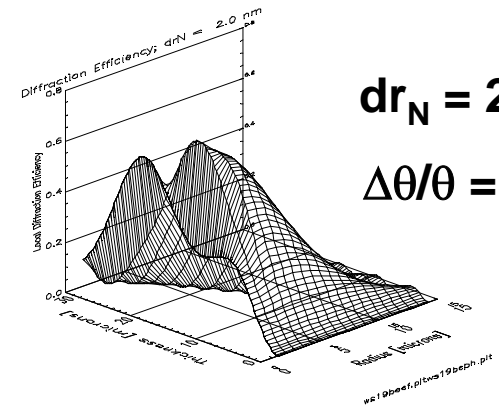
Reduced efficiency

Calculation of diffraction efficiency for $E' - E_0 = 10\%$

Imaging of a large field by VDO



$$\frac{\Delta\theta_A}{NA} = 1 - A/D, \dots, 1 + A/D \quad \text{TXM: } A/D = 0.2 - 0.5$$



$dN = 2 \text{ nm},$
 $\Delta\theta/\theta = 10\%$

Ideal VDO: Bragg condition satisfied for on-axis imaging

Imaging of off-axis points: Bragg condition *not* satisfied!

IV) Technical Approach to Nanofocusing: Multilayer Laue Lens

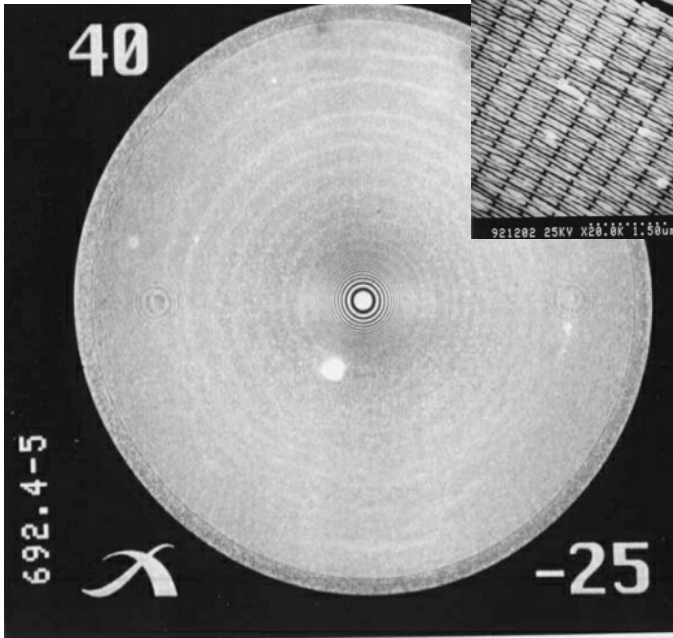
■ Challenge: Manufacture High aspect ratios

Required: $A \sim 1000 - 10000+$

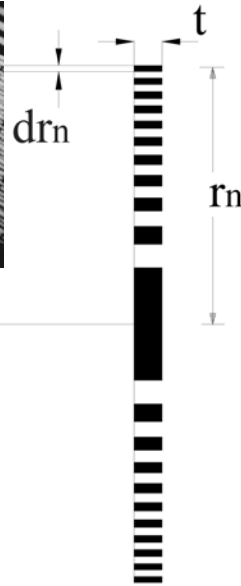
E-beam Lithography:

$dr_N = 15 \text{ nm}$ (CXRO)

