

Jet Energy Scale Determination at CDF

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Talk Overview

- ➔ Introduction
 - ➔ Jets
 - ➔ Physics with jets

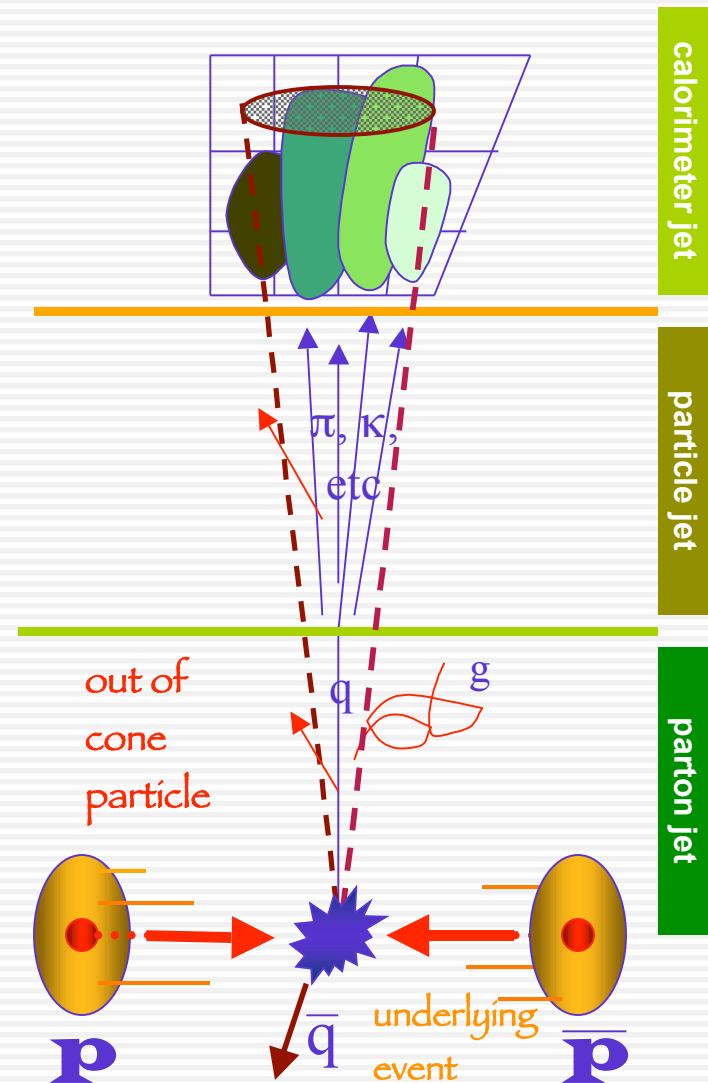
- ➔ Corrections and uncertainties
 - ➔ Different levels of jets
 - ➔ Does the Monte Carlo reproduce the data?

- ➔ Tests and cross-checks
 - ➔ Are the corrections accurate?
 - ➔ Are the uncertainties believable?

- ➔ Conclusions

Jets

- ➔ Measurements of hard scattering processes in $p\bar{p}$ collisions depend on the determination of the 4-momenta of quarks and gluons produced in the hard scatter
- ➔ The measurement of these 4-momenta relies on the reconstruction of hadronic jets resulting from the quark or gluon fragmentation
- ➔ Jets are complicated objects measured by **calorimeter towers** and defined by a **clustering algorithm**
- ➔ To convert **jet energies** to **parton energies** we need to correct for:
 - ➔ Instrumental effects
 - ➔ Physics effects
 - ➔ Jet algorithm effects



Jets

Instrumental effects:

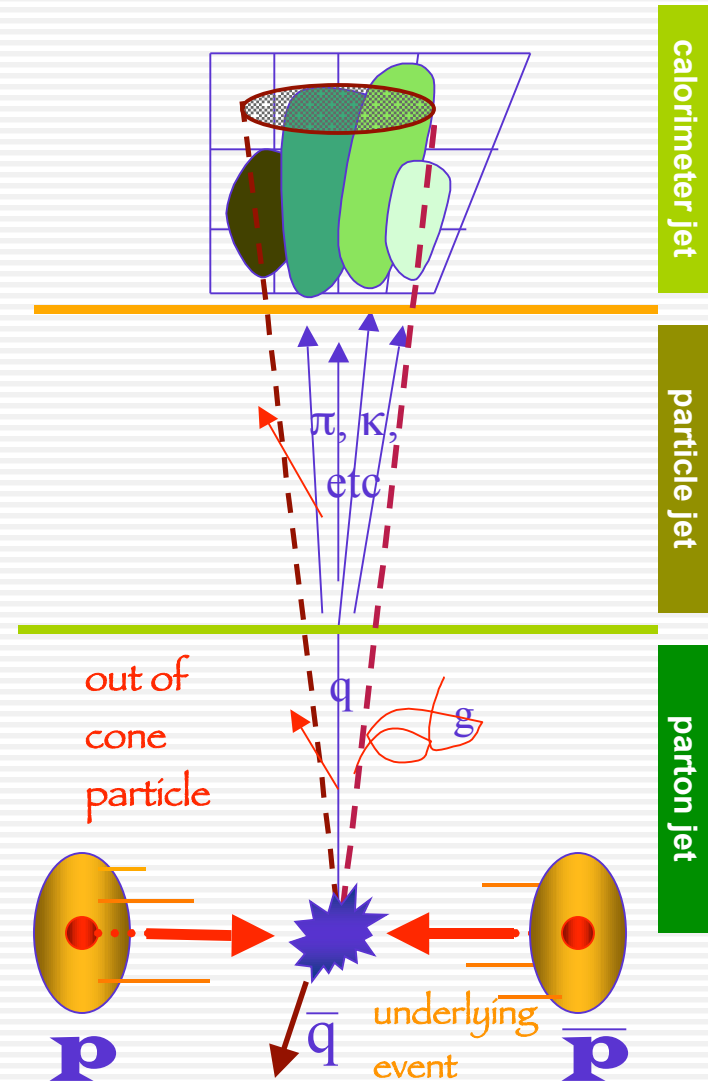
- non-linear calorimeter
- non-instrumented regions
- non-compensating calorimeter
- may not contain low energy deposition

Algorithm effects:

- might not capture all particles
- low energy jets might not be possible to define

Physics effects:

- hadronization
- spectator interactions
- radiation
- multiple ppbar interactions
- flavor of the parent parton



Physics with Jets

⇒ Much interesting physics is done with jets.
Some analyses require a better (or different)
knowledge of the jet energies

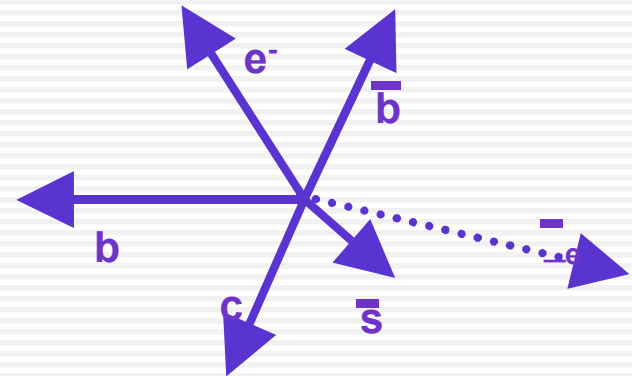
⇒ QCD

⇒ Searches

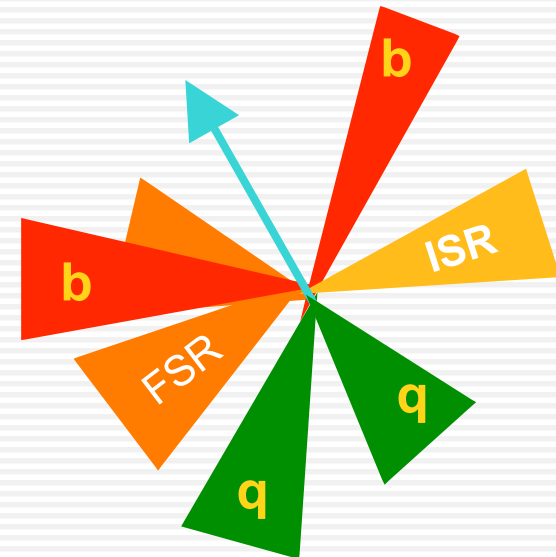
⇒ Top

- ⇒ mainly central jets (with the exception of single-top)
- ⇒ usually smaller cone sizes since they are crowded events
- ⇒ parton-level corrections
 - ⇒ not needed for cross section
 - ⇒ necessary for top mass

Final State from LO Diagram



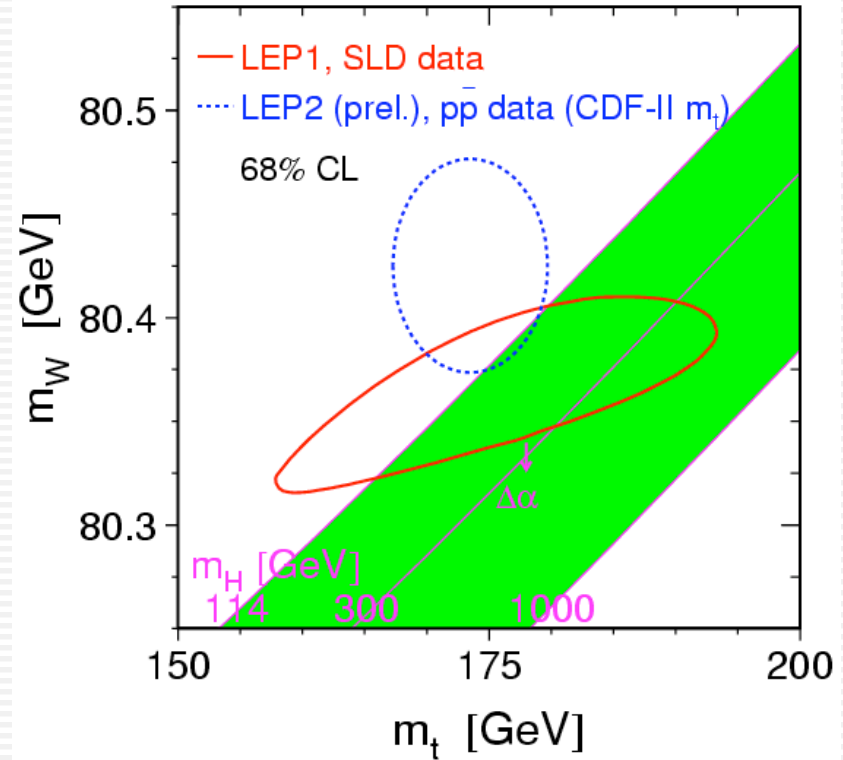
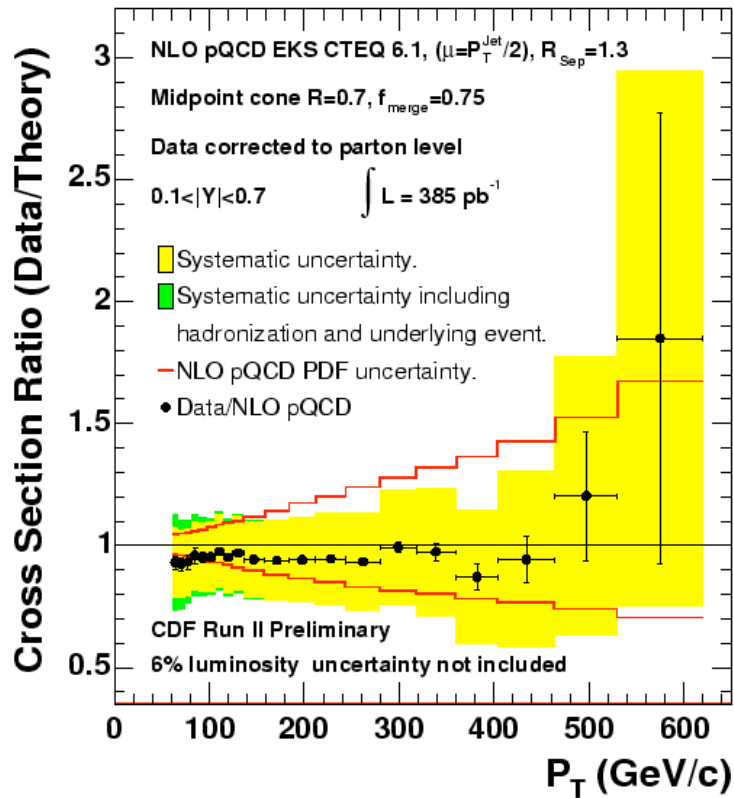
What we measure



+ underlying event from proton remnants +
multiple interactions!

