

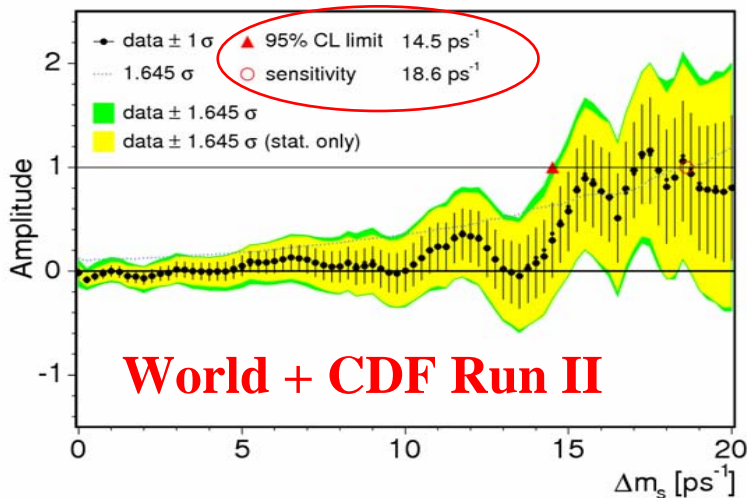
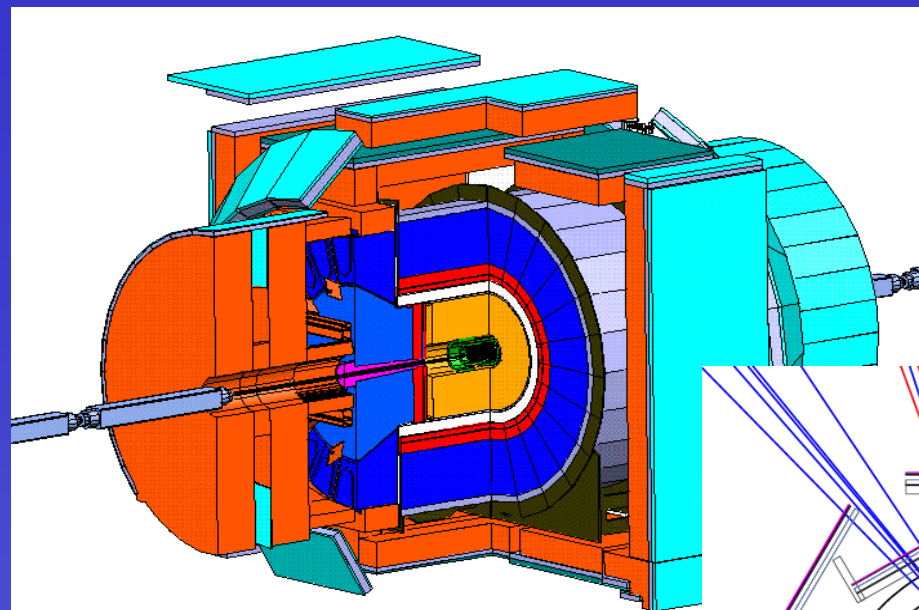
B⁰ mixing at CDF

Marco Rescigno –
INFN/Roma



Event 1191211
Muon Pt = 31 GeV
Missing Et = 69 GeV
Number of Jets = 4

- Bs Mixing predictions
- Tevatron & CDF
- CDF analysis
 - Collecting B(s)
 - Flavour Tagging
 - Measuring Δm_d
 - Δm_s limit
- Tevatron Sensitivity extrapolation



Tagged Jet 1: Et = 62 GeV, Phi = 291, L2d = 2 mm
Tagged Jet 2: Et = 40 GeV, Phi = 291, L2d = 2 mm

B⁰ Flavour Oscillations



Flavour oscillations occur through 2nd order weak interactions

$$\Delta m_q = \frac{G_F^2 m_W^2 \eta S(m_t^2 / m_W^2)}{6\pi^2} m_{Bq} f_{Bq}^2 B_{Bq} |V_{tq}^* V_{tb}|^2$$

$$\Delta m_d (\text{exp.}) = 0.510 \pm 0.005 \text{ ps}^{-1} \text{ (HFAG 2005)}$$

Lattice-QCD:

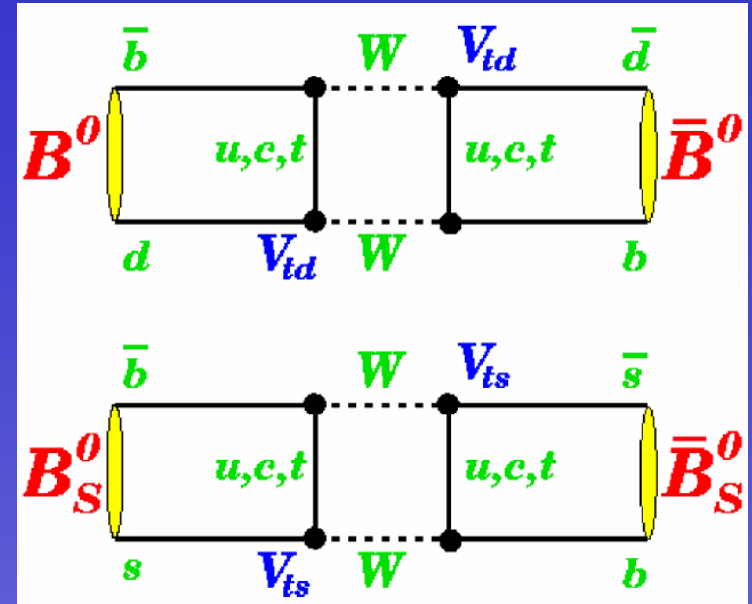
$$f_{Bd}^2 B_{Bd} = (223 \pm 33 \pm 12) \text{ MeV}$$

$$f_{Bs}^2 B_{Bs} = (276 \pm 38) \text{ MeV}$$

→ |V_{td}| determined at ~15%

But in the ratio uncertainties cancels:

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{Bs}}{m_{Bd}} \frac{f_{Bs}^2 B_{Bs}}{f_{Bd}^2 B_{Bd}} \frac{|V_{ts}|^2}{|V_{td}|^2} = \frac{m_{Bs}}{m_{Bd}} \xi^2 \frac{|V_{ts}|^2}{|V_{td}|^2}$$



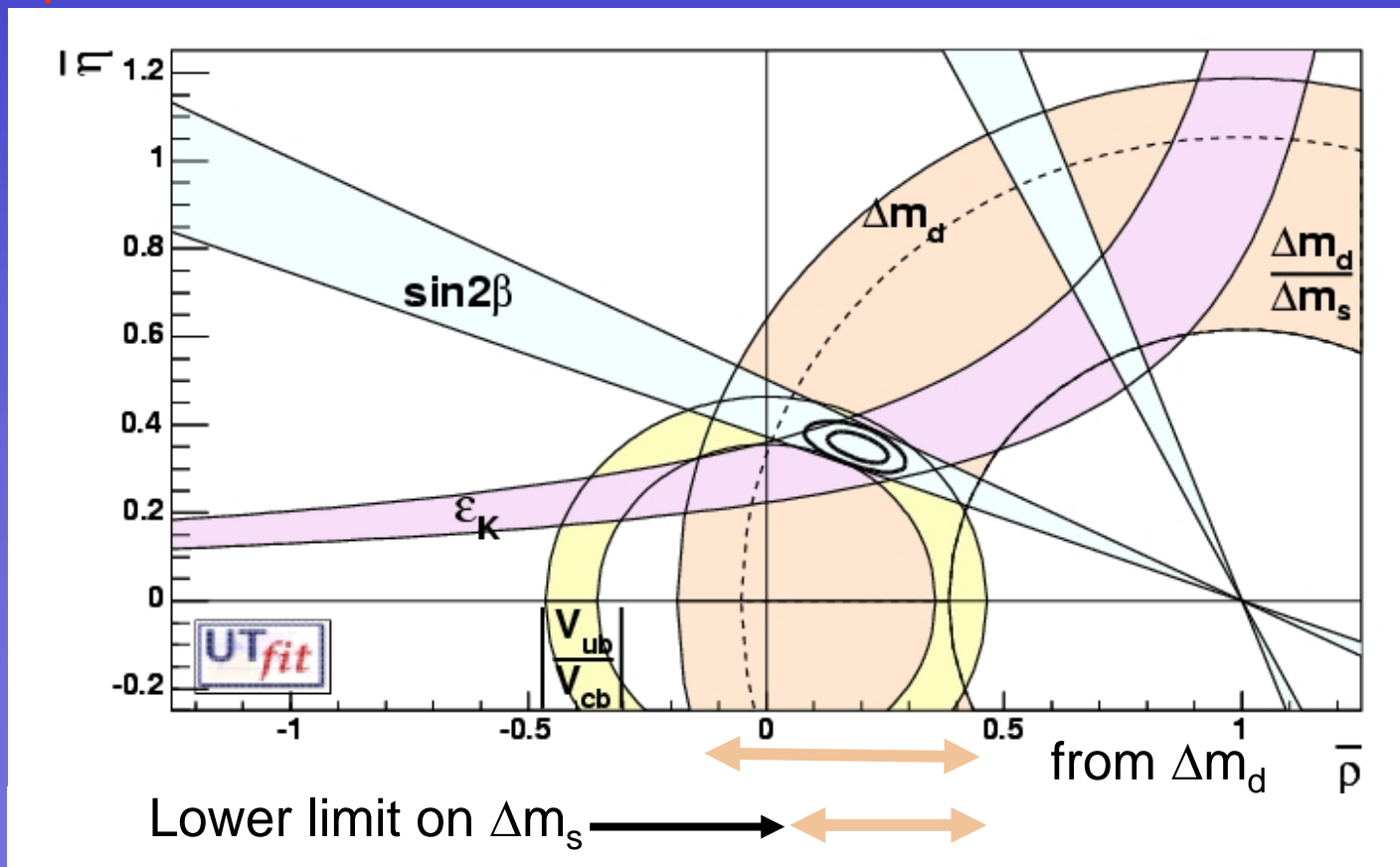
Measuring $\Delta m_s / \Delta m_d$ tests $|V_{ts}| / |V_{td}|$ with ~ 5% theory error

$$\xi = 1.24 \pm 0.04 \pm 0.06$$

Unitarity Triangle & Δm_s



- Brown Band: Δm_d measurement: $\sim 15\%$ uncertainty
- Dashed circle: lower limit on $\Delta m_s / \Delta m_d \rightarrow$ Upper Limit on $|V_{td}|$
 - The lower bound on Δm_s already gives a constraint to Unitarity Triangle
- <http://utfit.roma1.infn.it>



CKMfitter's
version

Input from
 $|V_{ub}/V_{cb}|$, Δm_d , ϵ_K , $\sin 2\beta$, $\cos 2\beta$, α and γ :

$$\Delta m_s = 20.4 \pm 2.8 \text{ ps}^{-1}$$

$$[15.1, 26.3] \text{ @ 95\% CL}$$

include also Δm_s limit:

$$\Delta m_s = 18.9 \pm 1.7 \text{ ps}^{-1}$$

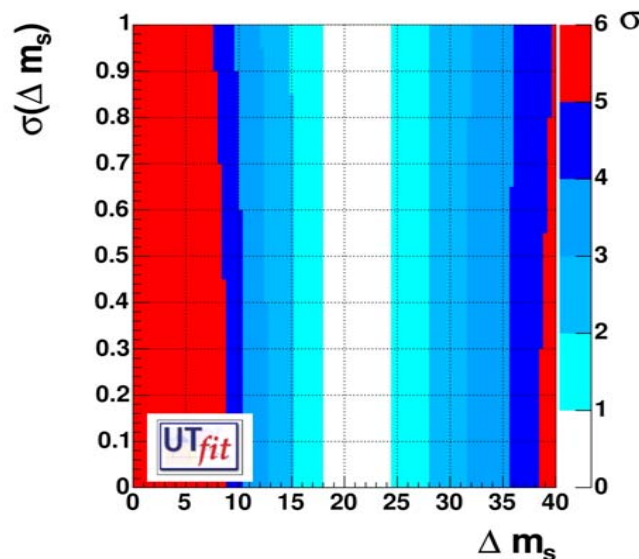
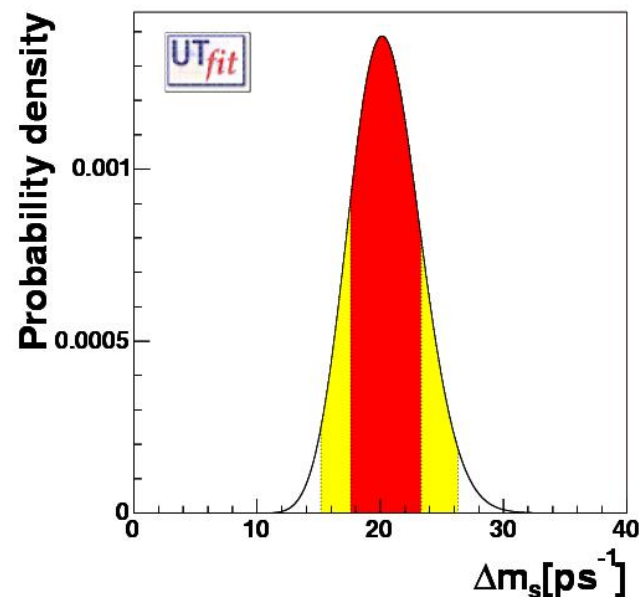
$$[15.7, 23.0] \text{ @ 95\% CL}$$

A very narrow shooting range for collider experiments!

New Physics @ 3σ for $\Delta m_s > 31 \text{ ps}^{-1}$

b-s sector much less constrained (yet) than b-d

Large New Physics contribution to B_s mixing and its phase still possible!



compatibility plot

Outline/RoadMap to Δm_s



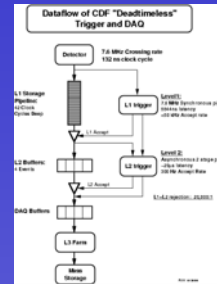
Recall: expression for significance in a mixing measurement

$$\text{Significance} = \sqrt{\frac{S \epsilon D^2}{2}} e^{-\frac{(\Delta m_s \sigma_t)^2}{2}} \sqrt{\frac{S}{S+B}}$$

5) Maximize tagging rate \times dilution²

Know your mistag rate from a Δm_d measure

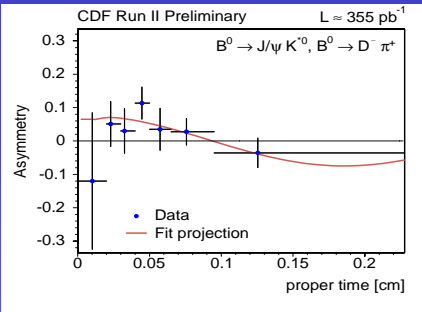
Need statistic!



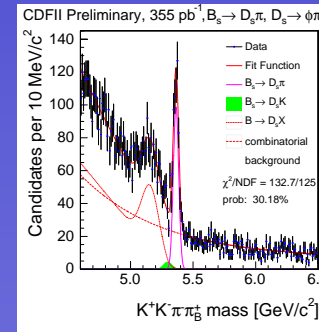
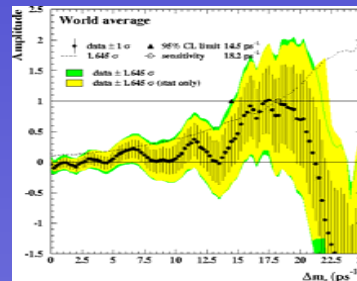
1) Trigger design to maximise Signal (S) \rightarrow highest BandWidth

Fight for your Band Width (if in a general-purpose exp.)

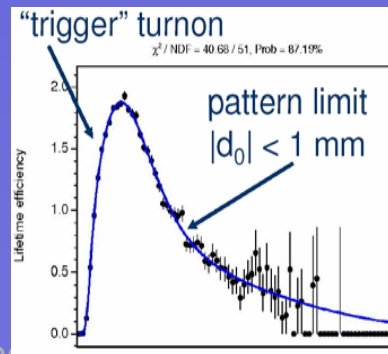
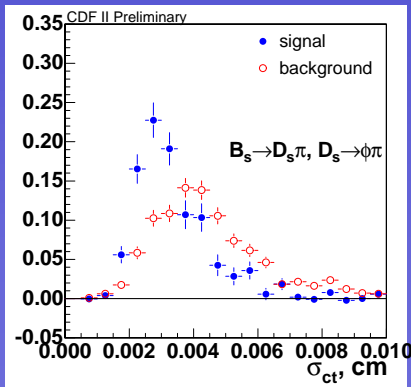
Keep your trigger alive!



Amplitude scan

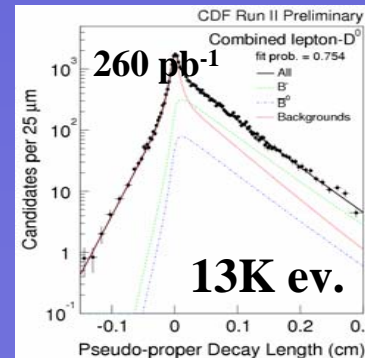


2) Good momentum (mass) and energy (!) resol. for max S/(S+B)



4) Improve σ_{ct} :

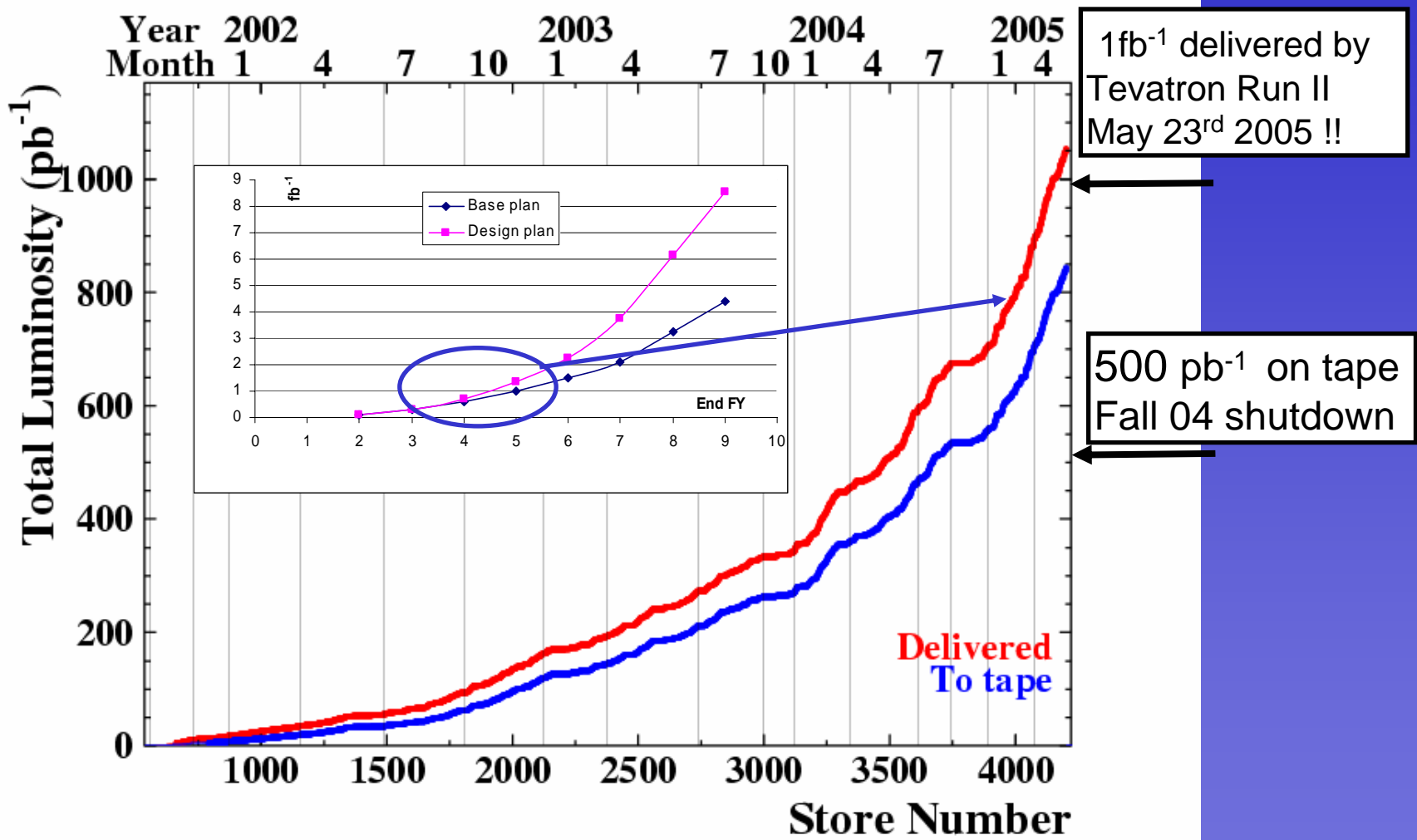
- fully reconstructed !
- L00 close to beam pipe
- Primary vertex resolution.



3) Measure τ_B on semileptonic & hadronic on multiple triggers (with/without lifetime bias)

Collecting data

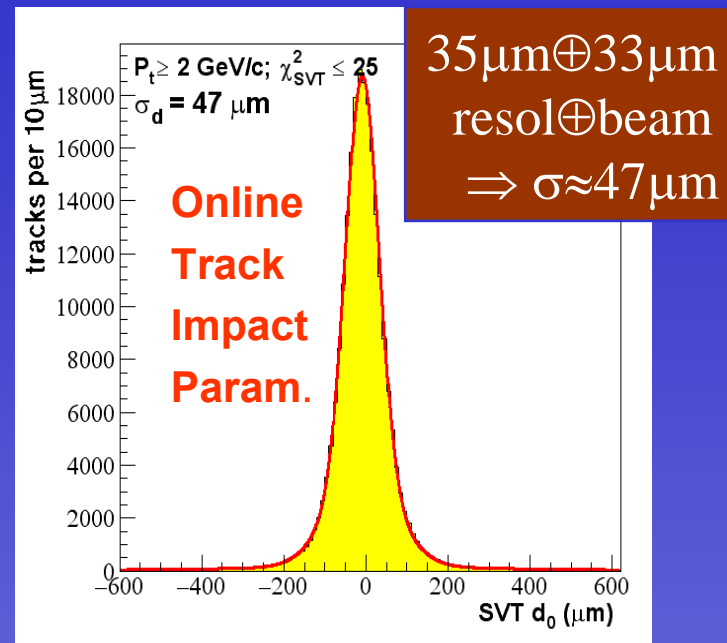
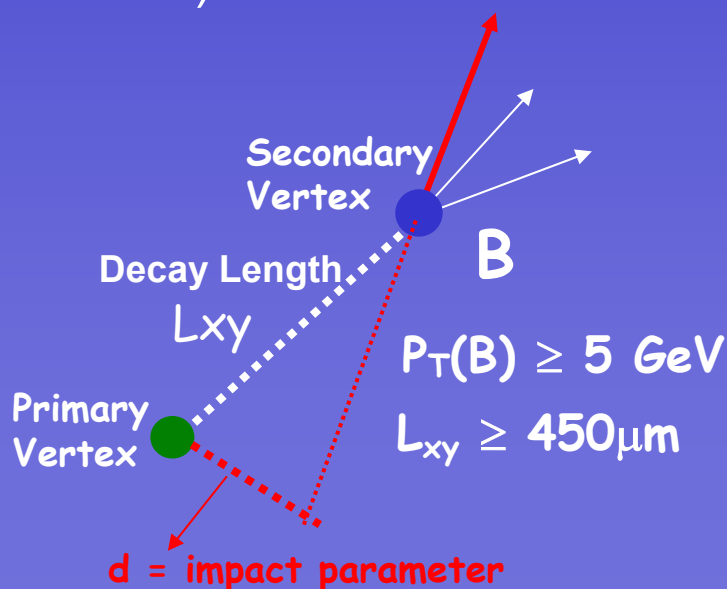
Luminosity Delivered/Recorded



Present result based on ~360 pb⁻¹

(100 pb⁻¹ lost due to drift chamber ageing problem, now solved)

- Triggering on displaced vertex at CDF using SVT main novelty in Run II, workhorse for CDF B-physics program. See at this conference:
 - Charmless decays (Donati)
 - SVT trigger (Dell'Orso)
- CDF way to get fully reconstructed decays useful for mixing (and other good stuff...)



Main Trigger requires:

- 2 opposite charge tracks,
- $P_t \geq 2 \text{ GeV}/c$,
- impact parameter $|d_0| > 120 \mu\text{m}$
- Scalar pt sum $> 5.5 \text{ GeV}/c$
- Projected decay length $L_{xy} > 200 \mu\text{m}$
- $2^\circ < \Delta\phi < 90^\circ$

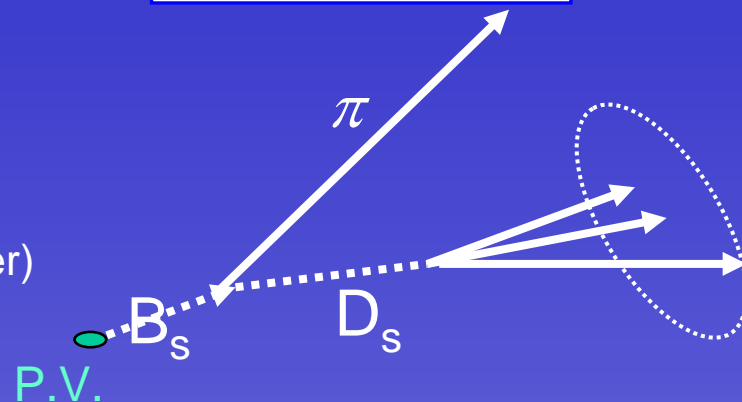
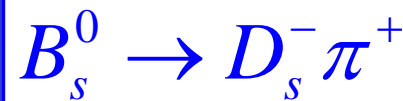
Add a dynamically prescaled LOWPT trigger with no opposite charge and no Pt sum to fill available bandwidth at low luminosity

Two different B_s signatures:



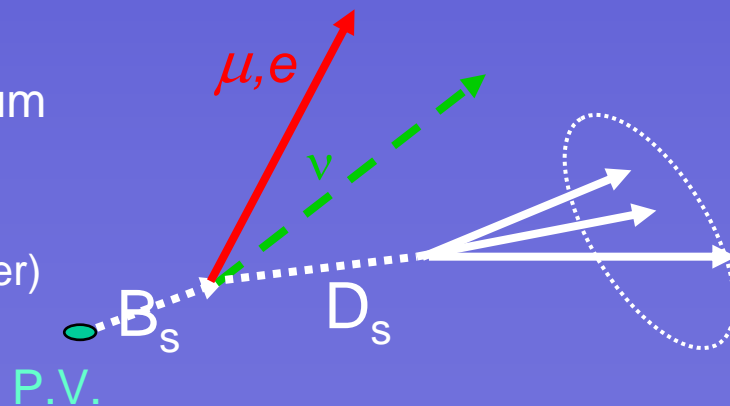
Fully reconstructed HADRONIC modes:

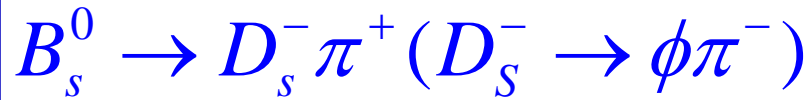
- Complete momentum reconstruction
- Good proper time resolution
- High B_s mass resolution \rightarrow high S/B
- Selected by Two Track Trigger (SVT)
 - Two displaced tracks (w large SVT Impact parameter)
- LOW statistics (useful BR)
- Demanding on L1 B/W: >30 KHz @ $1E32\text{cm}^{-2}\text{s}^{-1}$
 ~ 10 KHz @ $5E31\text{cm}^{-2}\text{s}^{-1}$



Partially reconstructed SEMILEPTONIC modes:

- Missing momentum carried by the ν
- Visible proper time corrected from MC (K factor)
- Proper time resolution diluted by missing momentum
- Cannot reconstruct B_s mass \rightarrow different S/B
- Selected by dedicated trigger (I+SVT):
 - One displaced tracks (w large SVT Impact parameter)
 - One Lepton μ, e ($p_T > 4$ GeV/c)
- HIGH statistics and well behaved trigger





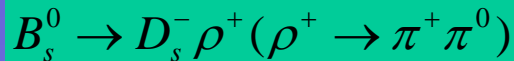
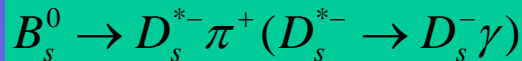
CDFII Preliminary, 355 pb^{-1} , $B_s \rightarrow D_s \pi$, $D_s \rightarrow \phi \pi$

$$N_{B_s} = 526 \pm 33$$

$$S/B \sim 2$$

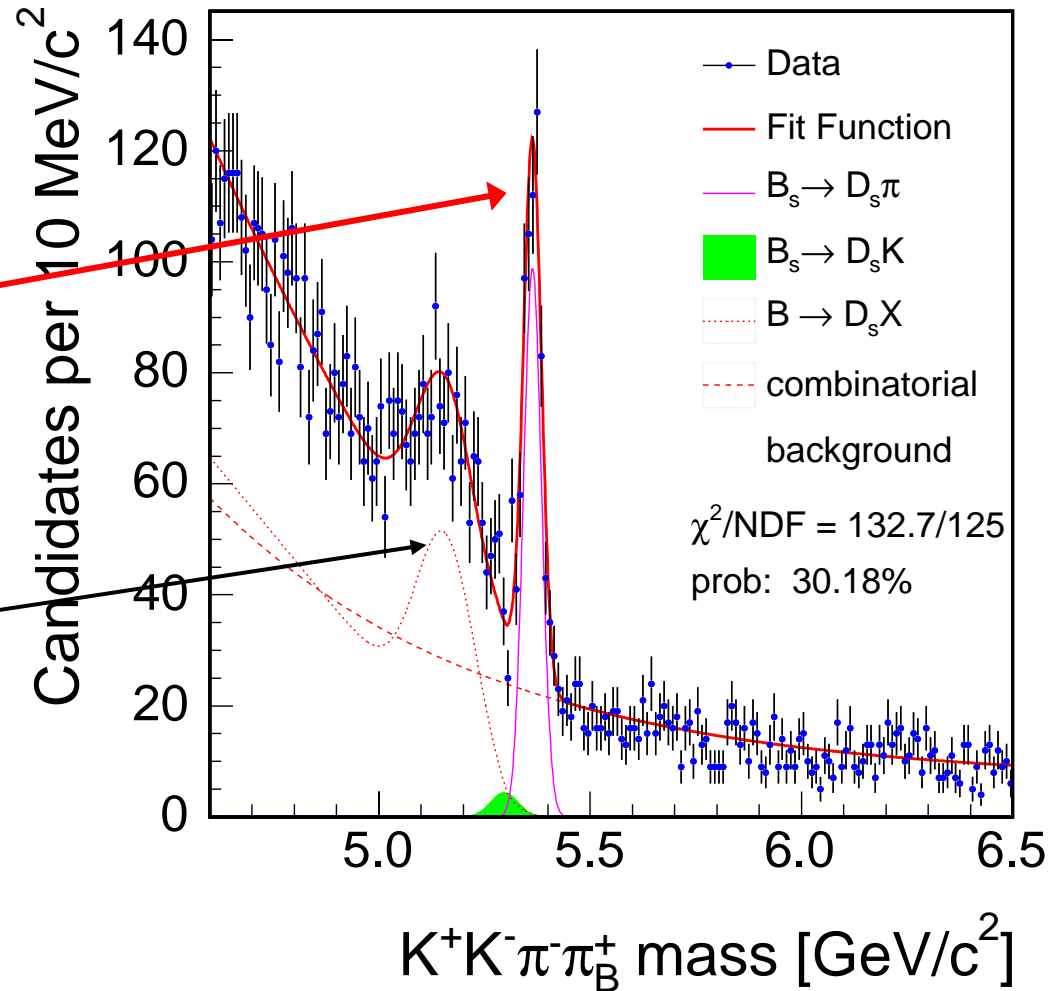
$$\sigma_M \approx 15 \text{ MeV}$$

“Satellites”:



