



Top Quark Cross Section and Spin Correlations



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for the CDF and DØ Collaborations
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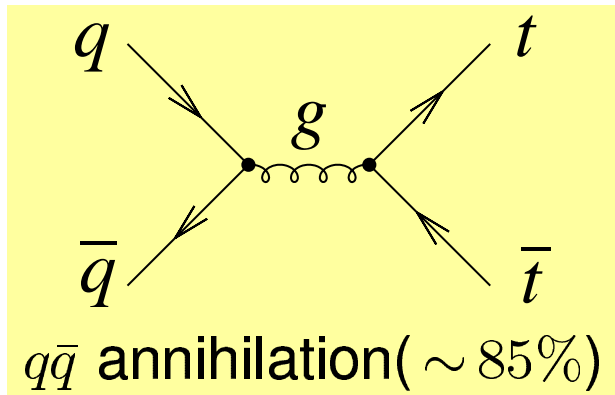
Top Quark Symposium at MCTP, University of Michigan

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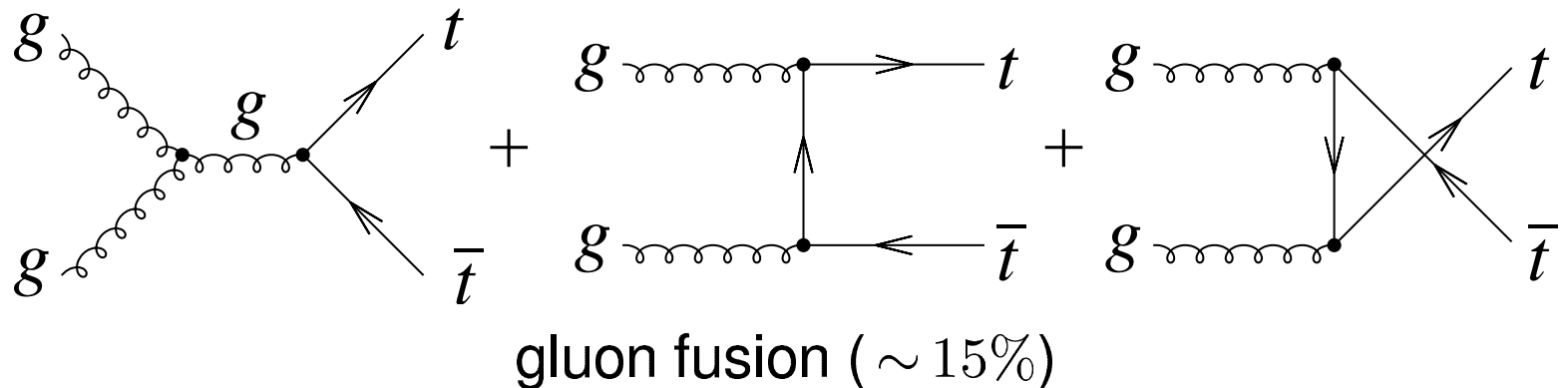
- $t\bar{t}$ Production Cross-section measurements at Tevatron
- $t\bar{t}$ Spin Correlation Prospects by Simulation
- Summary

$t\bar{t}$ Pair Production at the Tevatron

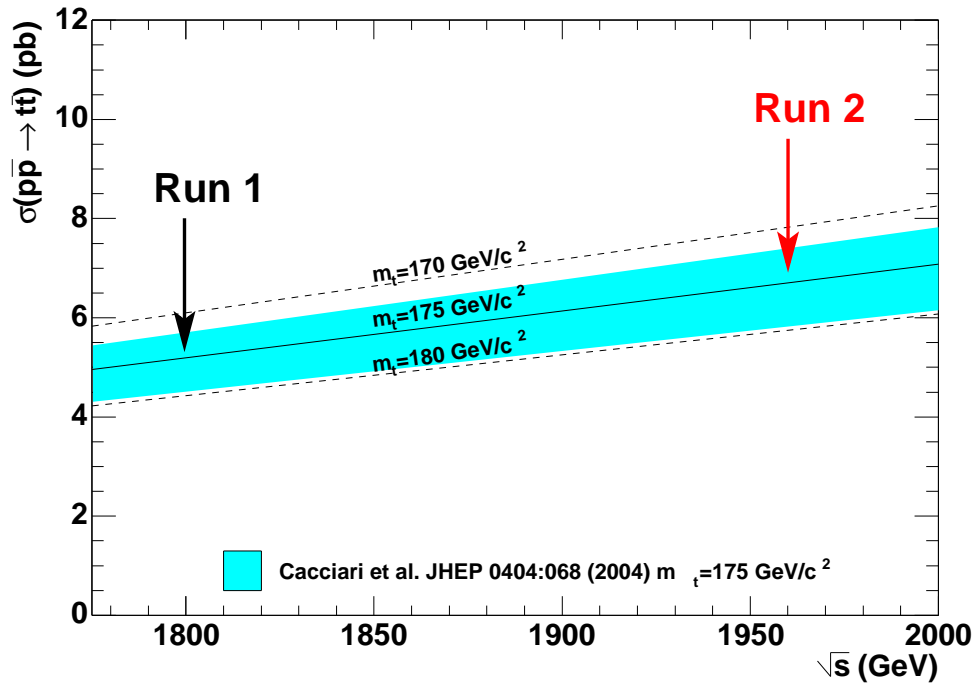
- Tevatron ($p\bar{p}$ collisions, $\sqrt{s} = 1.96$ TeV)
 - Pair production through strong interaction.
 - ⇔ Single top production through electro-weak interaction.
 - **$q\bar{q}$ annihilation is dominant process.**
 - ⇔ Gluon fusion is dominant for LHC.



$$\sigma(gg \rightarrow t\bar{t}) : \sigma(qq \rightarrow t\bar{t}) = 15\% : 85\% \text{ (NLO)}$$



Theoretical prediction for $t\bar{t}$ production cross-section at NLL



$$\Rightarrow \sigma(t\bar{t}) \sim 6.7 \text{ pb} \quad (M_t = 175 \text{ GeV}/c^2)$$

$$\text{uncertainty(PDF, } \alpha_s, \mu_R, \mu_F) \sim 15\%$$

M. Cacciari, et al., JHEP 404,68 (2004)

$t\bar{t}$ cross-section measurement is

- Important test of perturbative QCD.
- Sensitive to new physics (e.g. resonance production of $t\bar{t}$).

and

- To identify $t\bar{t}$ signal is a fundamental step to any top property analysis.

3 Categories of Event Signature in $t\bar{t}$ Production

Top quark decays to W and b at a rate of $\sim 100\%$ $\text{Br}(t \rightarrow W^+b) \simeq 1$

Decay channels of $t\bar{t}$

$t \rightarrow W^+b$	b	b	b	b
\hookrightarrow	$\ell^+\nu$	$q\bar{q}'$	$\ell^+\nu$	$q\bar{q}'$
$\bar{t} \rightarrow W^- \bar{b}$	\bar{b}	\bar{b}	\bar{b}	\bar{b}
\hookrightarrow	$\ell^-\bar{\nu}$	$\ell^-\bar{\nu}$	$q\bar{q}'$	$q\bar{q}'$

dilepton channel

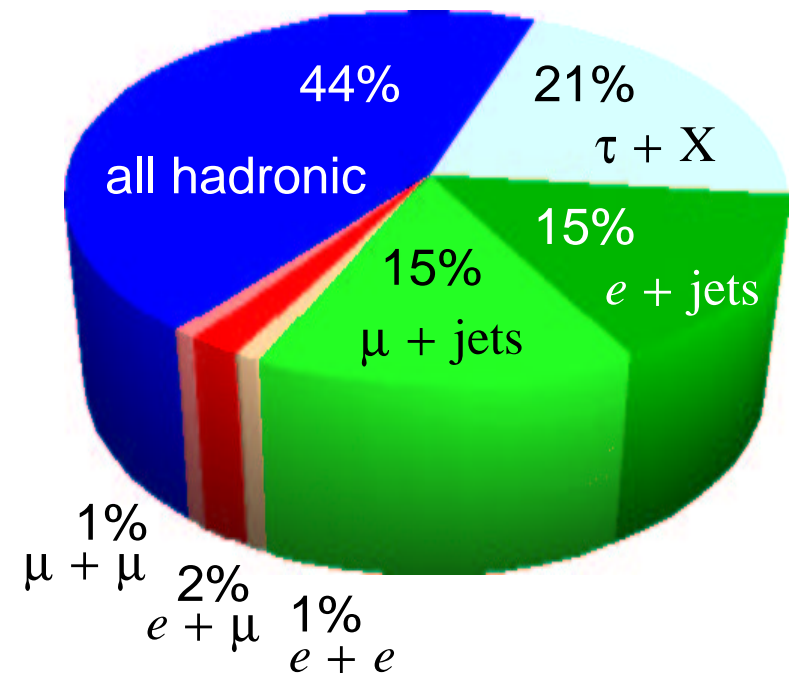
\Rightarrow 2 leptons, \cancel{E}_T , 2 b -jets

lepton+jets channel

\Rightarrow 1 lepton, \cancel{E}_T , 4 jets (including 2 b -jets)