Physics with Jets

Precision on the determination of jet energies is required by many analyses



1% uncertainty in jet \Rightarrow ~10% uncertainty in jet cross section

$$M_{\text{top}} = 173.5^{+2.7}_{-2.6}(\text{stat.}) \pm 2.5(\text{JES}) \pm 1.7(\text{syst.}) \text{ GeV}/c^2$$

CDF Jet Energy Scale Philosophy

- ➔ To accommodate the needs of **different physics analyses**:
 - ➔ Corrections from 8 GeV to 600 GeV
 - ➔ Corrections for different jet clustering algorithms: Cone 0.4, 0.7, 1.0, Midpoint, K_T
 - ➔ Different levels of jet energy corrections
 - ➔ Obtained from “generic” flavor jets
- ➔ They are **obtained from Monte Carlo** (generators+CDF simulation):
 - ➔ Need good models of hadronization and radiation in generators (Pythia, Herwig)
 - ➔ Need good CDF detector simulation (GFLASH)

Jet Energy Corrections Overview

⇒ Calibration:

- ⇒ Calorimeter energy scale
- ⇒ Detector simulation
- ⇒ Physics models

⇒ Corrections:

- ⇒ Obtain **calorimeter-to-particle** corrections using simulated dijet events (C_{Abs})
- ⇒ Obtain **particle-to-parton** corrections using Monte Carlo shower in dijet events (C_{OOC})
- ⇒ Make jet energy scale **uniform in η** using dijet balance (data and Monte Carlo) (C_{Rel})
- ⇒ **Pile-up and underlying event** are measured from data (C_{MI} and C_{UE})

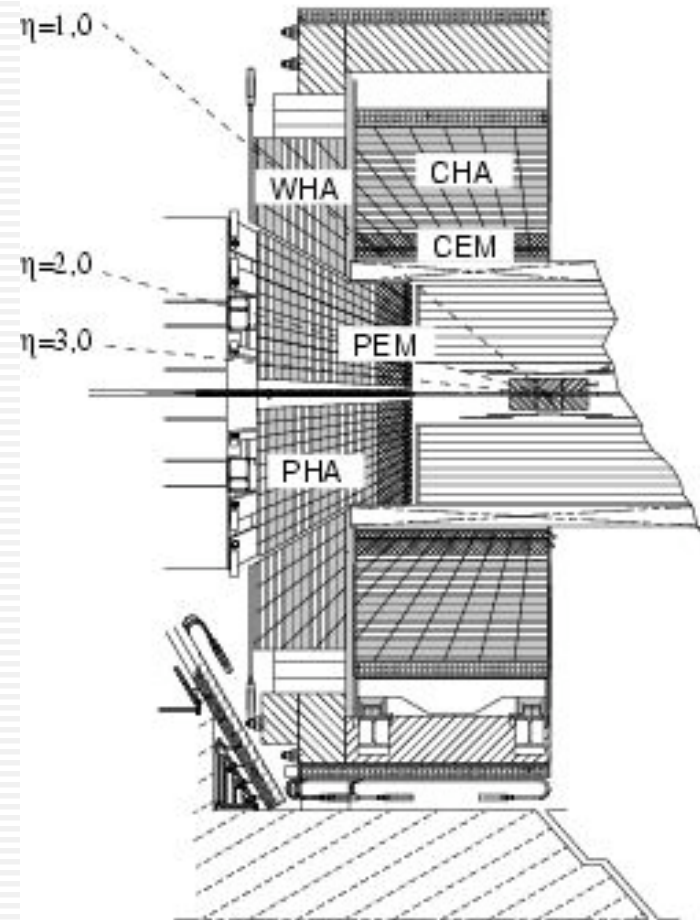
$$P_{Parton} = [P_{jet} \times C_{Rel} - C_{MI}] \times C_{Abs} - C_{UE} + C_{OOC}$$

⇒ Uncertainties:

- ⇒ Differences between **Monte Carlo and data**
- ⇒ Uncertainties from the **method** used to obtain the corrections

CDF Calorimeter

- Jets are measured with a calorimeter ...
- Scintillating tile with lead/steel absorbers $|\eta| < 3.6$:
 - CEM = $18 X_0$; CHA = 4.7λ ($0.0 < |\eta| < 1.0$)
 - PEM = $23 X_0$; PHA = 7λ ($1.3 < |\eta| < 3.6$)
 - Projective Towers $\Delta\eta = 0.11$; $\Delta\phi = 2\pi/24$ (central), $\Delta\phi = 2\pi/48$ (plug)
- Non-linear response to hadrons
- Linear response to electrons
- Coarse granularity
- Very low noise



Electrons and Photons:

$$\sigma_{ET} / E_T = 13.5\% / \sqrt{E_T} \oplus 1.5\% \text{ (central)}$$

$$\sigma_{ET} / E_T = 16\% / \sqrt{E_T} \oplus 1\% \text{ (plug)}$$

Charged Pions:

$$\sigma_E / E_T = 50\% / \sqrt{E} \oplus 3\% \text{ (central)}$$

$$\sigma_E / E = 80\% / \sqrt{E} \oplus 5\% \text{ (plug)}$$

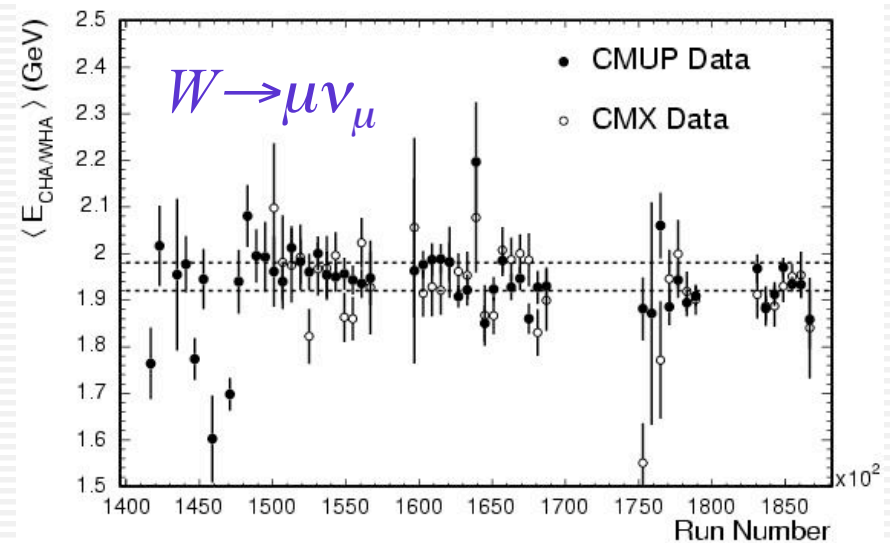
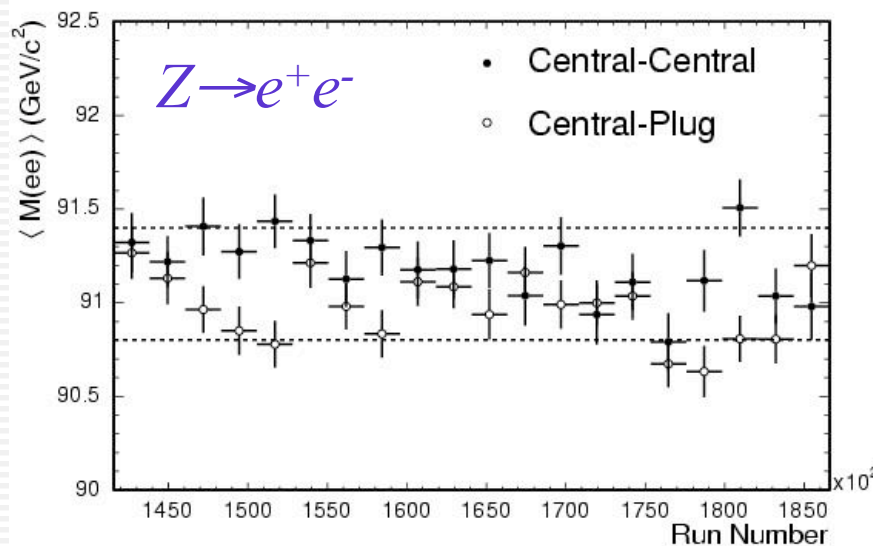
Calorimeter Energy Scale

➤ Scale

- CEM and PEM set using $Z \rightarrow e^+e^-$ = LEP measurement
- CHA and PHA set using test beam pions (57 GeV)
- Maintained using *in-situ* and test beam measurements

➤ Stability

- Scales decrease due to aging of photomultipliers and scintillators
- Online response is kept stable better than 3%
- Offline response is kept stable better than 0.3% for CEM, PEM and 1.5% for CHA, WHA, PHA



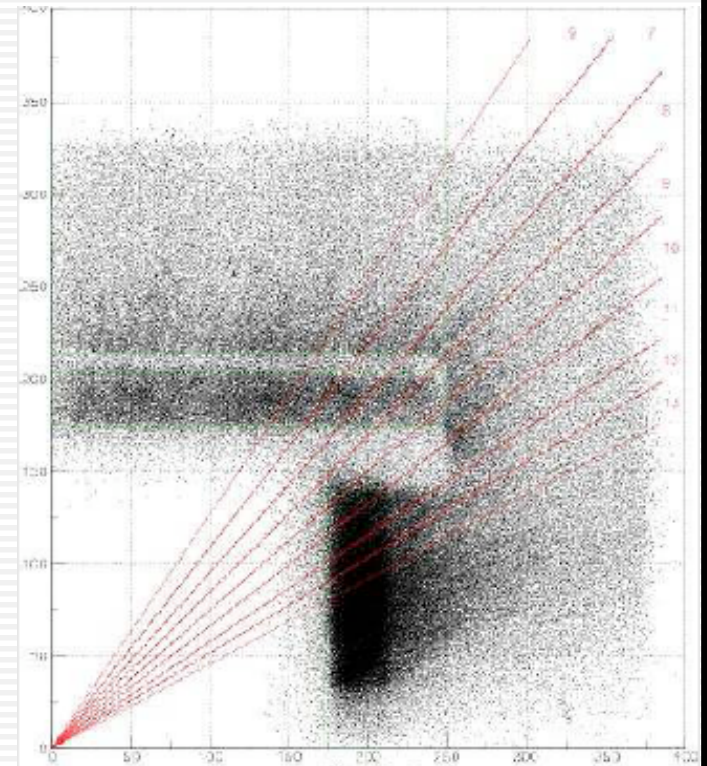
Calorimeter Simulation

➤ CDF Run II simulation:

- GEANT 3 propagates particles up to the first inelastic interaction in the calorimeter
- GFLASH (from H1) parameterize the electromagnetic and hadronic showers shapes in the calorimeter

➤ Calorimeter simulation (GFLASH) :

- Calculates spatial distribution of **energy deposited** by a shower and the energy which is **visible** to the active medium (using sampling fractions, 2 parameters)
- Longitudinal shower profile (18 parameters)
- Lateral shower profile (14 parameters)
- Energy is summed into towers based on the CDF calorimeter tower segmentation
- **Parameters are modified to reproduce energy deposition from data**
- Only a fraction of the available parameters are tuned, rest using default setting by H1 collaboration



Tuning of the Calorimeter Simulation

➔ Method uses mixture of in-situ and test beam data:

- ➔ Calorimeter energy E
- ➔ Reconstructed track momentum p

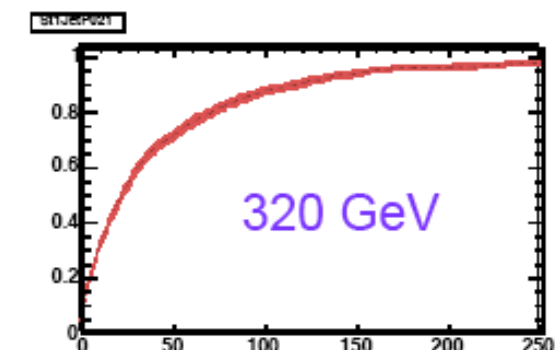
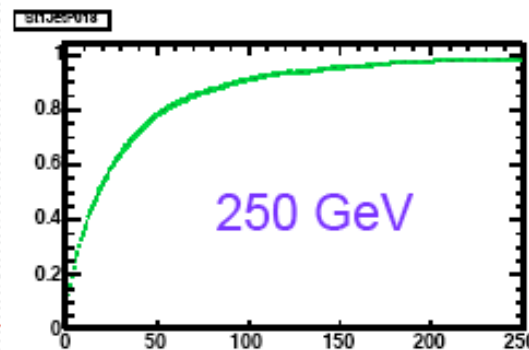
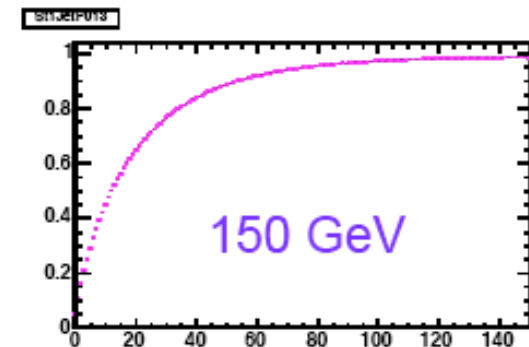
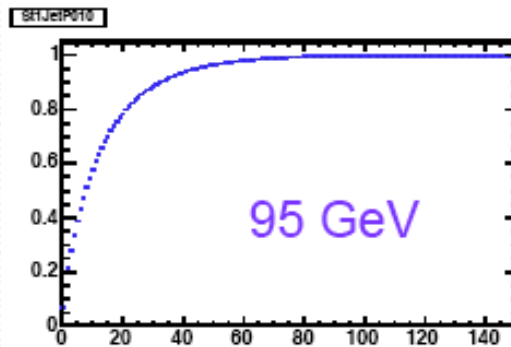
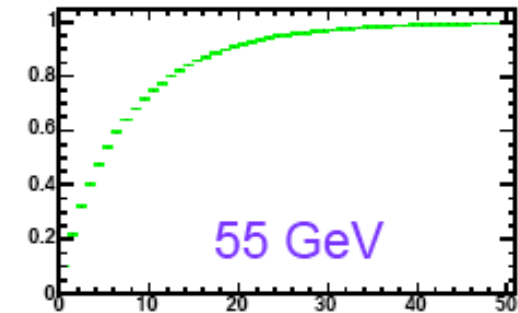
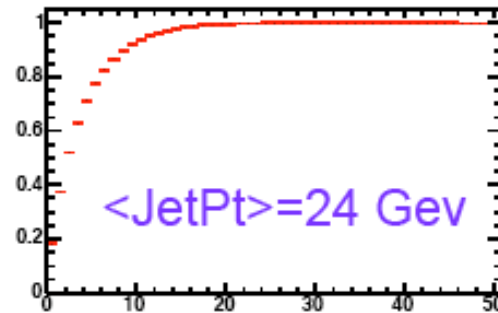
➔ How far do we need to tune the simulation?

- ➔ For 95 GeV jet ~70% of the energy is in particles with $p < 20$ GeV

➔ Different tuning for:

- ➔ Central and Plug
- ➔ EM and HAD particles

p_T of tracks in a cone of 0.7 around the jet axis

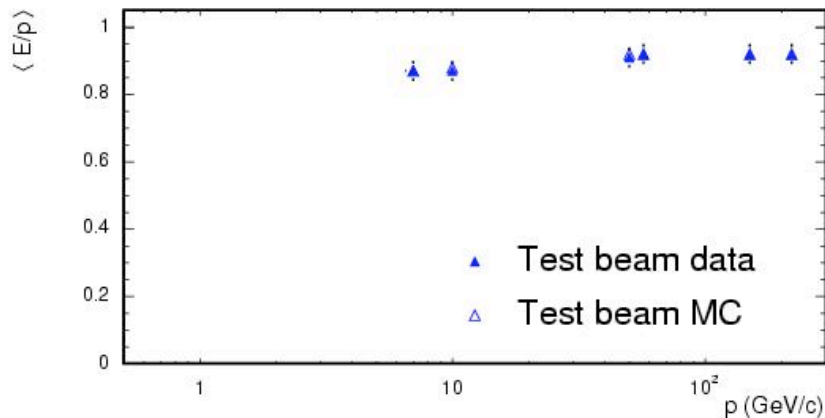
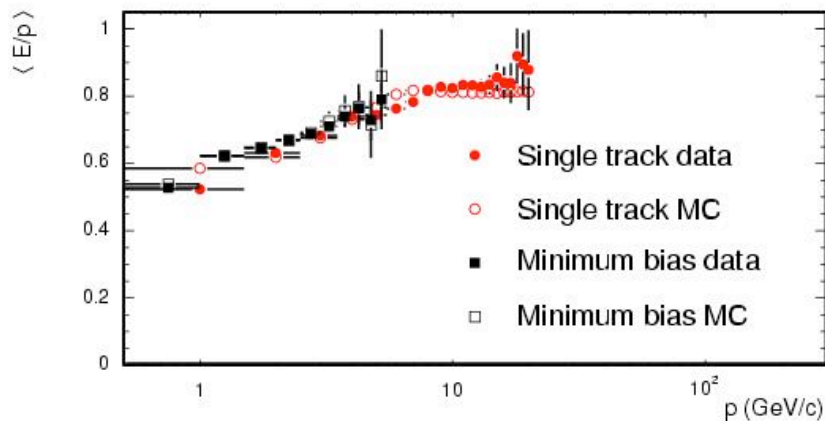


Single Particle Response - Central Region

➔ HAD particles:

- ➔ Isolated single track data from minimum bias ($0.5 < p < 2.5$ GeV) and pion test beam data ($7 < p < 227$ GeV)
- ➔ For testing the tuning, single track data up to $p < 20$ GeV is used

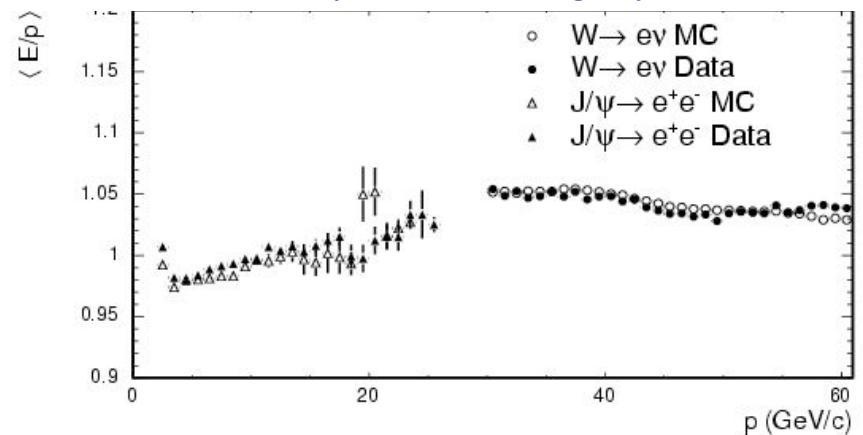
HAD (~70% of a jet)



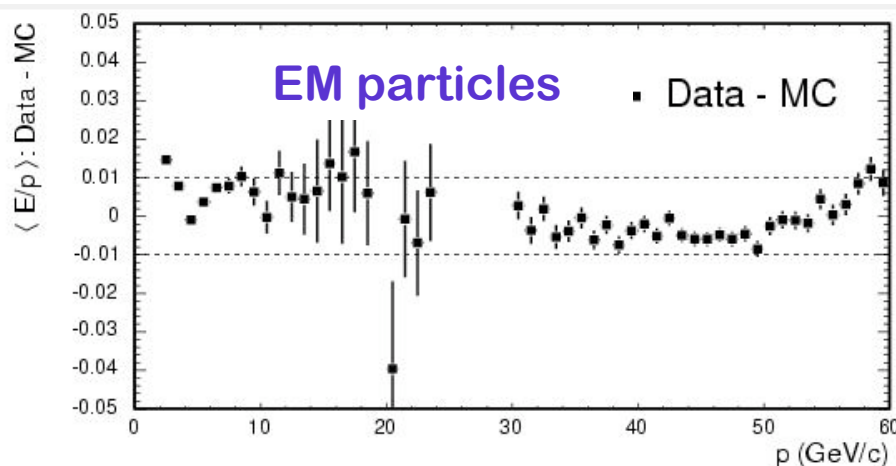
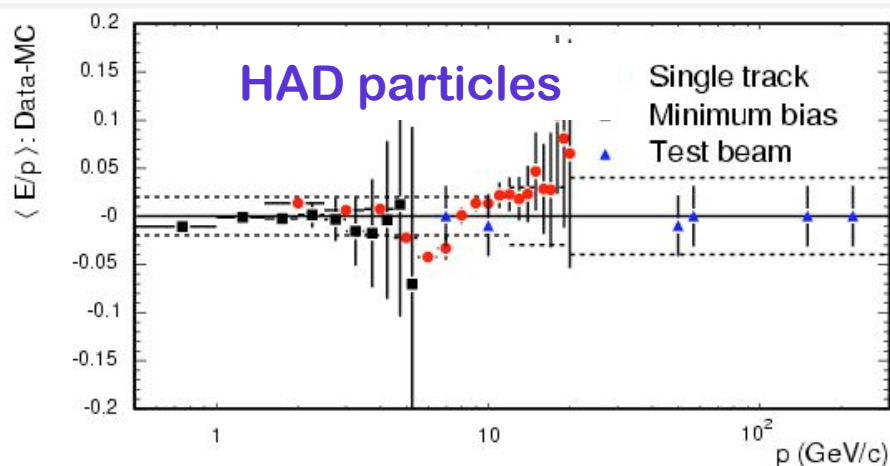
➔ EM particles:

- ➔ $Z \rightarrow e^+e^-$ in situ data
- ➔ Electrons from test beam

EM (~30% of a jet)



Single Particle Response - Central Region



Sources of uncertainty:

- data-MC (low p)
- statistical precision (medium p)
- test beam momentum scale (high p)
- test beam calibration stability (high p)
- tower boundaries