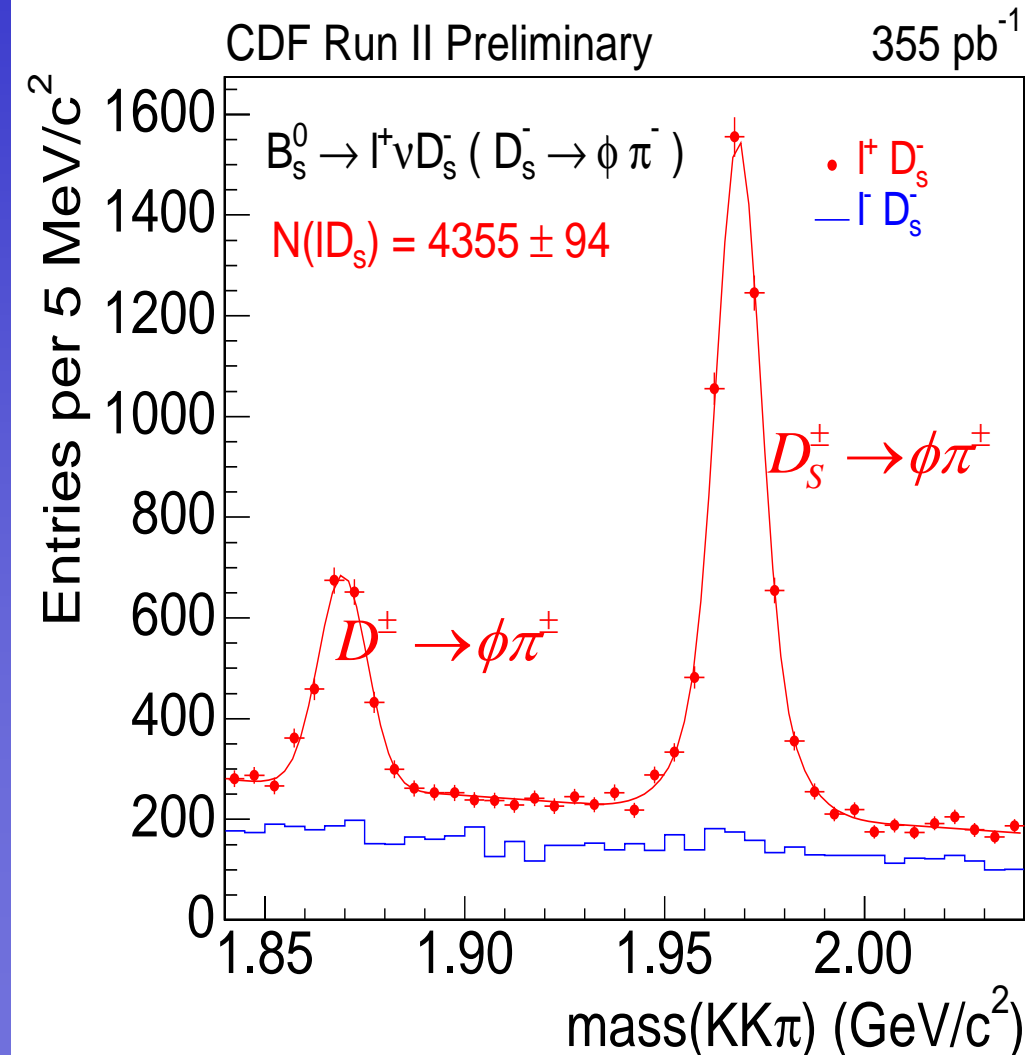
(Not used in this analysis)

Other signals:



$$B_s^0 \rightarrow D_s^- l^+ \nu X \quad (D_s^- \rightarrow \phi \pi^-)$$

- Missing $P_T \rightarrow$ No B_s mass peak
- Use D_s mass signals
- Charge correlation between l and D_s
 - $l^+ D_s^-$: “Right-sign” = **signal**
 - $l^- D_s^-$: “Wrong-sign” = **background**
- Right-sign peak is not pure signal
 - ~20% background:
 - » D_s + fake lepton from primary
 - » $B^0, B^+ \rightarrow D_s D X$ with $D \rightarrow l \nu X$
 - » $c\bar{c}$ backgrounds



(S/B)

$B_s \rightarrow D_s \pi ; D_s \rightarrow \phi \pi$	526 ± 33 (1.8)
$B_s \rightarrow D_s \pi ; D_s \rightarrow K^* K$	254 ± 21 (1.7)
$B_s \rightarrow D_s \pi ; D_s \rightarrow \pi \pi \pi$	116 ± 18 (1.0)
$B^+ \rightarrow D^0 \pi^+ ; D^0 \rightarrow K \pi$	~ 6200
$B^0 \rightarrow D^{*+} \pi^- ; D^{*+} \rightarrow D^0 \pi^+$	~ 2800
$B^0 \rightarrow D^+ \pi^- ; D^+ \rightarrow K \pi \pi$	~ 5600

Hadronic B_s modes
~900 events

$O(10^4)$ B^0/B^+ calibration modes

Semileptonic B_s modes
~7700 events

$O(10^5)$ B^0/B^+ calibration modes

(S/B)

$B_s \rightarrow \ell D_s ; D_s \rightarrow \phi \pi$	4355 ± 94 (3.1)
$B_s \rightarrow \ell D_s ; D_s \rightarrow K^* K$	1750 ± 83 (0.4)
$B_s \rightarrow \ell D_s ; D_s \rightarrow \pi \pi \pi$	1573 ± 88 (0.3)
$B^+ \rightarrow \ell D^0 ; D^0 \rightarrow K \pi$	$\sim 100K$
$B^0 \rightarrow \ell D^{*+} ; D^{*+} \rightarrow D^0 \pi^+$	$\sim 25K$
$B^0 \rightarrow \ell D^+ ; D^+ \rightarrow K \pi \pi$	$\sim 52K$

Measuring ct

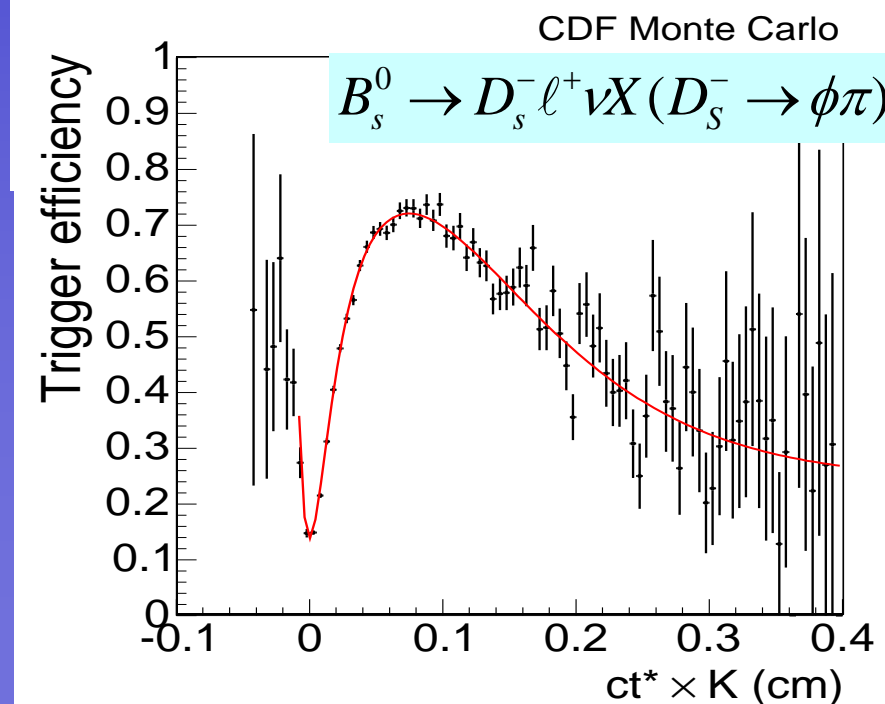
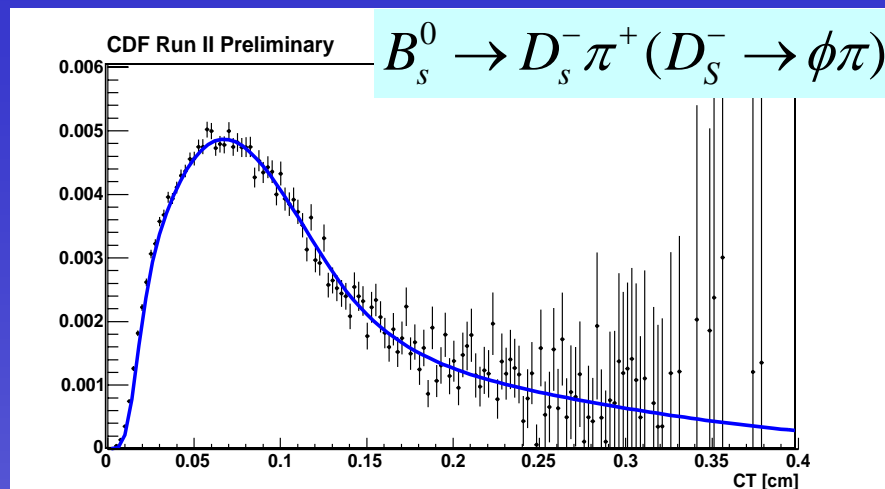
Extract proper time at decay from B flight distance in the transverse plane:

$$ct = \frac{L}{\beta\gamma} = L_{xy} \times \frac{m(B)}{p_T(B)}$$

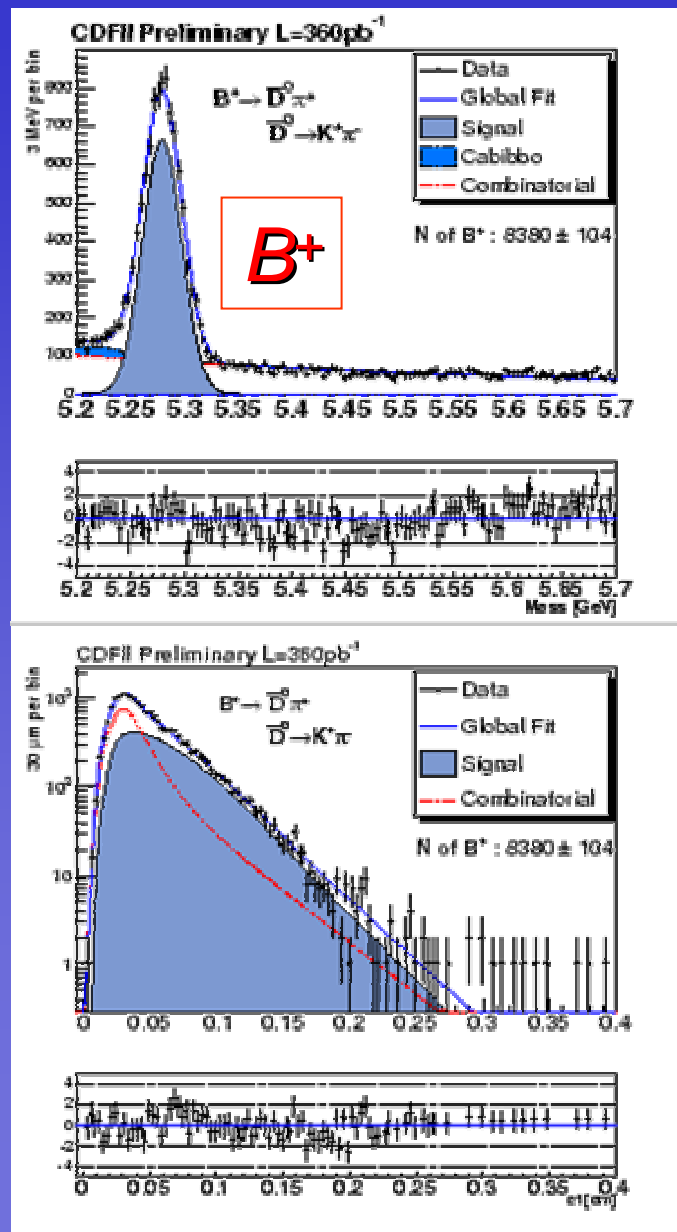
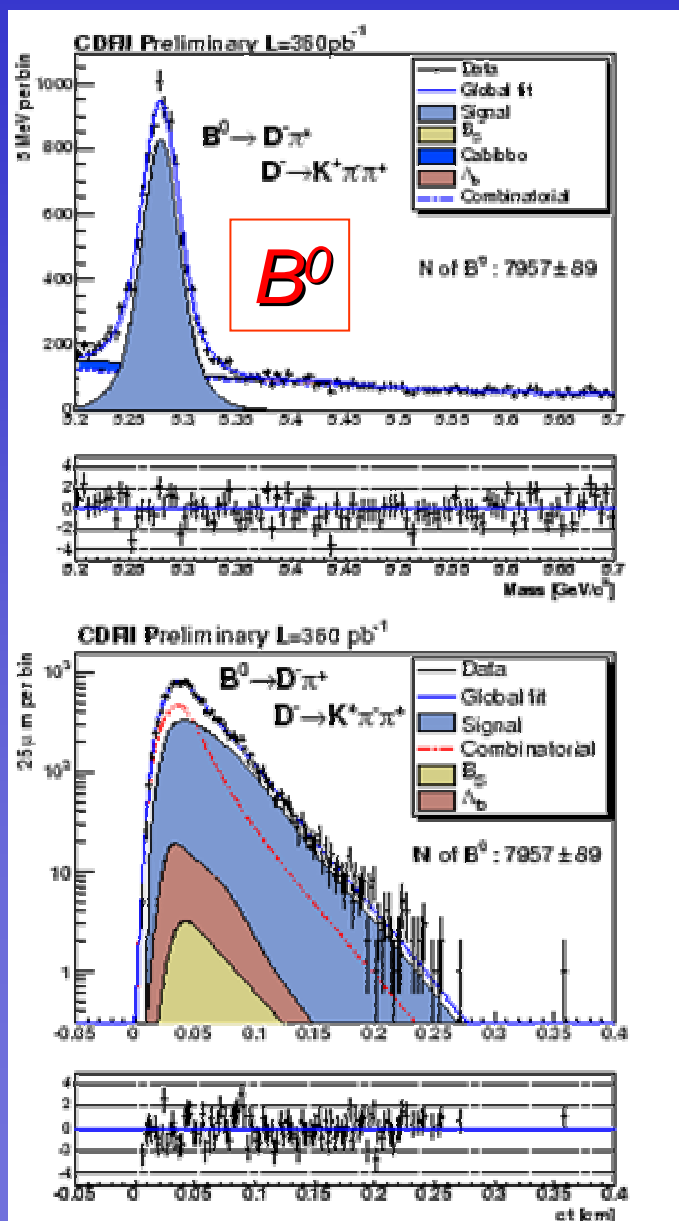
Two complications:

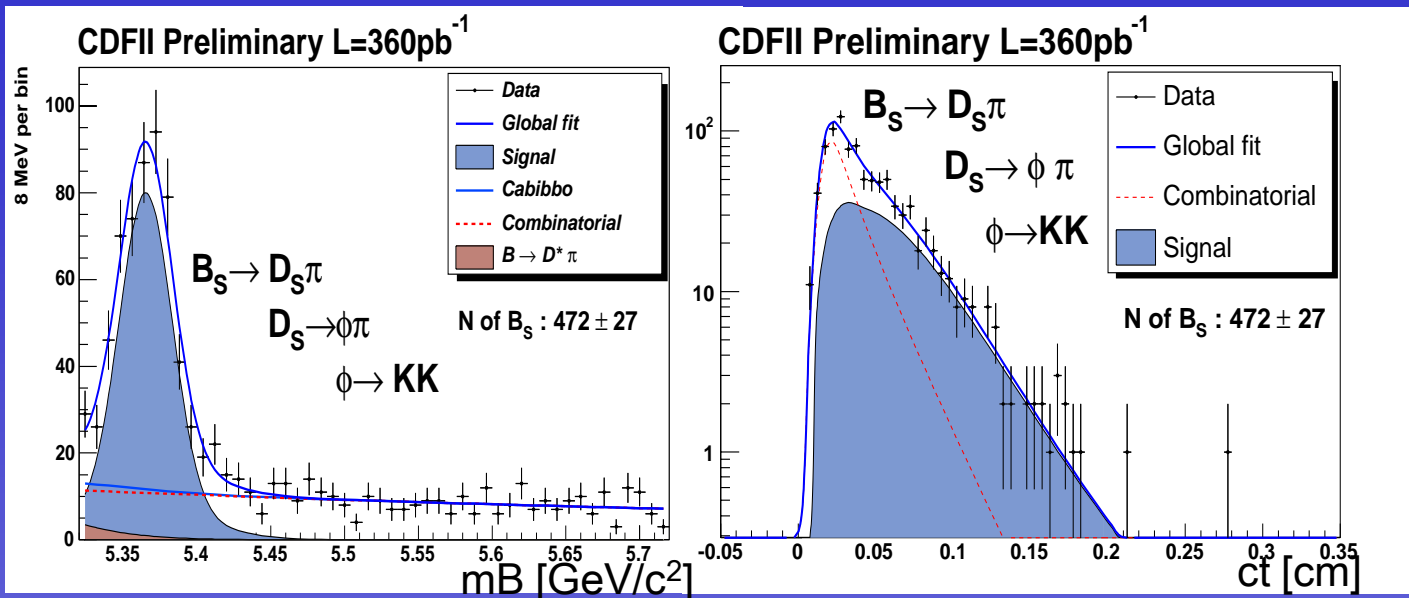
1. Trigger bias on L_{xy}
2. Correct for missing ν in semileptonic

- Trigger and reconstruction requirements affect L_{xy}
 - Trigger (impact parameter) cuts at low ct
 - SVT acceptance at high ct
- “ ct ” efficiency from Monte-Carlo:
 - B production/decay model
 - detailed Trigger/Detector simulation
- Test with high-statistic B^0/B^+ samples



B^0 and B^+ hadronic modes $c\tau$





\pm (stat) \pm (syst)

$\tau(B^+) = 1.661 \pm 0.027 \pm 0.013$ ps
 $\tau(B^0) = 1.511 \pm 0.023 \pm 0.013$ ps
 $\tau(B_S) = 1.598 \pm 0.097 \pm 0.017$ ps

HFAG 04 average

$\tau(B^+) = 1.653 \pm 0.014$ ps
 $\tau(B^0) = 1.534 \pm 0.013$ ps
 $\tau(B_S) = 1.469 \pm 0.059$ ps

SVT bias
syst. small

Systematic summary [%]

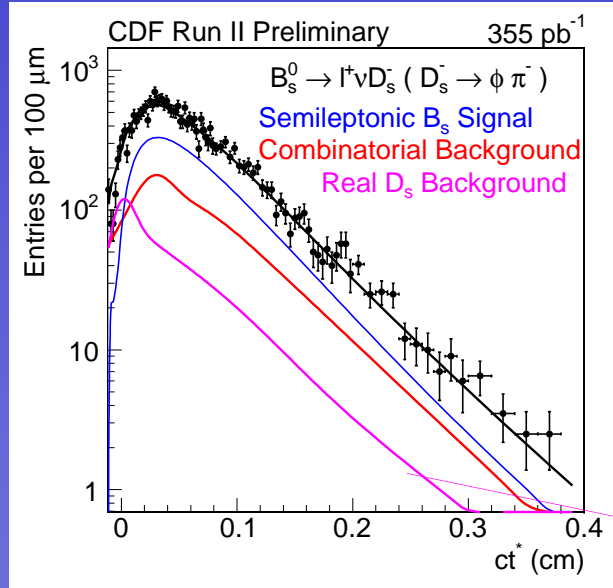
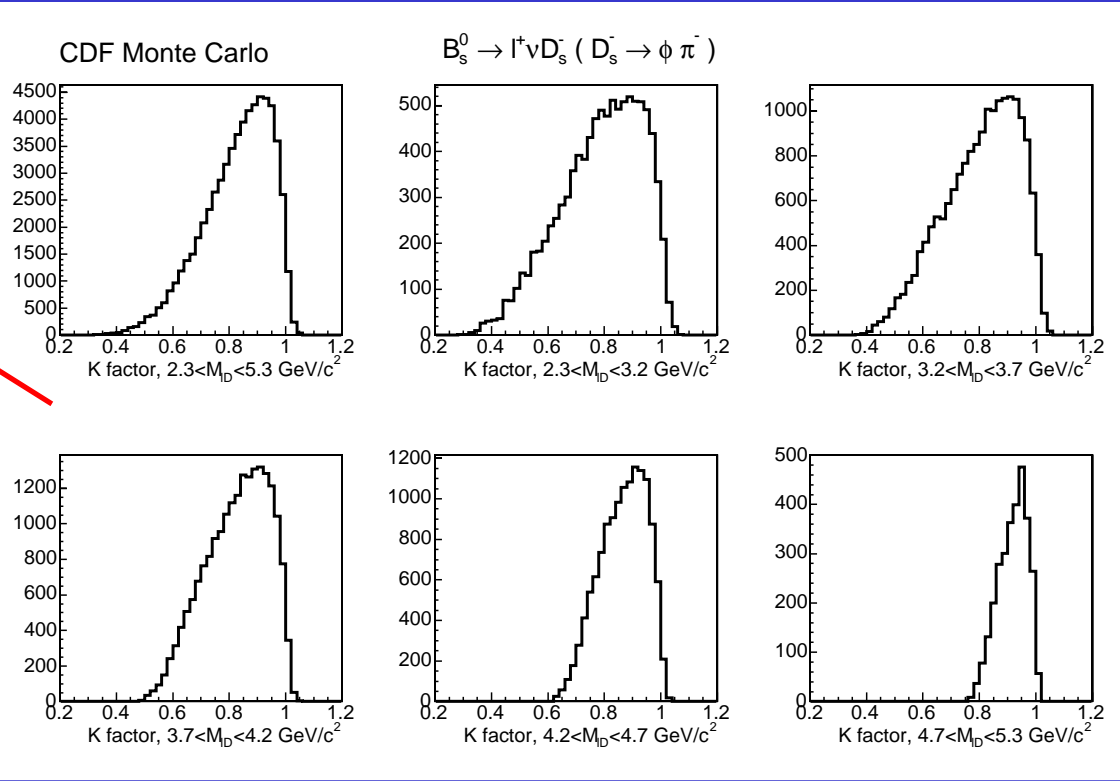
Effect	Variation (μm)	
	B^0	B_S
MC input $c\tau$	negligible	negligible
p_T reweight	1.9	1.9
Scale Factor	negligible	negligible
Bkg ct description	1.1	1.1
Bkg fraction	2.0	2.0
I.P. correlation	1.0	1.0
Eff. parameterization	1.5	1.5
L_{xy} significance	negligible	2
$\Delta\Gamma_s$	-	1.0
Alignm. + others	2.4	2.4
Total	4.2	4.7

Semileptonic B_s Modes Lifetime



Introduce K factor = $p(\ell D_s)/p(B)$
to account for missing ν

$$ct^* = L_{xy} \times \frac{m(B)}{p_T(\ell D_s)} \otimes K$$



Real D_s backgrounds: prompt and physics

$$\tau = 1.521 \pm 0.040 \text{ ps}$$

Combined ℓ - D_s lifetime result: $1.477 \pm 0.032 \text{ ps}$ *stat. err. only (analysis ongoing)*
 HFAG '05 flavour specific: $1.472 \pm 0.045 \text{ ps}$ (DØ '05 D_s !): $1.420 \pm 0.043 \pm 0.057 \text{ ps}$

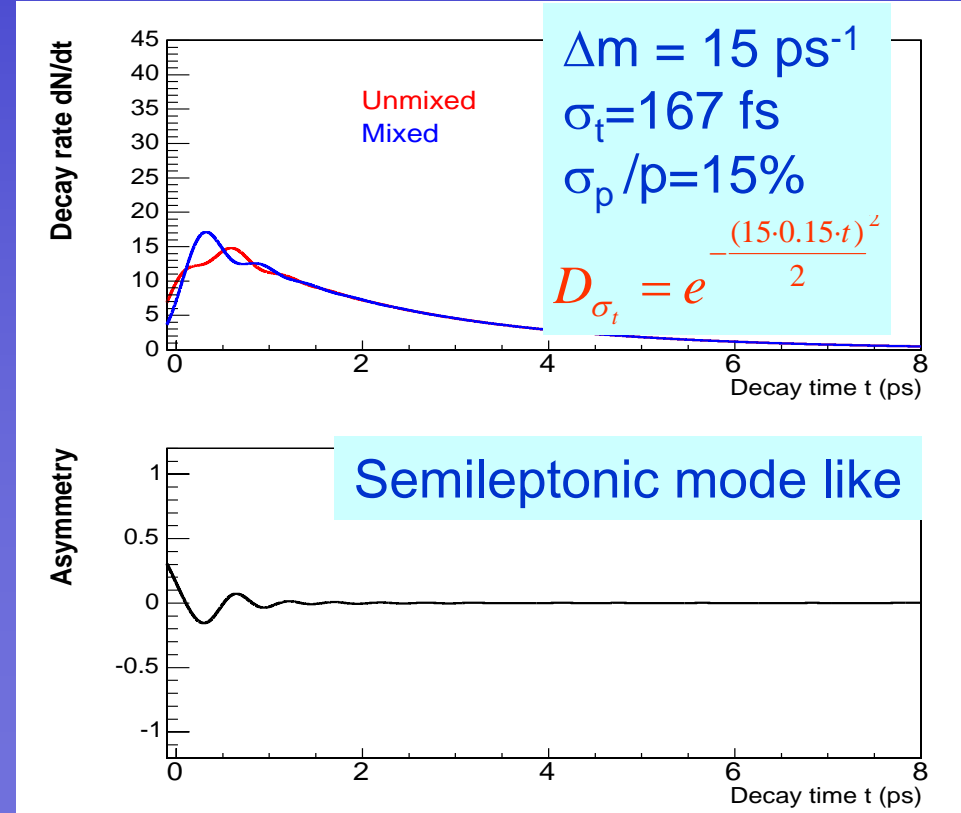
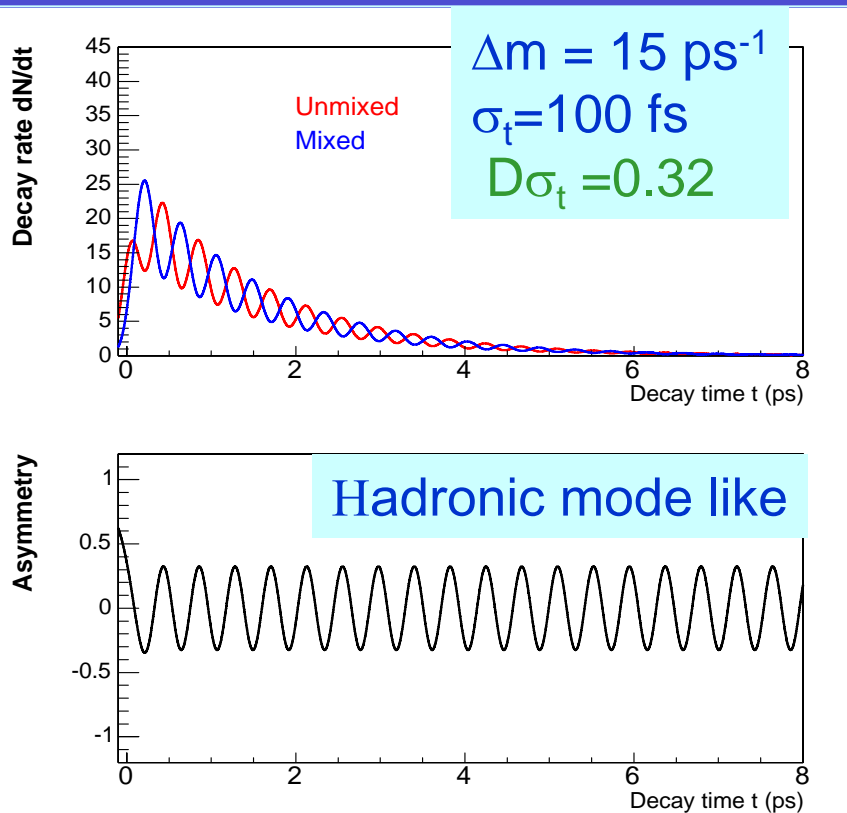
- The amplitude of mixing asymmetry is diluted by a factor

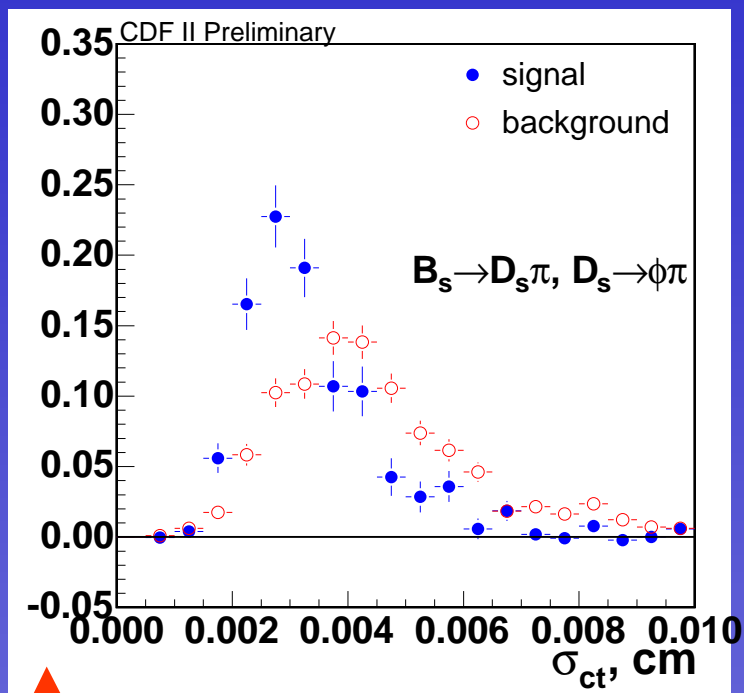
$$D_{\sigma_t} = e^{-\frac{(\Delta m \cdot \sigma_t)^2}{2}}$$

$$\sigma_{ct} = \sqrt{(\sigma_{ct}^0)^2 + \left(ct \times \frac{\sigma_p}{p}\right)^2}$$

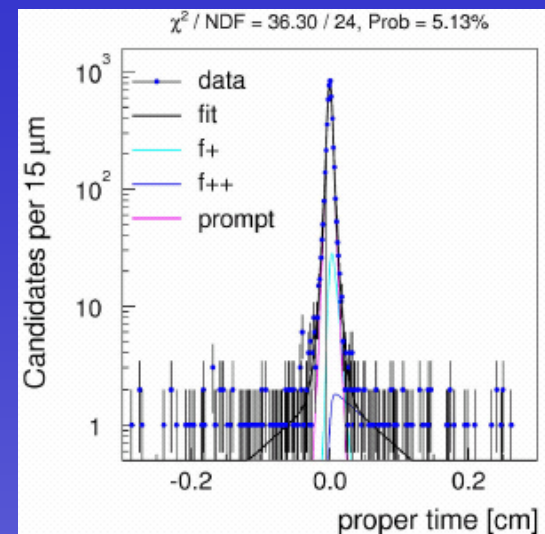
Vertex
resolution
(constant)

Momentum
resolution
(proportional to ct)





Huge prompt
(90%) D_s + track
sample to correct
 σ_{ct} error calculation
and parameterize
as a function of
several variables.