all hadronic channel

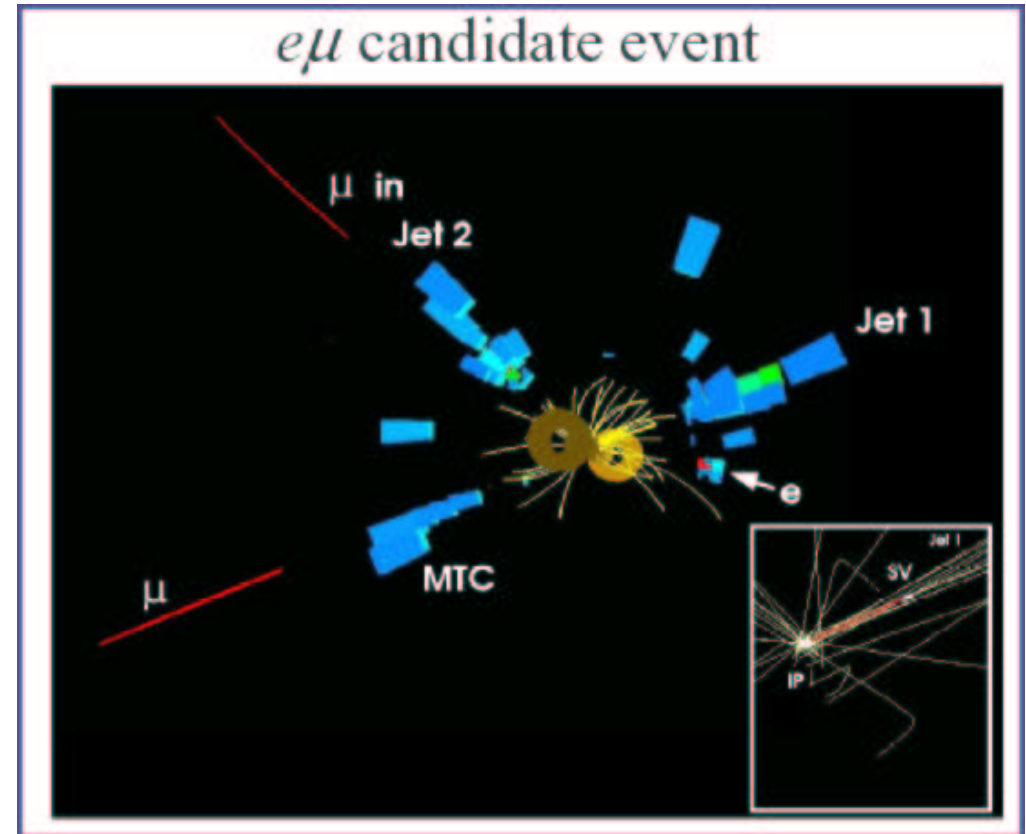
\Rightarrow 6 jets (including 2 b -jets)



Cross Section Measurements in Dilepton Channels

- $t\bar{t} \rightarrow W^+bW^-b \rightarrow \ell^+\nu b\ell^-\bar{\nu}b$
- Signature: 2 high P_T leptons, \cancel{E}_T , 2 b -jets
- Good signal to background ratio without b -tagging.
- Dominant backgrounds
 - Drell-Yan: $Z/\gamma^* \rightarrow ee, \mu\mu, \tau\tau$
 - Diboson: WW, WZ, ZZ
 - Fake: W +QCD jets
- Smallest branching fraction
 $\sim 5\%$

$t\bar{t}$ dilepton($e\mu$ channel) candidate at DØ \Rightarrow



Counting Method with Standard(Traditional) Selection

- Cross-section based on counting number of candidates and bkg.

$$\sigma(tt\bar{t}) = \frac{N_{\text{obs}} - N_{\text{bkg}}}{\epsilon_{\text{tot}} \int \mathcal{L} dt} \quad \begin{array}{l} N_{\text{obs}}: \text{Number of observed candidates} \\ \epsilon_{\text{tot}}: \text{Acceptance} \times \text{efficiency} \end{array}$$

- Signal selection

- 2 high P_T lepton (e or μ)
- Missing transverse energy (\cancel{E}_T)
- 2 (or more) jets
- Veto Z inclusive events

- Result at $D\emptyset$

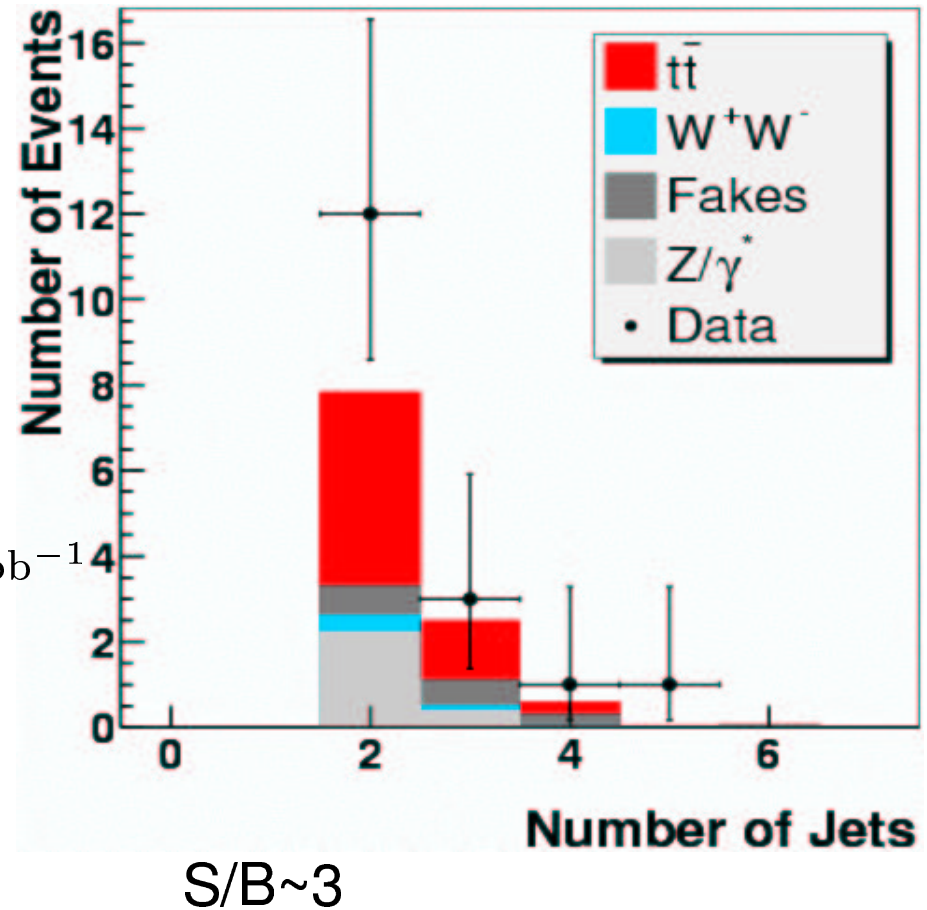
$$ee: 156 \text{pb}^{-1}, \mu\mu: 139.6 \text{pb}^{-1}, e\mu: 142.7 \text{pb}^{-1}$$

- Observed candidates

$$N_{\text{obs}} = 17$$

- Expected backgrounds

$$N_{\text{bkg}} = 4.76 \pm 0.65$$



$$\Rightarrow \sigma = 14.3_{-4.3}^{+5.1}(\text{stat})_{-1.9}^{+2.6}(\text{syst}) \pm 0.9(\text{lum}) \text{pb} \quad (D\emptyset \sim 150 \text{pb}^{-1})$$

Ready for kinematic distributions in the $t\bar{t}$ candidates with good S:B ratio

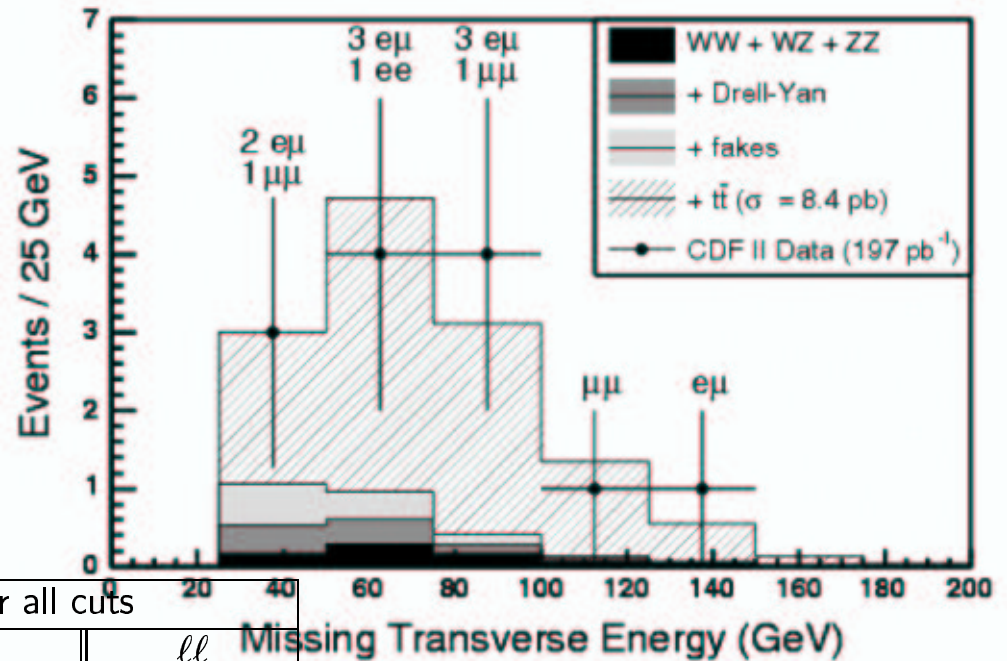
- Result at CDF (197pb^{-1})

- Observed candidates

$$N_{\text{obs}} = 13$$

- Expected backgrounds

$$N_{\text{bkg}} = 2.7 \pm 0.7$$



Source	Events per 193pb^{-1} after all cuts			
	ee	$\mu\mu$	$e\mu$	ll
WW/WZ	0.21 ± 0.06	0.18 ± 0.05	0.35 ± 0.10	0.74 ± 0.21
Drell-Yan	0.36 ± 0.28	0.07 ± 0.34	-	0.43 ± 0.44
$Z \rightarrow \tau\tau$	0.09 ± 0.03	0.11 ± 0.03	0.22 ± 0.07	0.42 ± 0.13
Fakes	0.26 ± 0.11	0.16 ± 0.07	0.69 ± 0.28	1.1 ± 0.45
Total Background	0.9 ± 0.3	0.5 ± 0.4	1.3 ± 0.3	2.7 ± 0.7
$t\bar{t}$ ($\sigma = 6.7\text{pb}$)	1.9 ± 0.3	1.8 ± 0.3	4.5 ± 0.6	8.2 ± 1.1
Total SM expectation	2.8 ± 0.4	2.4 ± 0.5	5.7 ± 0.7	10.9 ± 1.4
Run II data	1	3	9	13