Uncertainties for single particle response:

- HAD particles
 - 1.5% for $p < 12$ GeV
 - 2.5% for $12 < p < 20$ GeV
 - 3.5% for $p > 20$ GeV
- EM particles
 - 1% for all p

E/p only sensitive to ~80% of the calorimeter towers. ϕ -boundaries uncertainties:

- HAD = 1.9%; EM = 1.6%

Uncertainties from Single Particle Response

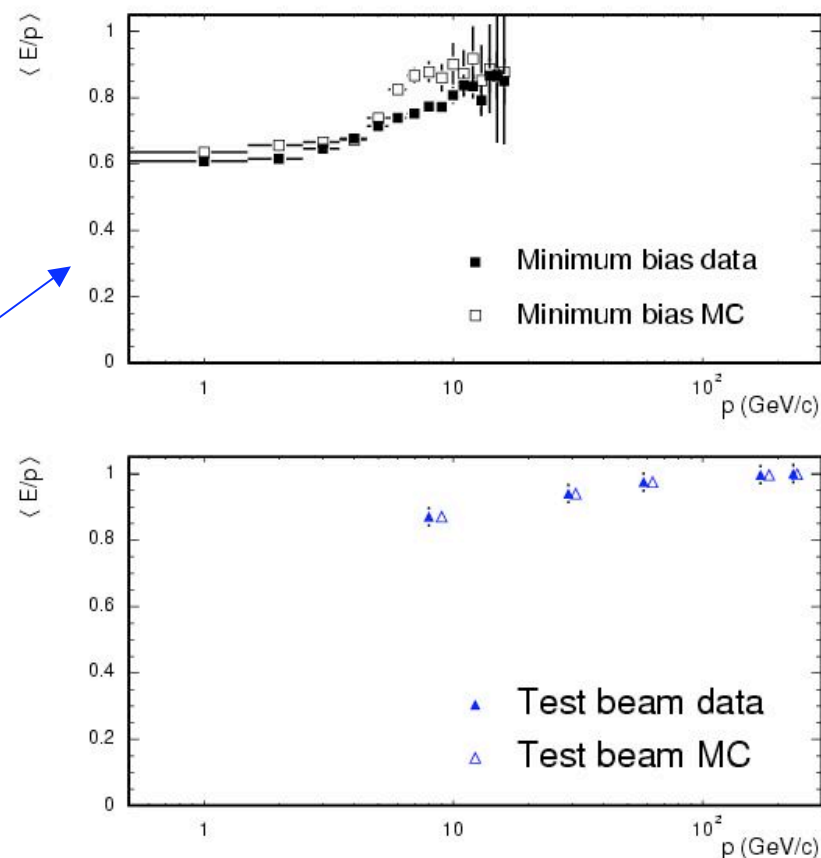
Central region

p(GeV/c)	0-12	12-20	>20
<E/p> response to hadrons			
in inner 81% (%)	1.5	2.5	3.5
in 19% near phi and eta boundaries (%)	1.9	1.9	1.9
Total hadrons (%)	2.5	3.0	4.0
<E/p> response to EM particles			
in inner 84% tower (%)	1.0	1.0	1.0
in 16% near phi boundary (%)	1.6	1.6	1.6
Total EM particles (%)	1.7	1.7	1.7

These numbers will be passed to the jet scale uncertainty

Calorimeter Simulation in the Forward Region

- ➔ Compared to the central region:
 - ➔ Tracking efficiency is lower
 - ➔ Momentum resolution for tracks is poorer
 - ➔ Background is larger
- ➔ Simulation has been tuned mostly to pion test beam ($8.6 < p < 231$ GeV) and some minimum bias data
- ➔ Previously only high momentum track trigger available up to $|\eta| < 1.0$: **new trigger available now**
- ➔ Working on improving forward simulation with new data
- ➔ For now, forward region is not used for obtaining JES corrections or uncertainties (replaced by η -dependent corrections)



η -dependent Corrections

➔ Recalibrate energy of non-central jets (“probe jet”) with energy of central jet (“trigger jet”) using dijet balance:

➔ Trigger jet: $0.2 < |\eta| < 0.6$

➔ Dijet balance:

$$\beta = \frac{p_T^{\text{probe}}}{p_T^{\text{trigger}}} = \frac{2 + \langle \Delta p_T f \rangle}{2 - \langle \Delta p_T f \rangle} \quad \Delta p_T f = \frac{p_T^{\text{probe}} - p_T^{\text{trigger}}}{(p_T^{\text{probe}} + p_T^{\text{trigger}})/2}$$

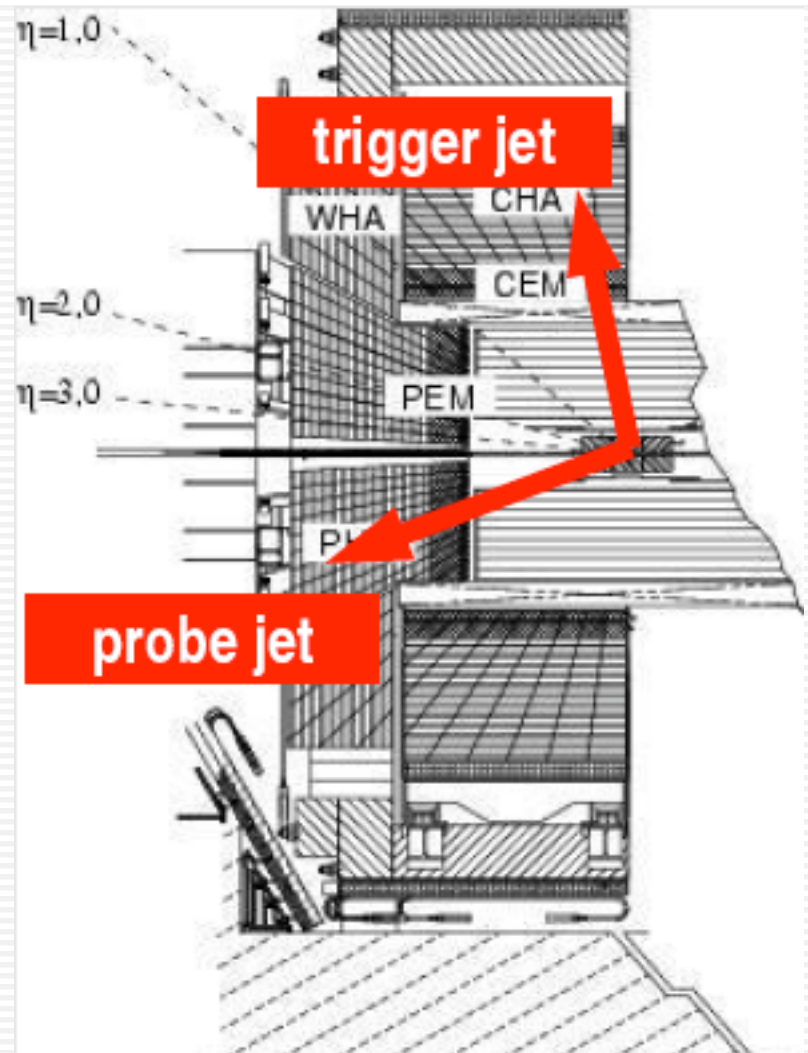
➔ Reduce effects from QCD radiation and ensure $p_T^{\text{probe}} = p_T^{\text{trigger}}$

➔ $\Delta\phi(\text{jet probe, jet trigger}) > 2.7$

➔ 3rd jet $p_T < 7, 8, \text{ or } 10 \text{ GeV}$

➔ $p_T^{\text{ave}} = (p_T^{\text{trigger}} + p_T^{\text{probe}})/2 > (5 + \text{jet } p_T^{\text{trigger}} \text{ threshold})$

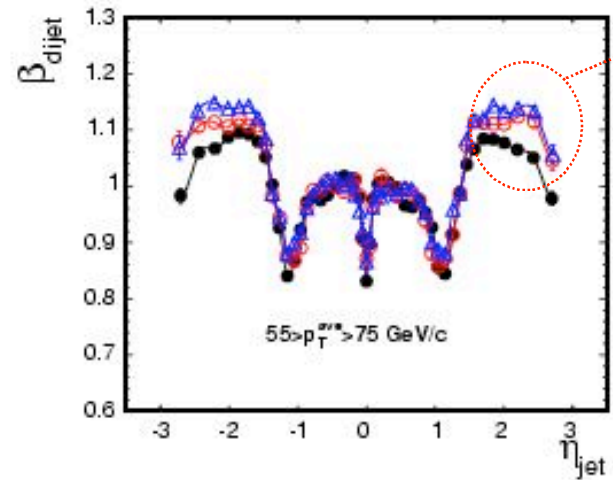
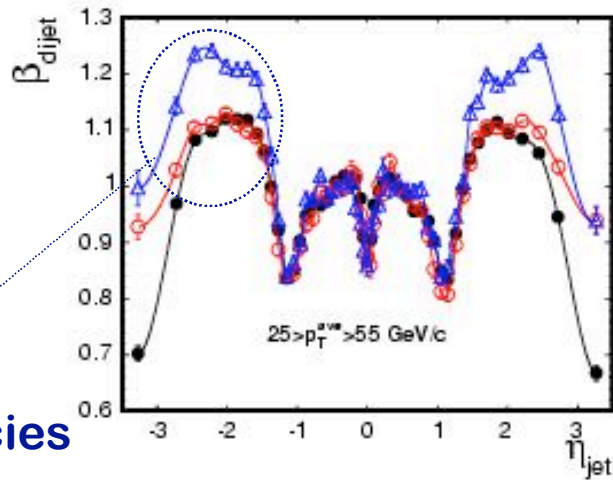
➔ Two corrections, one for data and another one for MC (Pythia)



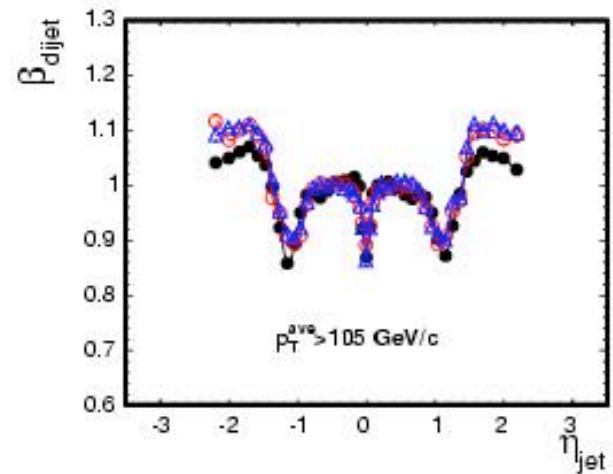
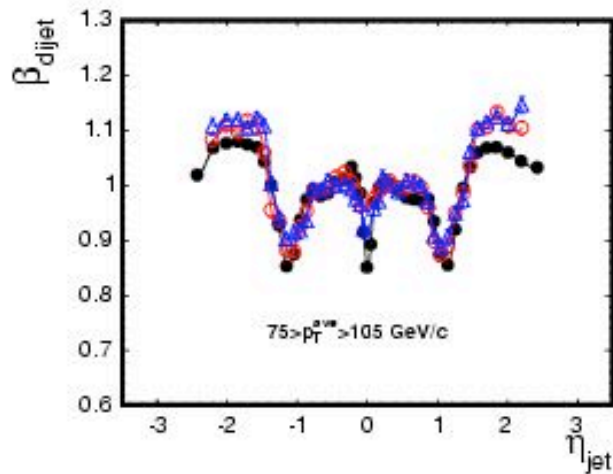
η -dependent Corrections