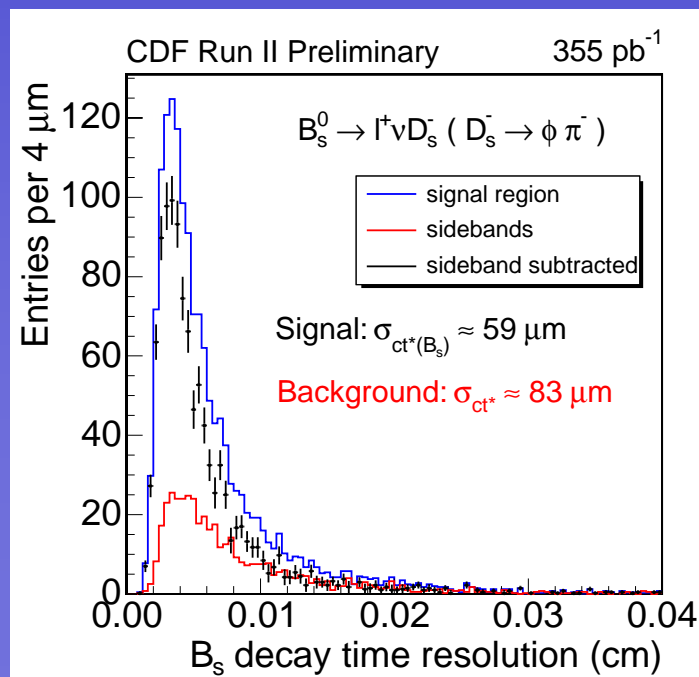


• **Hadronic:**

- $\langle \sigma_{ct}^0 \rangle$: $\sim 30 \mu\text{m}$ (100 fs)
- $\sigma_p/p < 1\%$

• **Semileptonic**

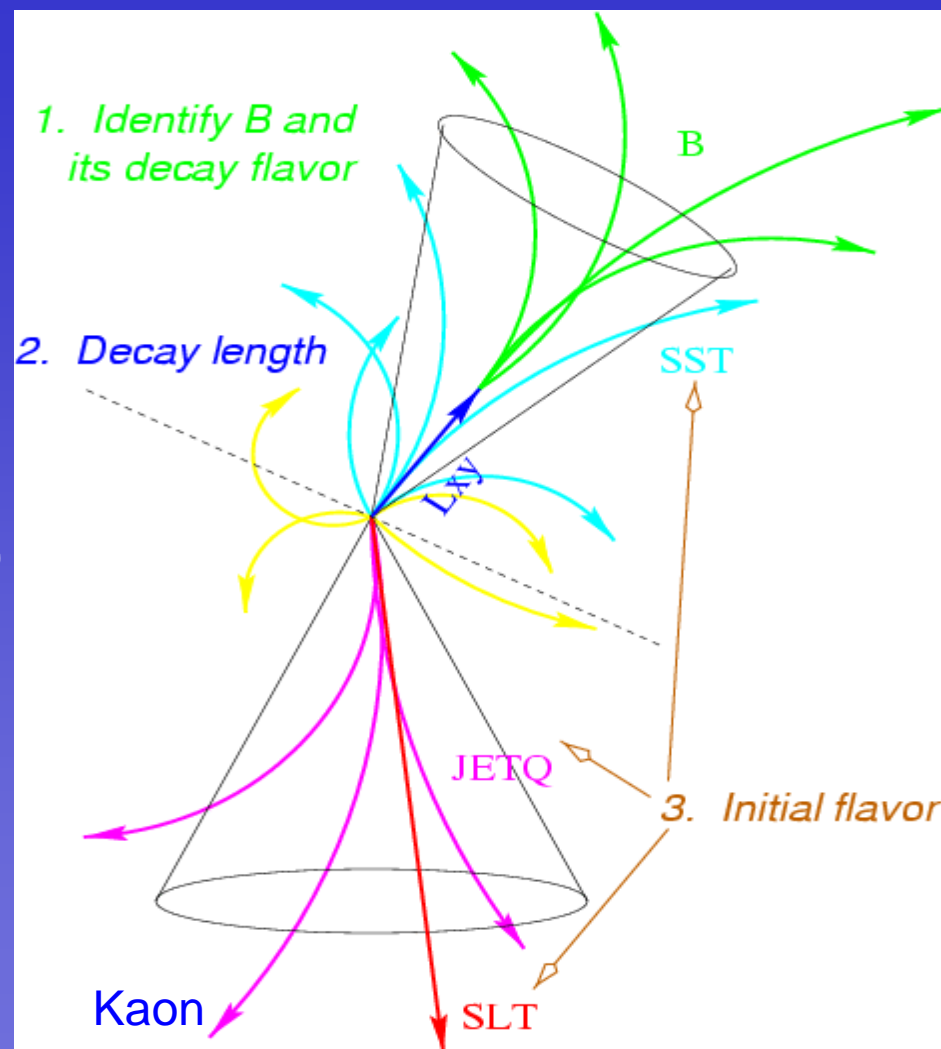
- $\langle \sigma_{ct}^0 \rangle$: $\sim 50 \mu\text{m}$ (167 fs)
- $\sigma_p/p \sim 15\%$ (K factor due to missing neutrino)



Flavour Tagging

- Same side tagging
 - Use fragmentation track
 - B^0 , B^+ , and B_s are different
 - Kaon around B_s : PID is important (more at the end of the talk)

- Opposite side tagging (5 algo)
 - Use the other B in the event
 - Semileptonic decay ($b \rightarrow l^-$)
 - (1) Muon, (2) Electron
 - Use jet charge ($Q_b = -1/3$)
 - (3) Jet has 2ndary vertex
 - (4) Jet contains displaced track
 - (5) Highest momentum Jet



Used only Opposite Side Tags so far for B_s

- Need high stat. sample to develop and calibrate tagging algorithm:



- Use inclusive semileptonic decays from the lepton+track trigger ($>10^6$ events)
 - Lepton charge gives “true” B flavour
 - Tag the other b

- High purity reached after lepton+track mass cut applied

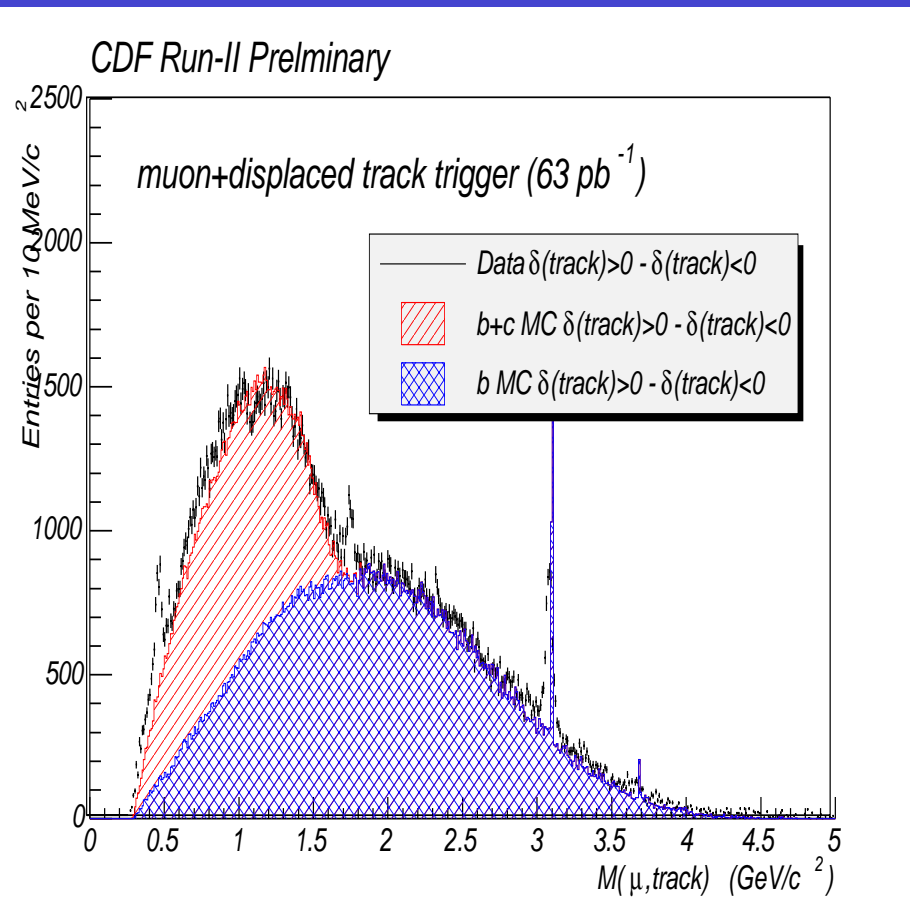
- Statistical Power of a tag: εD^2

- Tagging efficiency (ε)
- Tagging dilution ($D = 1-2w$)
 - w = mistag rate

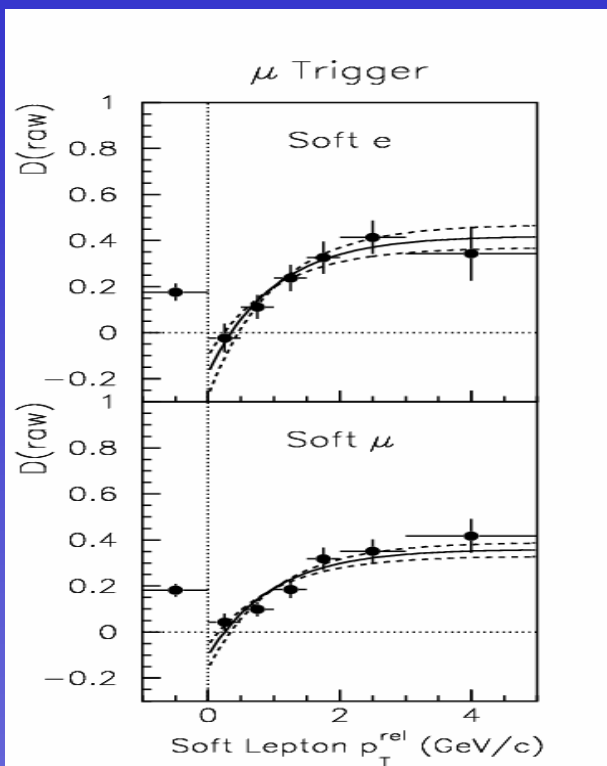
- Parameterize dilution as a function of relevant variables and weight events with their event-by-event dilution

- Dividing events into different classes based on tagging power improves combined εD^2

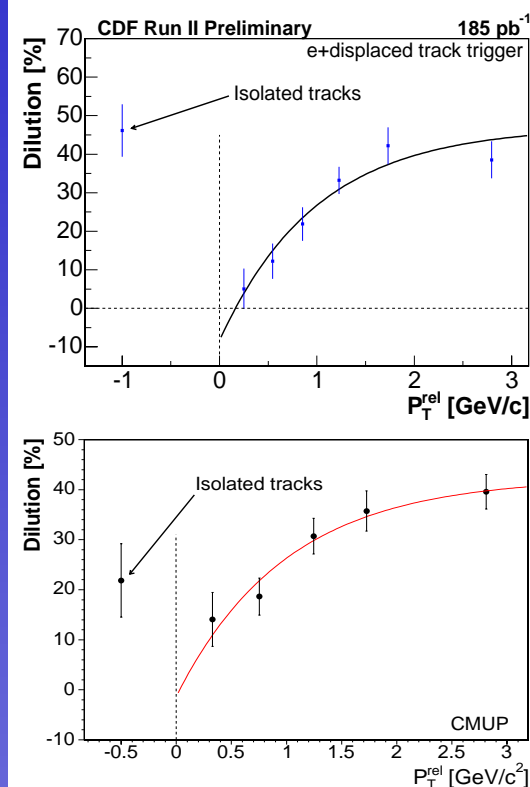
- Calibration of the tagger performance requires high statistics!



Run I



Run II



Likelihood based electron and muon ID

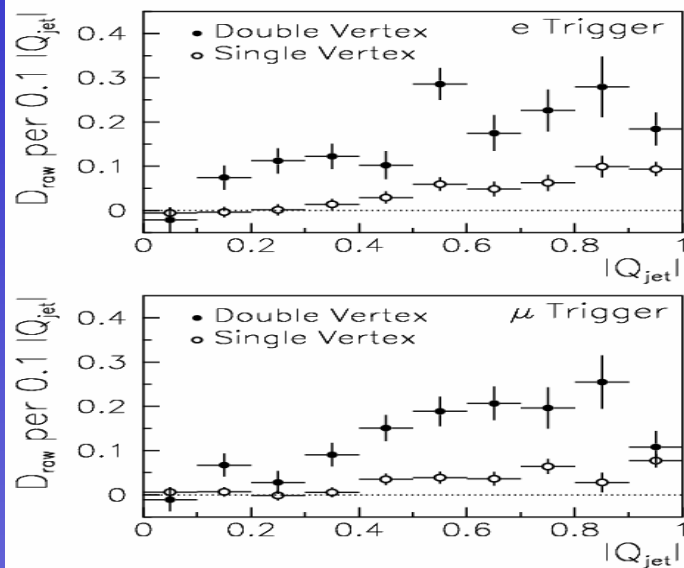
Using combination of calorimeter, muon detector, dE/dx info

Similar performance as in Run I ($\epsilon D^2 = 0.9 \pm 0.1$ %)

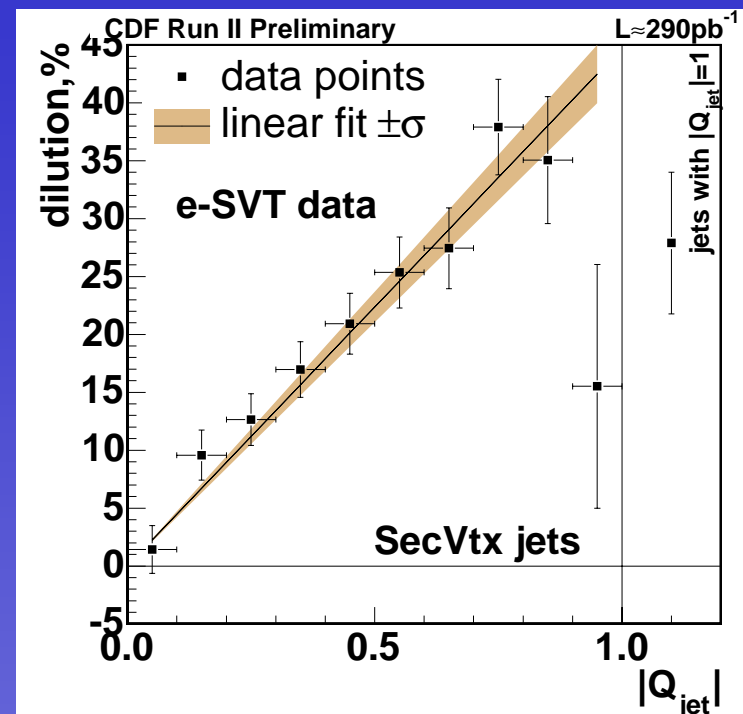
$D_{\max} \sim 0.4 \rightarrow 30\%$ mistag rate

Tag type	ϵD^2 (%)
Muon	$(0.70 \pm 0.04)\%$
Electron	$(0.37 \pm 0.03)\%$
2ndary vtx	$(0.36 \pm 0.02)\%$
Displaced track	$(0.36 \pm 0.03)\%$
Highest p jet	$(0.15 \pm 0.01)\%$
Total (exclusive)	$\sim 1.6\%$

Run I



Run II



Cone based jet algorithm: compute Jet Charge of

- Secondary Vertex tagged jets
- Jet Probability tagged jet
- Highest P jet

Similar performance as in Run I ($\epsilon D^2 = 0.8 \pm 0.1$ %)

$D_{\max} \sim 0.4 \rightarrow 30\%$ mistag rate

Tag type	ϵD^2 (%)
Muon	$(0.70 \pm 0.04)\%$
Electron	$(0.37 \pm 0.03)\%$
2ndary vtx	$(0.36 \pm 0.02)\%$
Displaced track	$(0.36 \pm 0.03)\%$
Highest p jet	$(0.15 \pm 0.01)\%$
Total (exclusive)	$\sim 1.6\%$

- Validation of the flavor tag calibration using B^0 and B^+ sample
 - $B^0 \rightarrow D\pi$, $B^+ \rightarrow D^0\pi$
 - $B^0 \rightarrow J/\psi K^{*0}$, $B^+ \rightarrow J/\psi K$

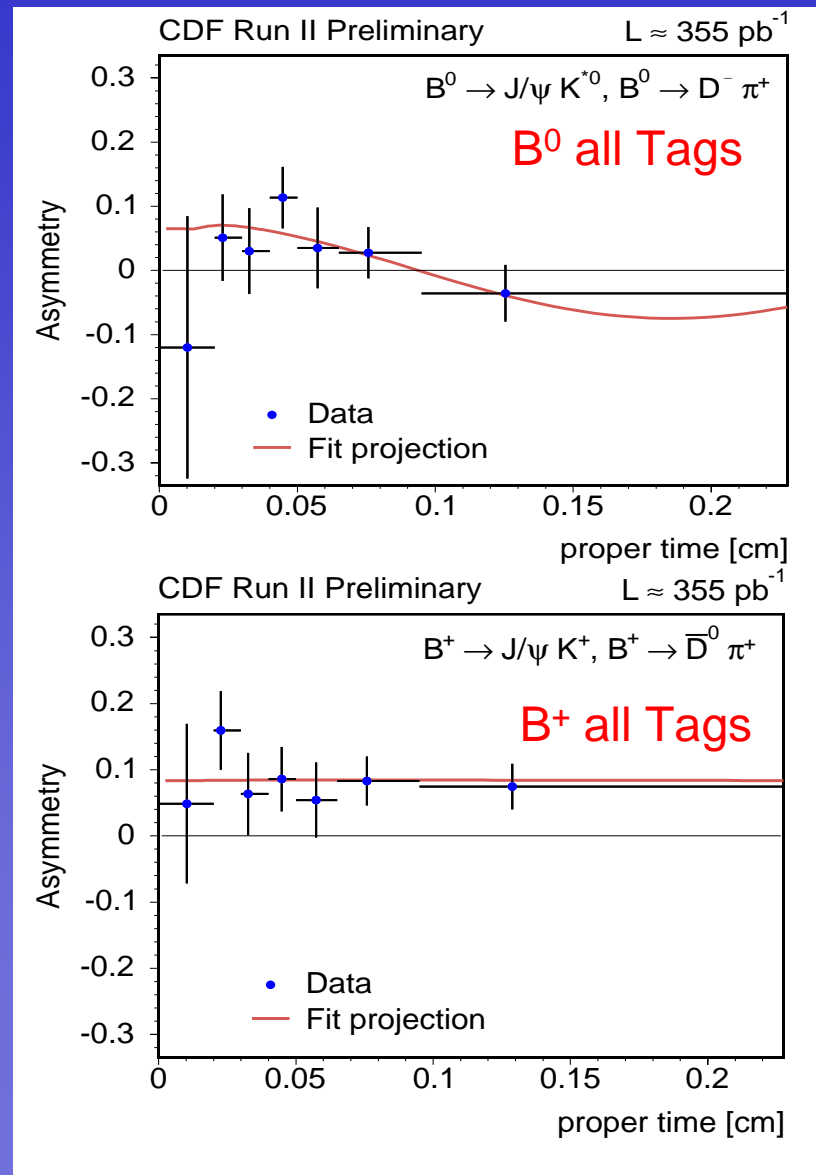
$$B^0 : e^{-t/\tau} (1 \pm S \cdot D \cdot \cos(\Delta m_d t))$$

$$B^+ : e^{-t/\tau} (1 \pm S \cdot D)$$

- Fit the “Dilution scale factor” S
 - =1 if the tag calibration is correct.
 - 5 scale factors for 5 tag types
- Effective Dilution depend on detail of the samples (e.g. P_t spectra)

→ Scale factors are then used for B_s mixing analysis for hadronic channels

→ Same thing for semileptonic decays



Dilution scale factor

	HADRONIC	SEMILEPTONIC
Δm_d	$(0.503 \pm 0.063 \pm 0.015) \text{ ps}^{-1}$	$(0.498 \pm 0.028 \pm 0.015) \text{ ps}^{-1}$
Total ϵD^2	$(1.12 \pm 0.23)\%$	$(1.43 \pm 0.09)\%$
Muon	$0.83 \pm 0.10 \pm 0.03$	$0.93 \pm 0.04 \pm 0.03$
Electron	$0.79 \pm 0.14 \pm 0.04$	$0.98 \pm 0.06 \pm 0.03$
Vertex	$0.78 \pm 0.19 \pm 0.05$	$0.97 \pm 0.06 \pm 0.04$
Track	$0.76 \pm 0.21 \pm 0.03$	$0.90 \pm 0.08 \pm 0.05$
Jets	$1.35 \pm 0.26 \pm 0.02$	$1.08 \pm 0.09 \pm 0.09$

- Δm_d consistent with WA: $0.510 \pm 0.005 \text{ ps}^{-1}$
- Total ϵD^2 : 1.1—1.4%
- All dilution scale factors consistent with 1
 - Hadronic: 15~25% uncertainty
 - Semileptonic: 5~15% uncertainty

Δm_s scan

- Introduce “Amplitude” in Likelihood

$$L_{sig}^t = \frac{1}{\tau} e^{-t/\tau} (1 \pm A \cdot D \cdot \cos(\Delta m \cdot t))$$

- Amplitude scan

– Fit the amplitude for fixed Δm

- Amplitude: A , uncertainty: σ_A

– Repeat the fit for different Δm

- Amplitude will be consistent with:

– 1 if mixing detected at the frequency Δm

– 0 if there is no mixing

- Example for B^0 Hadronic sample

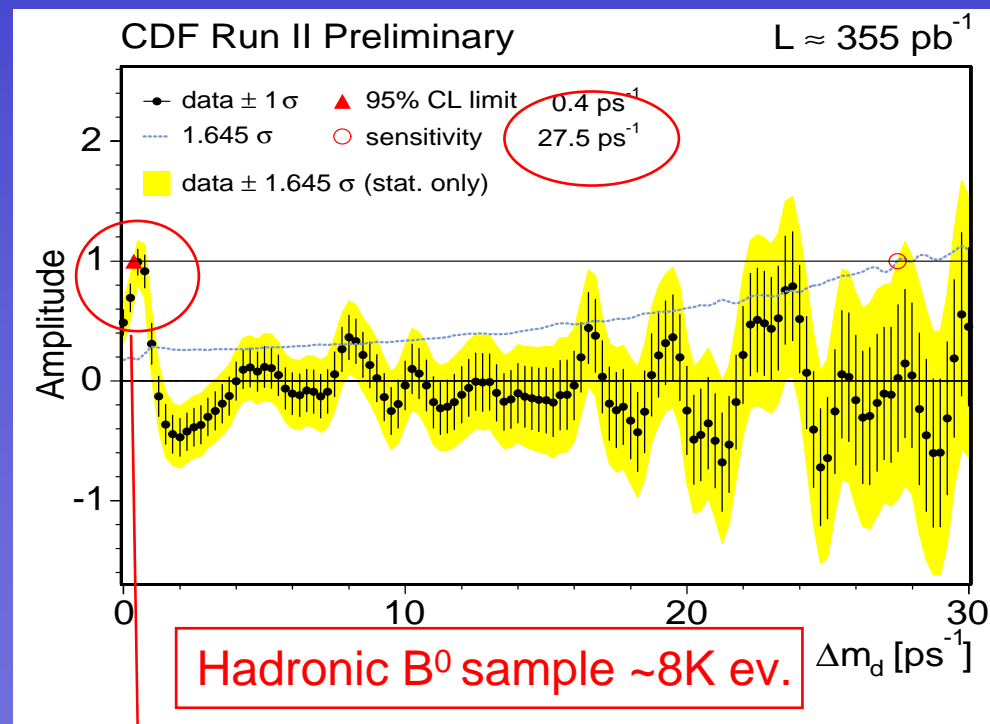
– Amplitude = 1 at $\Delta m = 0.5 \text{ ps}^{-1}$

– Amplitude = 0 at $\Delta m \gg 0.5 \text{ ps}^{-1}$

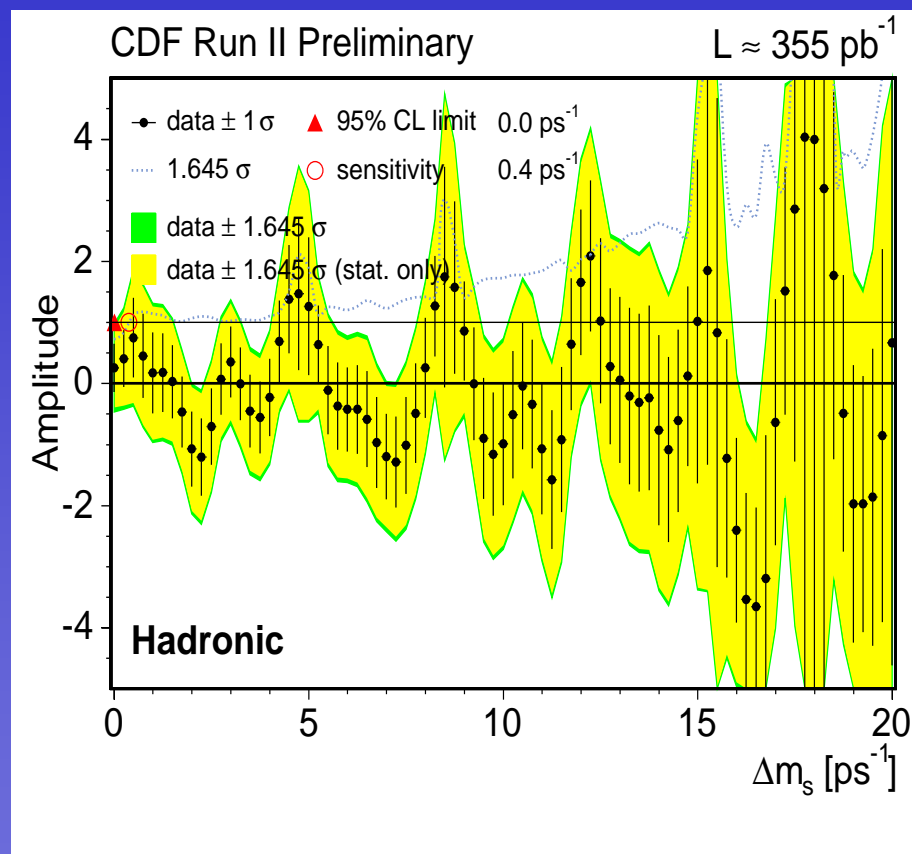
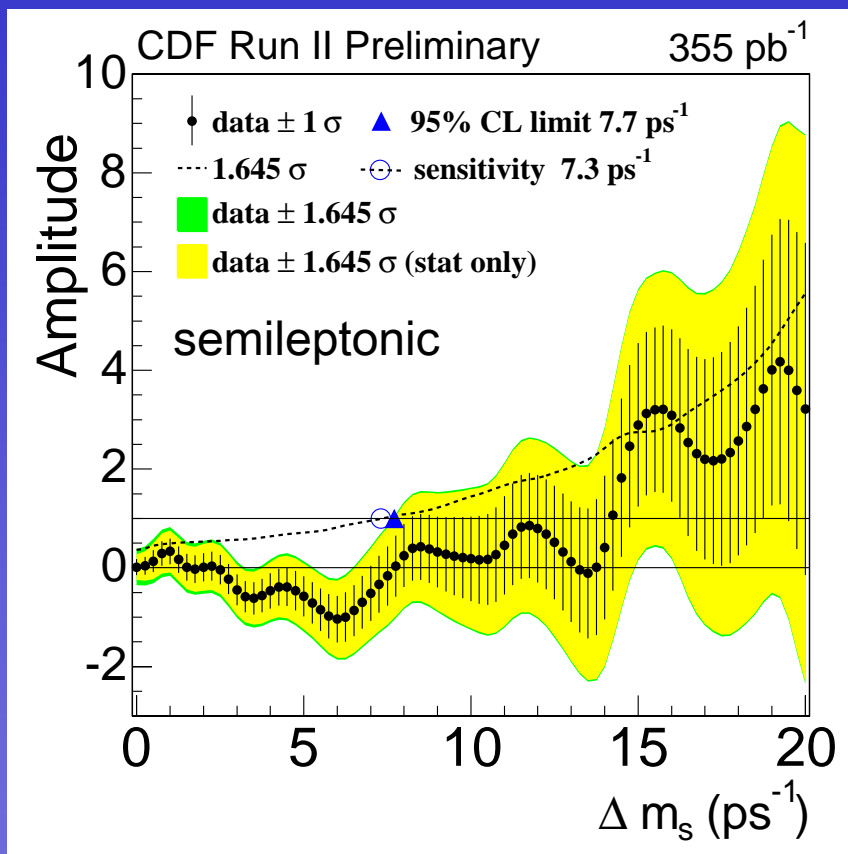
HFAG 04

• 95% CL limit is : $\Delta m_s > 14.5 \text{ ps}^{-1}$

• Sensitivity: 18.2 ps^{-1}



Mix at
 Δm_d

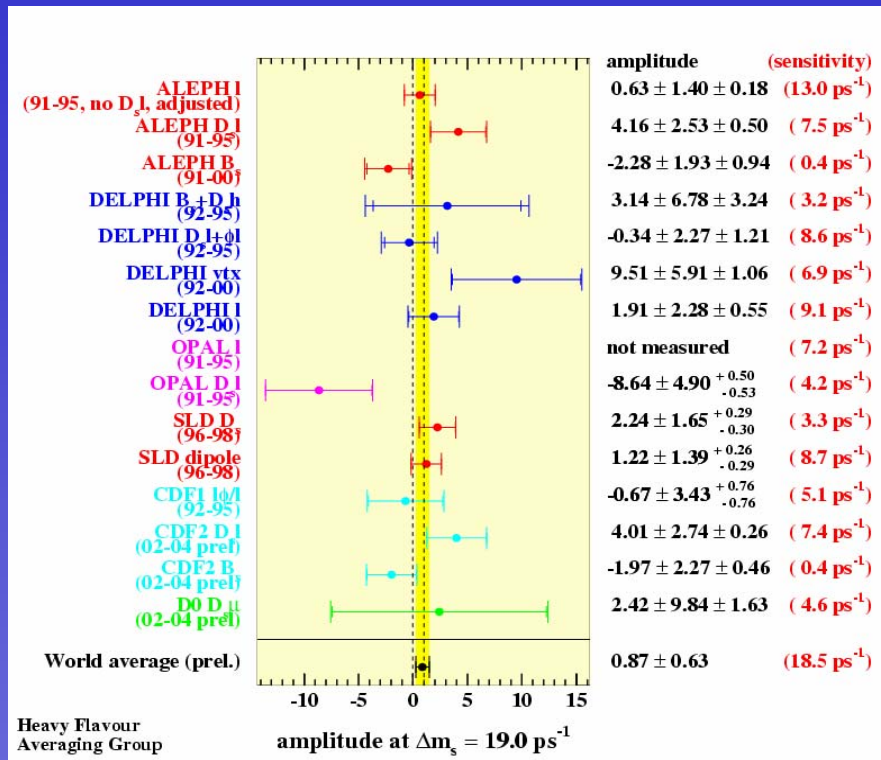
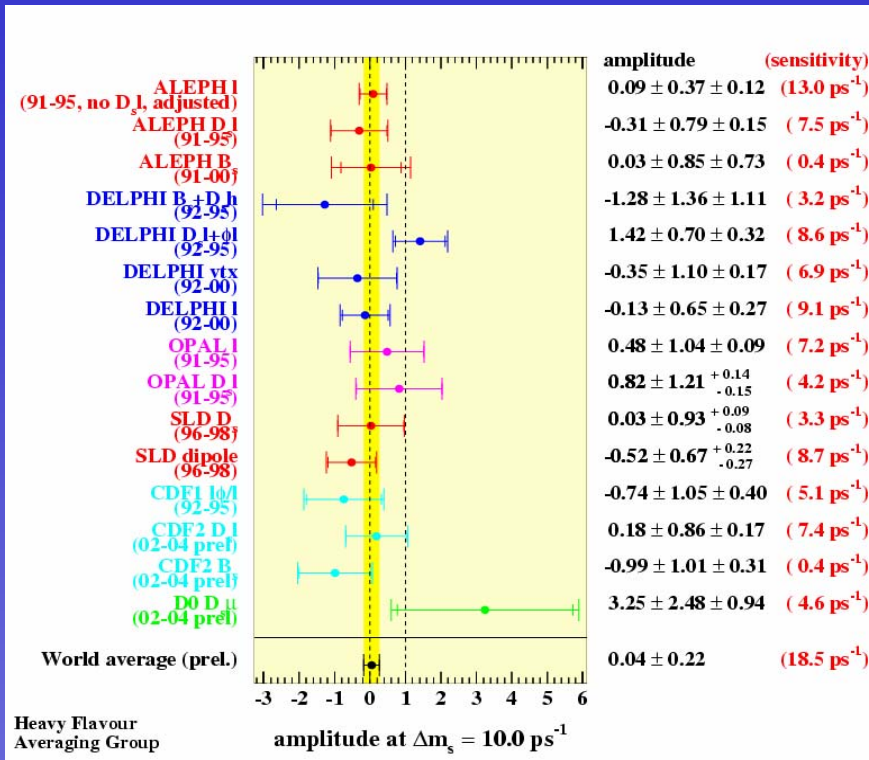


Hadronic has no sensitivity (yet) but is better behaved at high Δm_s

****Systematic errors are negligible with respect to statistical in both cases****

[details](#)

CDF/World Comparison



CDF2 B (hadronic) 9th best @ $\Delta m_s = 10 \text{ ps}^{-1}$ → 5th best @ $\Delta m_s = 19 \text{ ps}^{-1}$

[180% → 60 % worse sensitivity than best experiment]

CDF2 DI (semil.) 7th best @ $\Delta m_s = 10 \text{ ps}^{-1}$ → 8th best @ $\Delta m_s = 19 \text{ ps}^{-1}$

[130% → 95 % worse sensitivity than best experiment]

Stat. only!