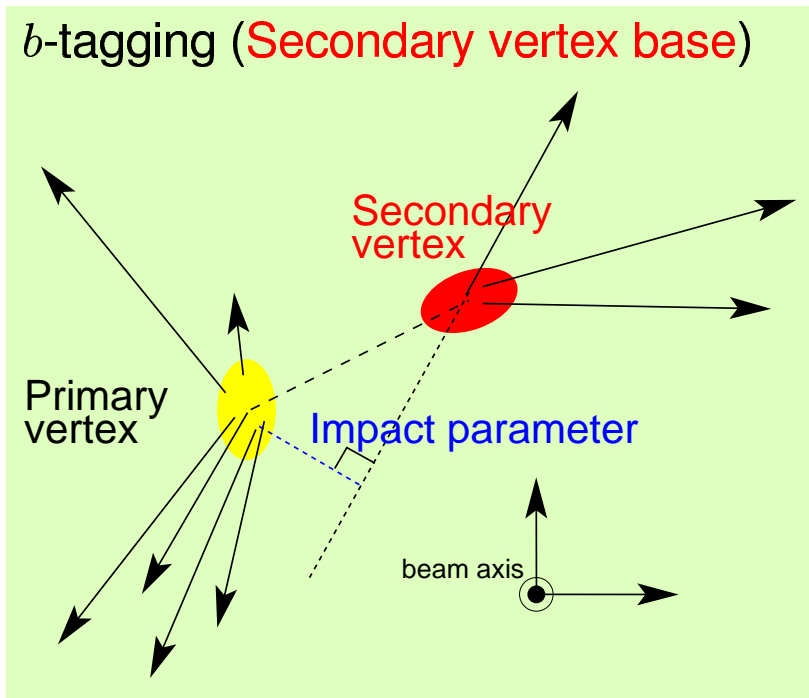
S/B~4

$$\rightarrow \sigma = 8.4^{+3.2}_{-2.7}(\text{stat})^{+1.5}_{-1.1}(\text{syst}) \pm 0.5(\text{lum})\text{pb (CDF } 197\text{pb}^{-1}\text{)}$$

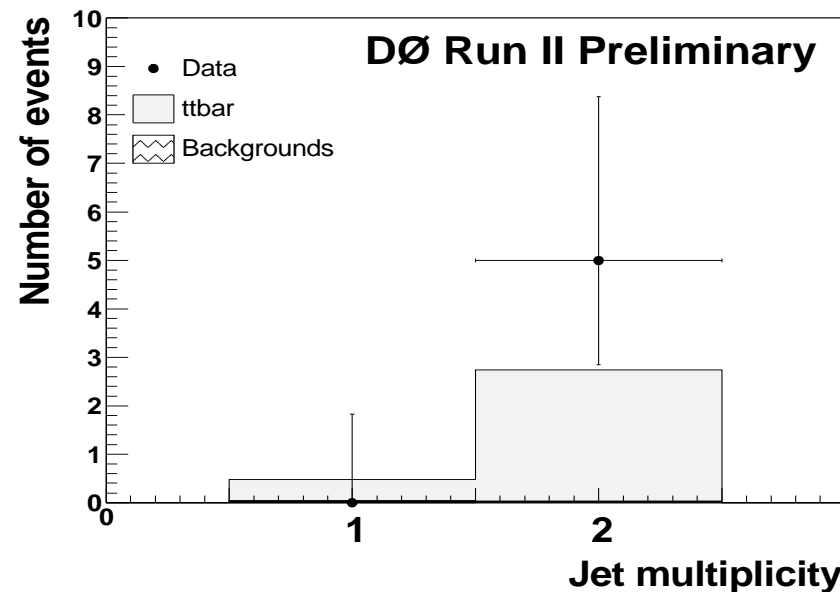
Tighten selection \Rightarrow Trade off signal efficiency for S:B

- Signal selection

- Use only $e\text{-}\mu$ channel candidate \rightarrow Suppress Z bkg
 - Branching fraction $\sim 50\%$ eff.
- At least 1 b -tagged jet \rightarrow Suppress light flavor or gluon QCD jets
 - ≥ 1 b -tagging $\sim 60\%$ eff. (\Leftrightarrow mistag rate for $W+4$ jets $\sim 2.4\%$)
- \cancel{E}_T



$N_{\text{obs}} = 5$ with expected $N_{\text{bkg}} = 0.04$



$\Rightarrow \sigma = 11.1^{+5.8}_{-4.3}(\text{stat}) \pm 1.4(\text{syst}) \pm 0.7(\text{lum}) \text{ pb (DØ } 158 \text{ pb}^{-1})$

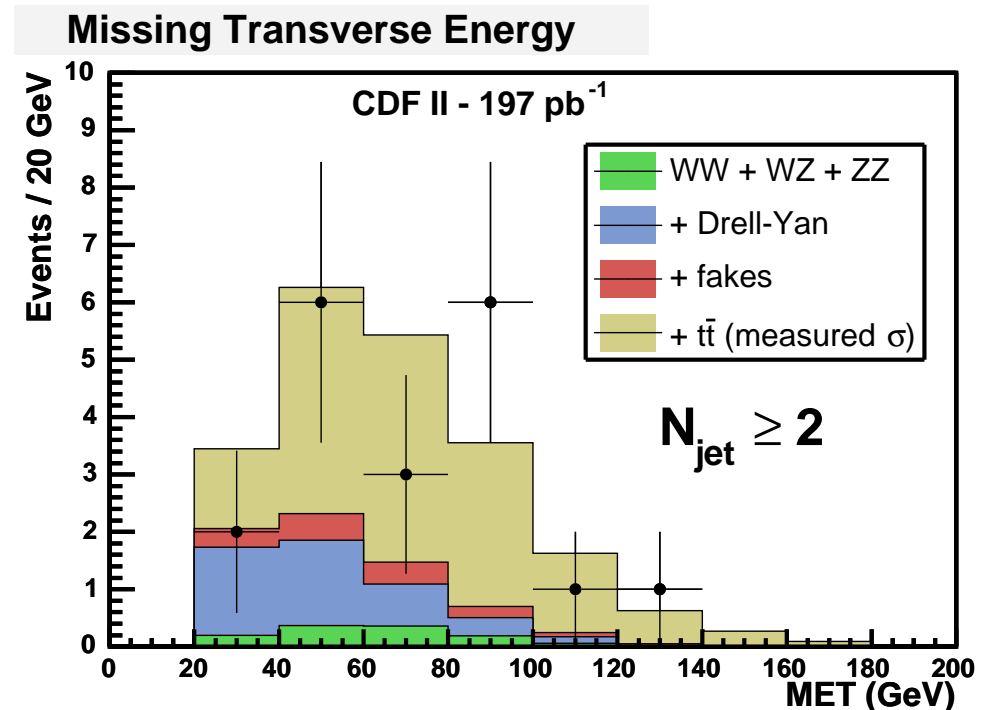
Almost background free $t\bar{t}$ sample!

Loosen selection \Rightarrow Trade off S/B for signal efficiency

- ℓ +isolated track selection
 - 1 tight lepton(e, μ)+1 isolated track
 - \cancel{E}_T , 2 or more jets
 - \rightarrow Worse S:B ratio, but better signal efficiency.
 - \rightarrow $t\bar{t}$ Cross-section with less uncertainty.
- CDF result (197pb^{-1})

- Observed candidates
 $N_{\text{obs}} = 19$
- Expected backgrounds
 $N_{\text{bkg}} = 6.9 \pm 1.7$

S/B \sim 2

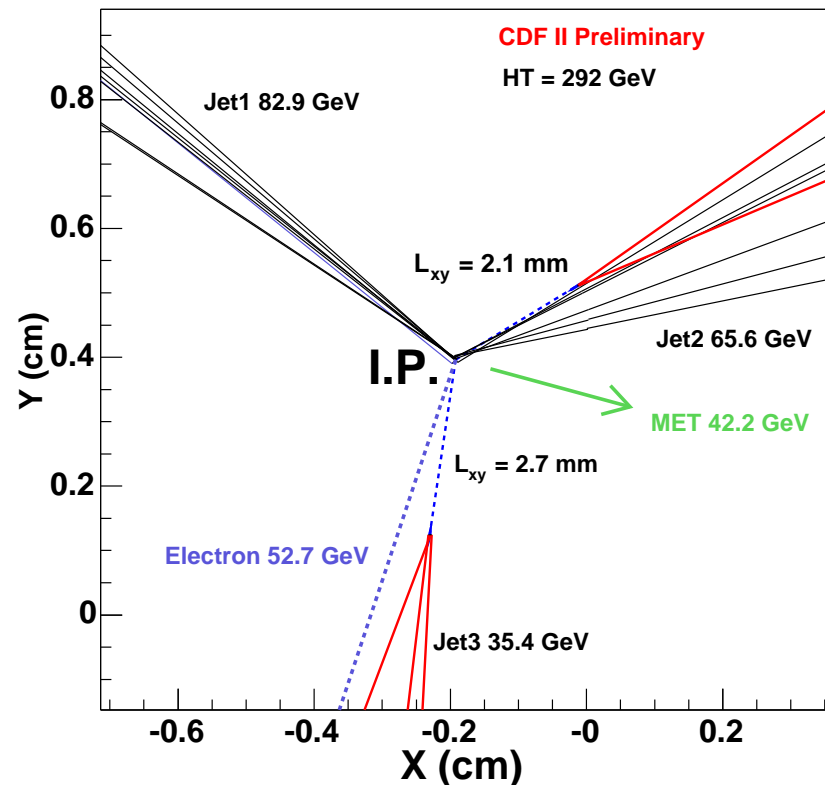


$$\Rightarrow \sigma = 7.0_{-2.3}^{+2.7}(\text{stat})_{-1.3}^{+1.5}(\text{syst}) \pm 0.4(\text{lum})\text{pb (CDF } 197\text{pb}^{-1}\text{)}$$