Aspect ratio 10:1 - 20:1 feasible

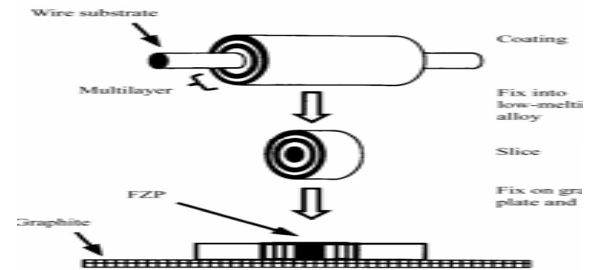


XRADIA: $dr_N = 40 \text{ nm}$



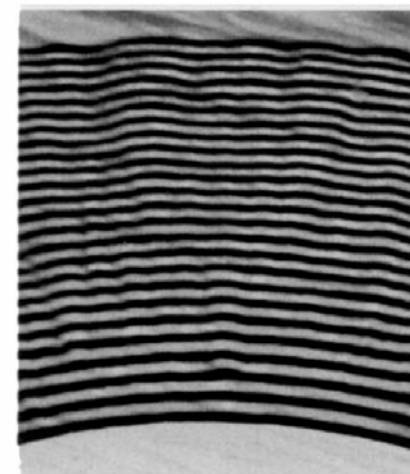
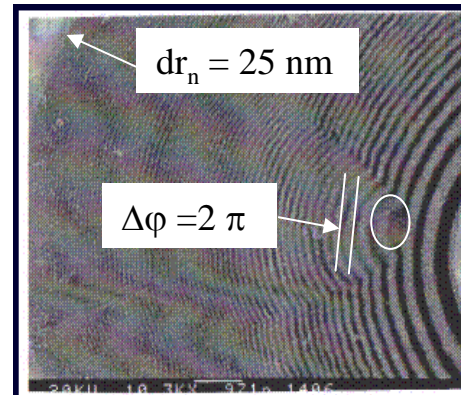
Side view

Sputtered Sliced Approach:



Kaulich, Dissertation, 1996

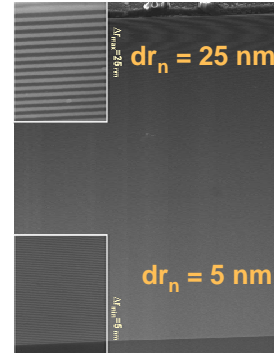
Tamura, 2002



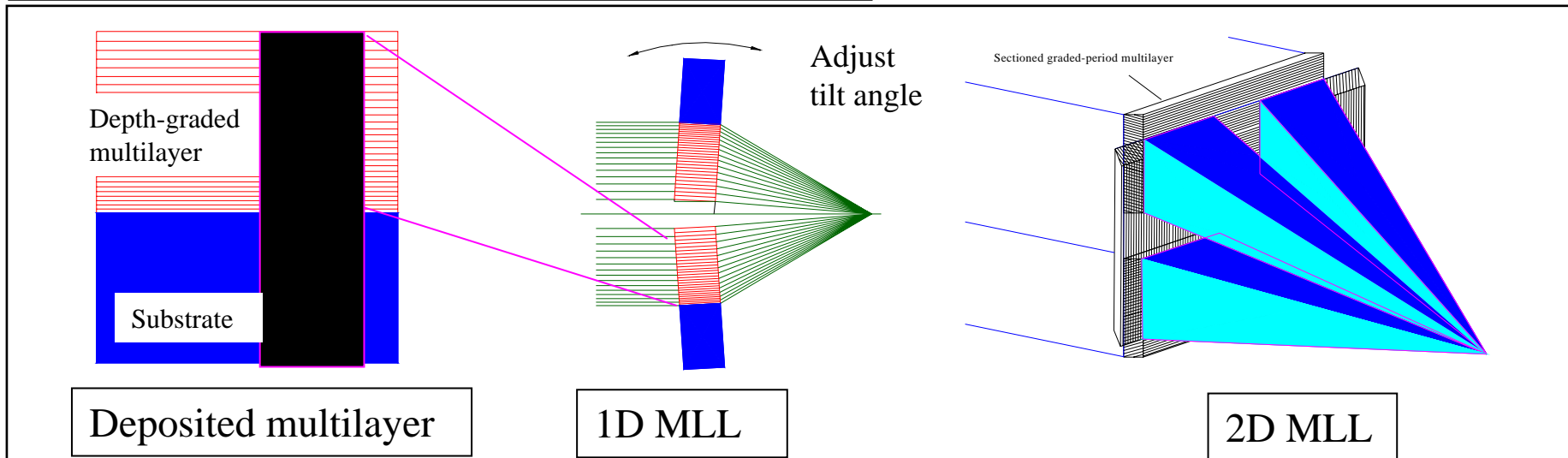
5 μm

Multilayer Laue Lens – Concept

- Deposit varied depth-graded multilayer on plane substrate (**thinnest structures first**)
- Section to 5-20 μm depth
- Assemble into a linear MLL
- Assemble two linear MLL's into a 2D MLL.