- CDFII combined result

- Sensitivity: 8.4 ps^{-1}

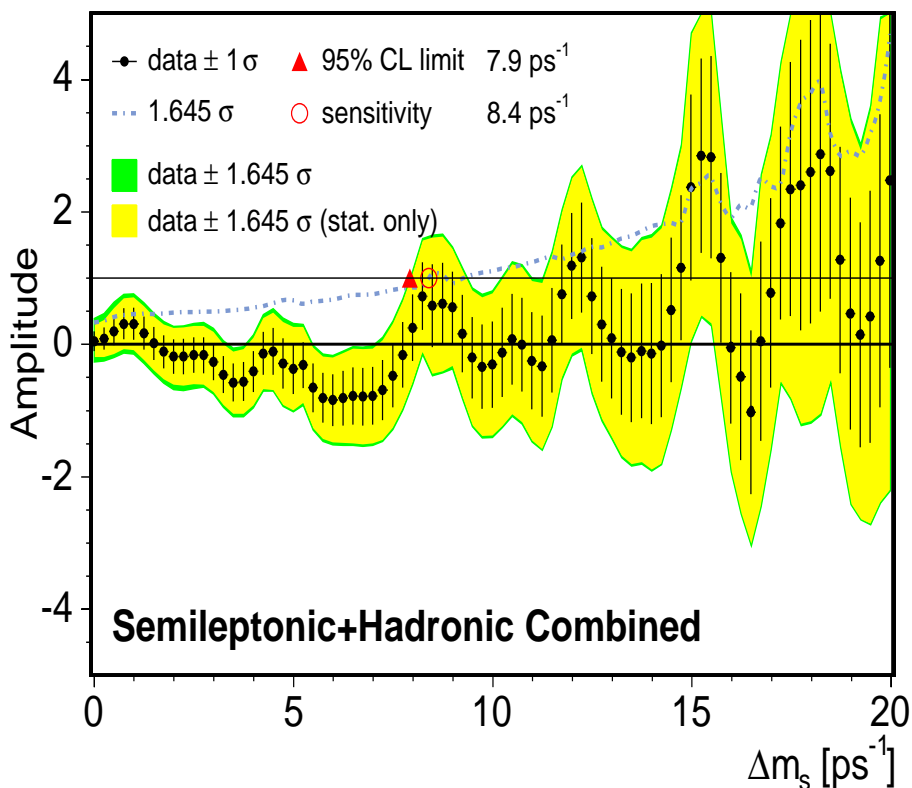
- Limit: $\Delta m_s > 7.9 \text{ ps}^{-1}$ @ 95% CL

- World Average + CDF Run II

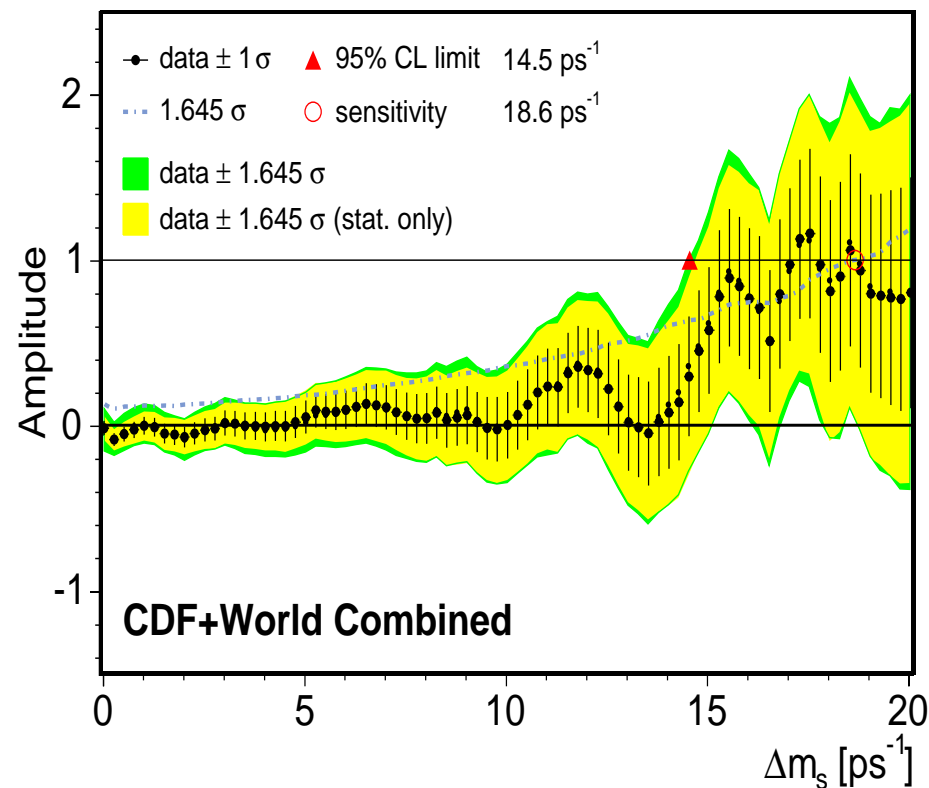
- Sensitivity: 18.6 ps^{-1}

- Limit $> 14.5 \text{ ps}^{-1}$ @ 95% CL

CDF Run II Preliminary $L \approx 355 \text{ pb}^{-1}$

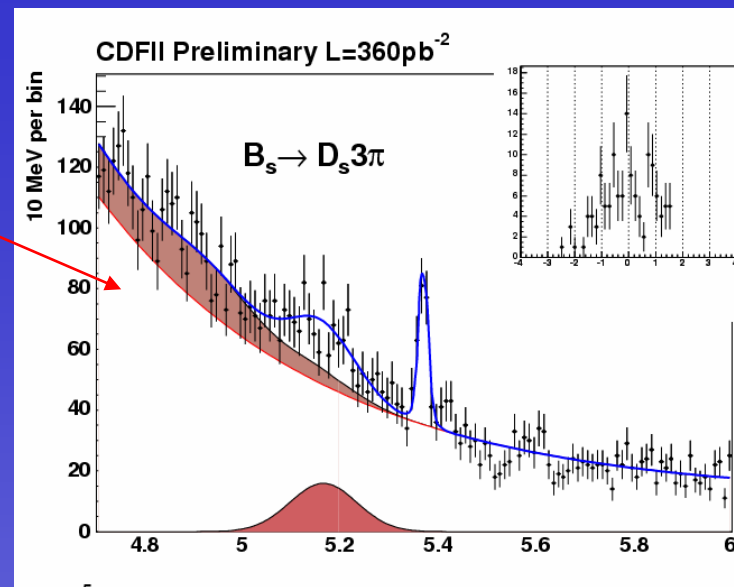


CDF Run II Preliminary $L \approx 355 \text{ pb}^{-1}$



Future perspectives

- Add more channels
 - $B_s \rightarrow D_s 3\pi$ (130 events +20%)
 - $B_s \rightarrow D_s^* \pi$
- Add semileptonic B_s decays from the hadronic trigger (S. De Cecco talk)
X2 semileptonic statistic



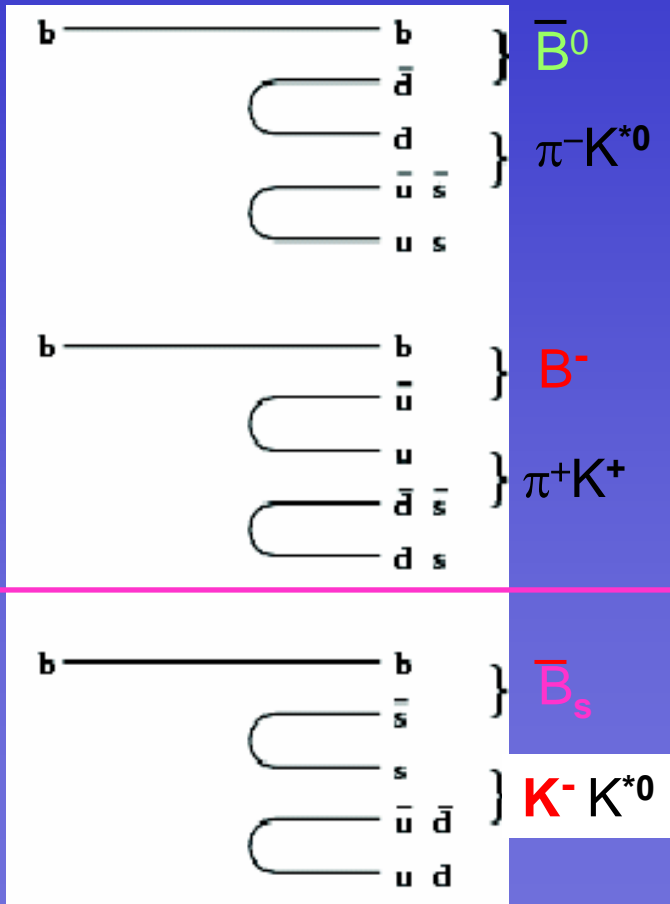
- Improve decay time resolution with PV event by event ([detail](#))
- Incremental changes in existing algorithm (new Jet Charge +20% ϵD^2)
- Add new tagging algorithm Same Side Kaon Tag

- New data rolling in, but increasingly peak luminosity:
 - Keep alive as much as possible present triggers \rightarrow SVT upgrade
 - Use new trigger strategies
 - 2 SVT Tracks + opposite side muon ($pt > 1.5$ GeV) at trigger level
(already in place since summer 2004 can survive at higher luminosity)

Same side Kaon tagging



Exploits the charge correlation between the b quark flavour and the leading product of b hadronization.



Already used in Δm_d measurement, gives an $\epsilon D^2 = 1.1 \pm 0.4 \%$

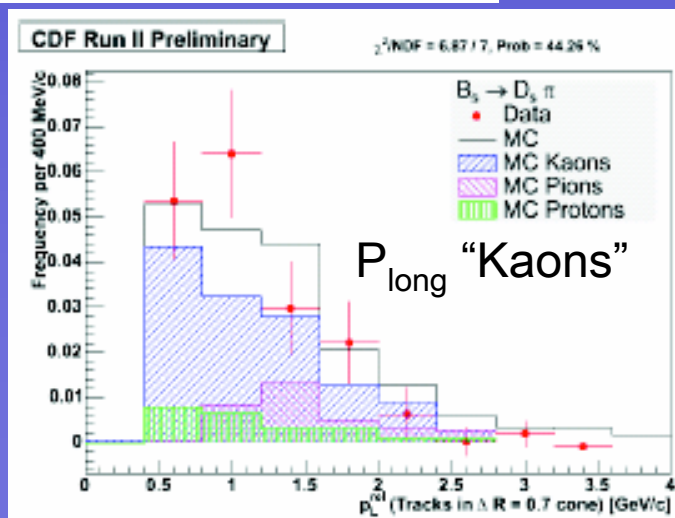
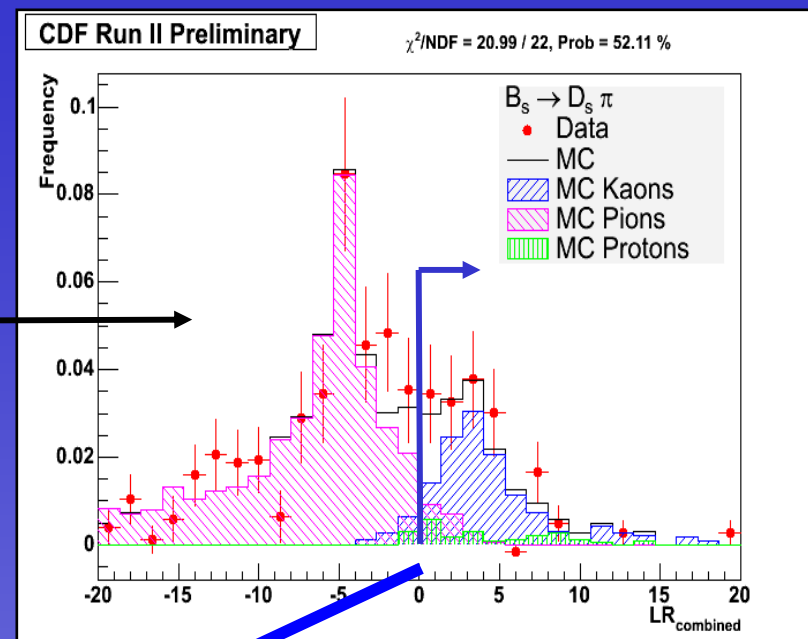
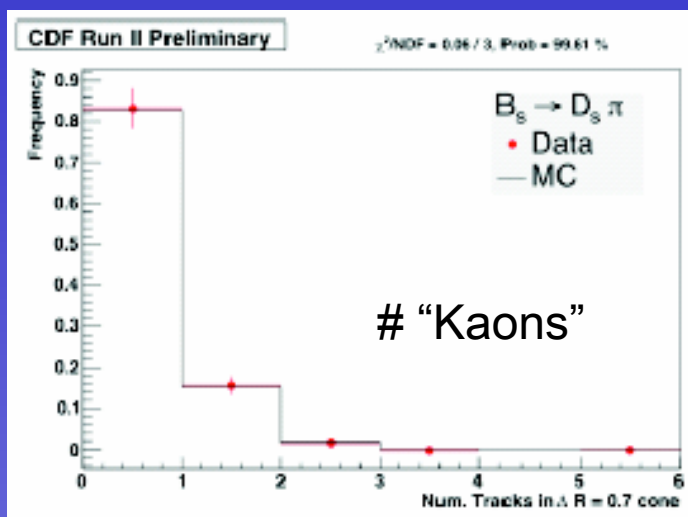
B^+ case is complicated by the contribution of excited B_d and B_s states

SS Kaon tag possible with PID

Issues:

- Unlike opposite side tagger cannot calibrate using B^0 and B^+
- Need to know ϵD^2 from MC to set a limit on Δm_s
- MC tuning crucial

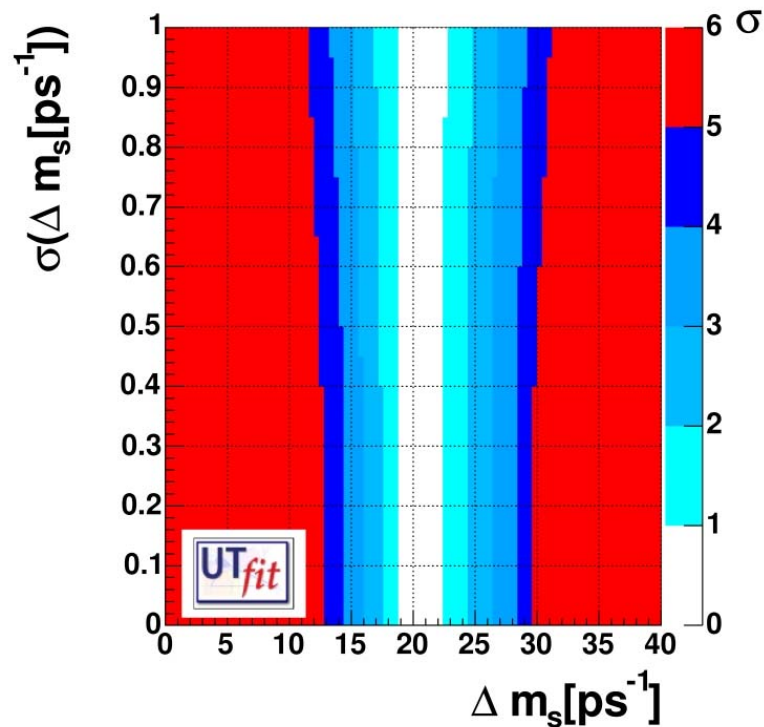
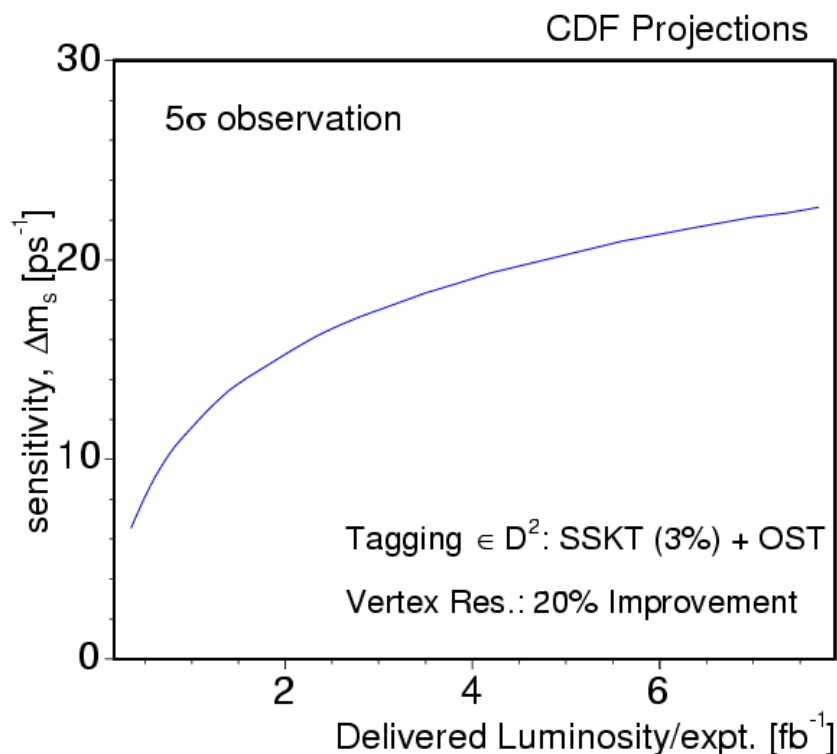
Apply PID, T.O.F. and dE/dx combined
In a Likelihood ratio $L(K)/L(\pi)$



Encouraging agreement!

Issues:

- Particle fractions in MC
- PID resolution tuning
- Backgrounds
- MC predict ϵ_{D^2} can be 2-3%



- Analytic extrapolation, reproduce present result with current inputs
- Prediction include a reduced (50%) effective luminosity usable for B-physics from 2007 onwards
- Sensitivity to the favorite CKM range
- In case of no signal 95% C.L. up to 30 ps⁻¹ with 4 fb⁻¹
- CKM fit will imply New Physics if $\Delta m_s > 28$ ps⁻¹ by then...

[More
projections](#)

- First attempt at this (very) complex analysis!
- Expect close to 1fb^{-1} good data on tape by fall shutdown:
 - x3 statistics w.r.t to present result ?
 - Additional channels can be used both for fully reconstructed and semileptonic
 - Incremental improvements to existing opposite tagging algorithm expected
 - Building confidence on Same Side Kaon tagging
 - Better reconstruction of primary/secondary vertex improve proper time resolution
- Improved limit (15ps^{-1} sensitivity?) expected by winter 06!
- Extensive upgrade to DAQ/trigger will keep B-triggers alive with increasing luminosity and allow the exploration of the SM favourite range for Δm_s by the end of RunII

Backup

The Upgraded CDF Detector

New

Old

Partially new

Central calorimeters

Solenoid

Central muon

TOF

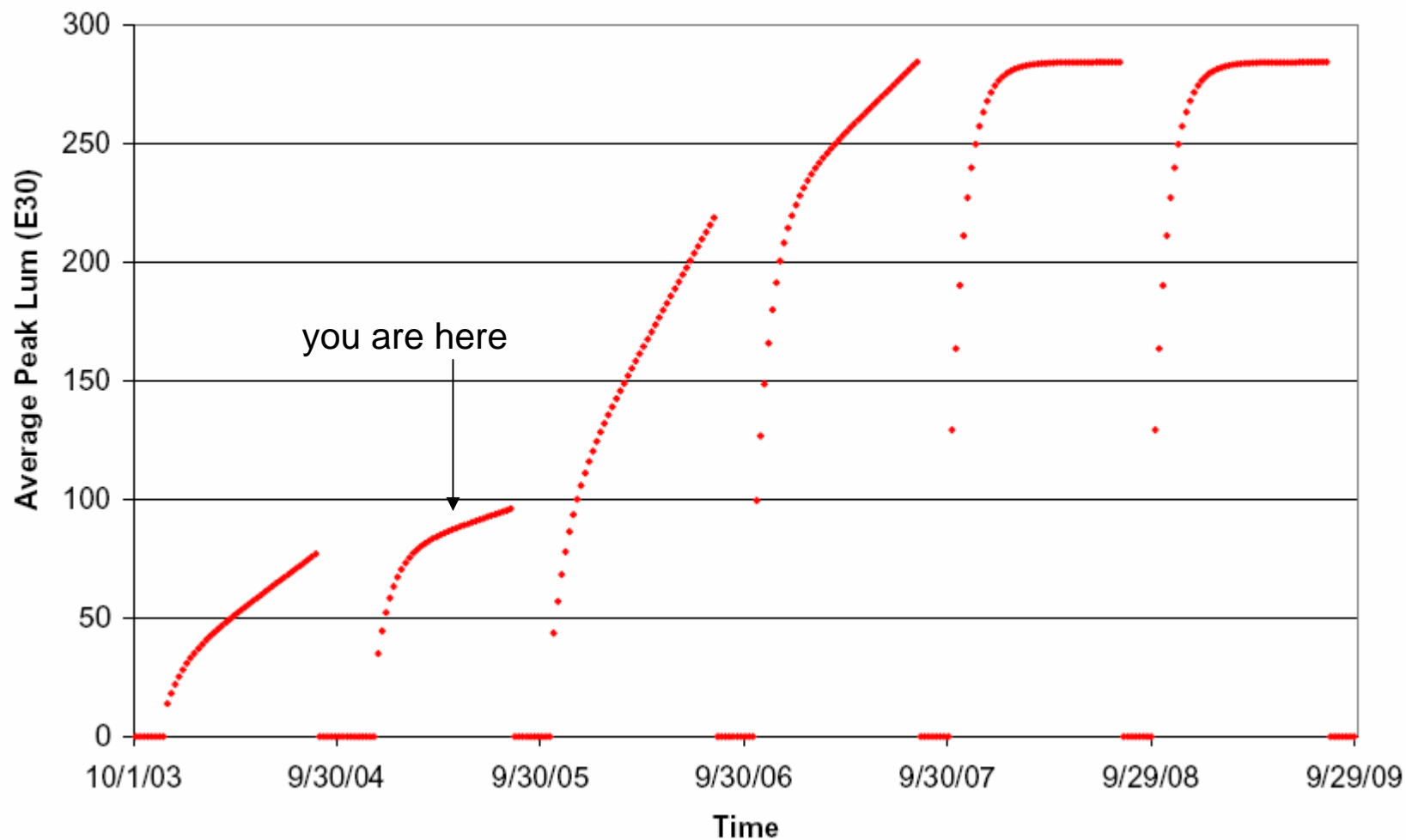
Front end
Trigger
DAQ
Offline

Forward muon

Endplug calorimeter

Silicon and drift chamber trackers

Average Peak Luminosity (E30) vs Time



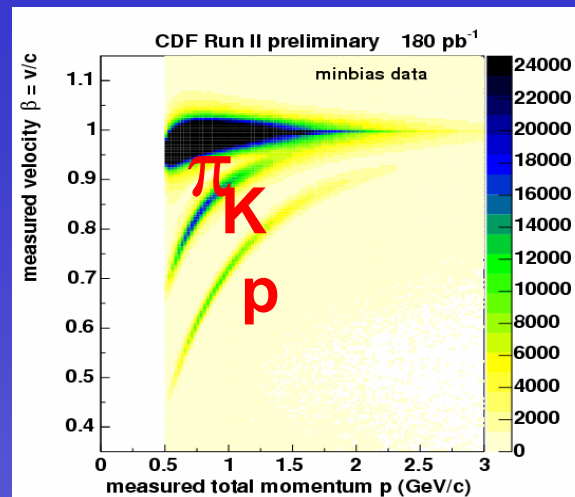
Basic tools: PID

- Improved TOF calibration (better resolution)
- + t₀ (reduced tails)

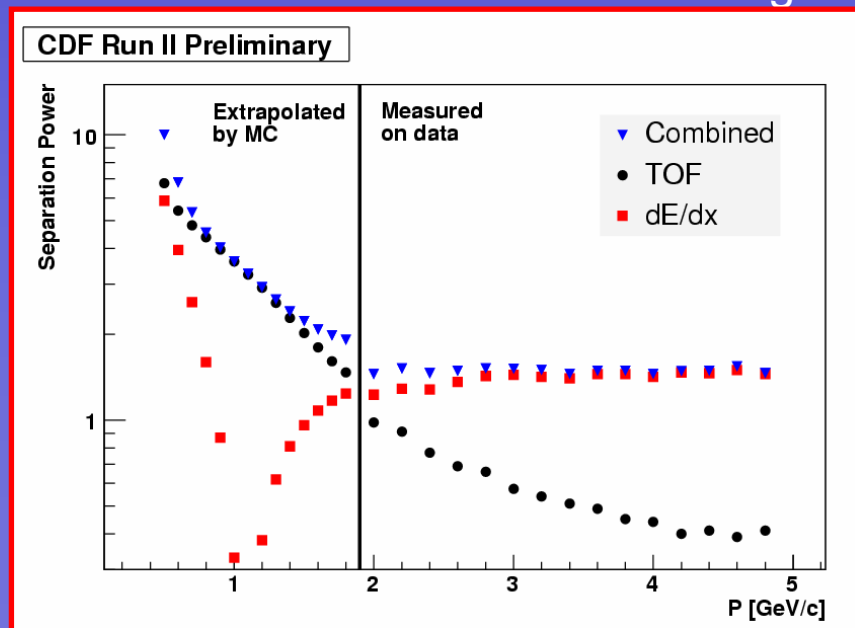
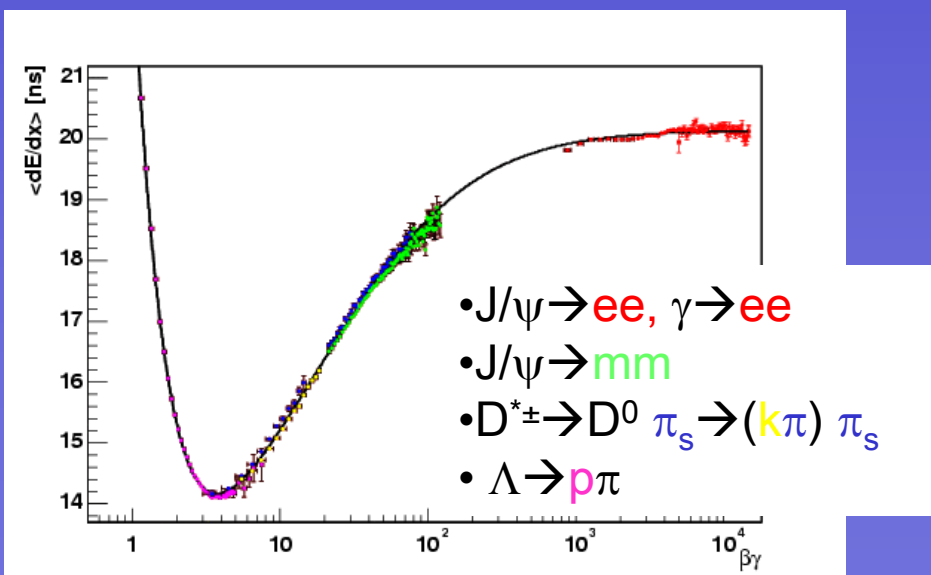
TOF: $>1\sigma$ K/ π separation up to p=2 GeV

- Improved COT dE/dx calibration over wider $\beta\gamma$ range

dE/dx in COT
K/ π sep. $>1.4\sigma$ @ P_T > 2 GeV



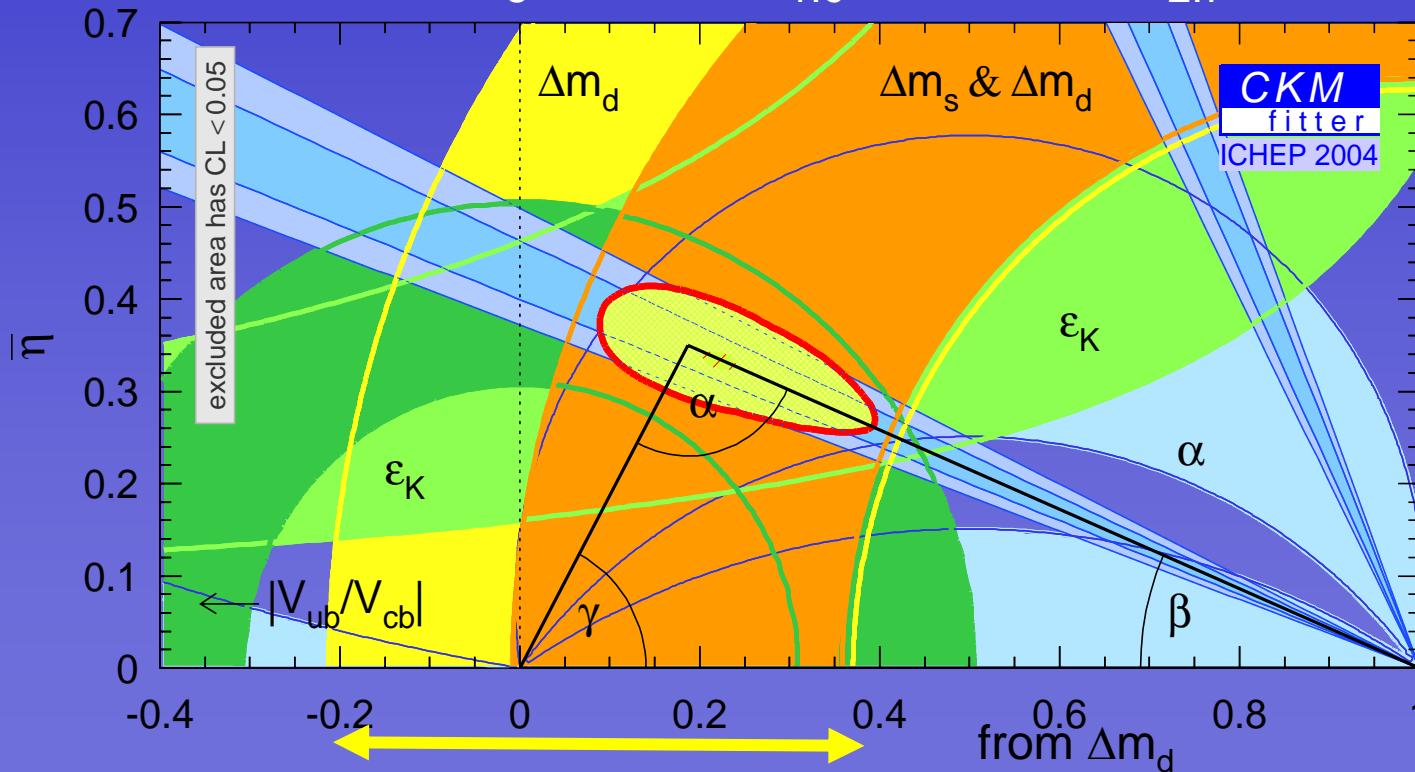
Combine TOF+COT in a likelihood ratio usable for all momentum range!