Cross Section Measurements in ℓ +Jets Channels

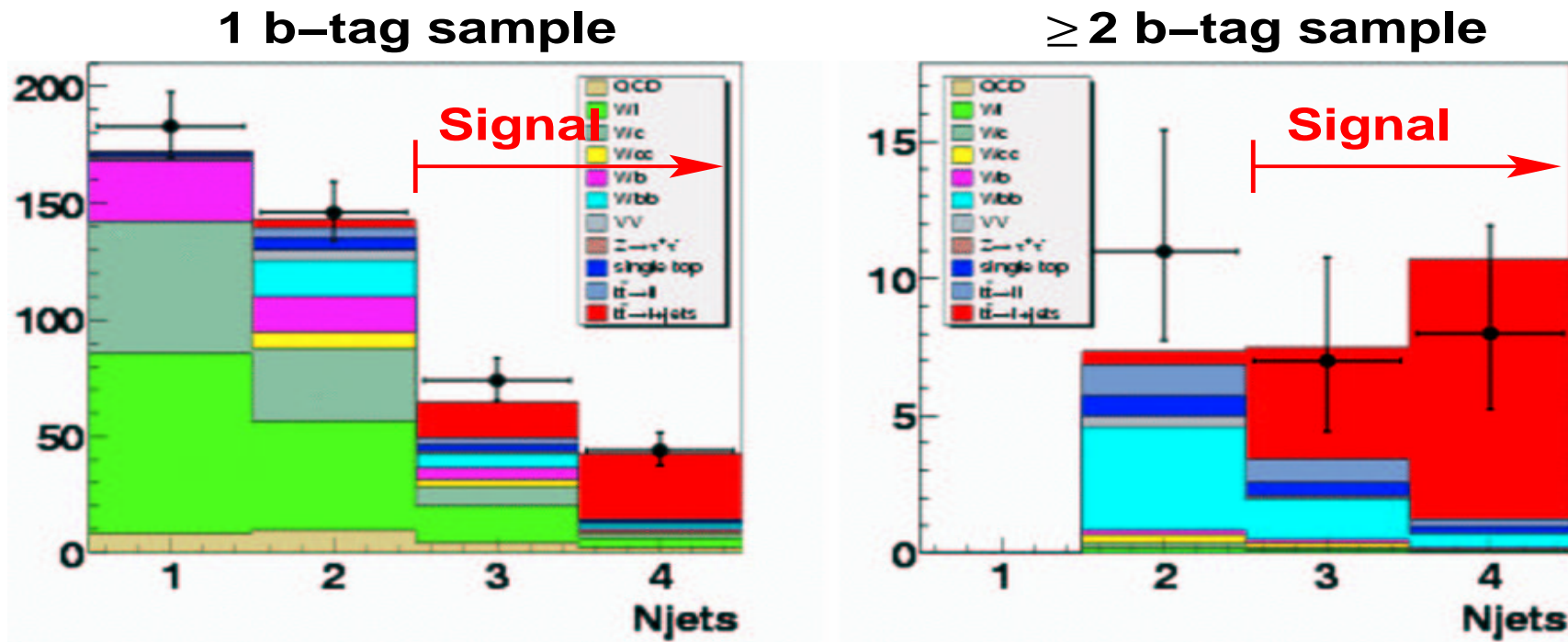
- $t\bar{t} \rightarrow W^+bW^-b \rightarrow \ell^+\nu bjj'\bar{b}$ or $jj'b\ell^-\bar{\nu}\bar{b}$
- Signature: 1 high P_T leptons, \cancel{E}_T , 4 jets (including 2 b -jets)
- Dominant backgrounds: W +jets.
- Good signal to background ratio **after b -tagging**.
- Large branching fraction $\sim 30\%$
 - Large sample suitable for top mass analysis. ($N_{\text{jet}} \geq 4$)
- Signal eff. and S/B depend on b -tagging eff. and mistag ratio.

$t\bar{t} \rightarrow e$ +jets channel candidate at CDF \Rightarrow



Based on Counting Method with Standard Selection

- Event selection
 - high P_T lepton (e or μ), \cancel{E}_T , and $N_{\text{jet}} \geq 3$
 - **At least 1 b -tagged jet**
- $D\emptyset$ result (e +jets: 169pb^{-1} , μ +jets: 158pb^{-1})
 - b -tagging eff.: **$\sim 60\%$** (Impact parameter based tag)
 - S/B for $N_{\text{jet}} = 4$ bin: **~ 2** (single tagged), **~ 5** (double tagged)

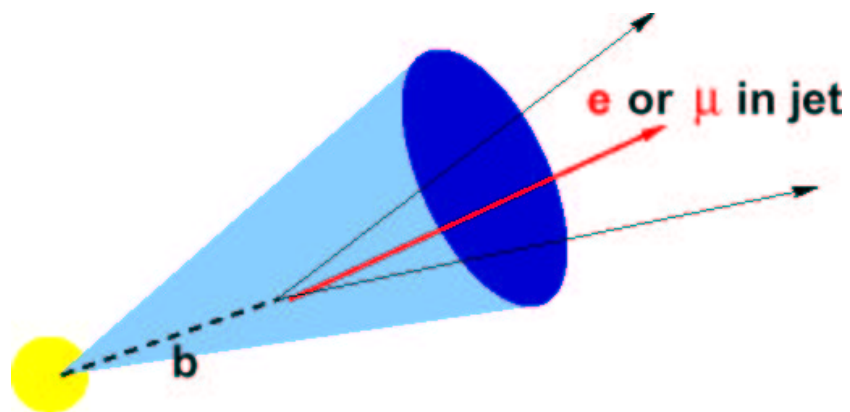


$$\Rightarrow \sigma = 7.2_{-1.2}^{+1.3}(\text{stat})_{-1.4}^{+1.9}(\text{syst}) \pm 0.5(\text{lum})\text{pb (D}\emptyset\text{)}$$

Result on another b -tagging tool

- Soft muon tag (identify semileptonic decay of B hadrons)
 - Tagging eff. : $\sim 15\%$ Mistag rate: $\sim 3.6\%$
 - Independent tagging information of secondary vertex tag

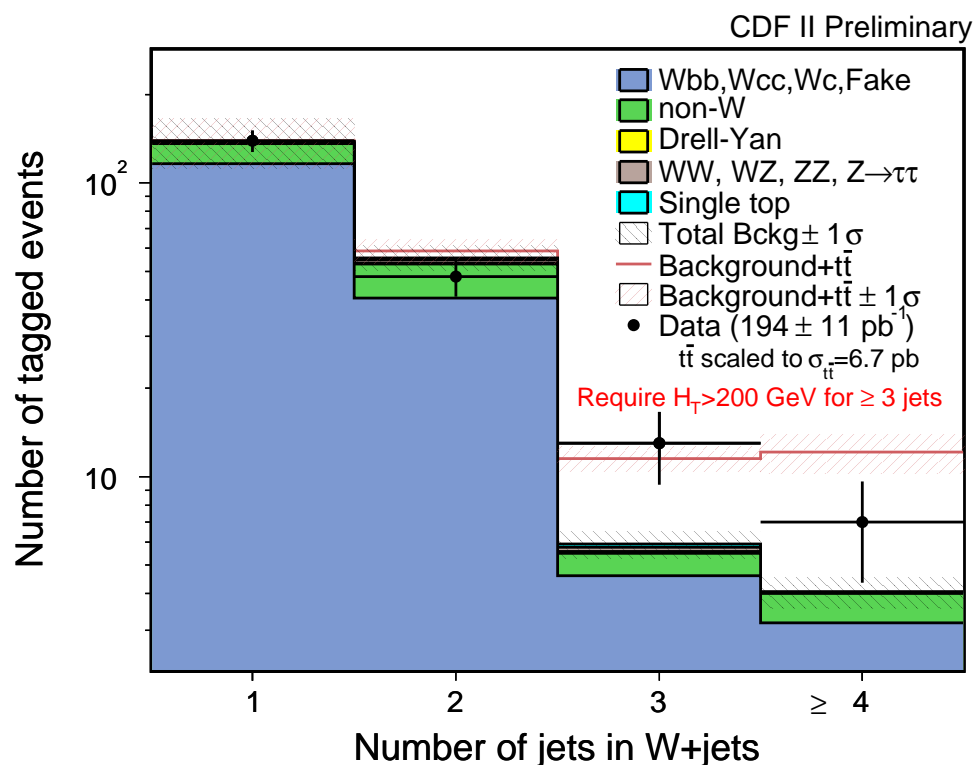
Based on semileptonic decay of B hadron



$$\text{Br}(b \rightarrow lvc) \sim 20\%$$

$$\text{Br}(b \rightarrow c \rightarrow lvs) \sim 20\%$$

Soft muon tag(CDF 193pb^{-1})



$$\Rightarrow \sigma = 5.2^{+2.9}_{-1.9}(\text{stat})^{+1.3}_{-1.0}(\text{syst}) \text{pb (CDF } 193\text{pb}^{-1})$$

Kinematical Fitting Technique \Leftrightarrow counting experiment

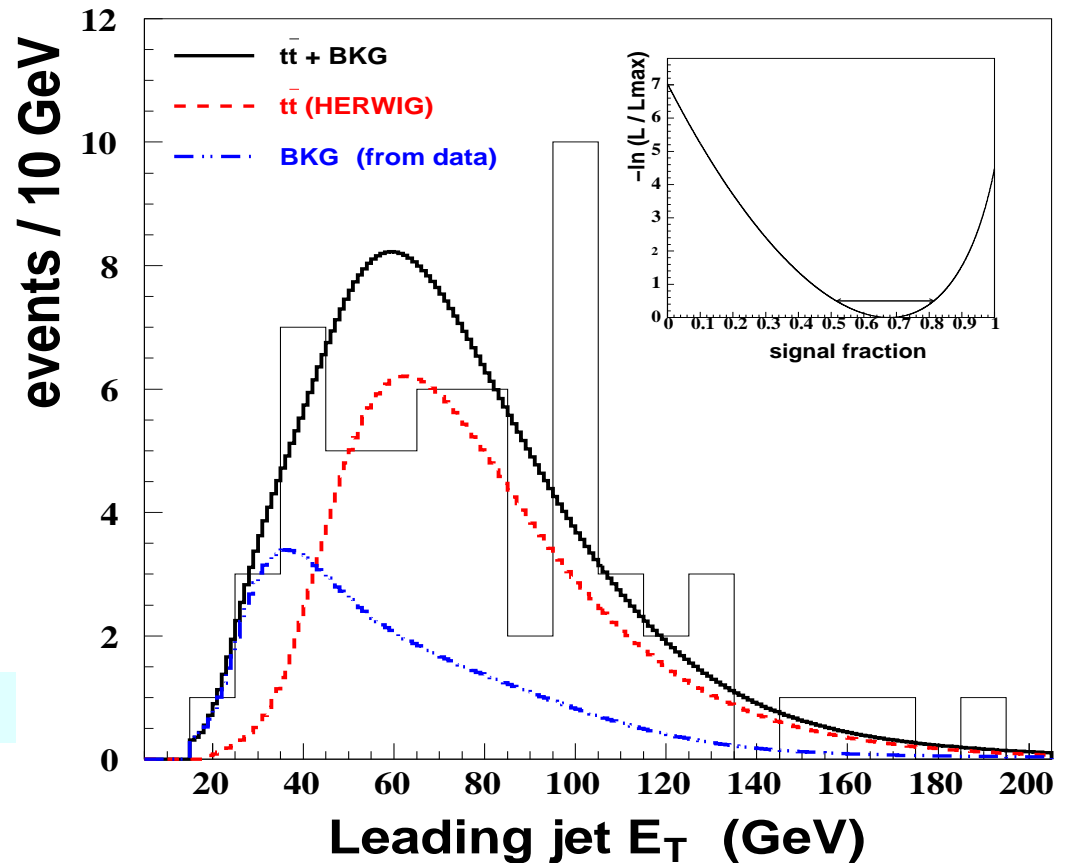
- Use $\ell_+ \geq 3$ jets sample with at least one b -tag (CDF 162pb^{-1})
- Fit to leading jet E_T distribution to extract signal fraction.