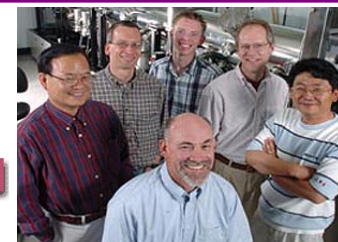


Material: WSi_2/Si
 Total deposition thickness: 13.25 μm
 d-spacing: 5 – 25 nm



2005 R&D 100 Award

The 43rd Anniversary R&D 100 Awards



Requirements for fabrication of MLL structure

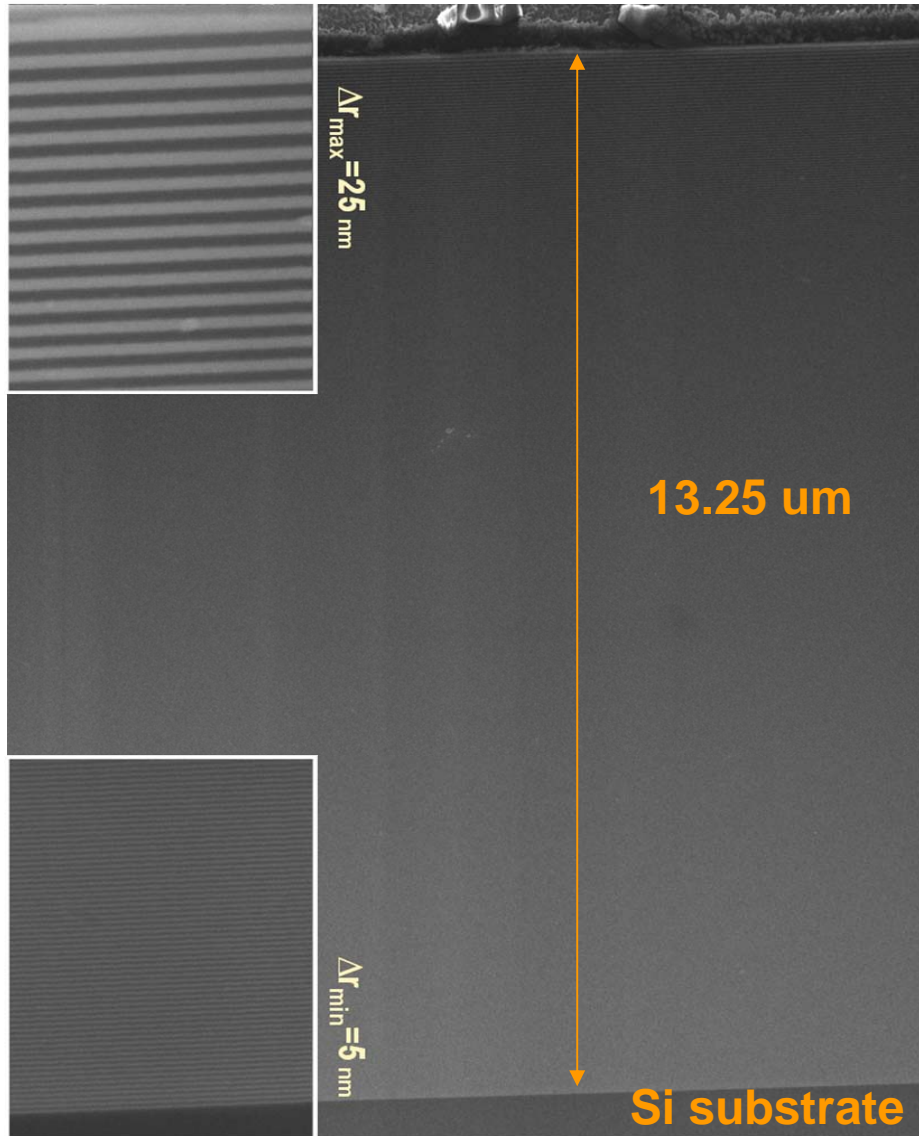
■ Parameters:

Example for $dr_N = 5$ nm structure:

- Material: WSi_2/Si
- $dr_N = 5$ nm ($2d = 10$ nm)
- $r_n = 15$ μm (13.3 μm deposited)
- $N = 1500$ (~ 1480 deposited)
- Usable aperture fraction: 44%

■ Challenges:

- Large deposition thickness requires low stress: $\rightarrow WSi_2/Si$
- High accuracy of layer placement:
 - $f = (2 r_n / \lambda) \cdot dr_n(r_n)$
- Thinning/Polishing: avoid distortions of structure