UT fit and Δm_s (CKMfitter)



- Yellow Band: Δm_d measurement: $\sim 15\%$ uncertainty
- Orange Band: Lower limit on $\Delta m_s =$ Upper Limit on $|V_{td}|$
 - The lower limit on Δm_s already gives a constraint to the Triangle
- CKM Fit result: $\Delta m_s: 17.8^{+6.7}_{-1.6} (1\sigma) : ^{+15.2}_{-2.7} (95\%CL)$



Lower limit on Δm_s \longleftrightarrow ρ \longleftrightarrow from Δm_d
 \longleftrightarrow from $\Delta m_d/\Delta m_s$

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- ~70 physicists (22 italians, 9 phd/post-doc) in CDF are actively involved in the B_s mixing project

- Improving the trigger strategy
- Understanding the detector
- B Lifetime Measurements
- Flavor Tagging
- B⁰ Mixing
- B_s Mixing

- Big collaborative effort:

- Analyse 3 different datasets
- Reconstruct 0(20) different decay modes
- Perform 2 parallel analysis for both hadronic and semileptonic modes
- Study 4 different tagging algorithms
- TOF and dE/dx calibrations

CDF/ANAL/BOTTOM/CDFR/7531

Version 1.0

March 9, 2005

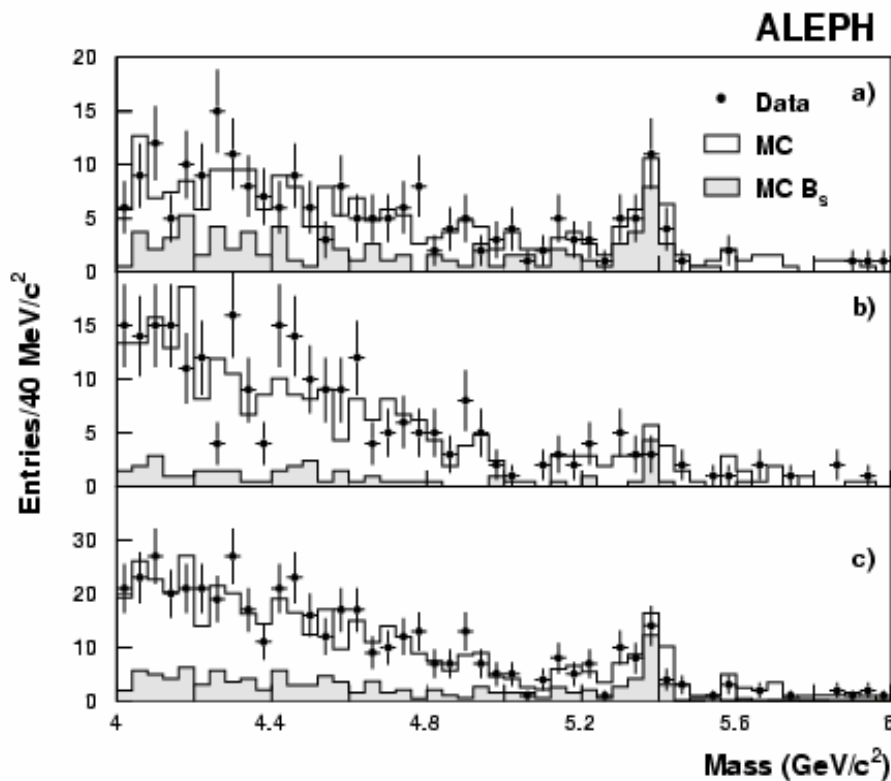
Result of Unblinded Δm_s Amplitude Scan Using Semileptonic $B_s^0 \rightarrow D_s^- \ell^+ \nu$ Decays

B_s⁰ Mixing Group

Farrukh Azfar¹⁹, Gary Barker⁸, Gerry Bauer¹³, Franco Bedeschi¹¹, Satyajit Behari¹⁵, Stefano Belforte¹², Alberto Belloni¹³, Eli Ben-Haim⁷, Arkadiy Bolshov¹³, Joe Boudreau²², Massimo Casarsa¹², Pierluigi Catastini¹¹, Alessandro Cerri⁵, Agnese Ciocci¹¹, David Clark², Saverio D’Auria⁶, Saverio Da Ronco²⁰, Sandro De Cecco¹⁰, Amanda Deisher⁵, Francesco Delli Paoli²⁰, Simone Donati¹¹, Mauro Donega¹⁶, Sinéad Farrington¹⁸, Armando Fella¹¹, Ivan Furic⁴, Stefano Giagu¹⁰, Karen Gibson³, Kim Giolo¹⁴, Gavril Giurgiu³, Guillermo Gomez-Ceballos⁹, Robert Harr²⁴, Matt Herndon¹⁵, Todd Huffman¹⁹, Boris Iyutin¹³, Matthew Jones¹⁴, Ilya Kravchenko¹³, Joe Kroll²¹, Tom LeCompte¹, Claudia Lecci⁸, Nuno Leonardo¹³, Donatella Luchesi²⁰, Petar Maksimović¹⁵, Stephanie Menzemer¹³, Jeffrey Miles¹³, Michael Morello¹¹, Reid Mumford¹⁵, Steve Nahn²⁵, Rolf Oldeman¹⁸, Manfred Paulini³, Christoph Paus¹³, Jónatan Piedra⁹, Kevin Pitts¹⁷, Giovanni Punzi¹¹, Jonas Rademacker¹⁹, Azizur Rahaman²², Marco Rescigno¹⁰, Alberto Ruiz⁹, Giuseppe Salamanna¹⁰, Fabrizio Scuri¹¹, Marjorie Shapiro⁵, Paola Squillacioti¹¹, Masa Tanaka¹, Vivek Tiwari³, Fumi Ukegawa²³, Satoru Uozumi²³, Denys Usynin²¹, Ivan Vila⁹, Barry Wicklund¹, Chun Yan²⁵

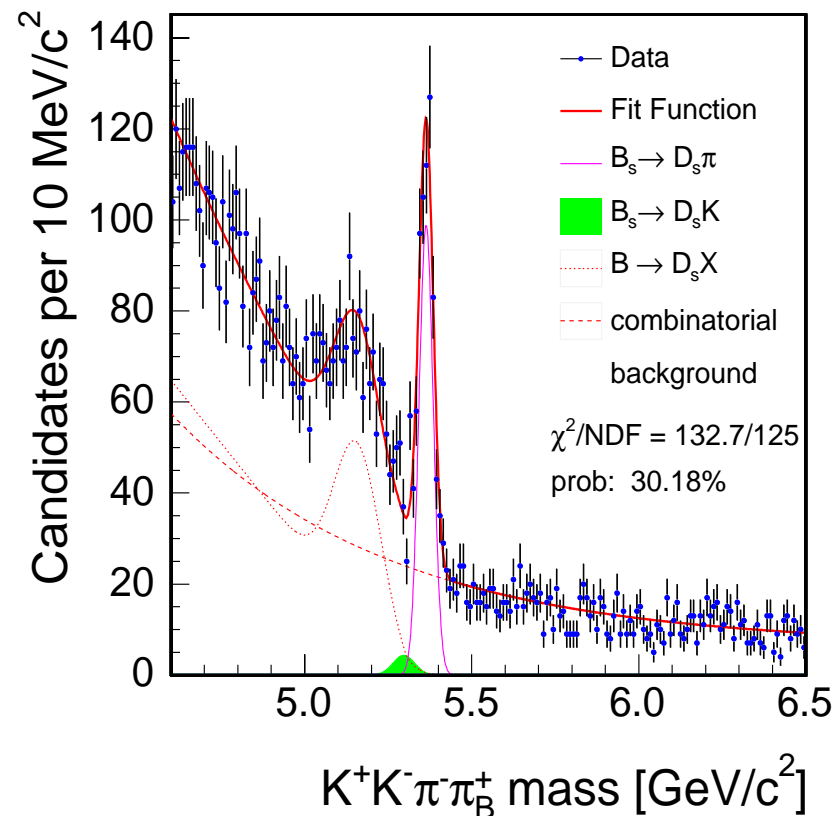
Institutions:

- (1) Argonne National Laboratory, Argonne, Illinois 60439
- (2) Brandeis University, Waltham, Massachusetts 02254
- (3) Carnegie Mellon University, Pittsburgh, PA 15213
- (4) Enrico Fermi Institute, University of Chicago, Chicago, Illinois 60637
- (5) Ernest Orlando Lawrence Berkeley National Laboratory, Berkeley, California 94720
- (6) Glasgow University, Glasgow G12 8QQ, United Kingdom
- (7) IN2P3, Paris, France
- (8) Institut für Experimentelle Kernphysik, Universität Karlsruhe, 76128 Karlsruhe, Germany
- (9) Instituto de Fisica de Cantabria, CSIC-University of Cantabria, 39005 Santander, Spain
- (10) Istituto Nazionale di Fisica Nucleare, Sezione di Roma 1, University di Roma “La Sapienza,” I-00185 Roma, Italy
- (11) Istituto Nazionale di Fisica Nucleare, University and Scuola Normale Superiore of Pisa, I-56100 Pisa, University of Siena, I-53100 Siena, Italy



~30 events

CDFII Preliminary, 355 pb⁻¹, $B_s \rightarrow D_s \pi$, $D_s \rightarrow \phi \pi$



~500 events

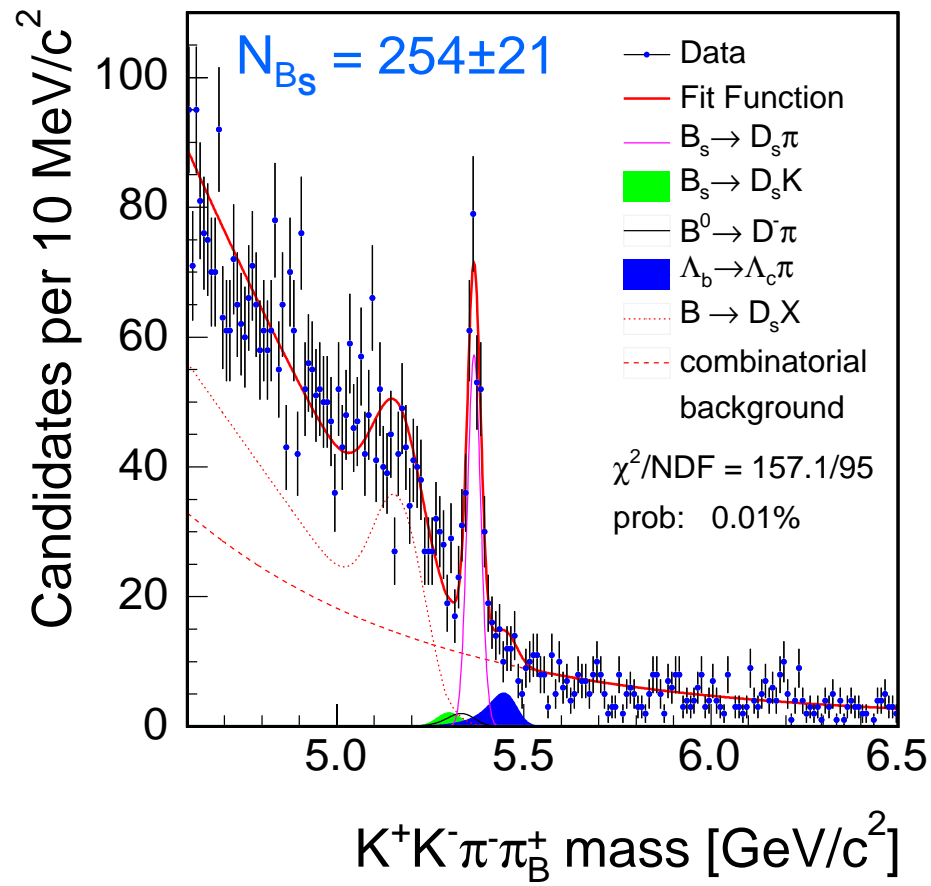
Hadronic B_s signals (2)



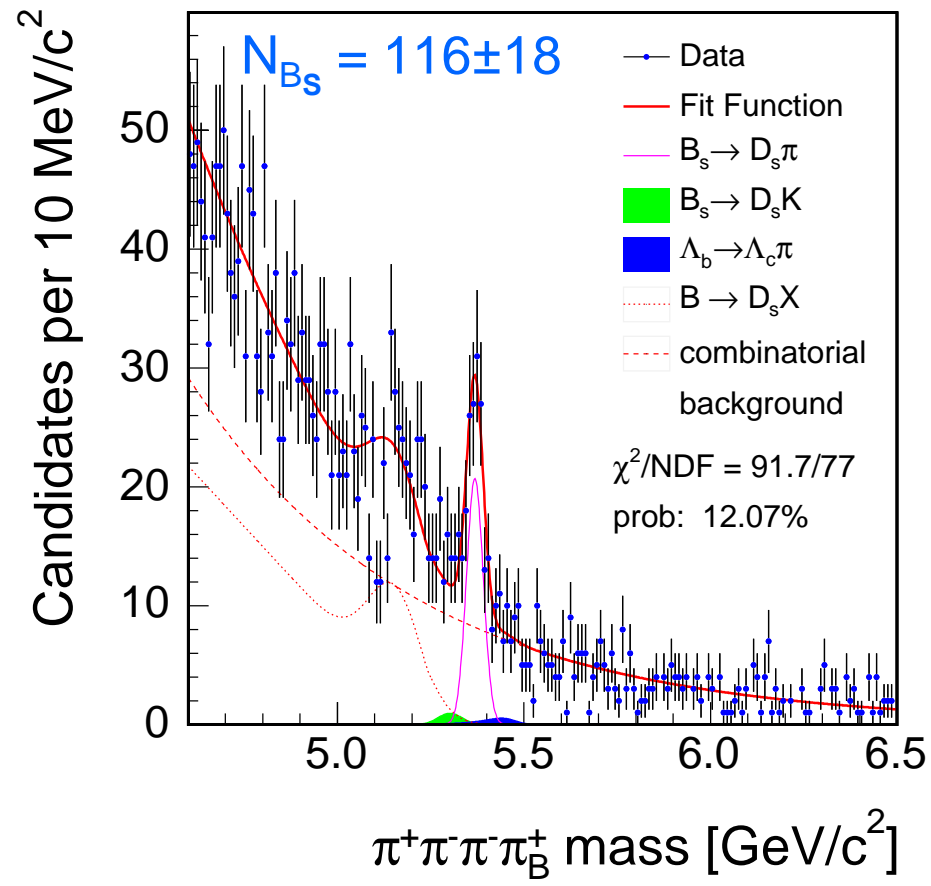
$$B_s^0 \rightarrow D_s^- \pi^+ (D_s^- \rightarrow K^{*0} K^-)$$

$$B_s^0 \rightarrow D_s^- \pi^+ (D_s^- \rightarrow \pi^+ \pi^- \pi^-)$$

CDFII Preliminary, 355 pb^{-1} , $B_s \rightarrow D_s \pi$, $D_s \rightarrow K^* K$



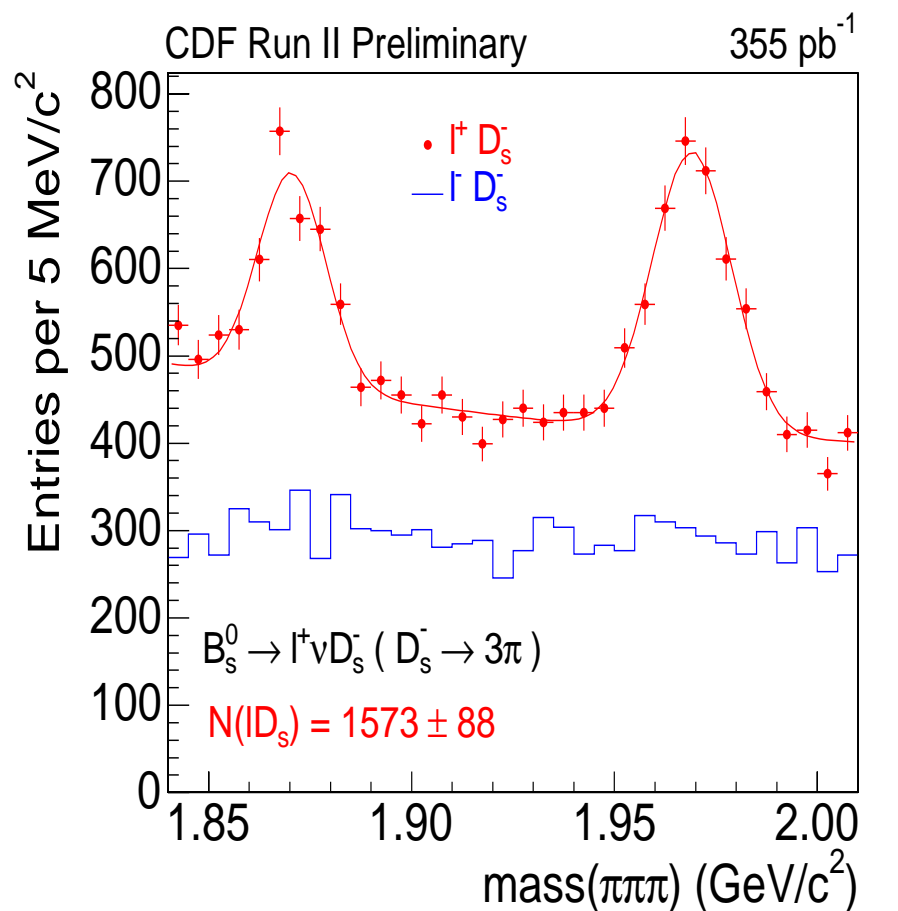
CDFII Preliminary, 355 pb^{-1} , $B_s \rightarrow D_s \pi$, $D_s \rightarrow \pi \pi \pi$



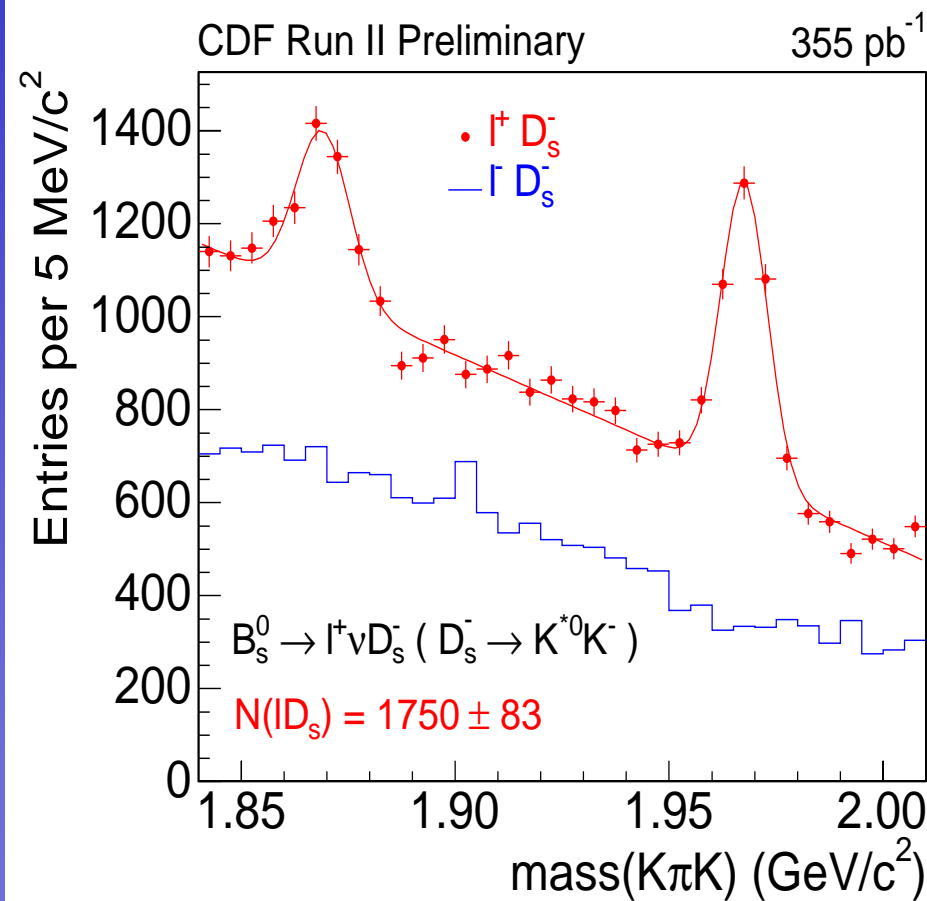
[back](#)

$$B_s^0 \rightarrow D_s^- l^+ \nu (D_s^- \rightarrow K^{*0} K^-)$$

$$B_s^0 \rightarrow D_s^- l^+ \nu (D_s^- \rightarrow \pi^- \pi^+ \pi^-)$$



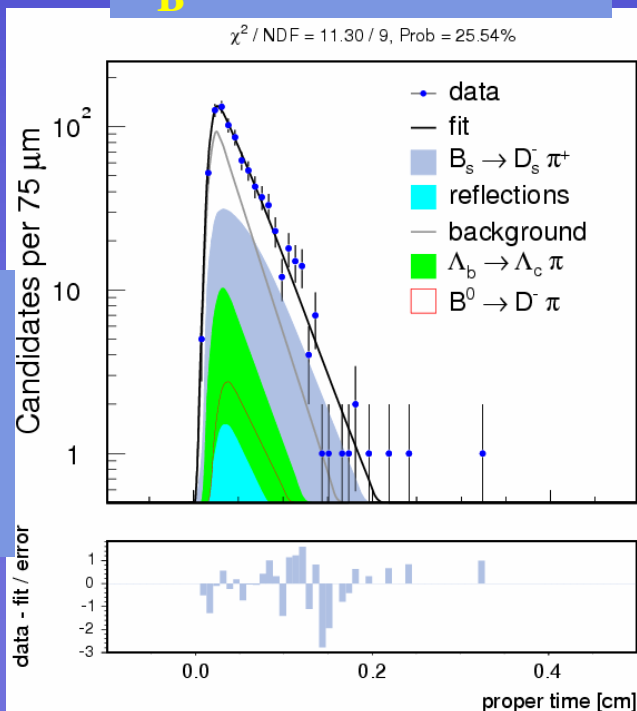
1573±88 events



1750±83 events

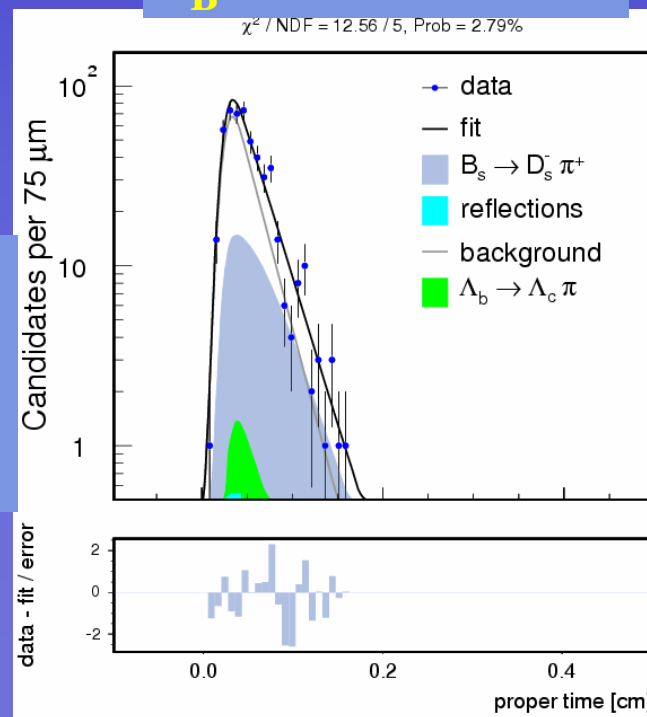
- Raw lifetimes from mixing fit – not good for averaging
 - Average: $\tau_B = 1.515 \pm 0.070$ ps no systematics evaluated
 - **D0**: $\tau(B_s) = 1.420 \pm 0.043 \pm 0.057$ ps, **WA**: $\tau(B_s) = 1.469 \pm 0.059$ ps

$\tau_B = 1.550 \pm 0.131$

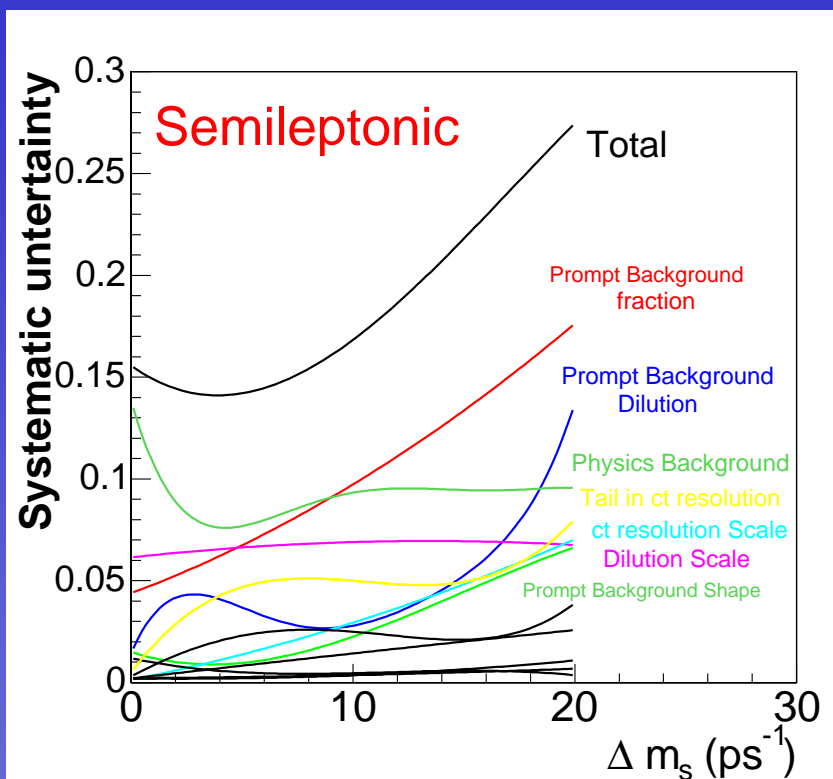


D_s → K*K

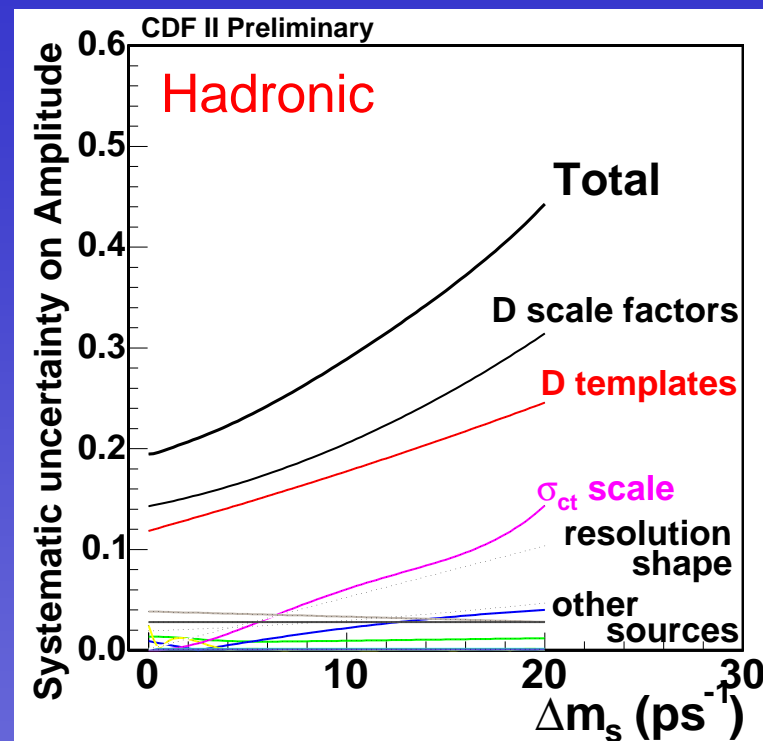
$\tau_B = 1.377 \pm 0.186$



D_s → πππ



- **Physics** background at low Δm_s
- **Prompt** background at high Δm_s



- **Dilution scale factors** and templates systematic limited from control sample statistics

****Systematic errors are negligible with respect to statistical in both cases****

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Systematics Summary Table (Hadronic)



source	selected Δm_s scan points				
	0.0	5.0	10.0	15.0	20.0
$B_s \rightarrow D_s K$ level	0.019	0.024	0.030	0.037	0.047
dilution scale factors	0.143	0.168	0.205	0.254	0.314
dilution templates	0.119	0.147	0.178	0.211	0.246
fraction of Λ_b	0.014	0.009	0.009	0.011	0.012
Punzi term for σ_{ct}	0.009	0.008	0.022	0.033	0.030
dilution of $B \rightarrow DX$	0.025	0.001	0.000	0.000	0.001
σ_{ct} scale factor	0.000	0.024	0.061	0.090	0.144
usage of L00 in bias curve	0.001	0.001	0.001	0.001	0.001
Bs lifetime uncertainty	0.001	0.001	0.001	0.001	0.001
reweighted p_t spectrum	0.001	0.001	0.001	0.001	0.001
non-Gaussian tails in ct resol.	0.001	0.027	0.052	0.078	0.104
neglect B^0 in fit	0.039	0.036	0.033	0.031	0.028
effect of $\Delta\Gamma/\Gamma = 0.2$	0.028	0.028	0.028	0.028	0.028
Total systematic	0.195	0.232	0.289	0.357	0.443
Statistical	0.393	1.129	1.010	2.652	5.281

Systematics Summary Table (Semileptonic)



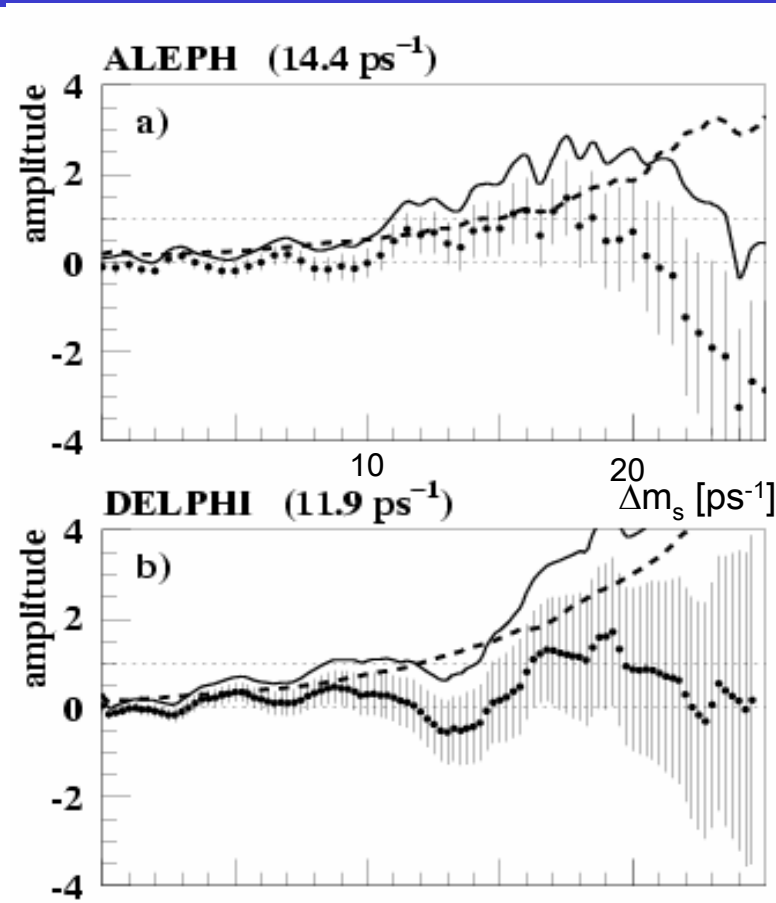
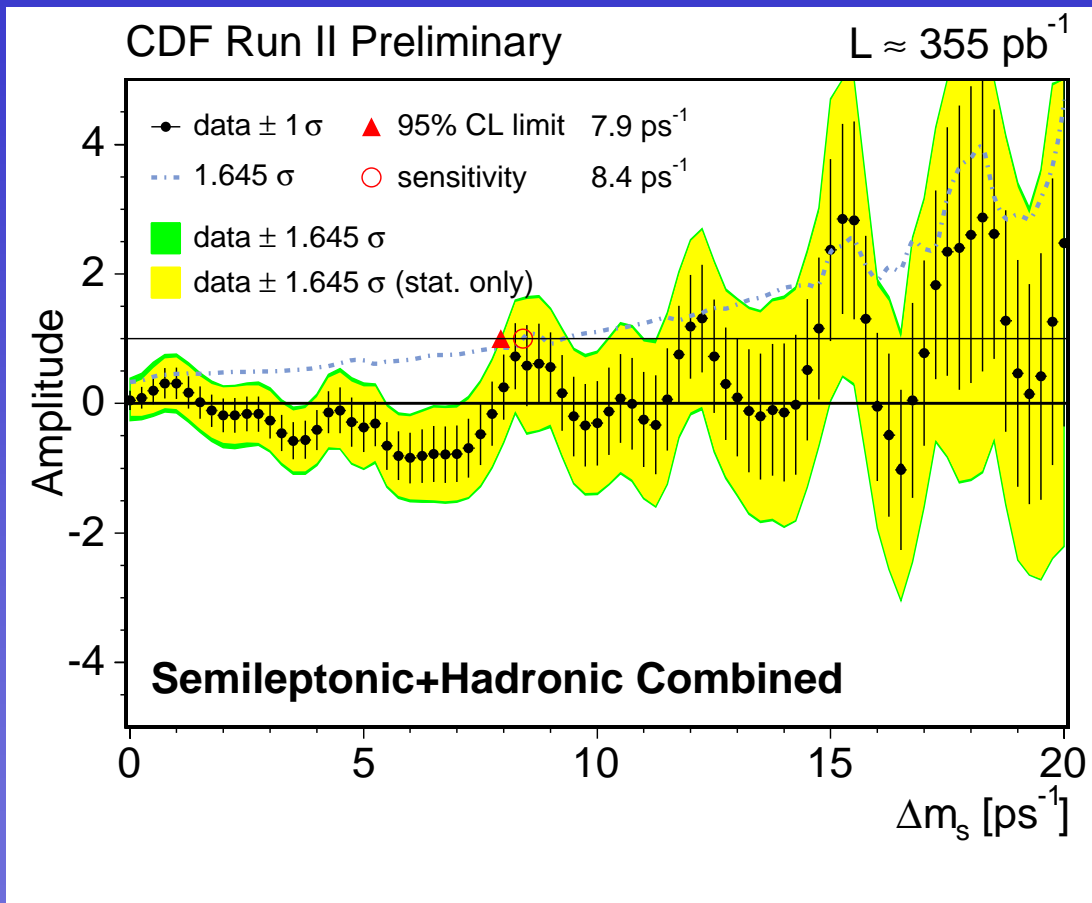
Source	selectex Δm_s scan points				
	0.0	5.0	10.0	5.0	20.0
Prompt background fraction	0.044	0.065	0.102	0.145	0.143
Prompt background dilution	0.014	0.040	0.027	0.062	0.157
Prompt background shape	0.015	0.010	0.019	0.054	0.057
Physics background fraction	0.134	0.078	0.093	0.096	0.103
Sample composition	0.002	0.015	0.022	0.021	0.039
Dilution scale factors	0.061	0.071	0.068	0.070	0.069
σ_{ct^*} scale factor	0.002	0.012	0.033	0.047	0.065
SVT bias curve	0.002	0.001	0.005	0.005	0.012
Primary vertex	0.007	0.003	0.003	0.005	0.007
B_s lifetime	0.001	0.011	0.014	0.020	0.026
non-Gaussian tails in ct resol.	0.005	0.047	0.049	0.052	0.078
effect of $\Delta\Gamma/\Gamma=0.2$	0.012	0.005	0.005	0.005	0.009
Total Systematics	0.156	0.142	0.167	0.220	0.273
Statistical	0.159	0.406	0.856	1.654	3.364

Error Source	S_D^{SMT} (%)	S_D^{SET} (%)	S_D^{JVX} (%)	S_D^{JJP} (%)	S_D^{JPT} (%)	Δm_d (ps ⁻¹)
σ_{ct}	0.01	0.02	0.01	0.06	0.04	0.0014
SVT efficiency	0.05	0.03	0.09	0.02	0.02	0.0008
SVT $d0$ resolution	0.26	0.20	0.49	0.22	0.19	0.0011
Combinatorial background	0.12	0.02	0.13	0.17	0.21	0.0019
Fraction of prompt bckg.	1.86	2.00	2.20	1.67	2.65	0.0041
Dilution of prompt bckg	1.30	1.40	2.40	4.00	8.00	0.0090
$c\tau_{B^0}$ fixed	0.22	0.15	0.19	0.13	0.29	0.0003
Sample composition	1.38	0.96	1.74	1.44	0.97	0.0089
Physics background	0.63	0.63	0.45	0.45	2.06	0.0027
Dilution templates	0.40	0.90	0.40	0.30	0.30	0.0060

TABLE III: Table of systematic uncertainties for the dilution scale factors and Δm_d .