$$\rightarrow R = S/(S + B) = 0.68^{+0.14}_{-0.16}$$

$$\sigma(tt\bar{t}) = \frac{R \cdot N_{\text{obs}}}{\epsilon_{\text{tot}} \int \mathcal{L} dt}$$

- No assumption of absolute value of N_{bkg} .
- Bkg shape extracted from data
 \rightarrow Reliable prediction

$$\Rightarrow \sigma = 6.0 \pm 1.6(\text{stat}) \pm 1.2(\text{syst}) \text{ pb}$$



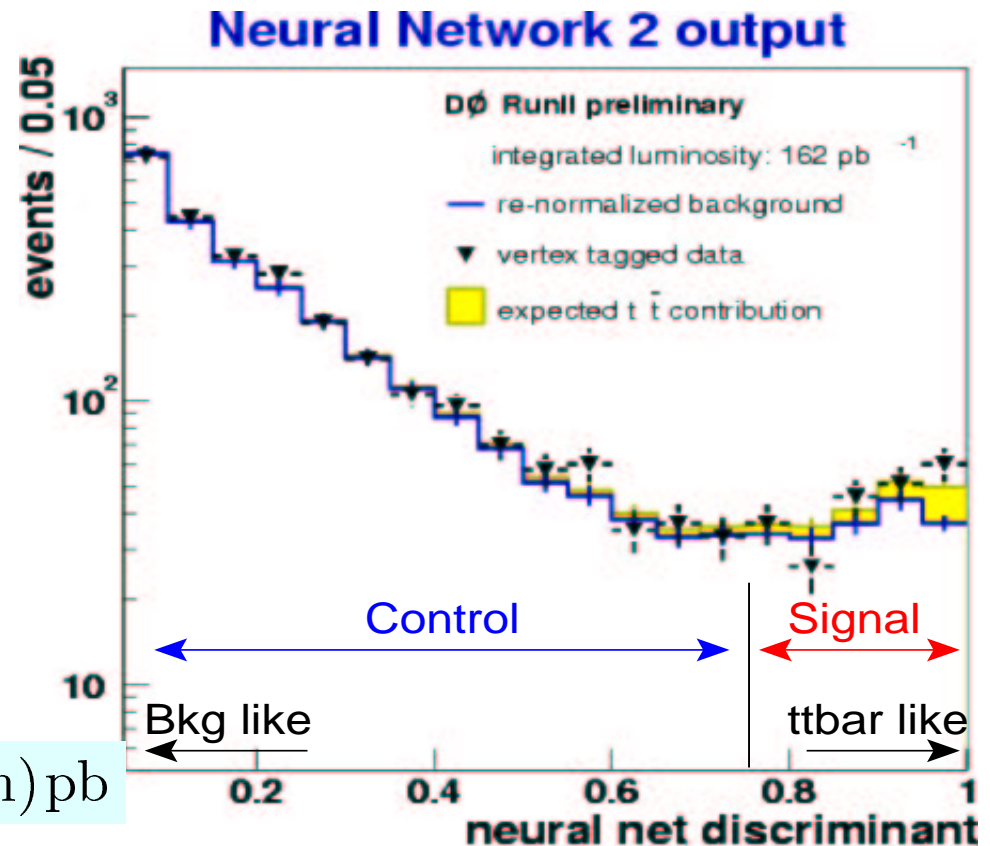
Cross Section Measurements in All-Hadronic Channels

- Final state: 6 jets including 2 b -jets
- Overwhelming QCD multijet background **even after b -tagging**.
- Data sample: ≥ 6 jets (1 b -tag) with no lepton
- Neural network technique (use H_T , Centrality, Aplanarity, ...)

DØ Run2 preliminary (162 pb⁻¹)

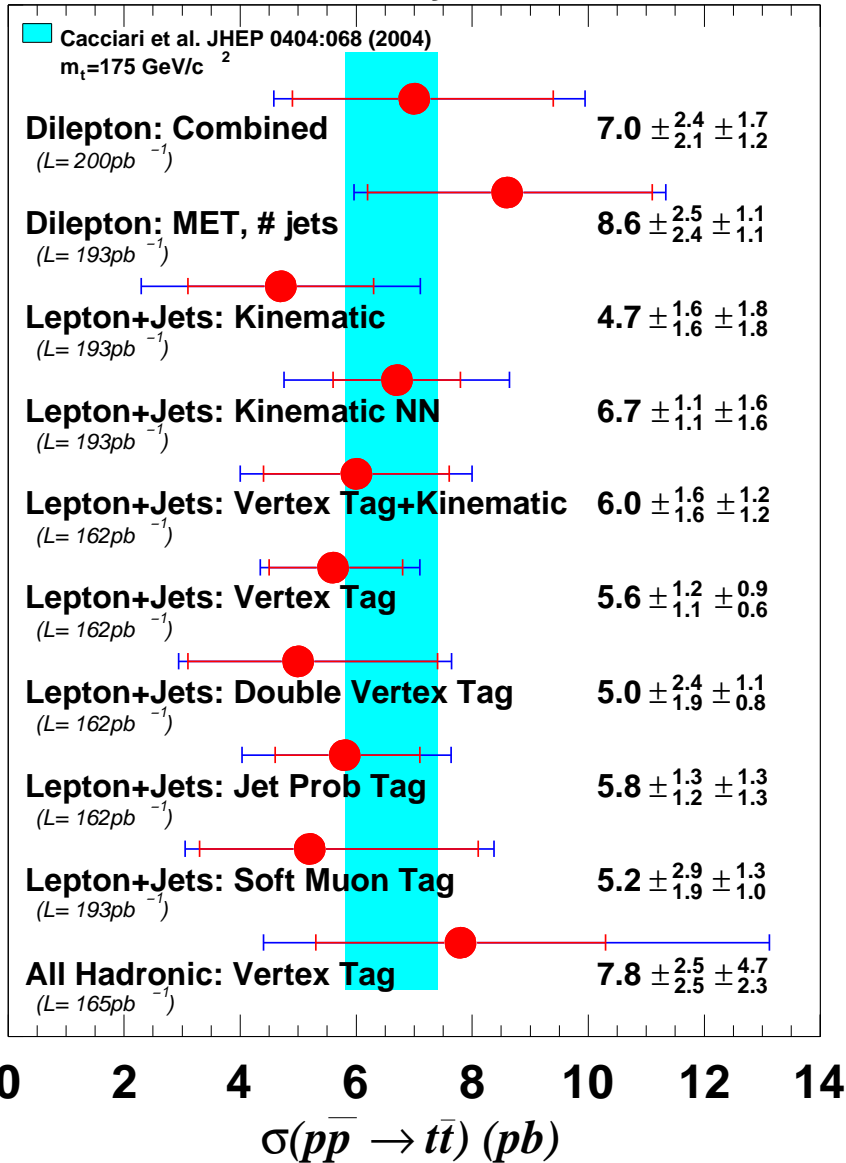
- $N_{\text{obs}} = 220$ in signal region
- expected $N_{\text{bkg}} = 186 \pm 5$

$$\Rightarrow \sigma = 7.7_{-3.3}^{+3.4}(\text{stat})_{-3.8}^{+4.7}(\text{syst}) \pm 0.5(\text{lum}) \text{ pb}$$