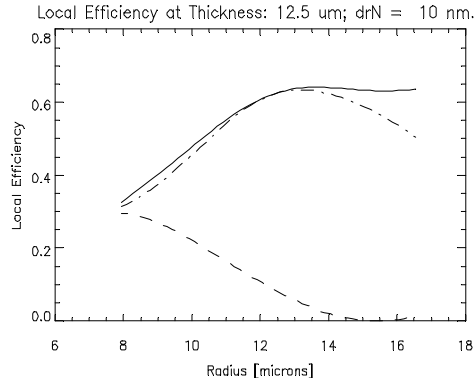
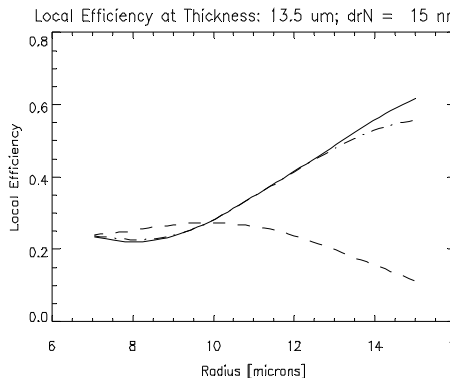
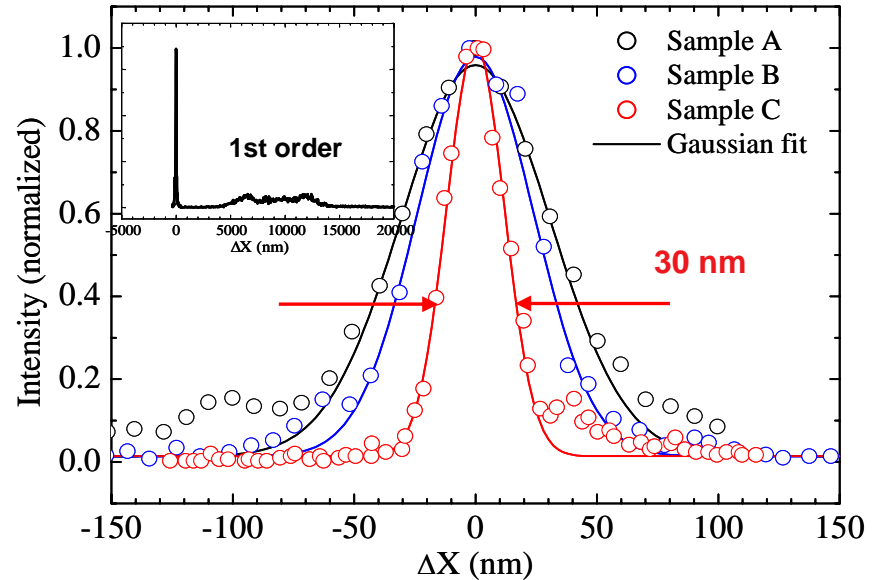


X-ray focusing with MLL sections, $dr_N = 15$, $dr_N = 10$ nm

Sample A: $dr_N = 15$ nm
 Sample B, C: $dr_N = 10$ nm

NA-limited resolution:
 Sample A: 57 nm (27% NA)
 Sample B: 44 nm (23% NA)
 Sample C: 24 nm (41% NA)

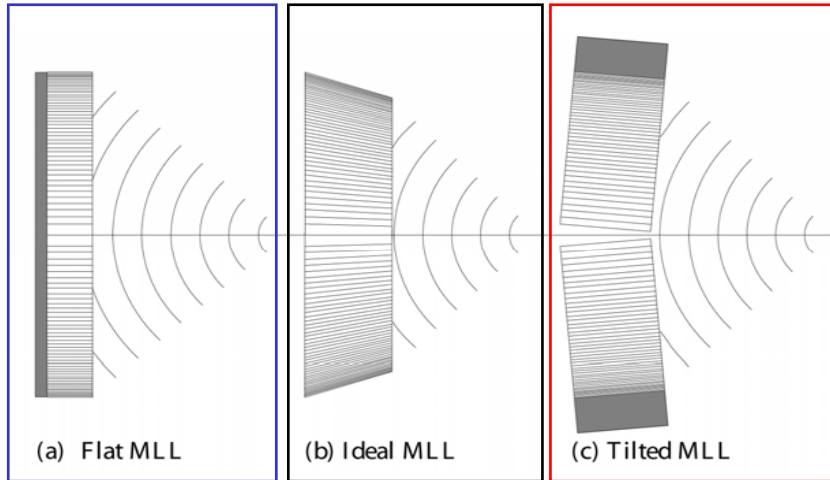
Resolution measurement



Photon Energy: 19.5 keV
 Measured Resolution: **30 nm**
 Diffraction Efficiency: **44%**