➔ Dijet balance as a function of η

Herwig discrepancies are only seen in dijet samples



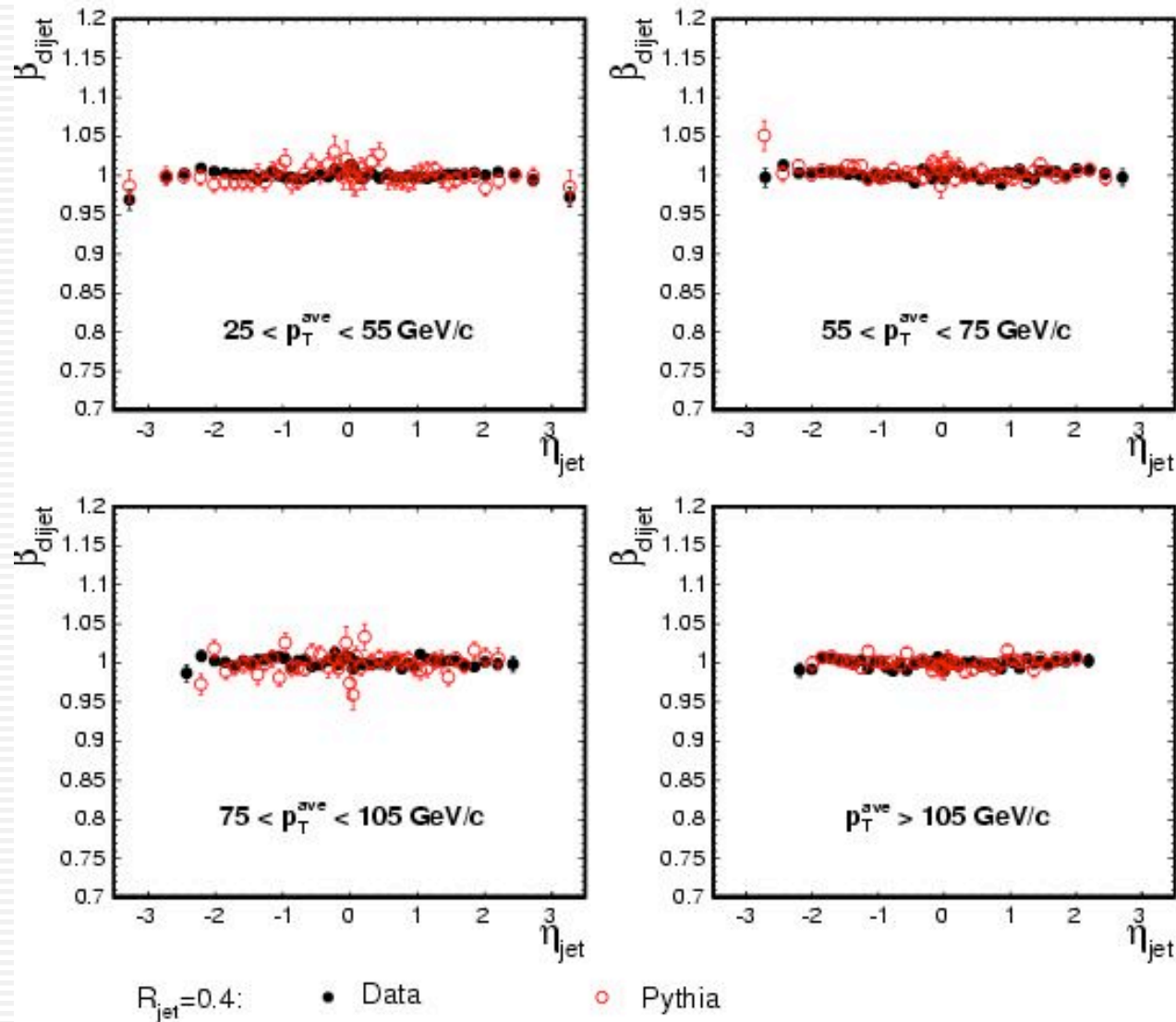
Not optimal MC tuning in plug region



$R_{jet} = 0.4$: ● Data ▲ Herwig ○ Pythia

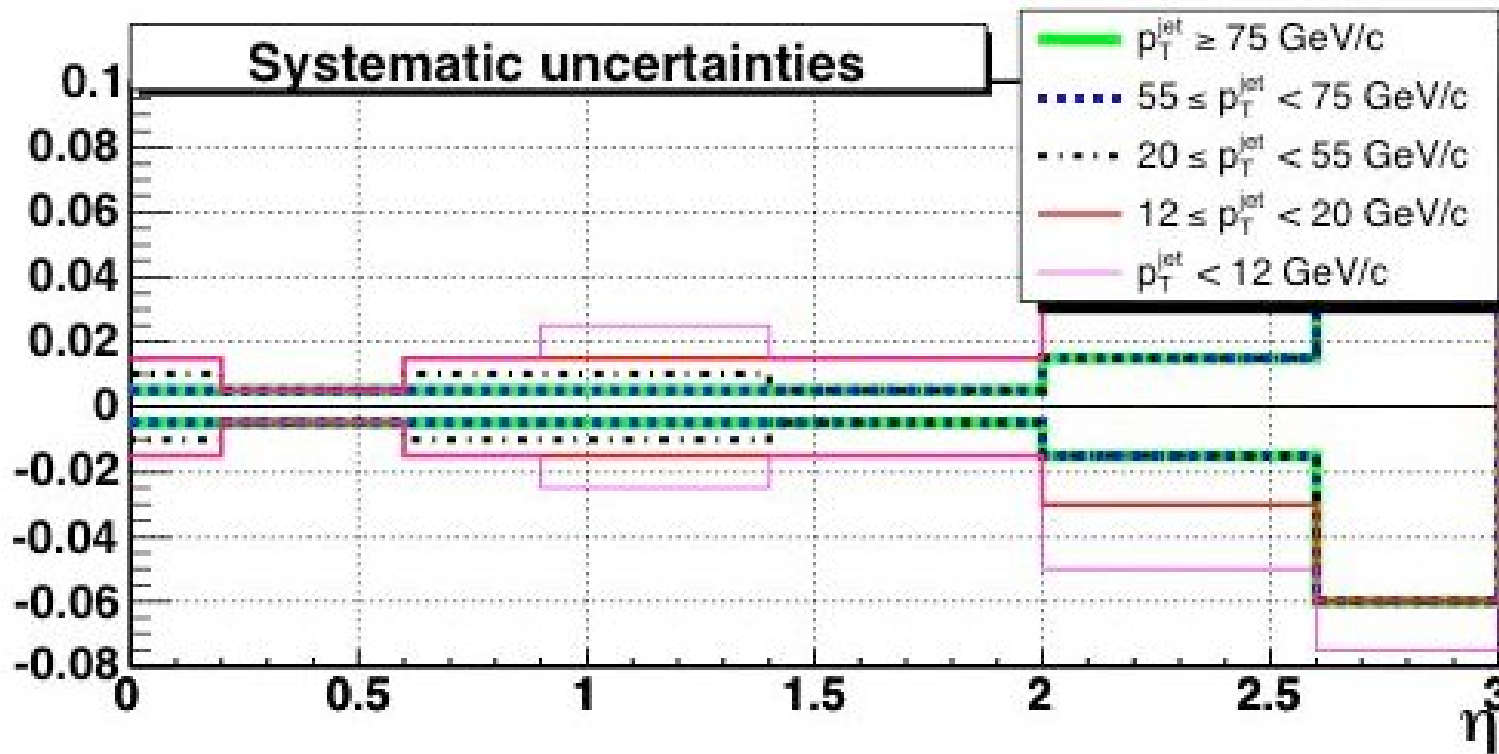
η -dependent Corrections

➔ Dijet balance as a function of η after corrections



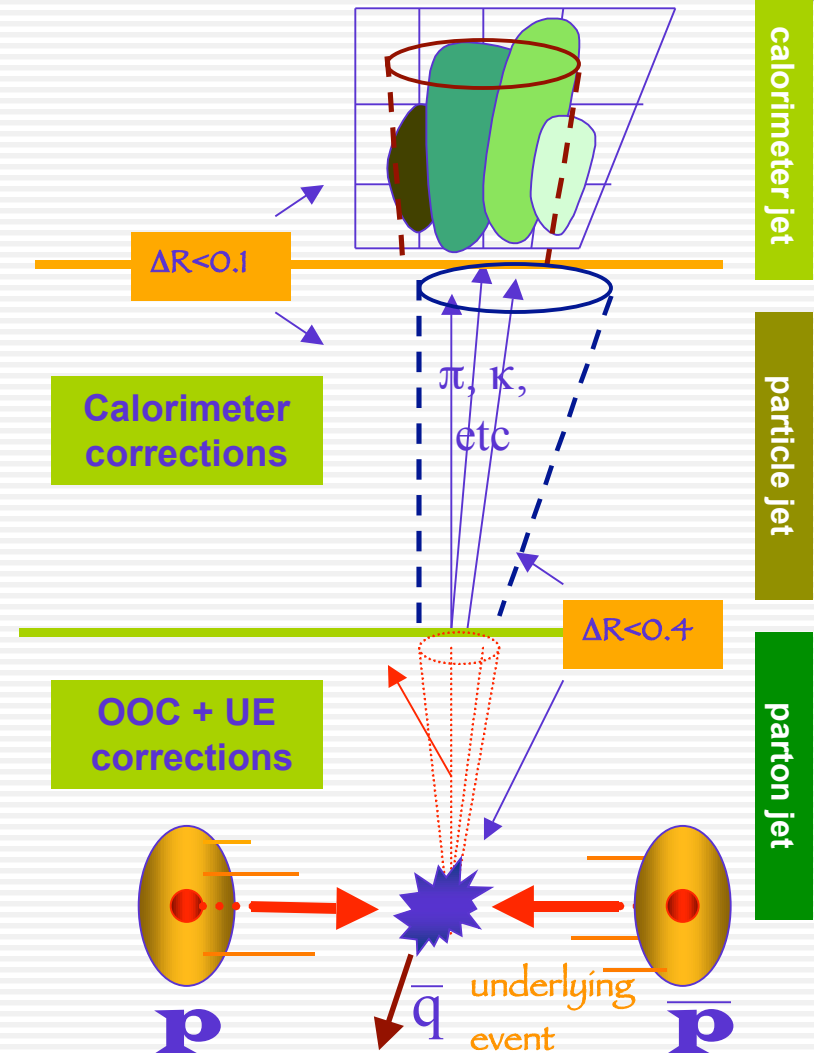
η -dependent Uncertainties

- ➔ Deviation of corrected response from unity
- ➔ Determined varying the **selection cuts** and the **fitting procedure**
- ➔ Difference between data and simulation in photon+jet events is also added to the uncertainties (certain P_T range)