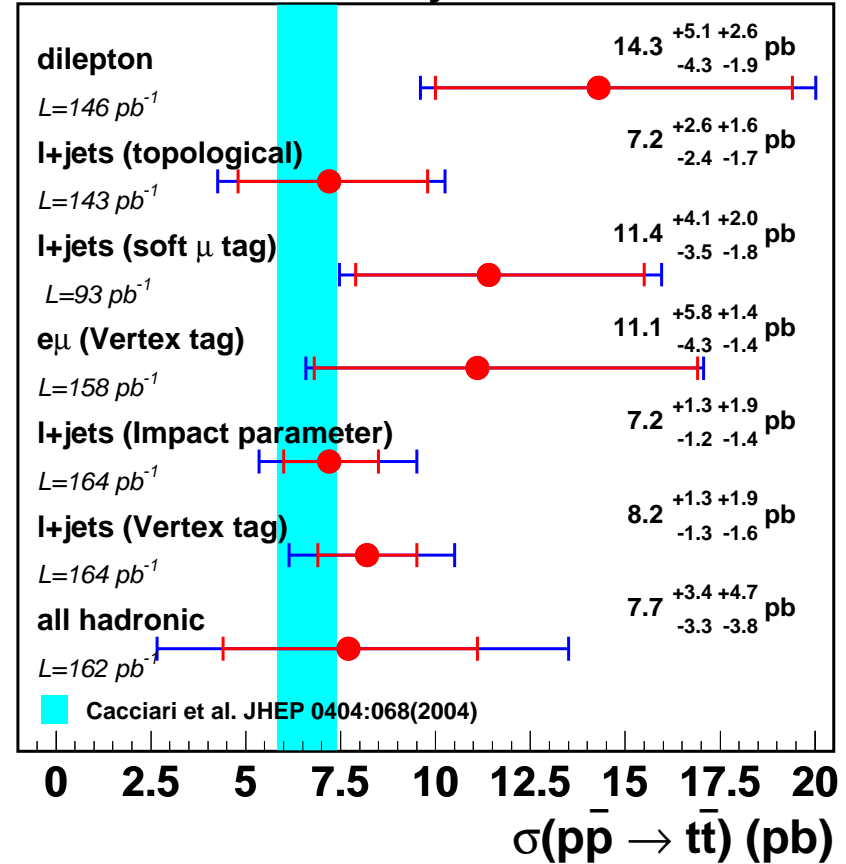


All Tevatron Run2 Results and Comparison with Prediction

CDF Run 2 Preliminary

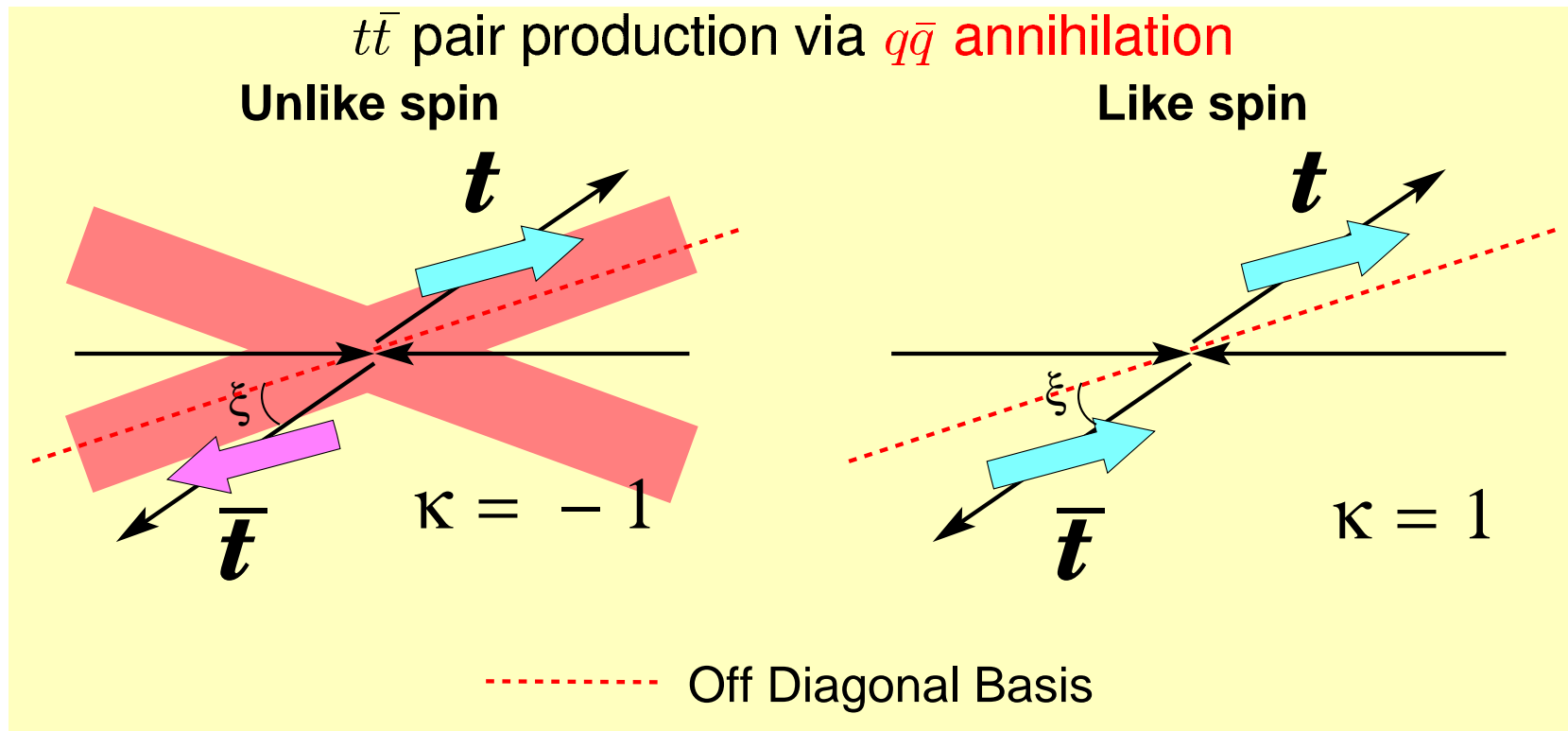


DØ Run II Preliminary



All results are consistent with prediction so far.

$t\bar{t}$ Spin Correlations



- At tree-level $q\bar{q}$ annihilation, **only like-spin combinations are allowed**, if take a proper basis so-called “off-diagonal”.
- Correlation parameter κ is defined as the correlation coefficient between top and anti-top spin polarizations.

Top Quark Decay

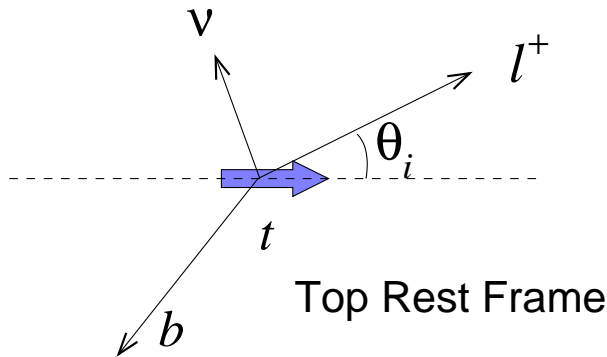
- Spin-flip time after hadronization: $O(m_t/\Lambda_{\text{QCD}}^2) \simeq (1.3 \text{ MeV})^{-1}$
- Top decay width: $\Gamma_t \simeq 1.42 \text{ GeV}$

$$O(m_t/\Lambda_{\text{QCD}}^2) \gg 1/\Gamma_t$$

⇒ Top quark decays before losing the spin information at the production.

- V-A decay

⇒ Flight direction of decay products has spin information of its mother.



Differential decay rate

$$\frac{1}{\Gamma} \cdot \frac{d\Gamma}{d \cos \theta_i} = \frac{1 + \alpha_i \cos \theta_i}{2}$$

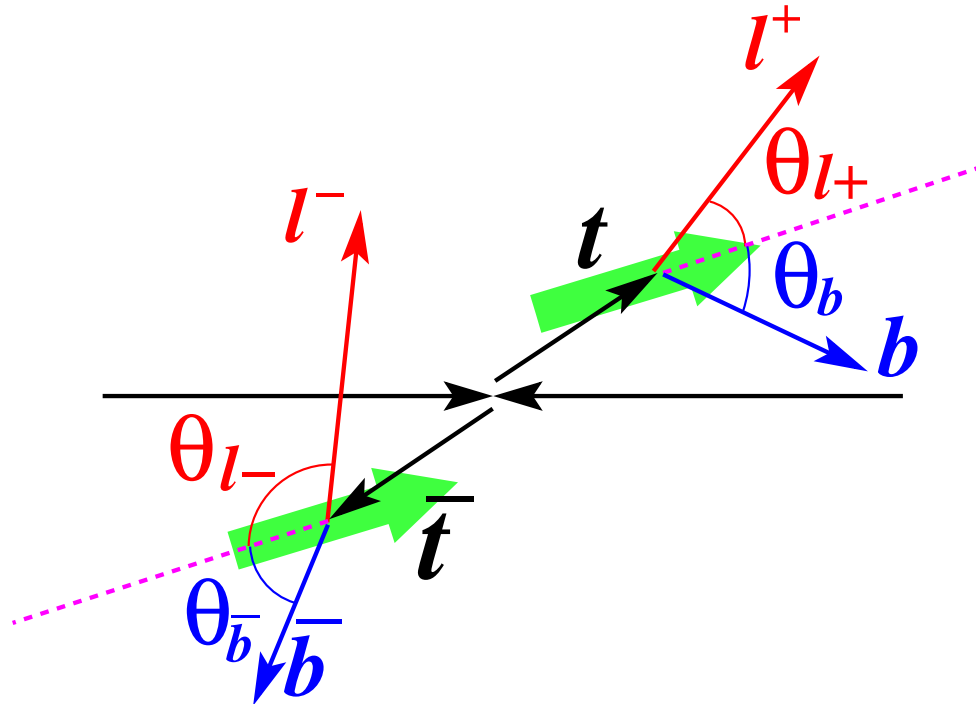
Particle	α_i
l^+	1
ν	-0.32
W^+	0.40
b	-0.40

θ_+ (θ_-): Angle of l^+ (l^-) flight direction w.r.t. quantization basis in $t(\bar{t})$ rest frame.

Top is the only quark we can study its spin polarization at the production.