Source	Relative error (%)					
	S_D^{SMT}	S_D^{SET}	S_D^{JVX}	S_D^{JJP}	S_D^{JPT}	Δm_d
Mass Parameterization						
Signal shape for $B^0 \rightarrow D^- \pi^+$						
ratio of widths	-	-	0.1	0.5	-	0.3
fraction of wide Gaussian	-	-	0.3	0.4	-	0.1
Comb. backgr. for $D\pi$ modes	-	-	-	-	-	-
ct Parameterization						
MC lifetime in SVT bias	-	-	-	-	-	-
L00 in SVT bias	0.1	0.4	-	0.7	0.9	-
Impact parameter in SVT bias	0.2	0.2	0.2	0.4	0.5	-
Scale factor on σ_{ct}	-	-	-	-	-	-
Scale factor σ_{ct} for backgr.	-	0.2	0.4	-	0.1	-
Backgrounds						
K^{*0} swap in $B^0 \rightarrow J/\psi K^{*0}$	0.4	-	0.2	-	0.2	0.1
Λ_b in $B^0 \rightarrow D^- \pi^+$	-	0.2	-	0.1	-	-
B_s in $B^0 \rightarrow D^- \pi^+$	-	-	-	-	-	-
Dilution systematics						
binning of templates	3.2	4.3	3.0	0.1	0.1	0.5
statistical smear of templates	2.6	2.9	5.5	3.3	0.7	2.8
backgr. tagging efficiencies	0.3	0.2	0.2	0.8	0.2	-
Λ_b dilution in $B^0 \rightarrow D^- \pi^+$	-	0.4	-	0.2	-	0.1
Total	4.2	5.2	6.3	3.6	1.3	2.9

TABLE III: Summary of all systematic errors.



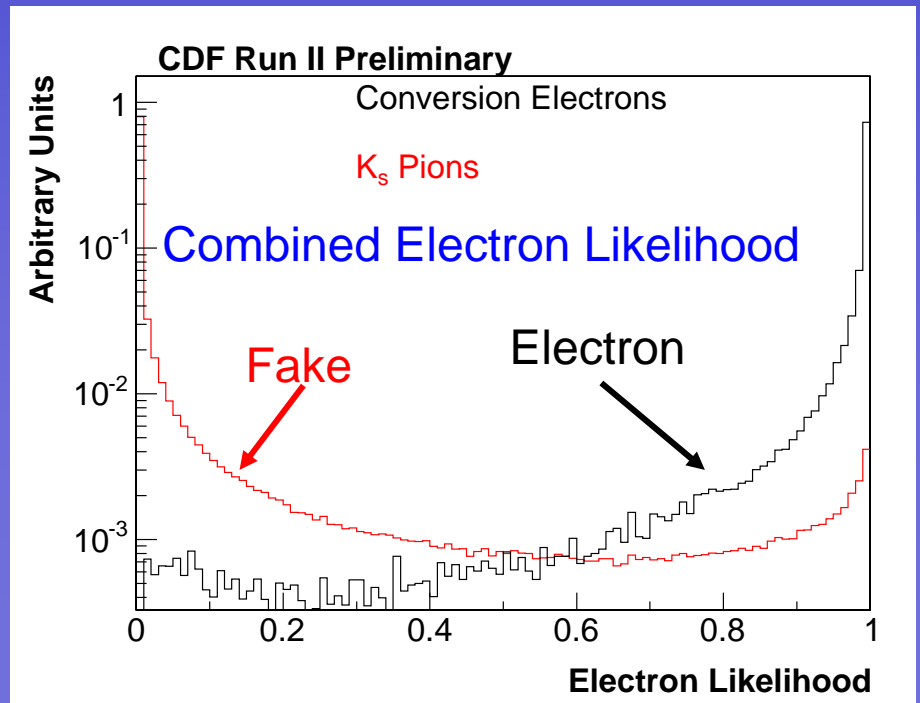
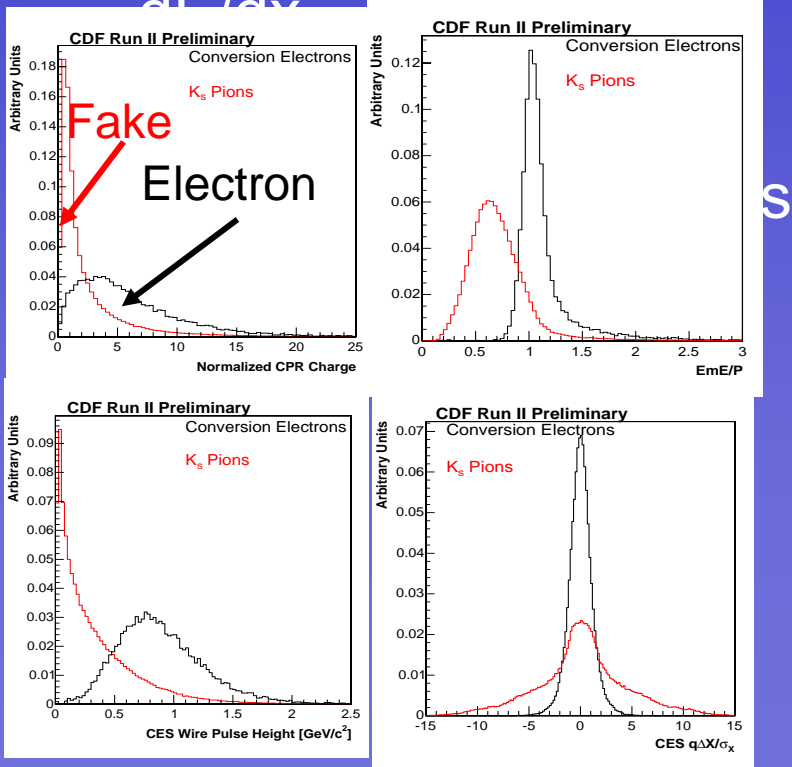
- In CDF electron ID uses
 - ~10 parameters
 - Calorimeter, tracking, dE/dx

- Use likelihood to improve separation

$$S = \prod_i S_i$$

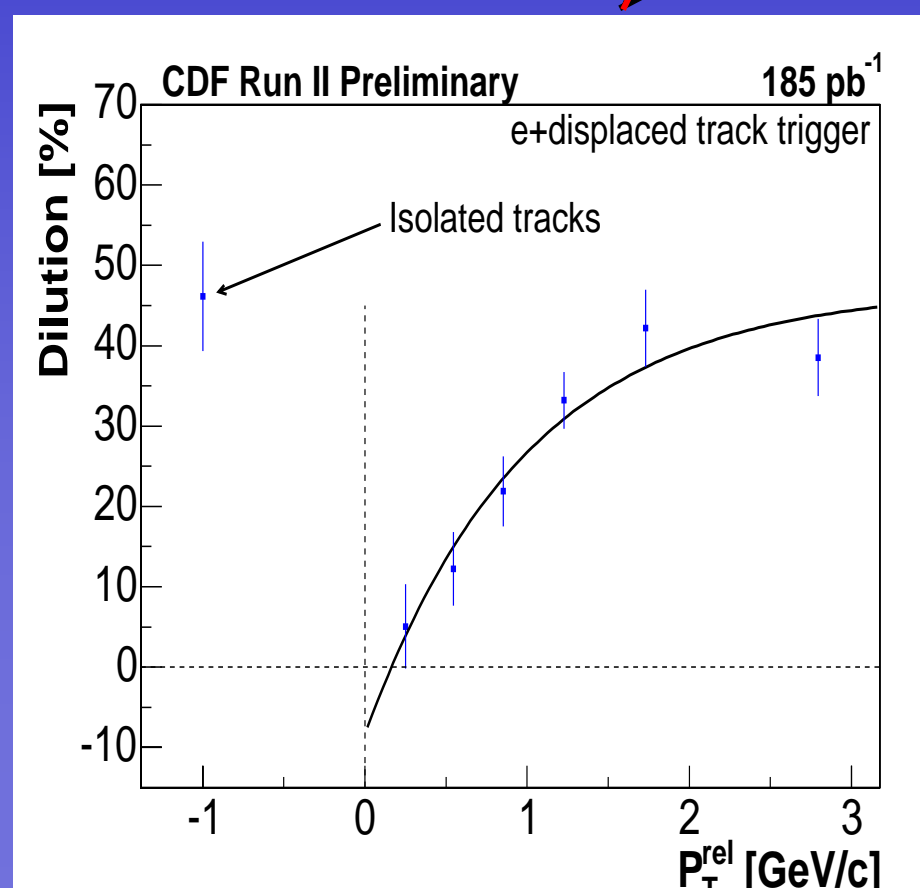
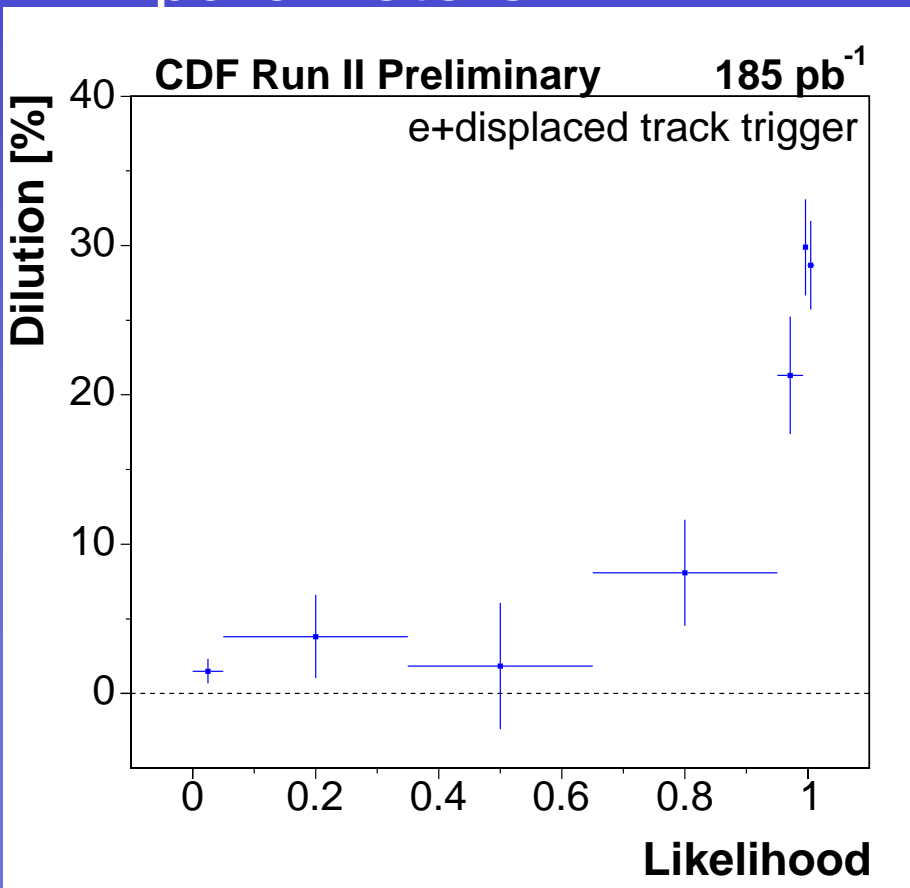
$$L = \frac{S}{S + B}$$

$$B = \prod_i B_i$$

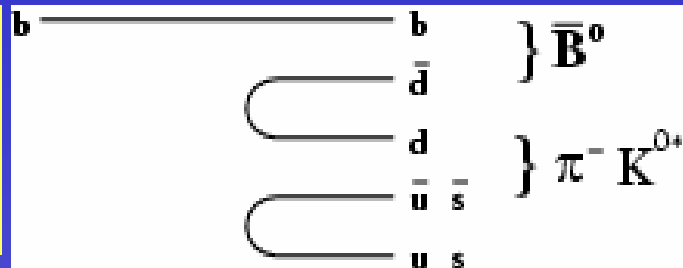


- For the Electron tagger, events are binnded in 2 parameters

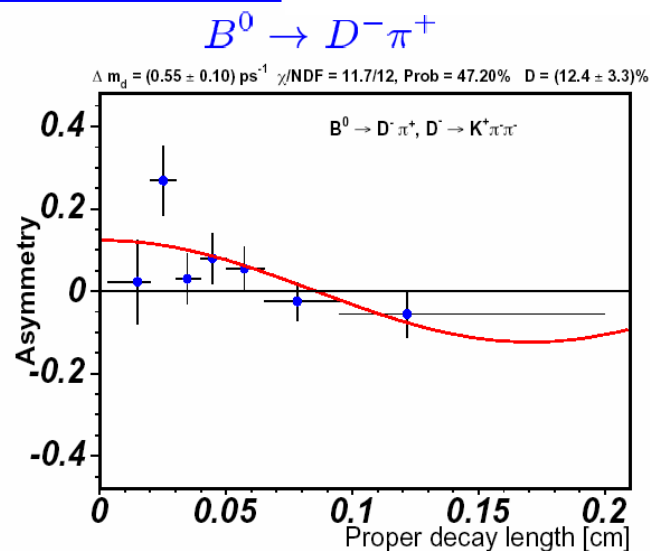
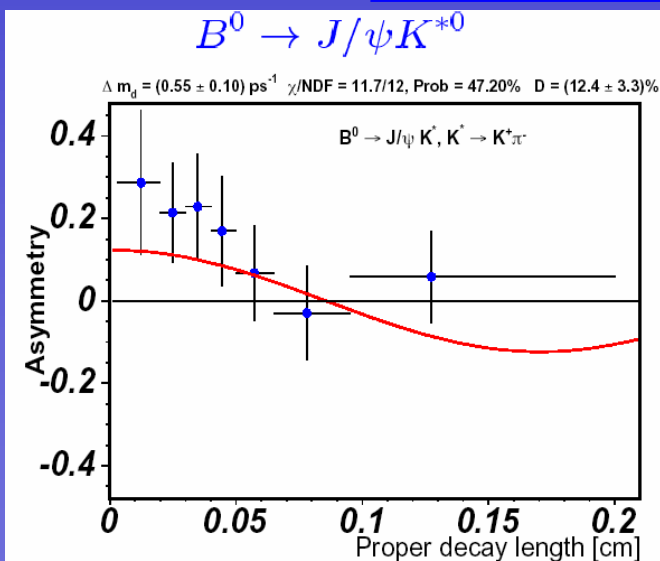
- Sequential B decay
 - $b \rightarrow c+l^-$
 - Higer p_T^{rel}
 - $b \rightarrow c \rightarrow s+l^+$



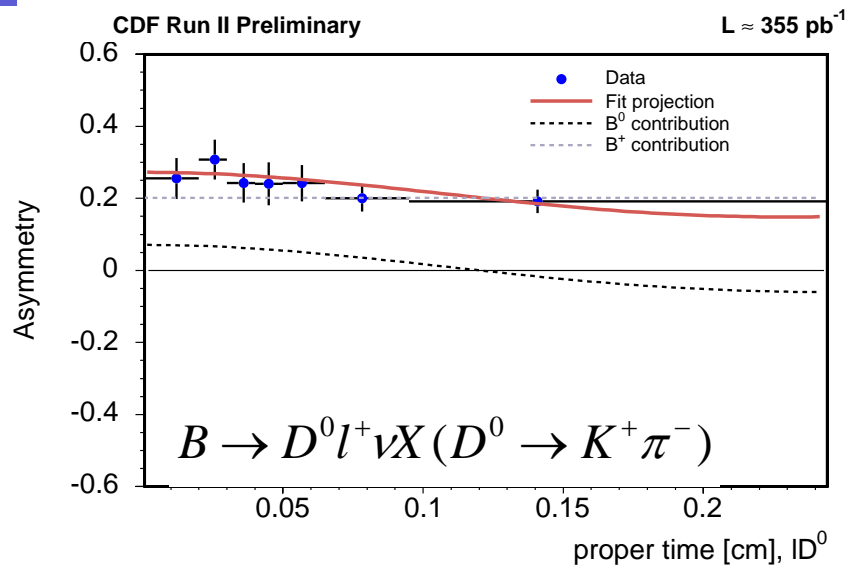
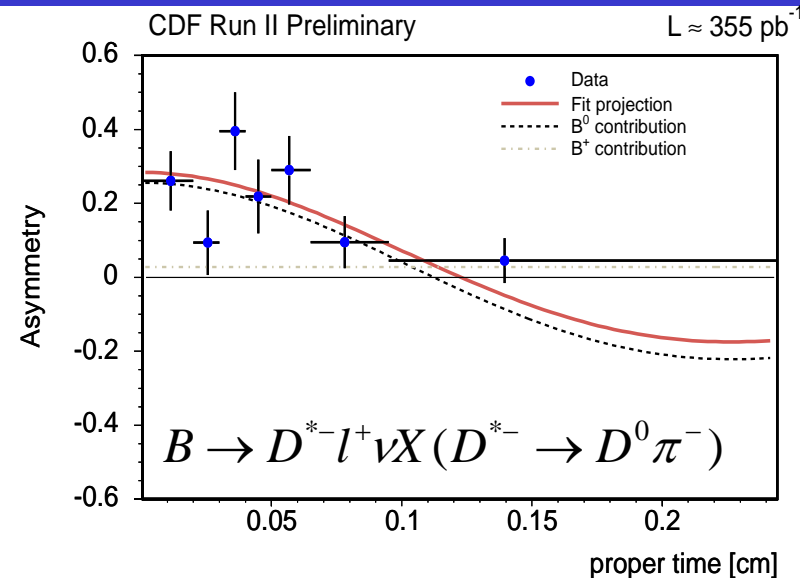
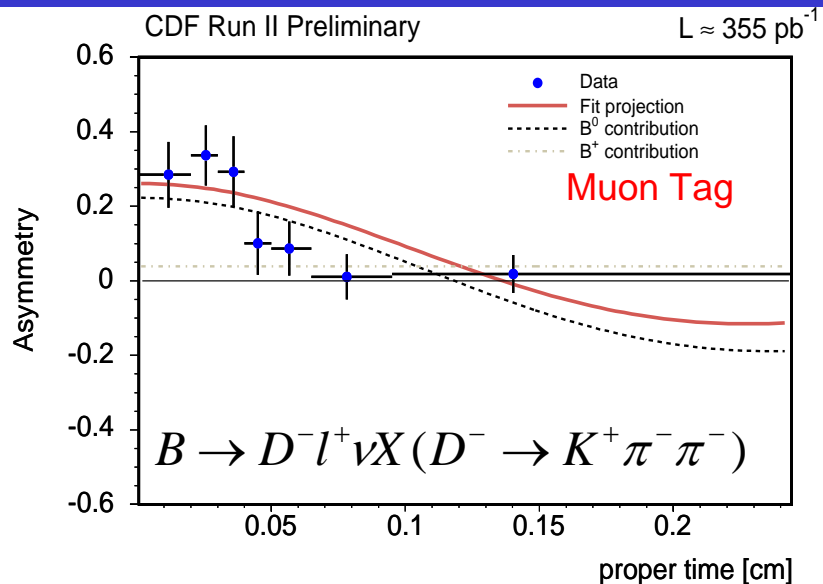
Based on correlation between charge of fragmentation π and flavor of b in B meson



Run II PRELIMINARY 2004



Δm_d (ps^{-1})	D_0 (%)	ϵD_0^2 (%)
0.55 ± 0.10	12.4 ± 3.3	1.0 ± 0.5

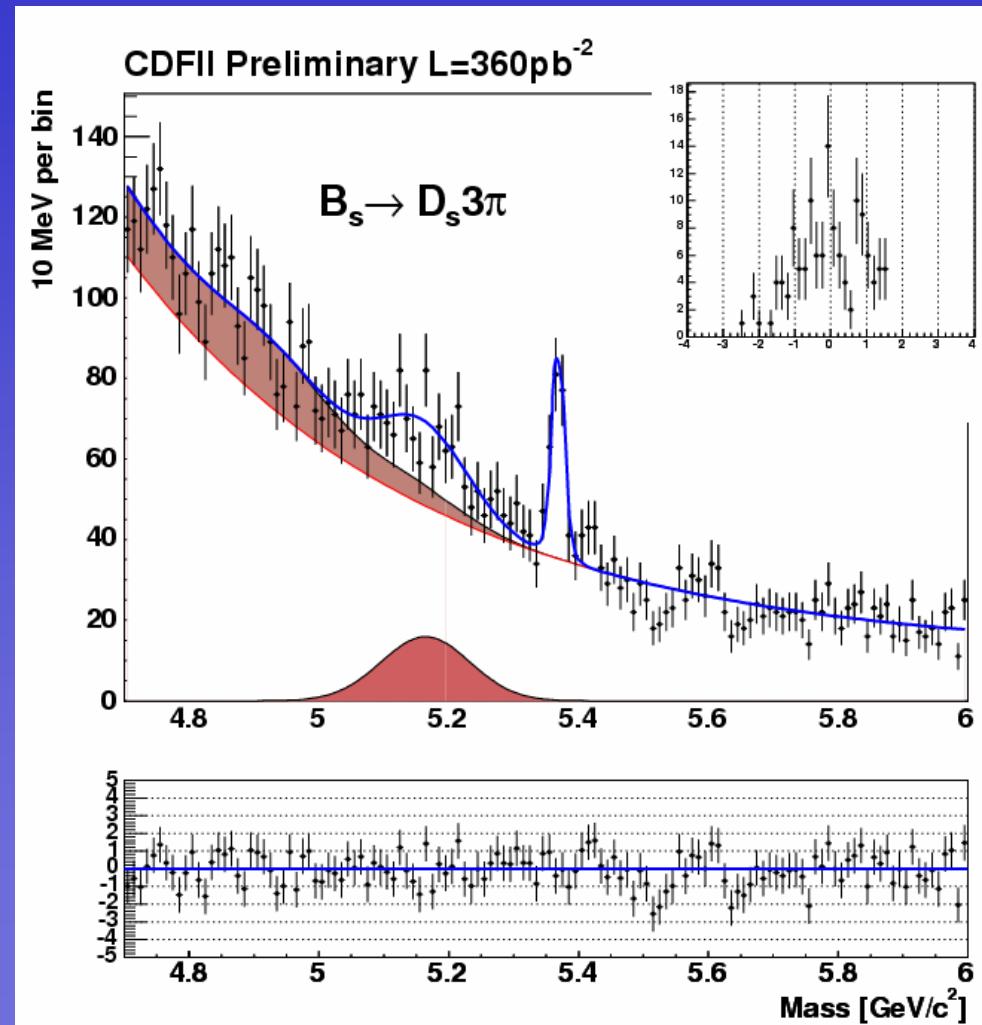


- Measure Δm_d
- Extract 5 dilution scale factors

→ The dilution scale factors are used for semileptonic B_s mixing analysis

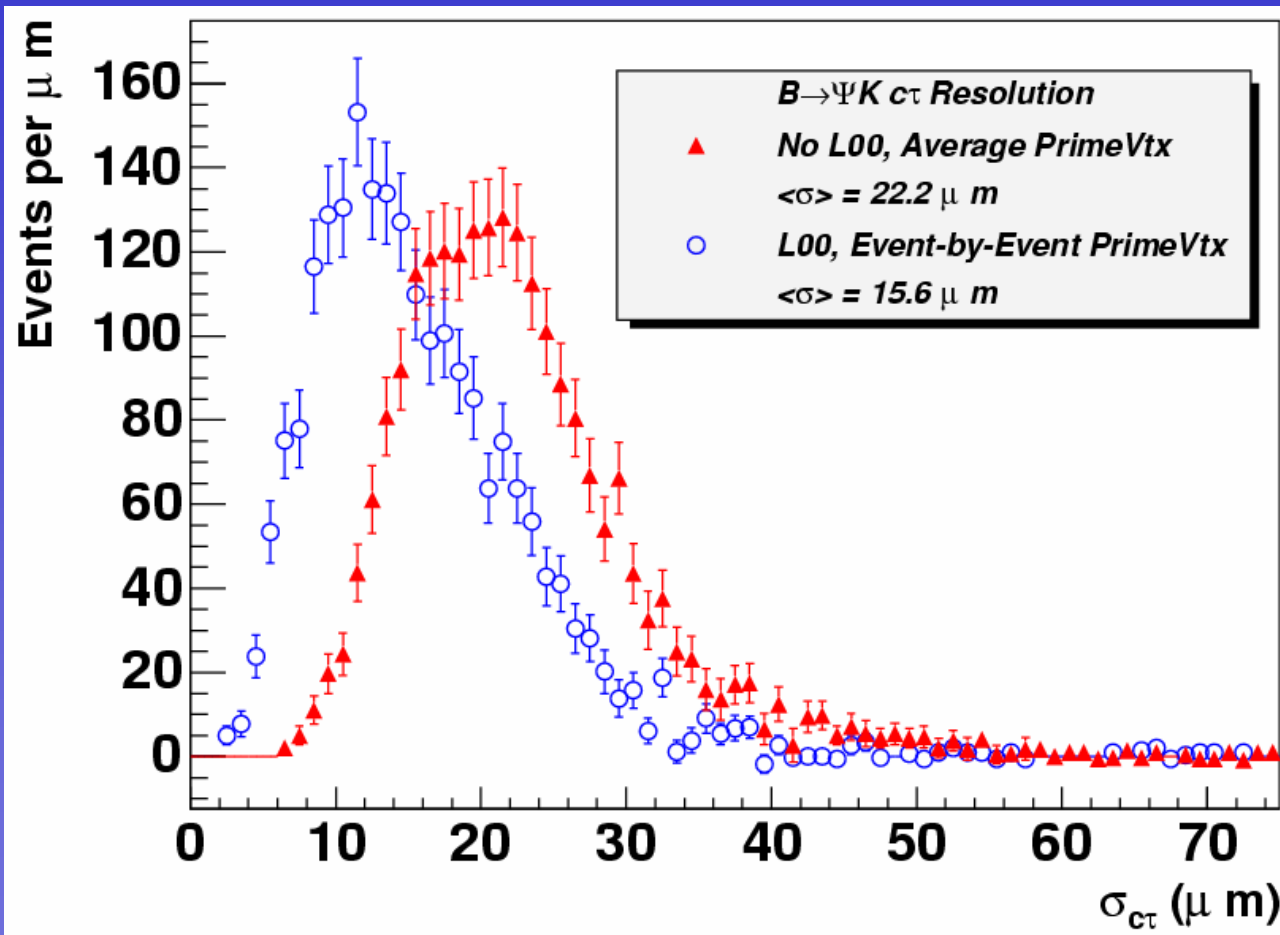
$$B_s^0 \rightarrow D_s^- \pi^+ \pi^- \pi^+$$

- 133 ± 23 B_s candidates
- Already used for lifetime
- But not for mixing
- 20% statistics



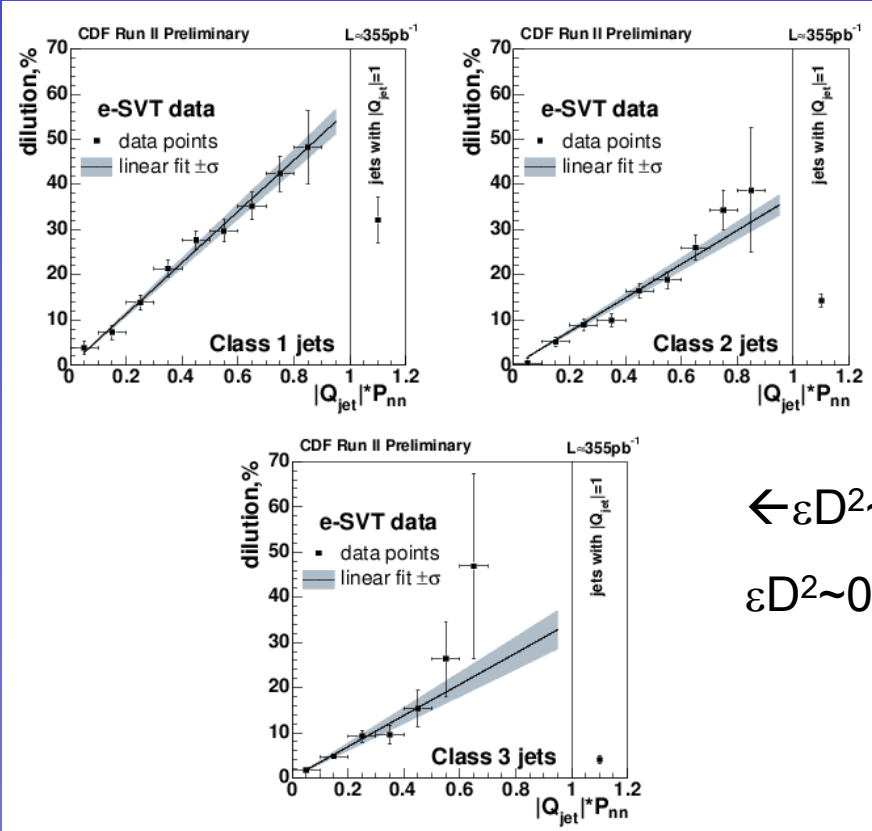
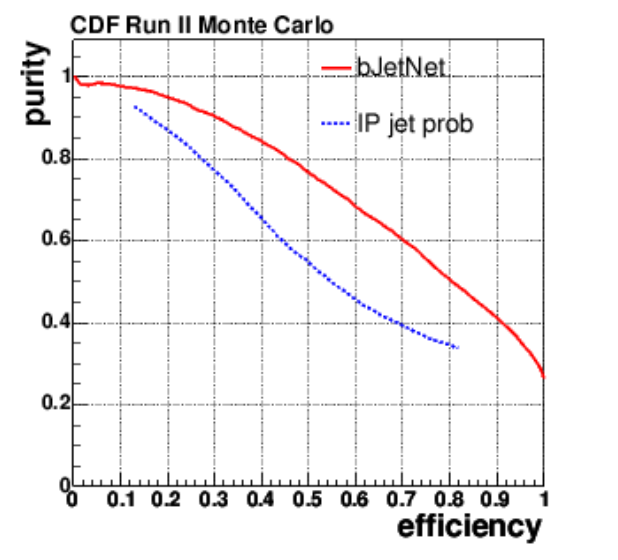
[example](#)

- No EbE/L00:
 - $\sigma \sim 67$ fs
- With EbE/L00:
 - $\sigma \sim 47$ fs
 - 30% improvement
- Not fully exploited yet (only L00)



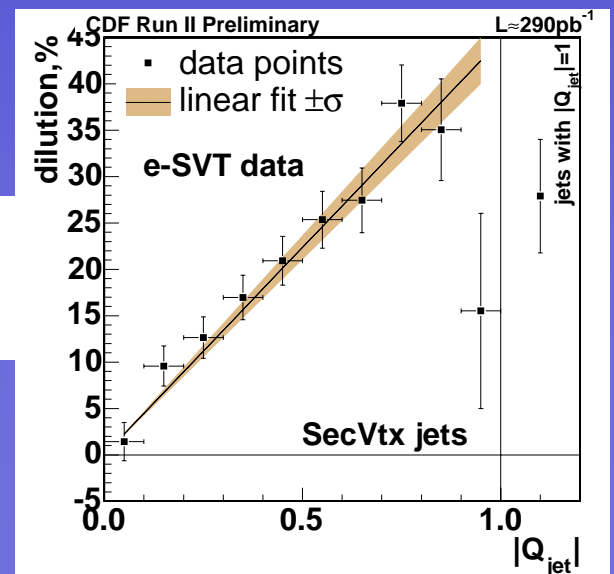
Nnet based

Weight each track by its probability to originate from b



$\leftarrow \epsilon D^2 \sim 0.9$

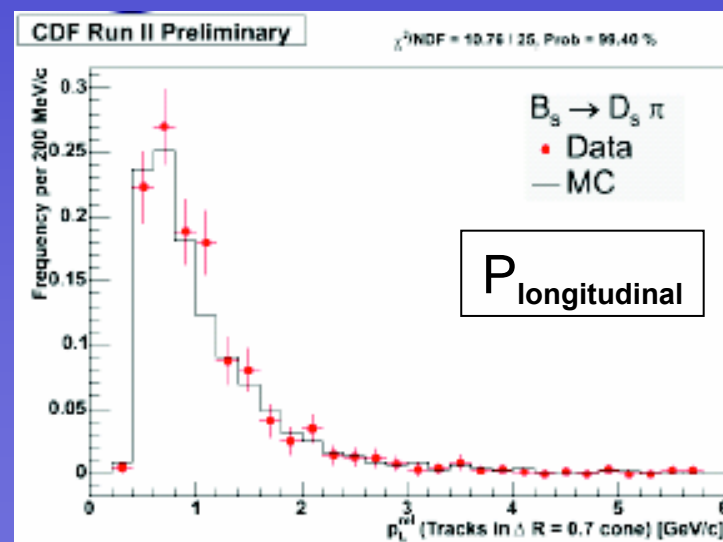
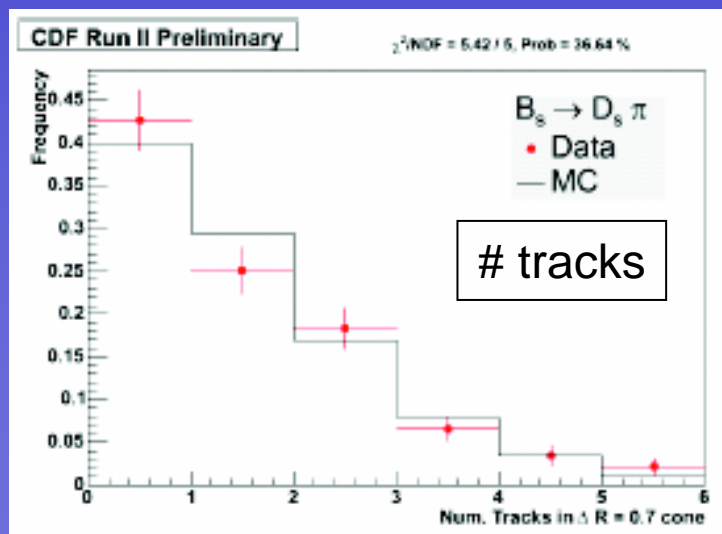
$\epsilon D^2 \sim 0.7 \rightarrow$



One possible way to solve the issue of having a prediction for the SSKT dilution is to extract it from MC.