Jet Energy Scale Corrections

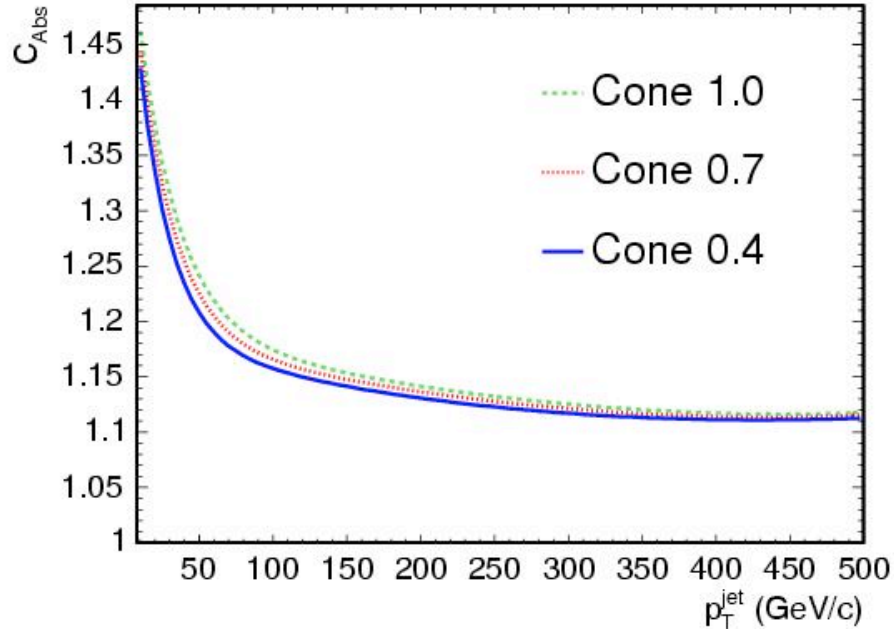
- ➔ Once the calorimeter simulation is done and the p_T response is uniform in η we need to correct for calorimeter effects
- ➔ Only obtained with central jets ($0.2 < |\eta| < 0.6$)
- ➔ Corrections obtained using two leading jets in MC PYTHIA dijet events with difference minimum P_T (0-600 GeV)
- ➔ Parameterize difference between calorimeter jet and particle jet (calorimeter corrections) and particle jets and parton (OOC+UE corrections)



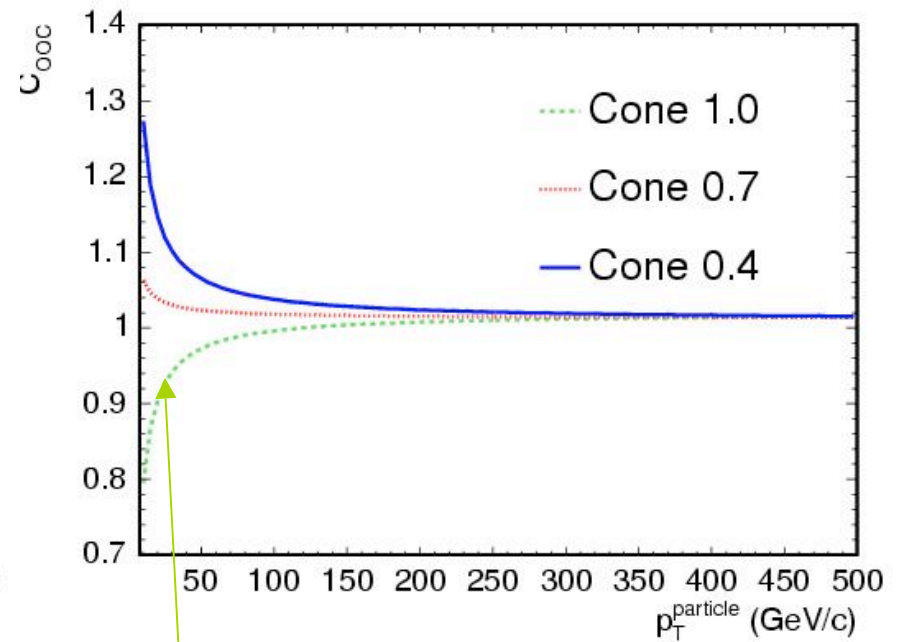
Jet Energy Scale Corrections

- ➔ Corrections are the **most probable value** for $\Delta p_T/p_T(\text{particle})$ for a given $p_T(\text{particle})$

Calorimeter Corrections



OOC+UE Corrections



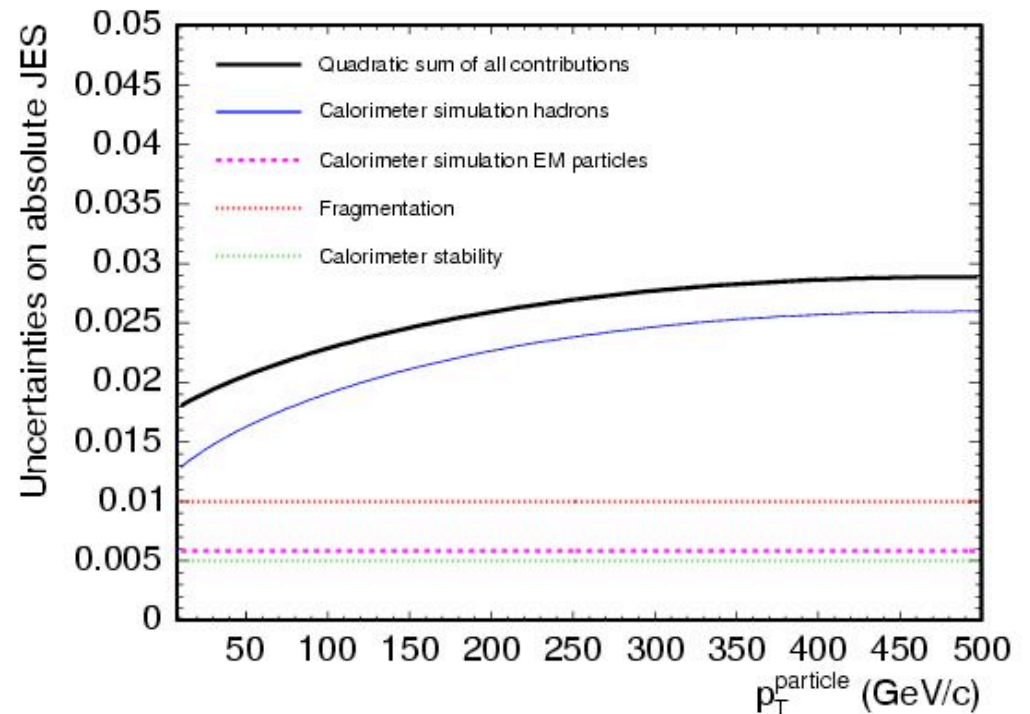
More energy from UE in the jet than lost outside the jet

Calorimeter Uncertainties

- ➔ Is the calorimeter energy scale **stable**?
 - ➔ Yes, up to 0.3%

- ➔ Are the **jets well modeled** by the simulation?
 - ➔ Is the response of the calorimeter to an individual particle correctly simulated?
 - ➔ Propagate EM and HAD single particle response uncertainty E/p to jets

 - ➔ Is the multiplicity and p_T spectrum of particles inside a jet the same for data and MC?
 - ➔ Propagate the difference between particle multiplicity in data and MC to jets

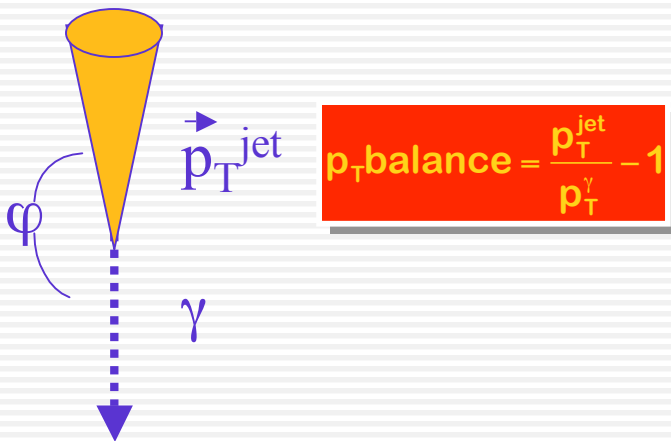


$$R_{\text{jet}} = \frac{\sum_{i=1}^{N_{\text{tracks}}} p_{T,i} R_{\text{single-particle}}(p_{T,i})}{\sum_{i=1}^{N_{\text{tracks}}} p_{T,i}}$$

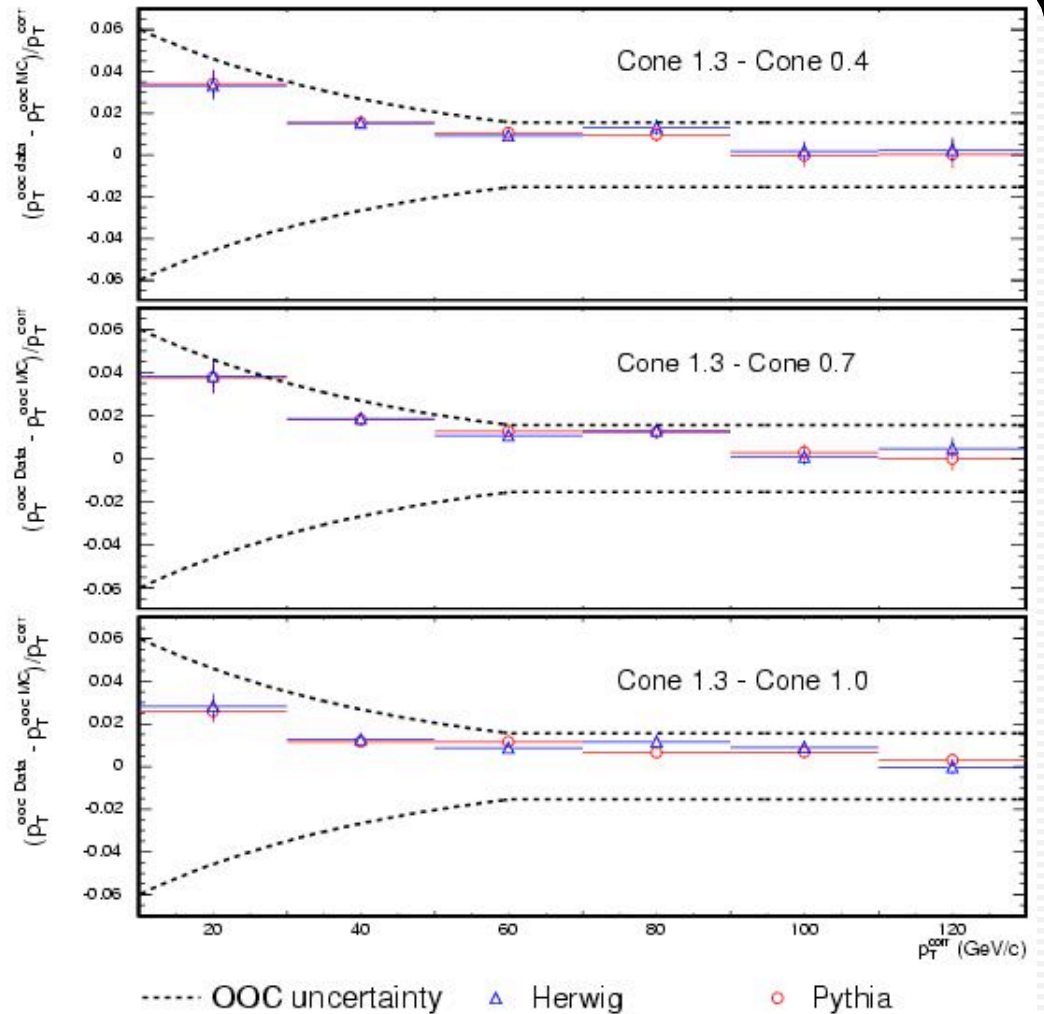
Out-of-Cone Uncertainties

→ Compare energy flow in annuli around the cone up to $R=1.3$ between data and MC in photon+jets events at the calorimeter level

→ Photon p_T should balance unknown jet parent parton p_T



→ Uncertainty is the largest difference between data, Pythia and Herwig, scaled with $C_{\text{Abs}}(p_T \text{ photon})$