Correlations in Angular Distributions of Decay Product

$t\bar{t}$ spin correlation can be seen as angular correlation of decay products



Differential production cross-section

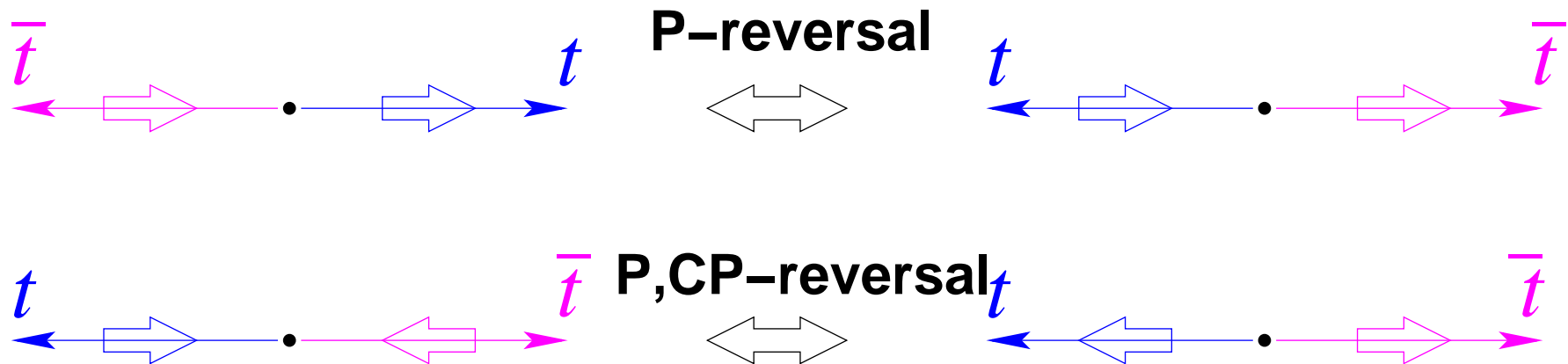
$$\frac{1}{\sigma} \cdot \frac{d^2\sigma}{d\cos\theta_+ d\cos\theta_-} = \frac{1 + \kappa \alpha_+ \alpha_- \cos\theta_+ \cos\theta_-}{4}$$

κ : correlation parameter (~ 0.8 in NLO prediction @ $\sqrt{s} = 2$ TeV)

Look at angular distribution such as $(\cos\theta_{l^+}, \cos\theta_{l^-})$ and $(\cos\theta_b, \cos\theta_{\bar{b}})$.

Physics Topics on $t\bar{t}$ spin correlation

- If correlation is observed,
 - Direct proof of $1/\Gamma_t \ll O(m_t/\Lambda_{\text{QCD}}^2)$
 - Lower bound on Γ_t
- Asymmetry in angular distribution will provide a probe into \not{P} and \not{CP} at $t\bar{t}$ production process.



Prospects for Spin Correlation at CDF Run2

- Use dilepton channel candidates in $t\bar{t}$ MC sample + backgrounds MC with CDF Run2 detector.
 - Lepton has maximum analyzing power to top spin polarization.
- For $t\bar{t}$ MC sample, prepare the sample with $\kappa = 1$ and $\kappa = -1$.
- Assume the expected numbers of signal and backgrounds from dilepton cross-section analysis at CDF Run2.

Expected distribution of $(\cos \theta_{\ell+}, \cos \theta_{\ell-})$ reconstructed with CDF detector

$t\bar{t} (\kappa = -1) + \text{bkg}$

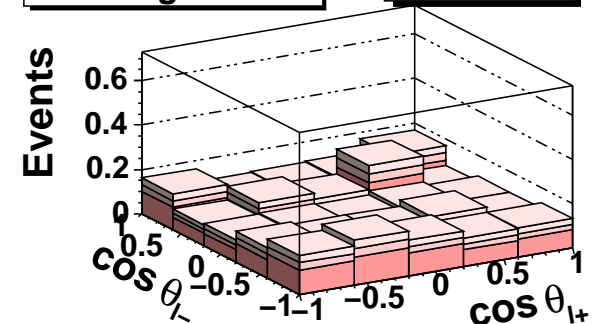
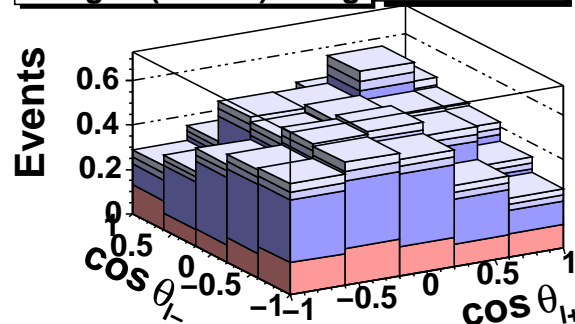
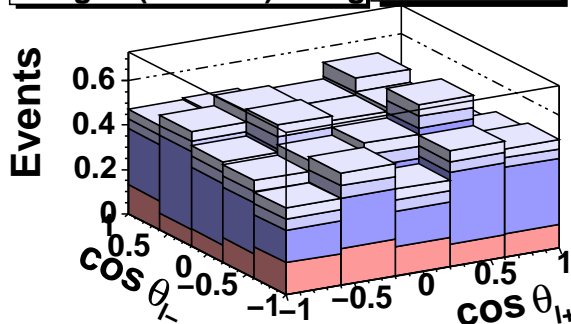
$t\bar{t} (\kappa = 1) + \text{bkg}$

$\text{bkg}(Z/\gamma^* \rightarrow \ell\ell, WW, WZ, W+\text{jets})$

$t\bar{t}$ signal($\kappa = -1.0$) + bkg Entries 10.9

$t\bar{t}$ signal($\kappa = 1.0$) + bkg Entries 10.9

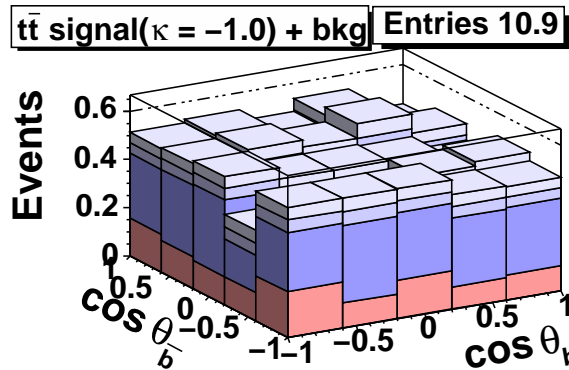
Background Entries 2.7



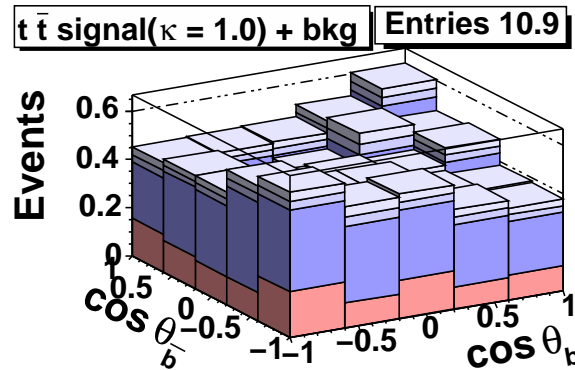
$t\bar{t}$
 $t\bar{t} + \text{Bkg. errors}$
 Bkg.
 Bkg. errors

Expected $(\cos \theta_b, \cos \theta_{\bar{b}})$ distributions

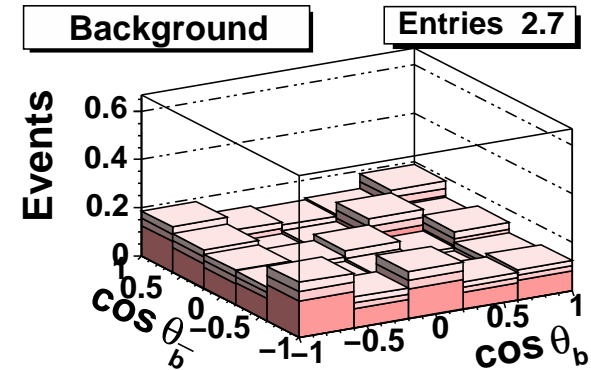
$t\bar{t}$ ($\kappa = -1$) + bkg



$t\bar{t}$ ($\kappa = 1$) + bkg



bkg

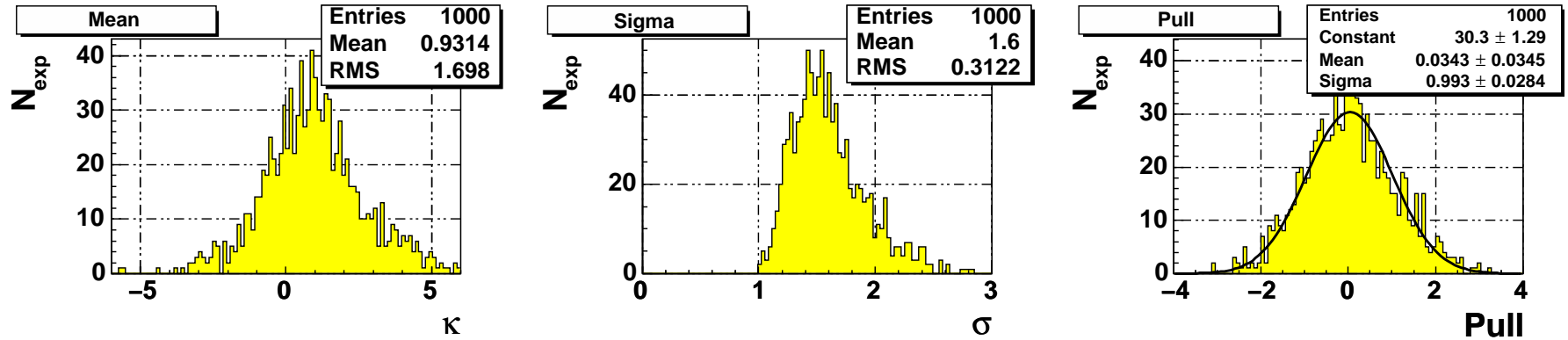


→ $(\cos \theta_b, \cos \theta_{\bar{b}})$ distribution also have sensitivity to correlation parameter κ .

- To extract correlation parameter κ , adopt binned 2D likelihood fit.
- Use $(\cos \theta_{\ell^+}, \cos \theta_{\ell^-})$ and $(\cos \theta_b, \cos \theta_{\bar{b}})$ distributions as templates.
- Perform pseudo-experiments
 - Obtain expected distribution of κ from each pseudo-experiments.