→ Compare DATA with Pythia b-antib production and hadronization with all the processes on, underlying event “tune A” from HF x-sec. CDF data.

Look at the charged tracks in a cone of $\Delta R=0.7$ around the B_s (no PID)



good agreement !

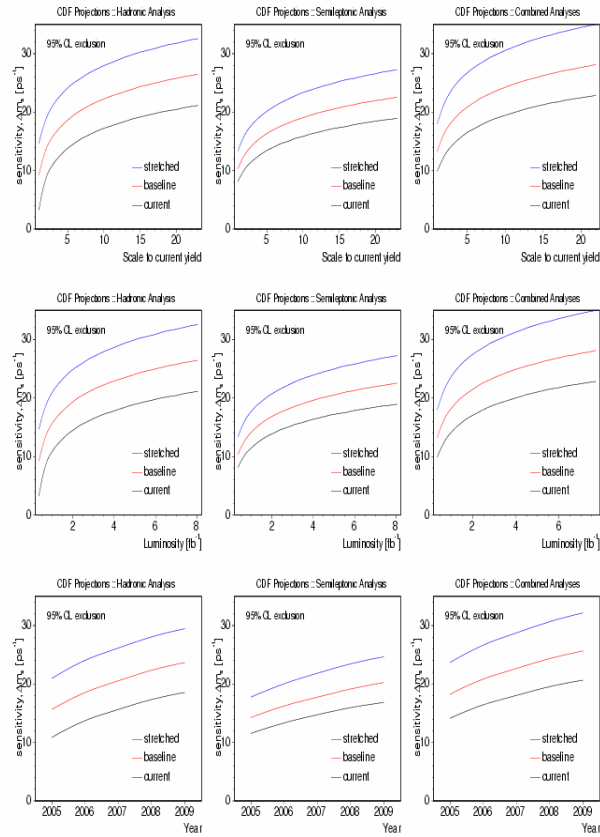


Figure 4: Sensitivity projections for 95% C.L. exclusion limit.

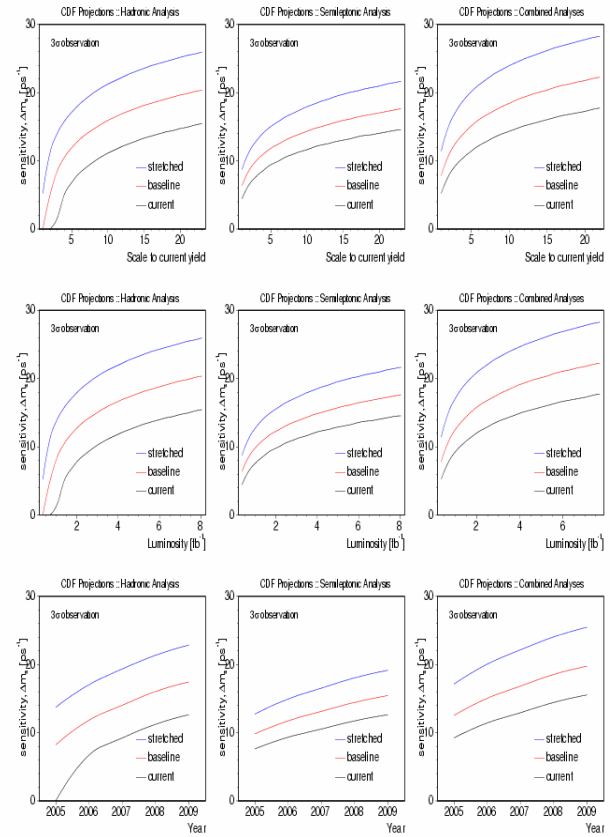
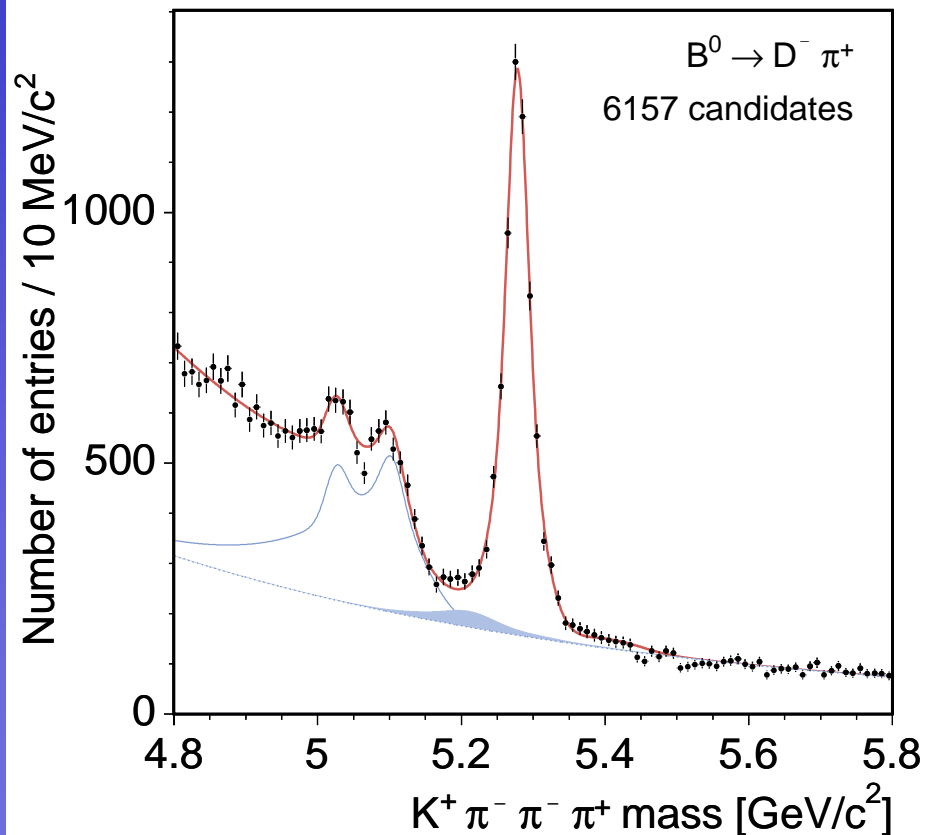


Figure 5: Sensitivity projections for 3σ observation.

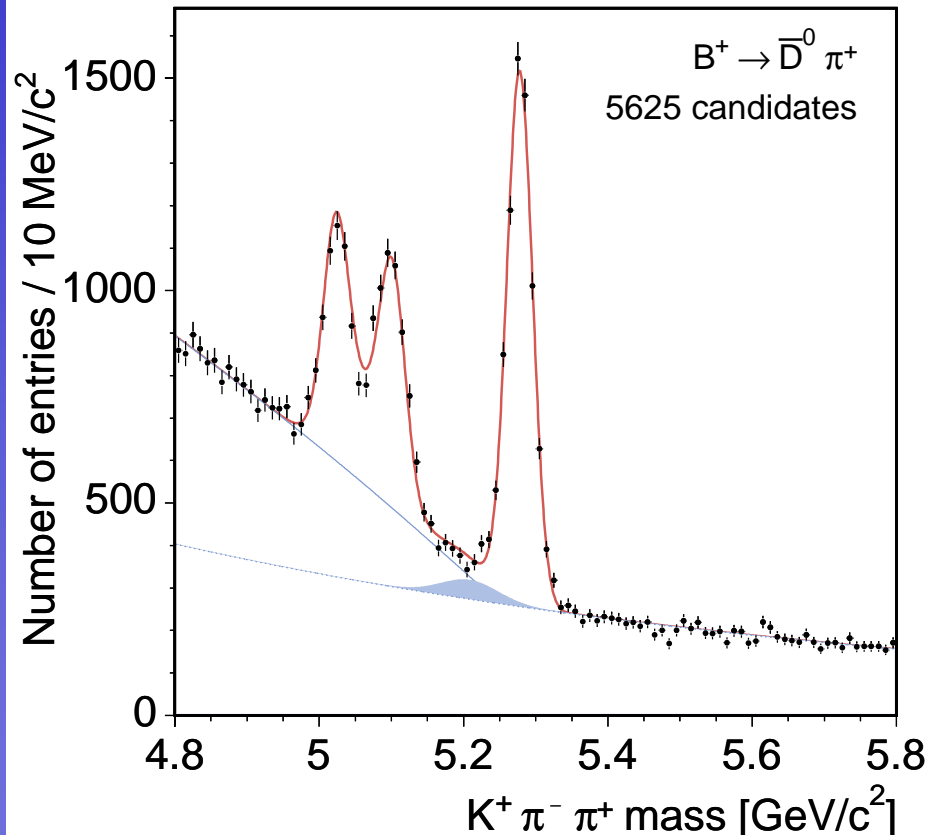
$$B^0 \rightarrow D^- \pi^+ (D^- \rightarrow K^+ \pi^- \pi^-)$$

$$B^+ \rightarrow D^0 \pi^+ (D^0 \rightarrow K^+ \pi^-)$$

CDF Run II Preliminary $L \approx 355 \text{ pb}^{-1}$



CDF Run II Preliminary $L \approx 355 \text{ pb}^{-1}$



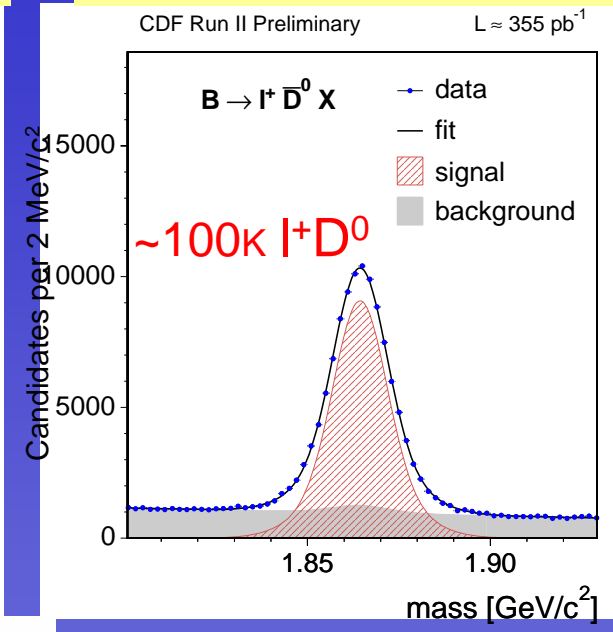
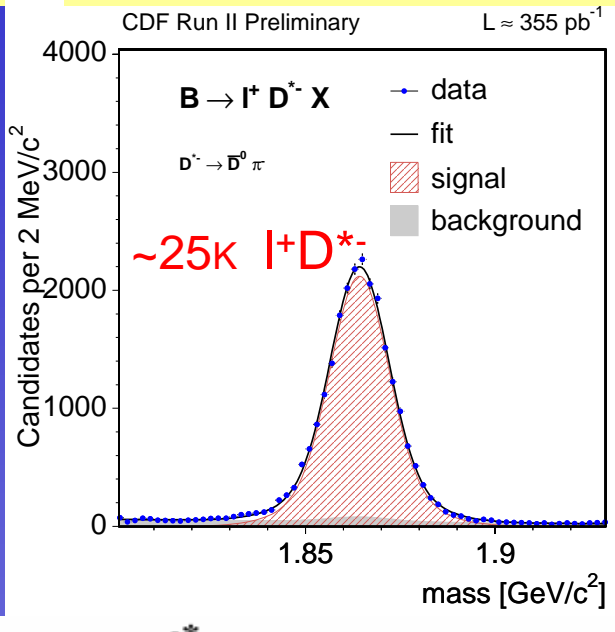
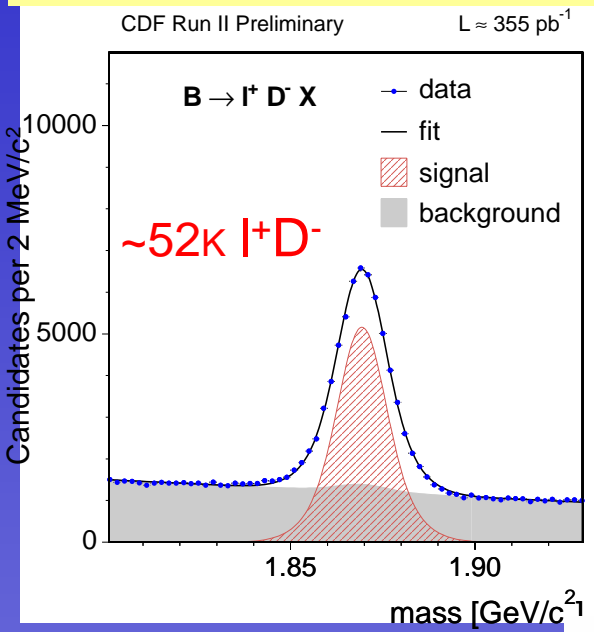
Semileptonic B^0 and B^+ Signals



$B \rightarrow D^- l^+ \nu X (D^- \rightarrow K^+ \pi^- \pi^-)$

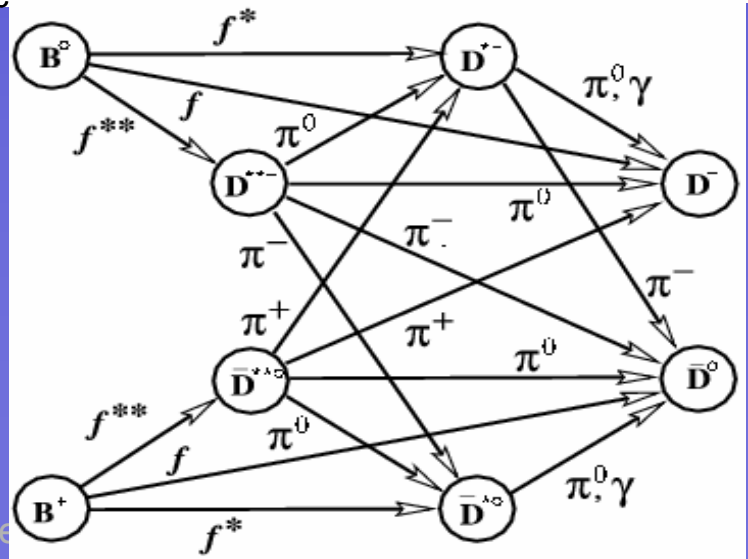
$B \rightarrow D^{*-} l^+ \nu X (D^{*-} \rightarrow D^0 \pi^-)$

$B \rightarrow D^0 l^+ \nu X (D^0 \rightarrow K^+ \pi^-)$



$B^0 \leftrightarrow B^+$ crosstalks:

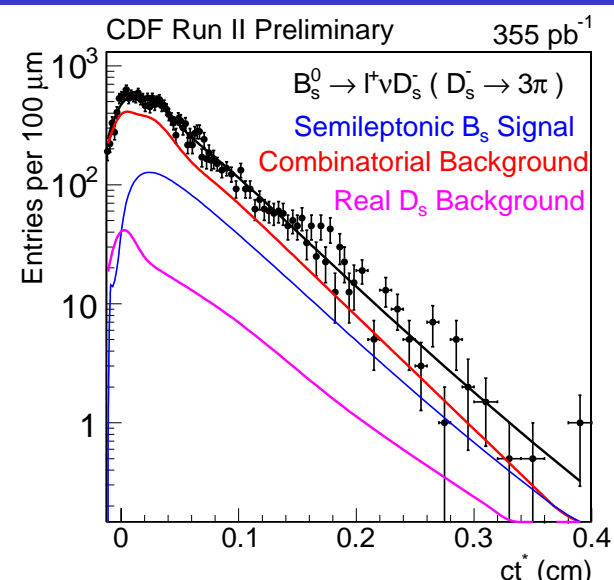
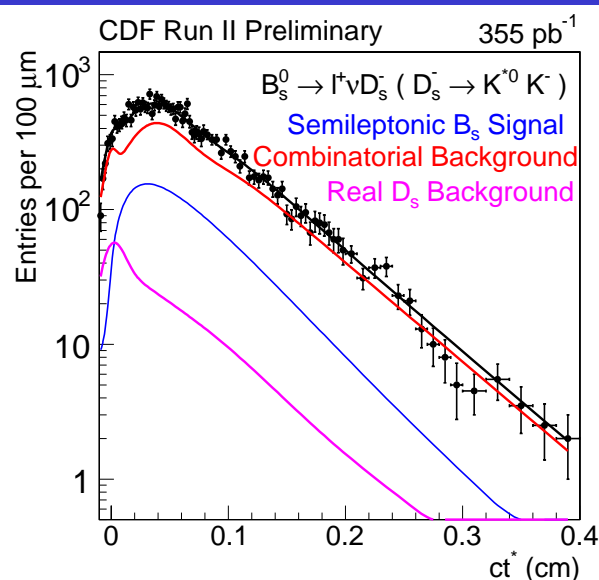
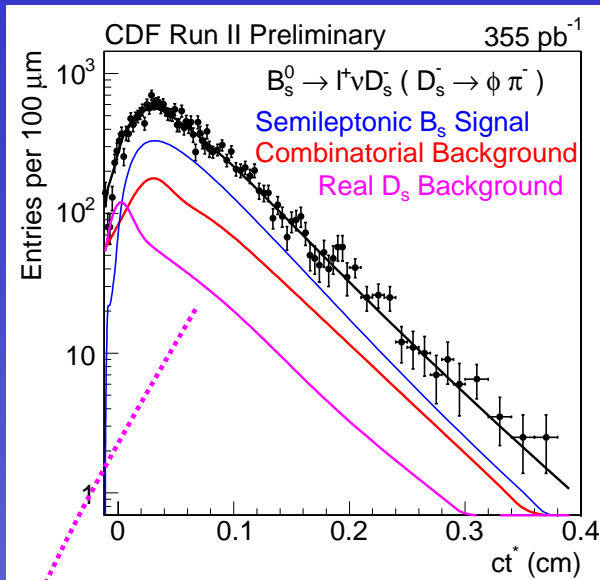
- $B^0 \rightarrow l^+ \nu D^-$
- $B^+ \rightarrow l^+ \nu D^{*0}$
- with ($D^{*0} \rightarrow D^0 \pi^+$)



Sample composition

- $l^+ D^+$: $B^0/B^+ \sim 85/15$
- $l^+ D^{*+}$: $B^0/B^+ \sim 85/15$
- $l^+ D^0$: $B^0/B^+ \sim 20/80$

Lifetime in the semileptonic B_s modes



$\tau = 1.521 \pm 0.040 \text{ ps}$

$c\tau = 413.8 \pm 20.1 \mu\text{m}$

$c\tau = 422.6 \pm 25.7 \mu\text{m}$

Combined ℓ - D_s lifetime result: **$445.0 \pm 9.5 \mu\text{m}$**

statistical err. only,

\rightarrow NOT for Averages \leftarrow

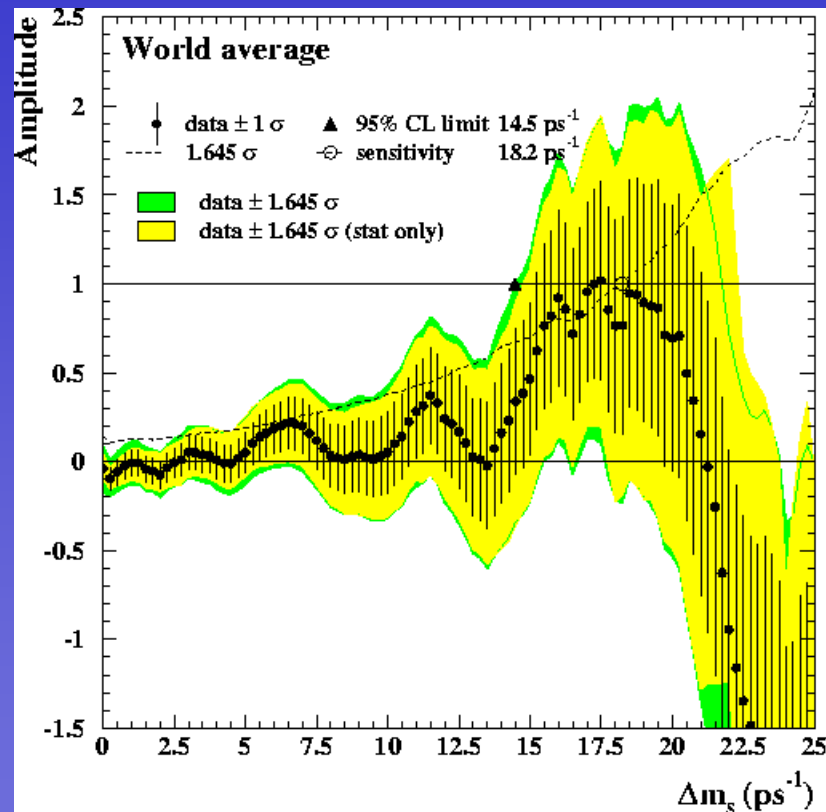
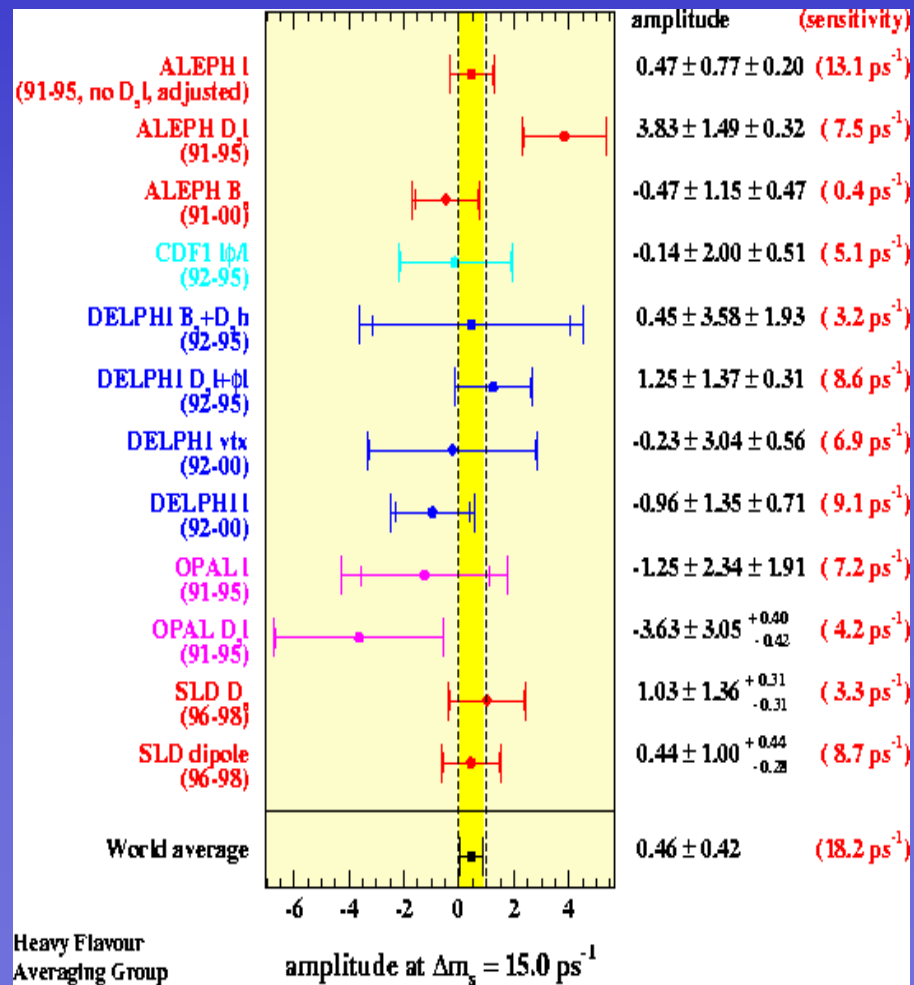
(W.A.: $438 \pm 17 \mu\text{m}$)

($D\emptyset$ '05: $426 \pm 13 \pm 17 \mu\text{m}$)

Real D_s backgrounds: prompt and physics

Present limit (HFAG 2004)
from: LEP / SLD / CDF run I

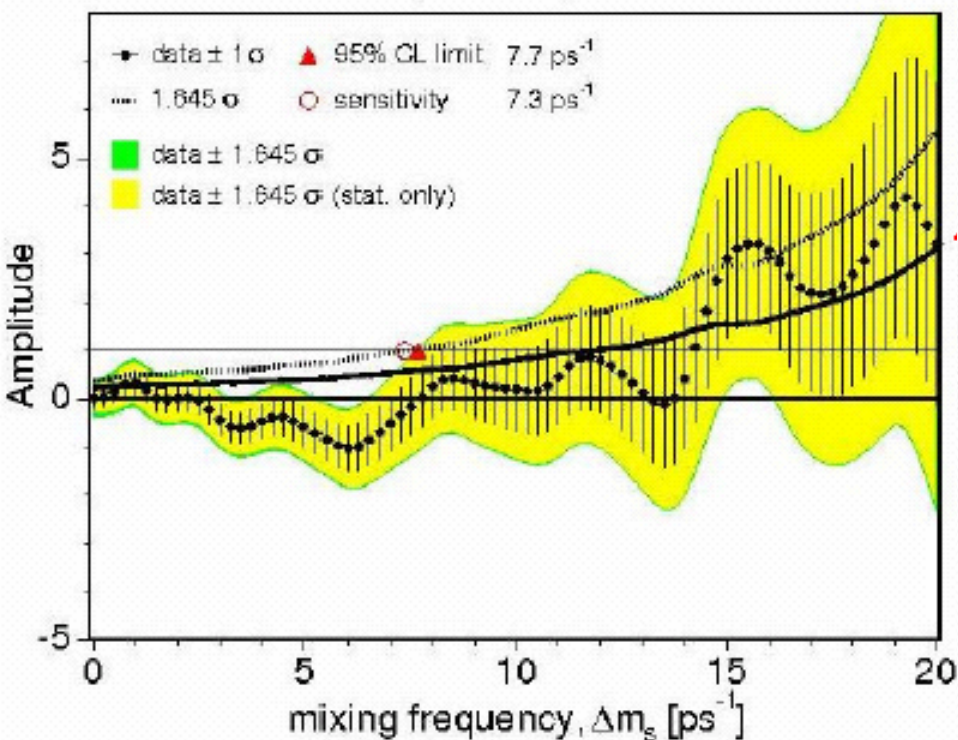
Amplitude scan method discussed later



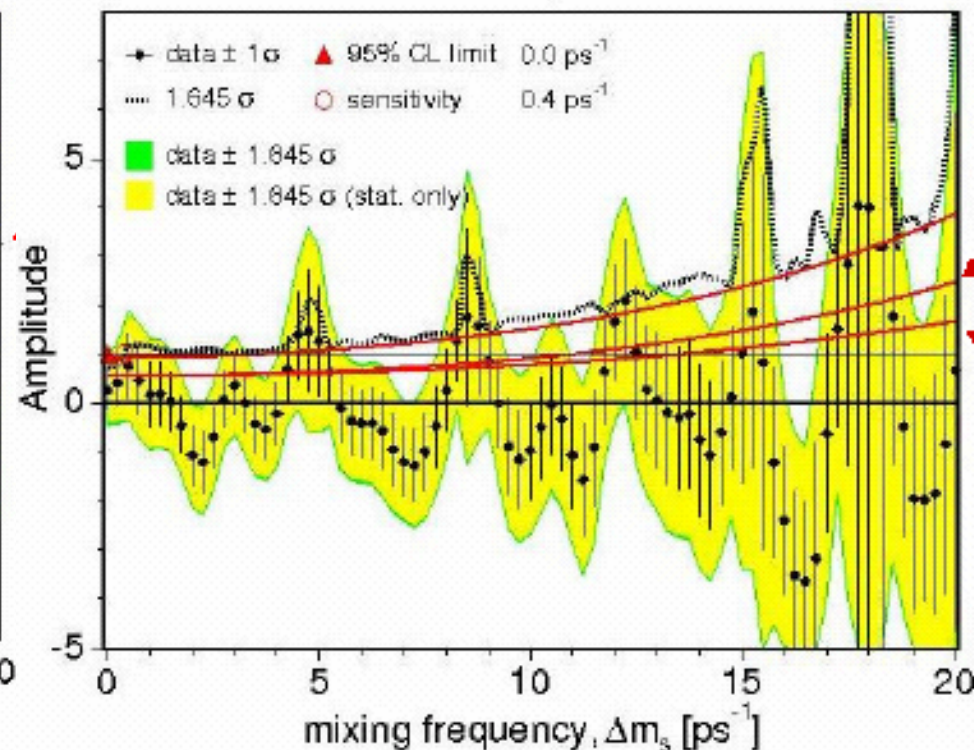
- 95% CL limit is : $\Delta m_s > 14.5 \text{ ps}^{-1}$
- Sensitivity: 18.2 ps^{-1}