→ Additional “Splash-Out” uncertainty accounting for energy flow outside the cone of $R=1.3$: 0.25 GeV

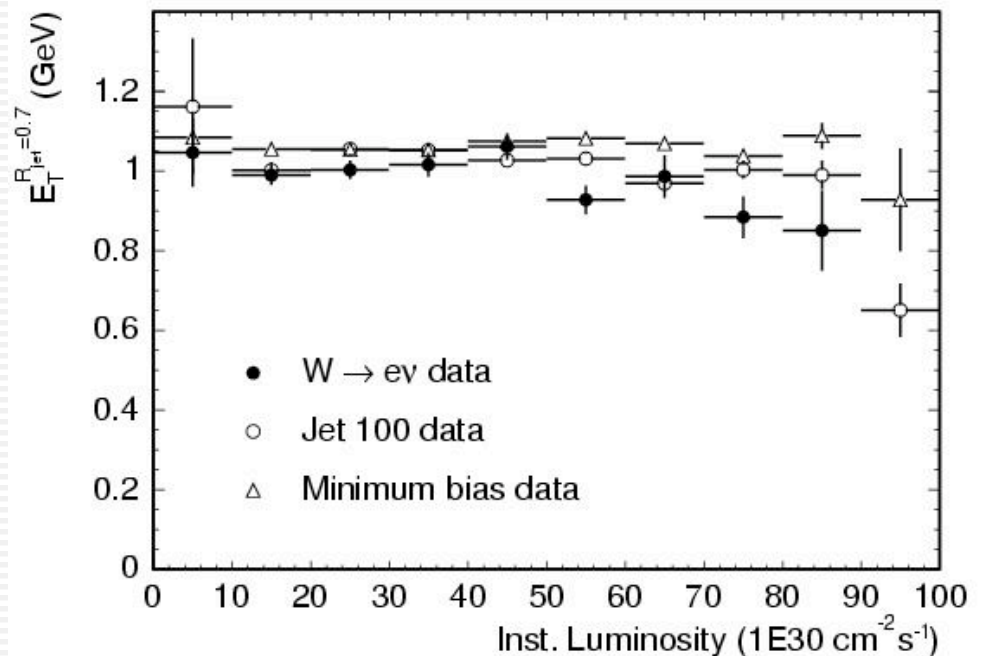
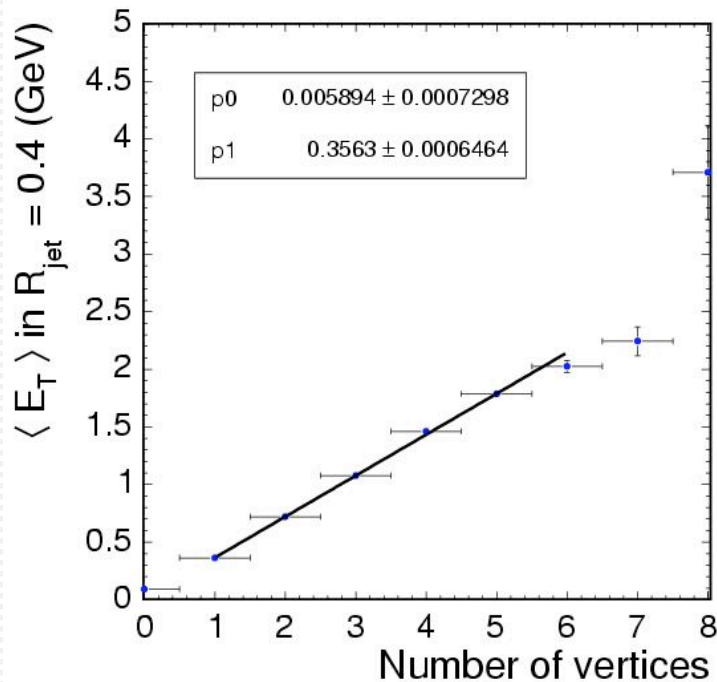
Physics Effects: Multiple Interactions

➤ Correction:

- Energy in a random cone in minimum bias events as a function of the number of reconstructed vertices (N_{vtx})
- Use parameterization to subtract corresponding energy

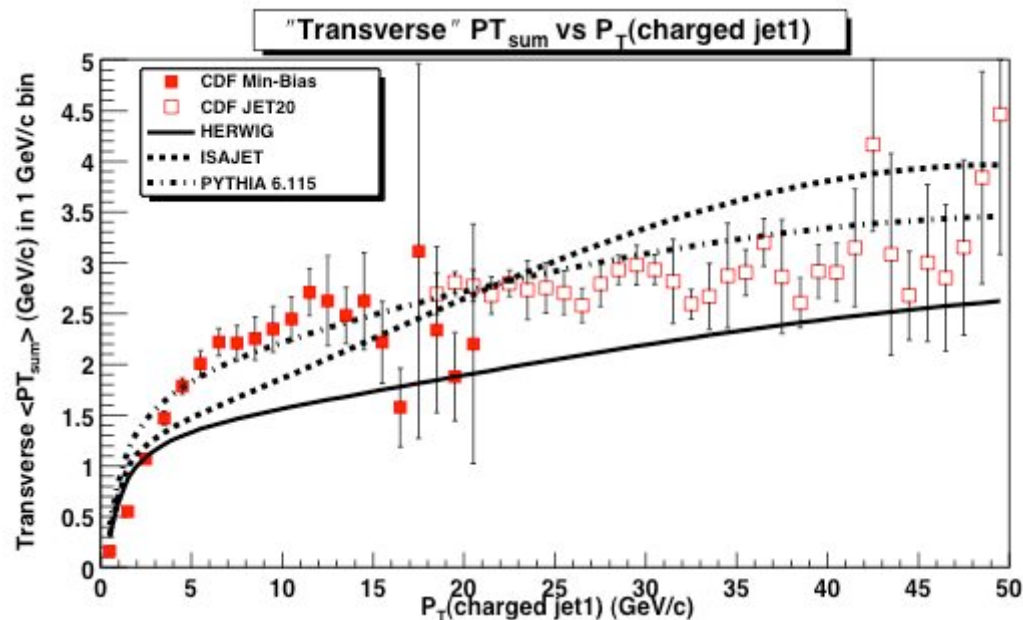
➤ Uncertainty (15% of correction):

- Vertex reconstruction efficiency
- Vertex fake rate



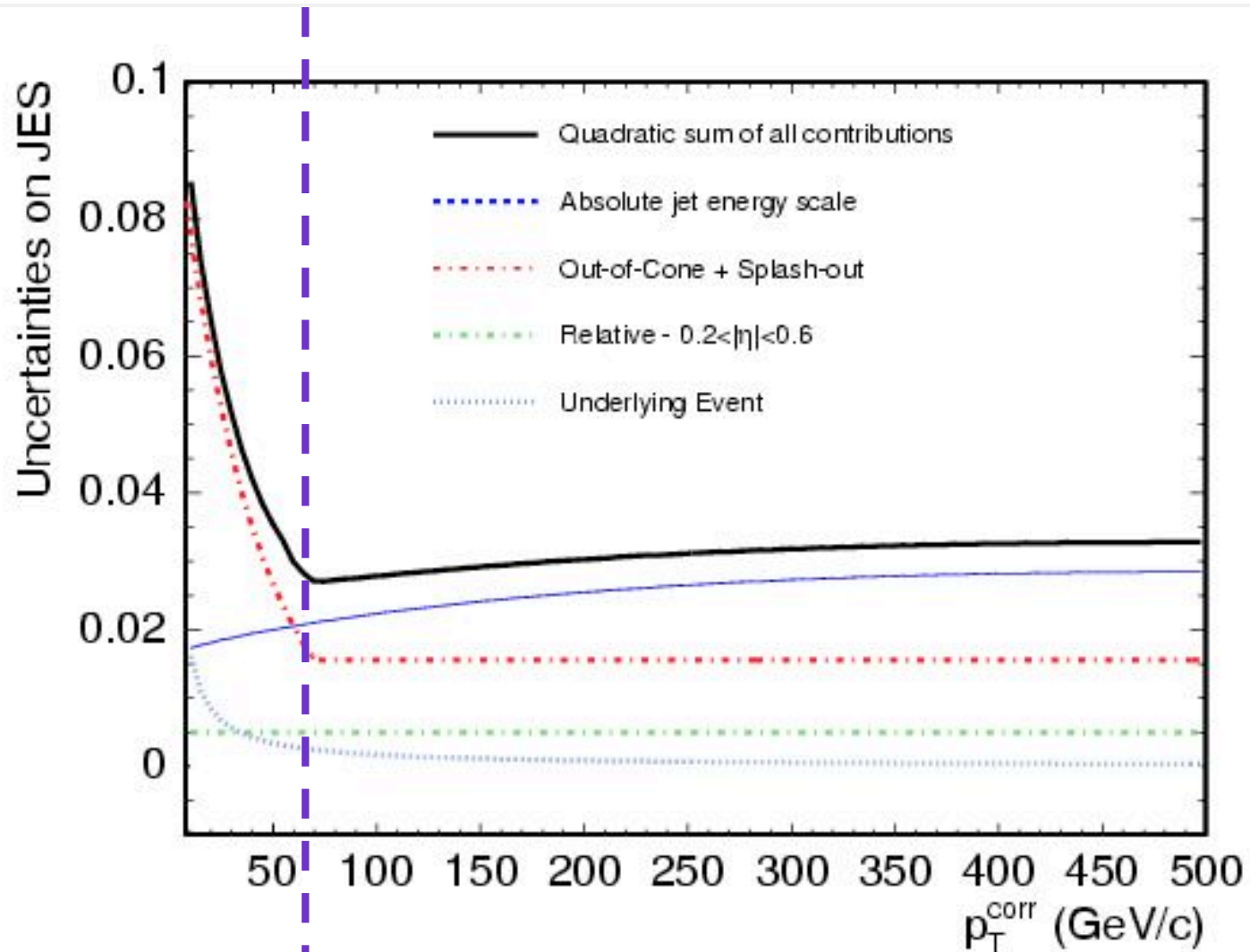
Physics Effects: Underlying Event

- ➔ **Correction:** Use Multiple Interactions correction at $N_{\text{vtx}}=1$
 - ➔ 0.11 GeV (R=0.4)
 - ➔ 0.32 GeV (R=0.7)
 - ➔ 0.66 GeV (R=1.0)
- ➔ **Uncertainty:** Quantify agreement between MC and data by comparing charged particle transverse energy densities in “transverse regions” w.r.t. leading jets in dijet events
 - ➔ 30% uncertainty of correction



- ➔ **Pythia UE** has been tuned to CDF data
- ➔ **Herwig UE** seems too small - we (Rick Field) are working on tuning Jimmy (Herwig UE model) to CDF Run II data