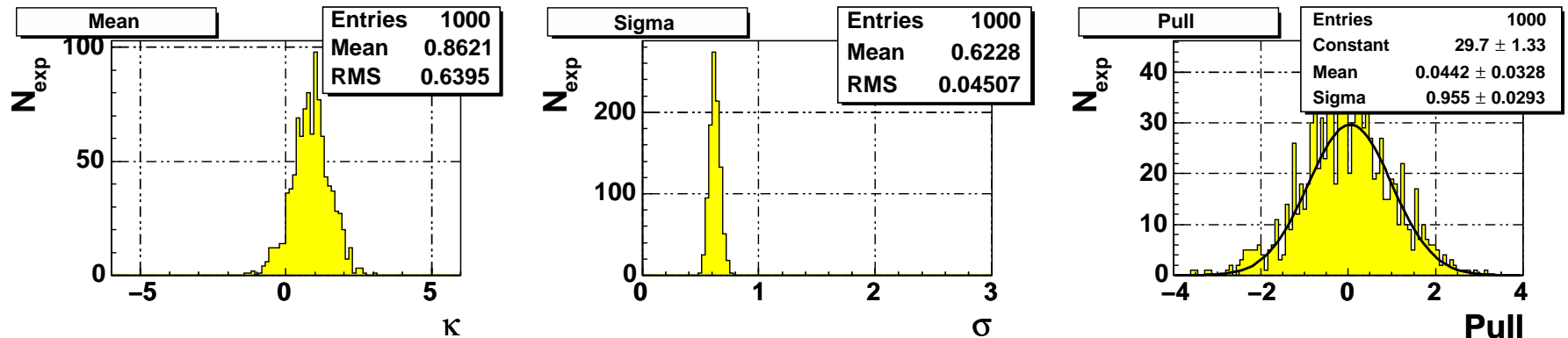
Pseudo Experiment Results

- Assume $\int \mathcal{L} dt = 340 \text{ pb}^{-1} \Rightarrow$ corresponding to $\langle N_{\text{obs}} \rangle = 19.2$
- input $\kappa = 0.88$



\Rightarrow Expected uncertainty for κ measurement is 1.6.

- Assume $\int \mathcal{L} dt = 2 \text{ fb}^{-1} \Rightarrow$ corresponding to $\langle N_{\text{obs}} \rangle = 113.0$

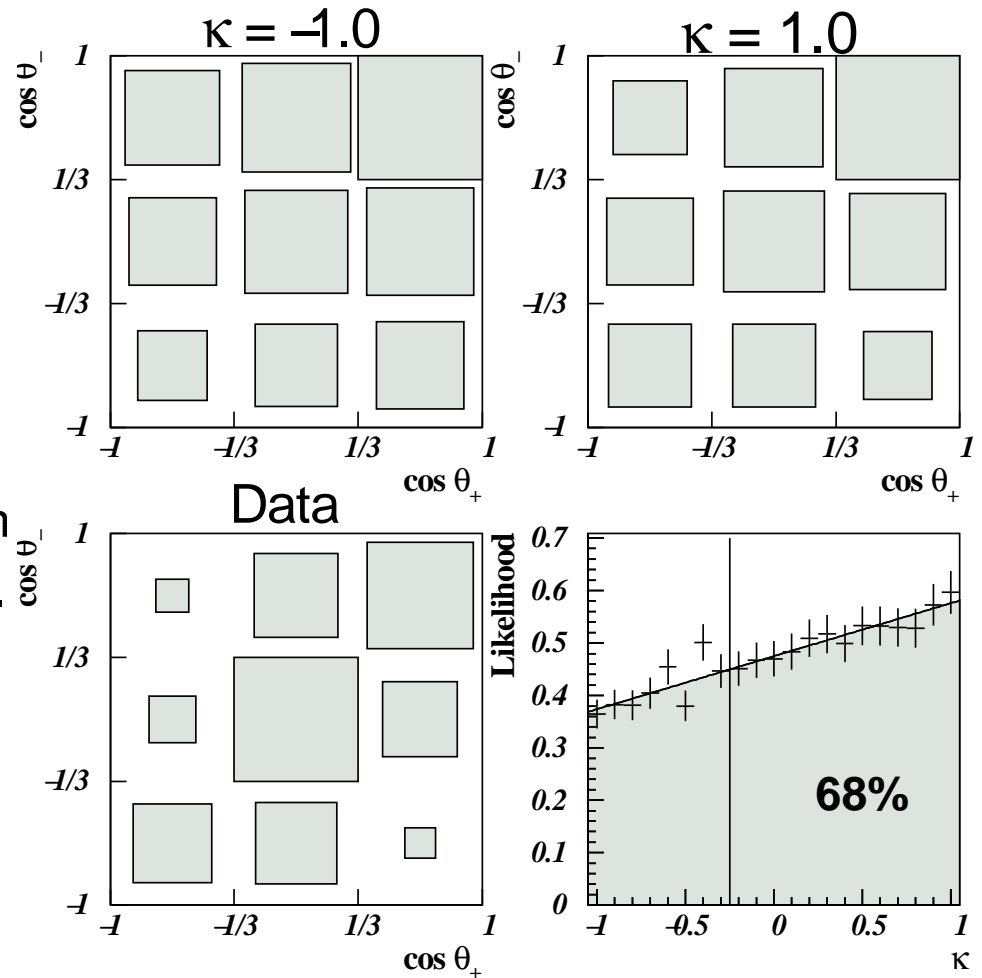


\Rightarrow Expected uncertainty for κ measurement is 0.62.

Comparing with Run1 DØ Results

Run1 DØ Results

- $\int \mathcal{L} dt = 125 \text{ pb}^{-1}$
- Based on $(\cos \theta_{\ell+}, \cos \theta_{\ell-})$ distribution from 6 candidates in dilepton channel.



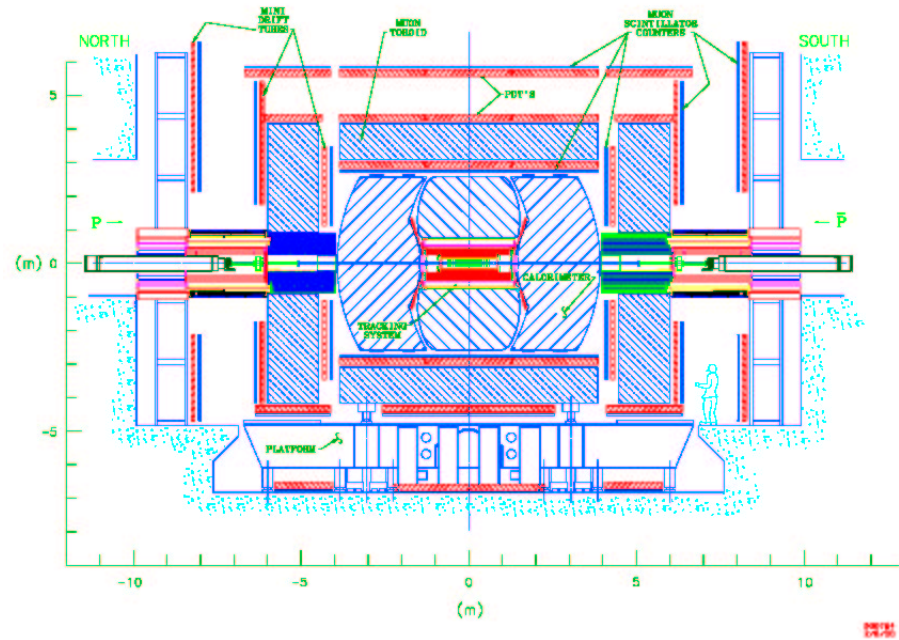
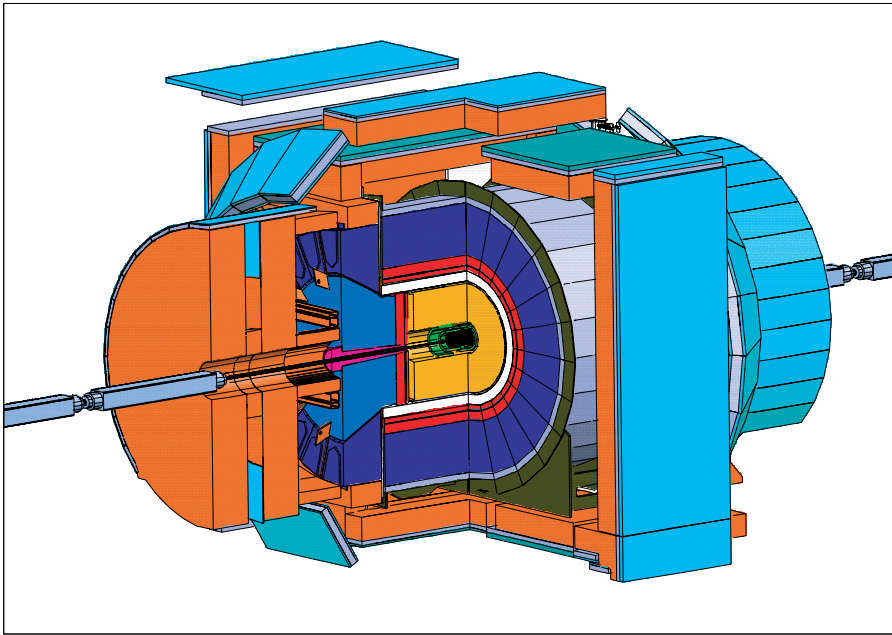
- Run1 DØ obtained $\kappa > -0.25$ (68%CL) corresponding to $\kappa = 2.3 \pm 2.5$
- CDF Run2 prospection for κ uncertainty ($1.6 @ 340 \text{ pb}^{-1}$) is improved comparing with 2.5.

Summary

- Top pair production cross-section measurements have been performed in many experimental signatures using various techniques.
- All cross-section measurements are consistent with perturbative QCD predictions so far.
 - Results based on $\int \mathcal{L} dt = 300 \sim 350 \text{ pb}^{-1}$ will coming soon.
- In the $t\bar{t}$ production at Tevatron, spin correlations can be observed.
 - Approach to Γ_t .
 - Sensitive to a new physics at $t\bar{t}$ production.
- Expected sensitivities (statistical only) to correlation parameter κ with CDF Run II detector by Monte Carlo simulations are:
 - Expected uncertainty for κ is 1.6 @ $\int \mathcal{L} dt = 340 \text{ pb}^{-1}$
 - 0.62 @ $\int \mathcal{L} dt = 2 \text{ fb}^{-1}$
- This will improve Run1 results for spin correlation.

Backups

Run 2 Detectors



CDF upgrades

- New silicon vertex detector(SVX)
- Faster tracking drift chamber(COT)
- Scintillating tile end-pulg calorimeters

DØ upgrades

- New silicon (SMT)
- Fiber tracker (CFT)
- 2T magnetic field
- Calorimeter supplemented with the preshower detectors
- Improved muon system