Kang et. al, PRL, Apr., 2006

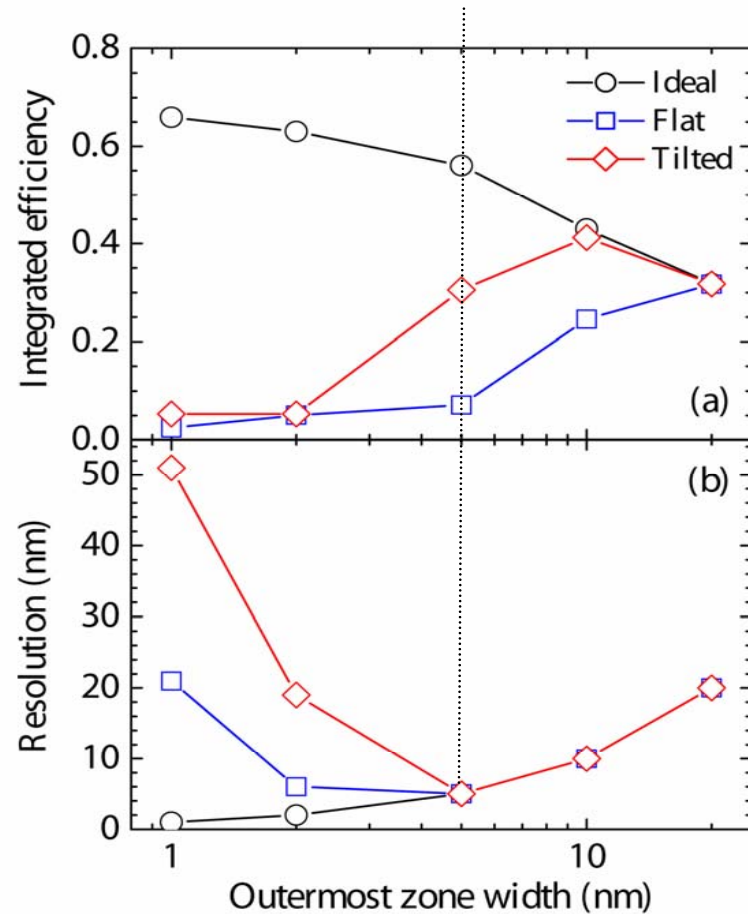
Where is the resolution limit for x-ray focusing (Diffractive Optics)?



- Ideal structure:
 - Resolution approaching 1 nm feasible,
 - Diffraction efficiency (2D) > 50%
- Tilted MLL: $\delta = 5$ nm feasible

- Locally 1D CWT valid to ~ 1 nm
- What is the effect of Borrmann-Fan on Phase?
- When is curvature of zones required?

Calculations for 1D MLL



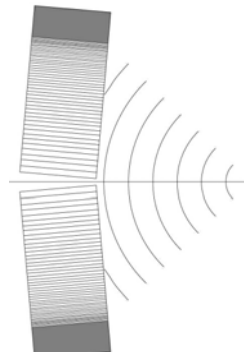
Kang et. al, PRL, 2006

V) Summary: Towards Nanofocusing of Hard X-rays.

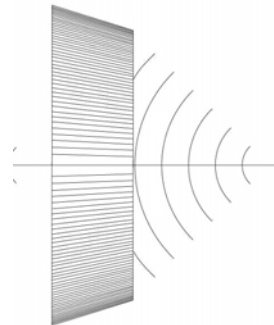
- Diffractive x-ray optics are capable of focusing x-rays to one nanometer or below.
 - Dynamic Scattering → Satisfy Bragg condition
 - Small Energy bandpass
 - Large acceptance: ok
 - Good Focusing efficiency: ok
 - Full-Field imaging: not for $\delta < \approx 5$ nm

- Multilayer Laue Lenses offer a feasible path towards true nanofocusing
 - 'Tilted' MLL approach provides $\delta_R \sim 5$ nm, 'Ideal' MLL < 5 nm
 - Materials System: WSi₂/Si
 - Accurate deposition of ≈ 1500 zones, total deposition thickness > 10 μ m
 - Sectioning/polishing to thickness of 5 μ m – 30 μ m
 - Achieved: line focus of 19.5 nm, E = 19.5 keV, 33% efficiency.

- Next steps:
 - toward 6 nm focus: engineering of 2D focusing structure (4 MLL sections)
 - Ideal structures required for < 5 nm focusing (5+ years?):
 - *Radial change of slant - R&D ongoing (Macrander, Liu, Conley)*
 - *Very significant engineering challenges to come (\$\$\$...)*



Tilted MLL



Ideal MLL

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- *ANL-LDRD, 2003-242-R1*
- *ANL-LDRD, 2006-225-N0*