Increase the actual effective statistics **x4** (i.e. increase $N\epsilon D^2$ x4)

Semileptonic Analysis CDF II



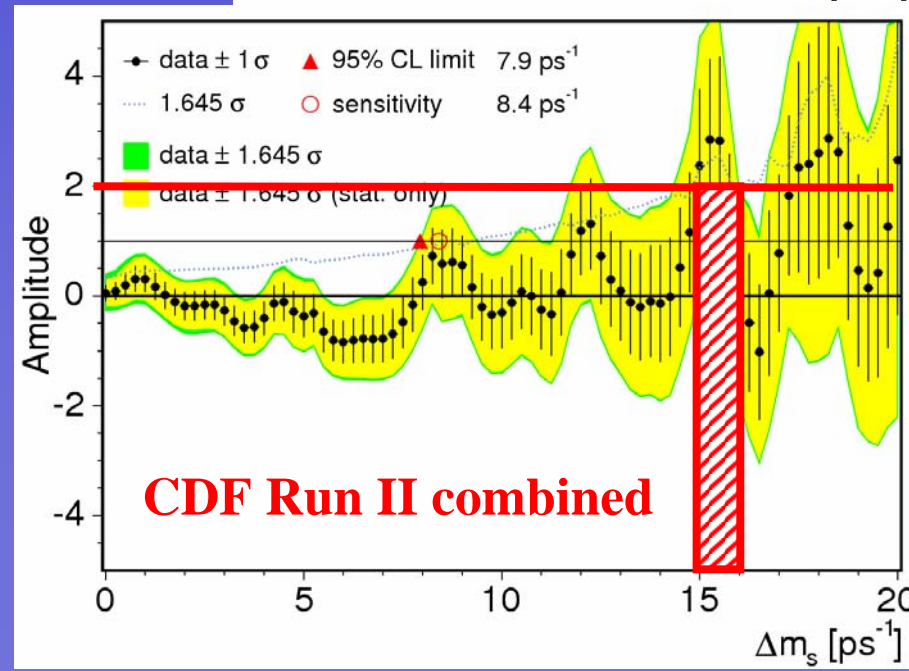
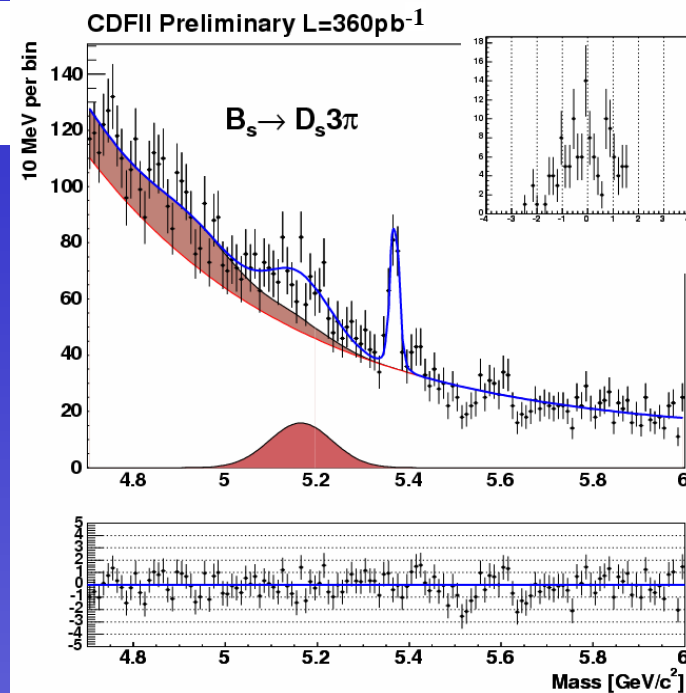
Hadronic Analysis CDF II



- Hadronic analysis will begin to lead the sensitivity
- Start to “eat” interesting Δm_s range combining the 2 analysis

MIXING Improvements

- Include Same Side (Kaon) Tagging
 - Expect twice tagging power than OST combined
 - x3 statistical power! ... but systematics limited in setting a limit
- Improve accuracy of primary vertex
 - - 20% on $\sigma(\text{ct}) \rightarrow$
 - +40% on εD^2 @ $\Delta m_s = 10 \text{ ps}^{-1}$
- Add more channels +30%
 - $B_s \rightarrow D_s 3\pi$
 - $B_s \rightarrow D_s^* \pi, B_s \rightarrow D_s \rho^+$
- x4 statistical power feasible with same data set \rightarrow x2 on amplitude error



Decay vertex error matrix overall correction for mis-knowledge of hit resolution

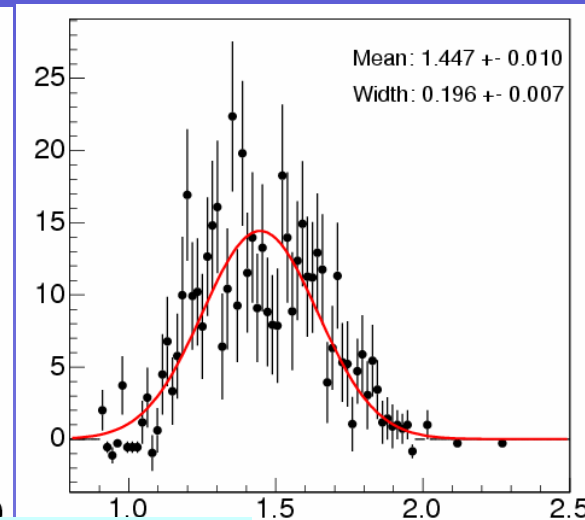
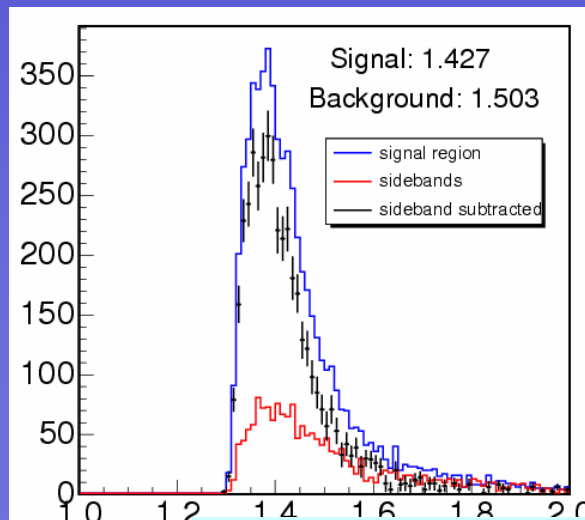
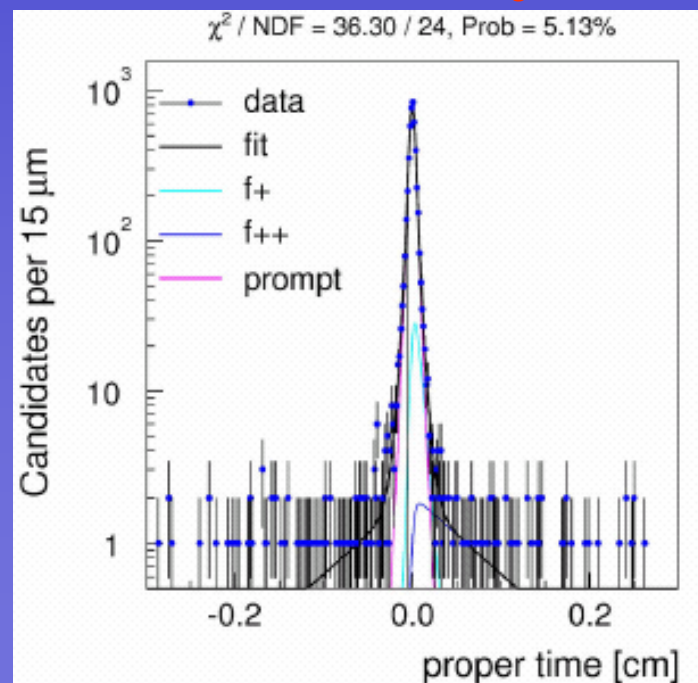
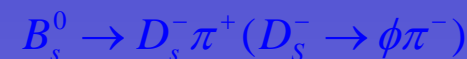
→ Apply a scale factor S to $\sigma(ct)$ from vertex fit:

- Huge control sample: D_s^\pm + random track to emulate B_s decay topology
- Correct for small (10%) secondary D_s^\pm in the sample
- Parameterize S in terms of several variables (P_T , Isolation,...)
- Correct $\sigma(ct)' = S \cdot \sigma(ct)$ event by event.

Prompt track + D_s vertex

“Semileptonic” B_s signal

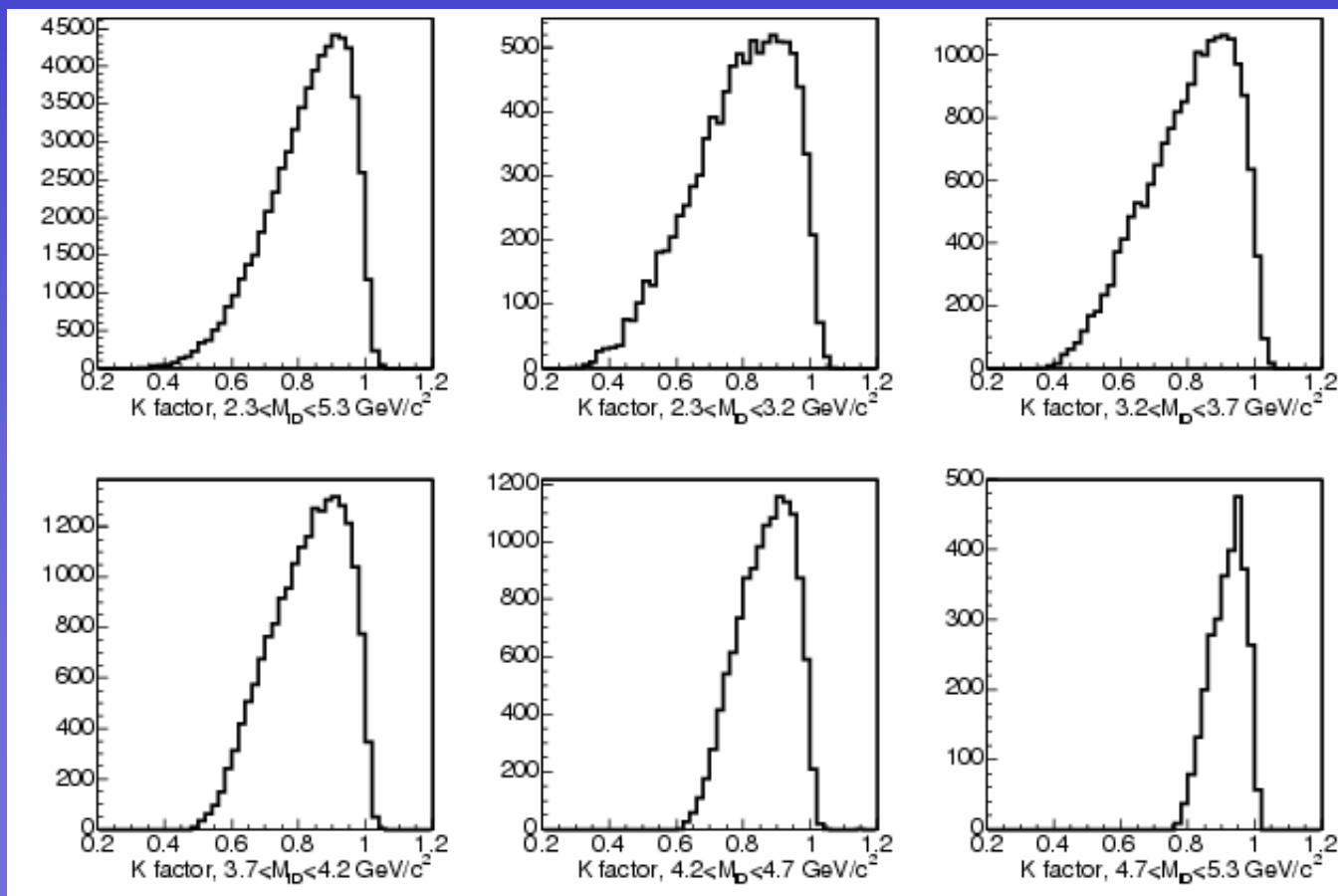
“Hadronic” B_s signal



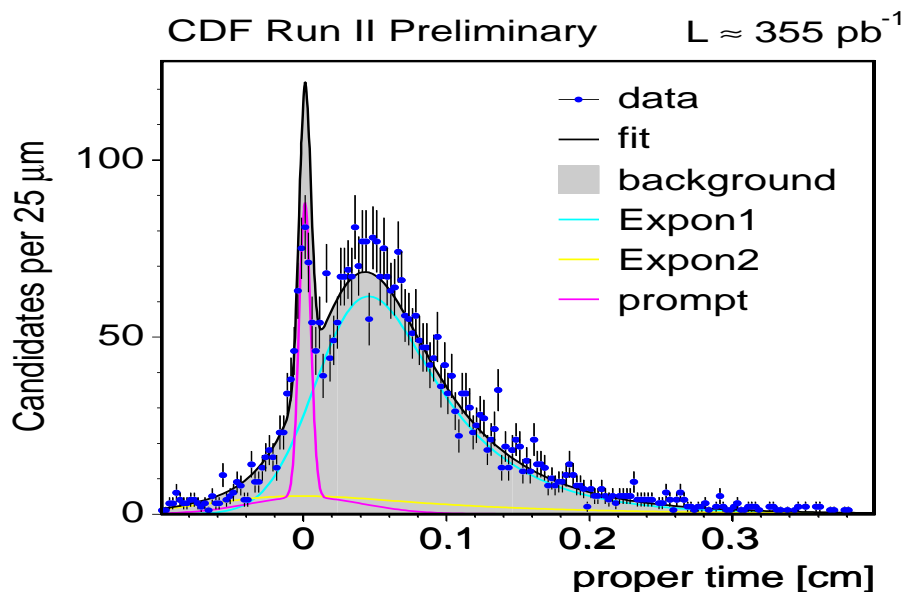
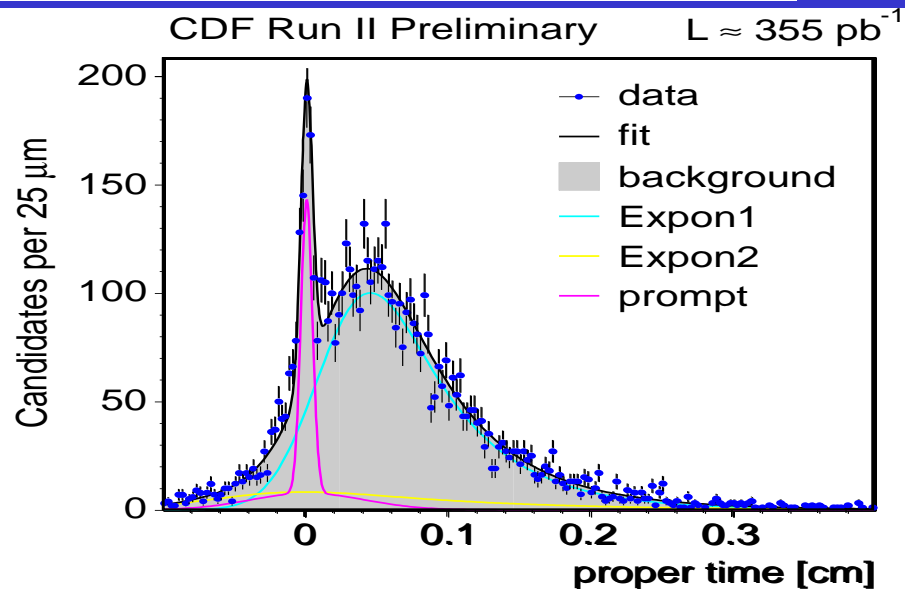
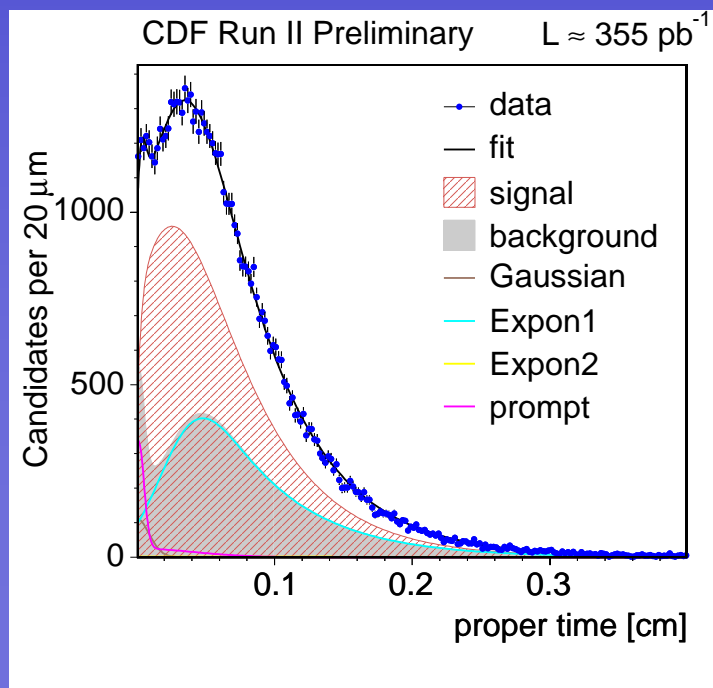
$$L(t) = Gaus(t;0, S \cdot \sigma_t)$$

tor, $B_s \rightarrow D_s \pi, D_s \rightarrow \phi \pi$

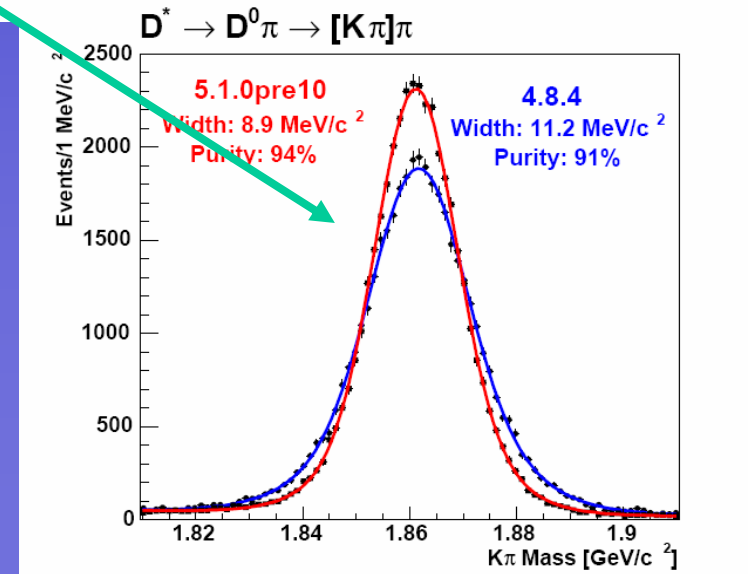
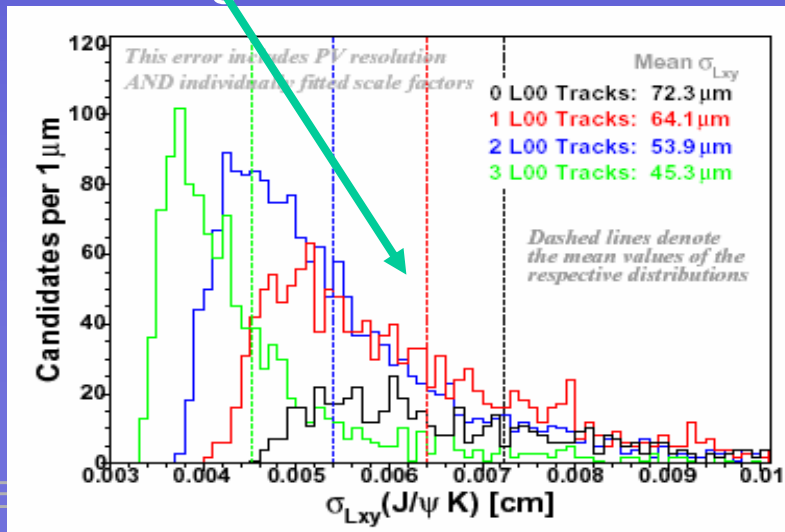
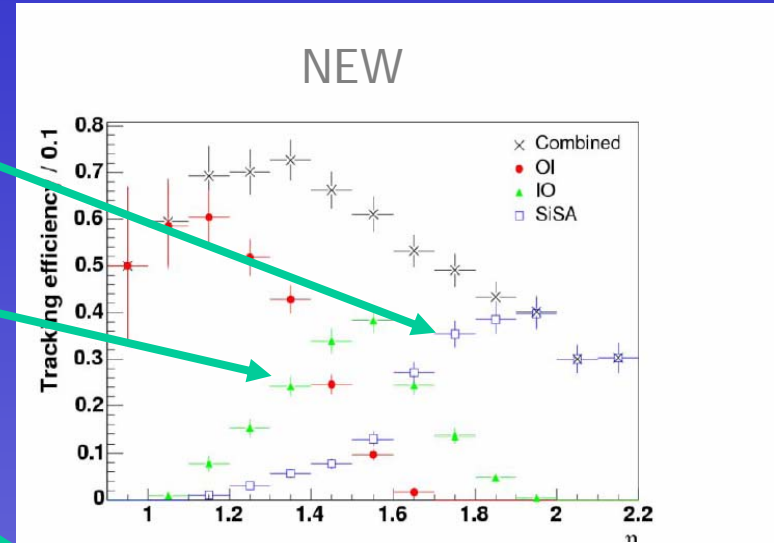
- Resolution of K factor:
 - better for high M(ID)
 - Dividing event in different M(ID)
- Evaluate K factor in each M(ID) bin
 - Improve the decay time resolution



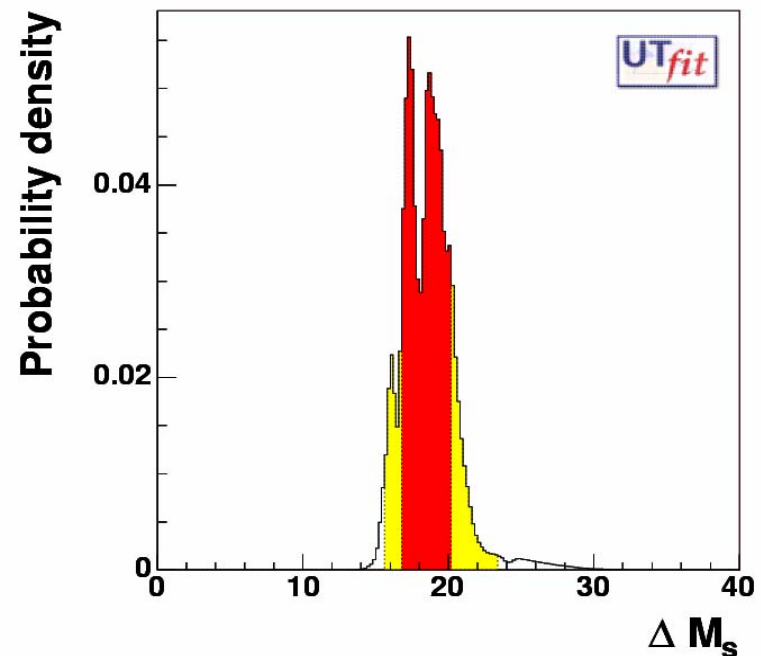
- Clear prompt peak also in the right sign lepton + D⁺ events
- Event tagged with high dilution tagger (Muon, Electron, Vertex)
 - Prompt background is reduced
 - No opposite side B for prompt BG



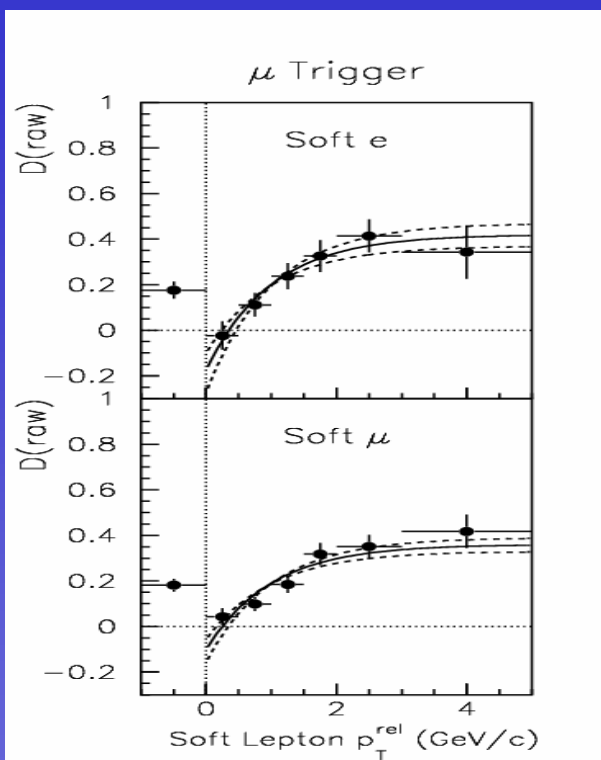
- Great progress in Si stand-alone
- Substantial efficiency improvement at large η and low- p_t
- Improved mass resolution
- L00 now ready for physics:
 - eff. 60% and growing
 - Clear improvement in $\sigma(L_{xy})$, crucial for Bs mixing



- Strange peaks in expected Dms being there already before Tevatron new input



Run I



Run II

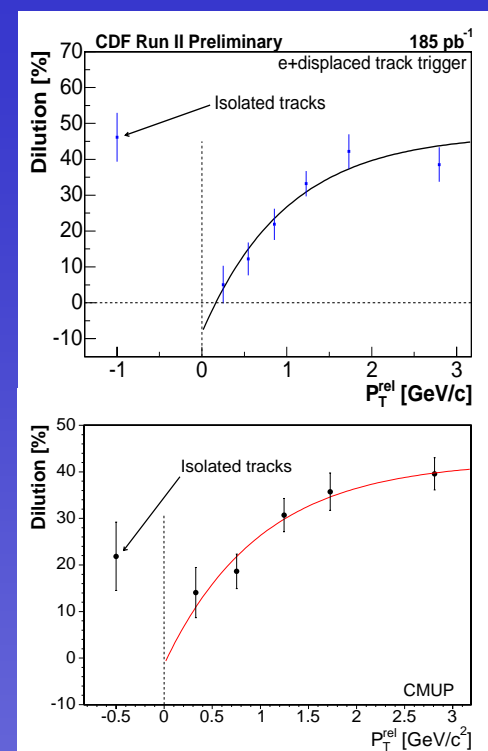
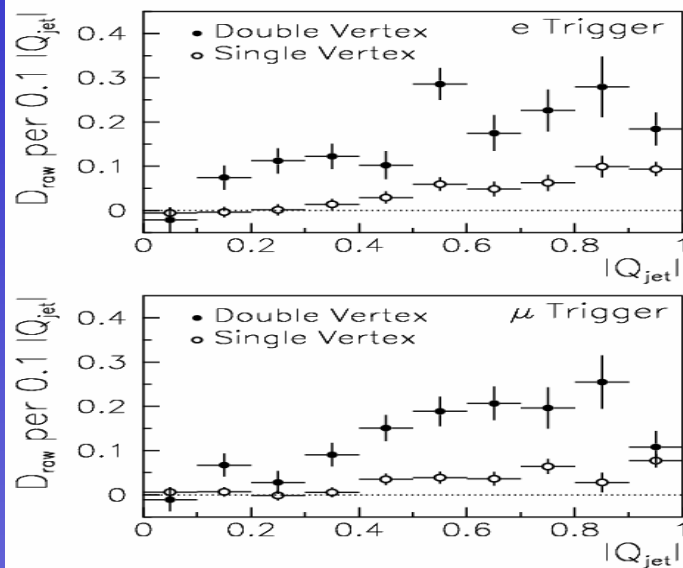


TABLE X. The statistical power ϵD^2 for the flavor tagging methods used: Jet-Charge Single Vertex (JCSV), Jet-Charge Double Vertex (JCDV), and Soft-Lepton Tag (SLT). Results for the e and μ trigger data are shown in separate rows. The sum is over bins of p_T^{rel} for the soft-lepton data and $|Q_{\text{jet}}|$ for the jet-charge data, as shown in Figures 7 and 9, respectively. The square of the dilution normalization factor N_D is used to rescale the $\sum_i \epsilon_i D_{\text{mw } i}^2$ value to give $\sum_i \epsilon_i D_i^2$. The first error is statistical, the second systematic.

Sample	Total ϵ	$\sum_i \epsilon_i D_{\text{mw } i}^2$	N_D	$\sum_i \epsilon_i D_i^2$
JCSV (e)	41.55 ± 0.14 %	0.077 ± 0.016 %	$1.88 \pm 0.20 \pm 0.15$	$0.27 \pm 0.06 \pm 0.04$ %
JCDV (e)	7.44 ± 0.08 %	0.159 ± 0.023 %	$1.76 \pm 0.13 \pm 0.09$	$0.49 \pm 0.10 \pm 0.05$ %
SLT (e)	4.38 ± 0.06 %	0.329 ± 0.033 %	$1.72 \pm 0.08 \pm 0.11$	$0.97 \pm 0.13 \pm 0.12$ %
JCSV (μ)	43.81 ± 0.14 %	0.048 ± 0.012 %	$2.41 \pm 0.29 \pm 0.39$	$0.28 \pm 0.06 \pm 0.05$ %
JCDV (μ)	7.66 ± 0.07 %	0.113 ± 0.018 %	$2.14 \pm 0.33 \pm 0.25$	$0.52 \pm 0.18 \pm 0.12$ %
SLT (μ)	4.54 ± 0.06 %	0.210 ± 0.026 %	$2.01 \pm 0.13 \pm 0.22$	$0.85 \pm 0.15 \pm 0.19$ %

	ϵD^2 (%)
Muon	(0.70 ± 0.04) %
Electron	(0.37 ± 0.03) %
	(0.36 ± 0.02) %
	(0.36 ± 0.03) %
	(0.15 ± 0.01) %
	~ 1.6 %

Run I



Run II

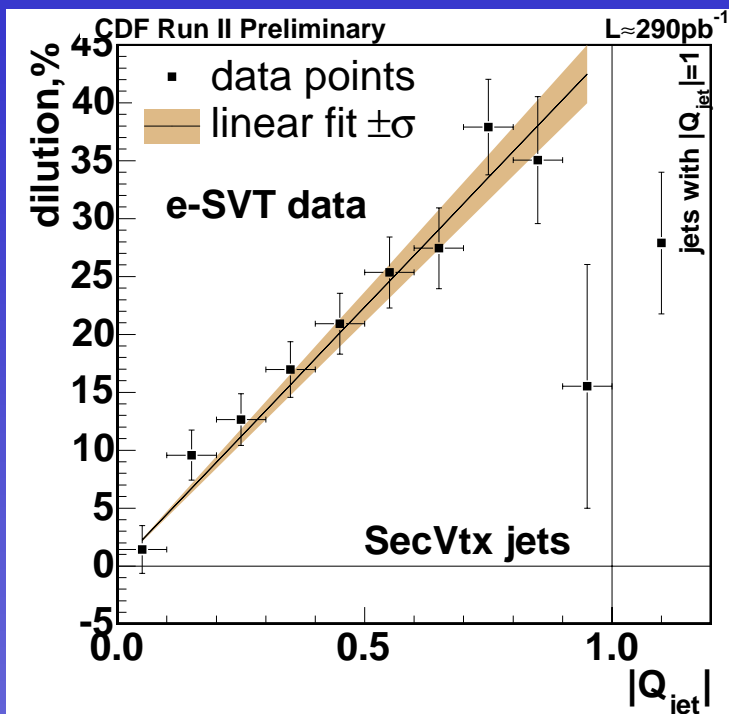


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SLT (μ)	4.54 ± 0.06 %	0.210 ± 0.026 %	$2.01 \pm 0.13 \pm 0.22$	$0.85 \pm 0.15 \pm 0.19$ %

	ϵD^2 (%)
	(0.70 ± 0.04) %
	(0.37 ± 0.03) %
2ndary vtx	(0.36 ± 0.02) %
Displaced track	(0.36 ± 0.03) %
Highest p jet	(0.15 ± 0.01) %
	~ 1.6 %