Total Uncertainties

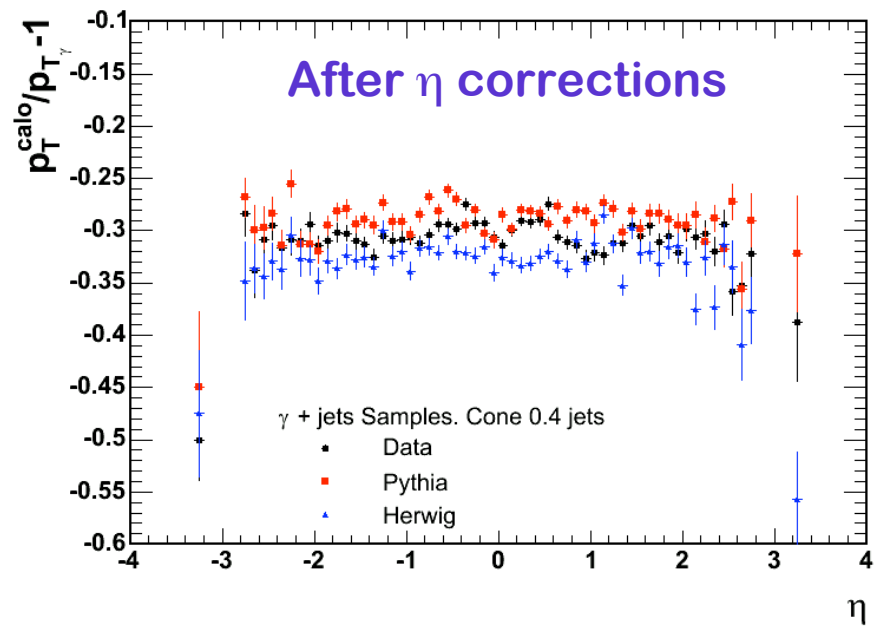
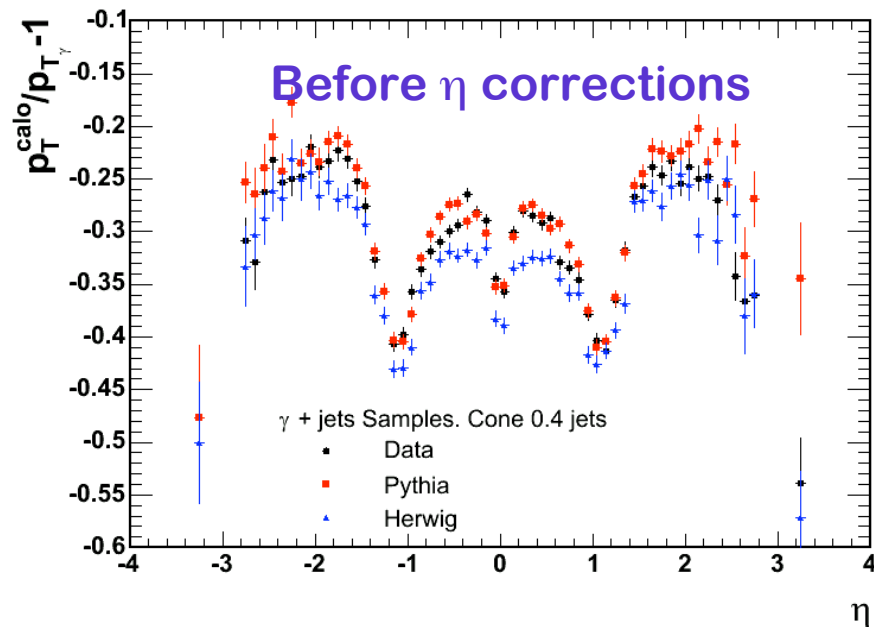


Dominated by physics
model uncertainties

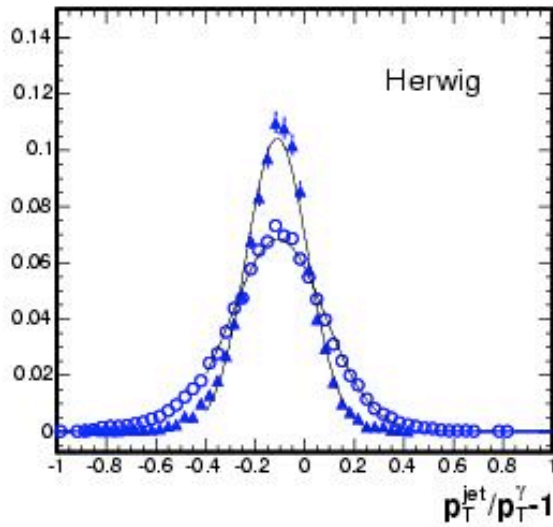
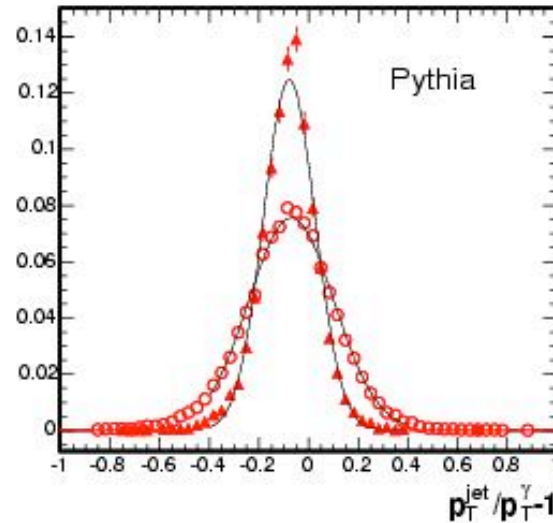
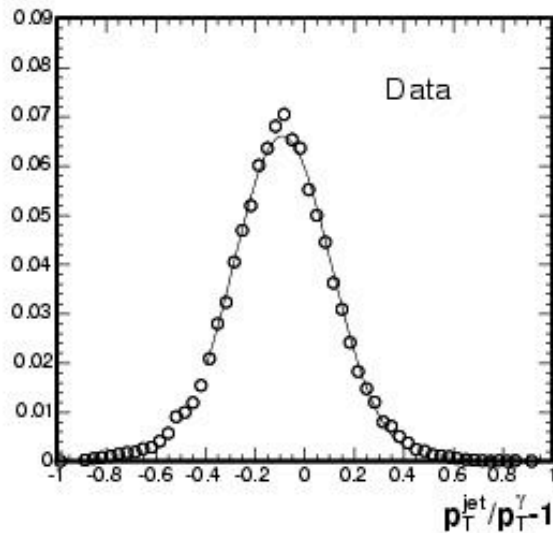
Dominated by calorimeter
simulation uncertainties

Validation of the η -dependent Corrections

P_T Balance = $P_T^{\text{Jet}}/P_T^\gamma - 1$ in Photon+Jets events



Validation of the Calorimeter Corrections



$R_{jet} = 0.4$

▲ Particle jets

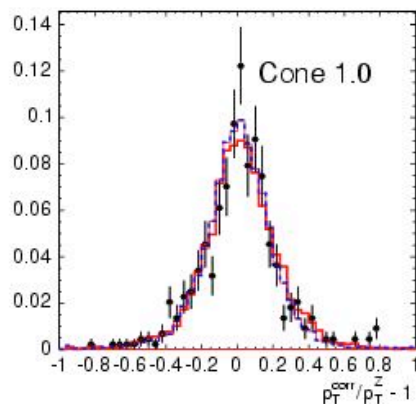
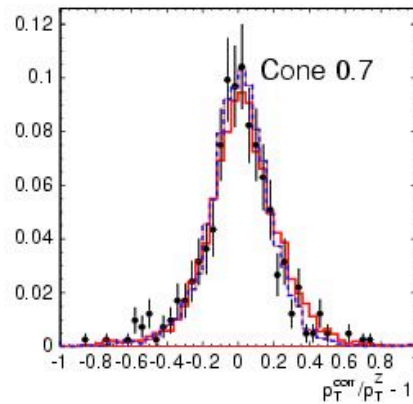
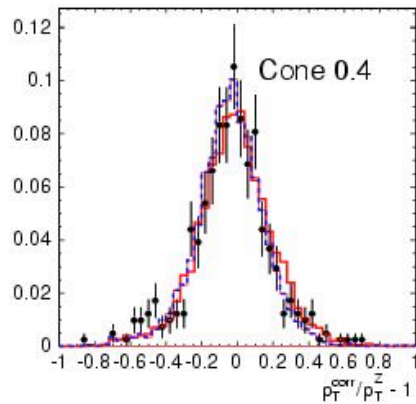
○ Calorimeter jets corrected

- ➔ Photon+jet data and MC after η -dependent and calorimeter corrections were applied to jets
- ➔ After corrections p_T balance of photon and jet should be similar to the particle level (p_T balance)

Validation of the OOC+UE Corrections

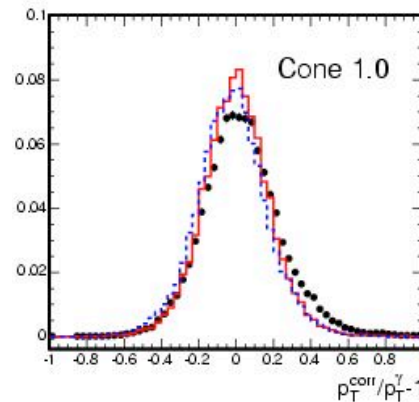
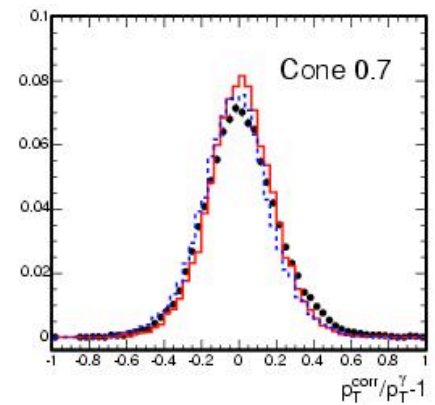
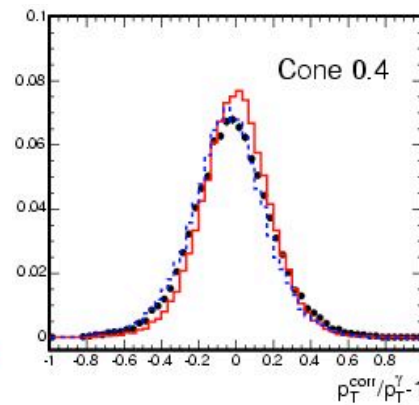
- ➔ After all corrections are applied the p_T balance between photon or Z and jet should be 0

Z+jets events



- Data
- Pythia
- - Herwig

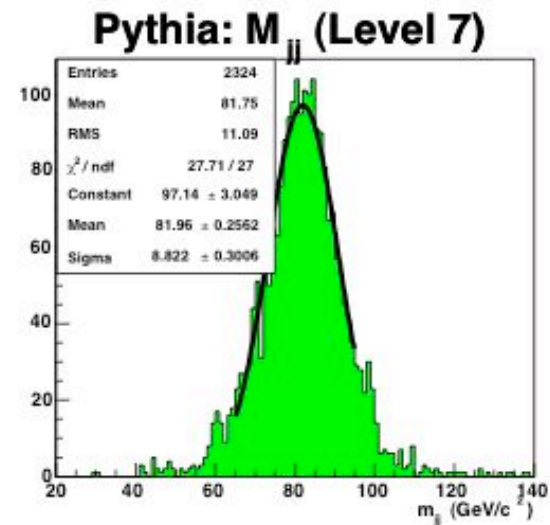
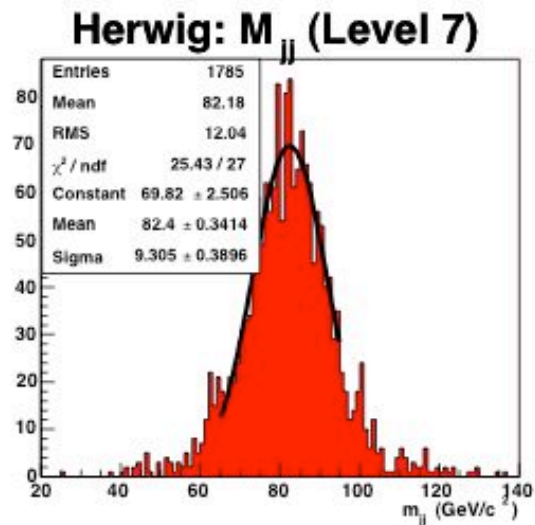
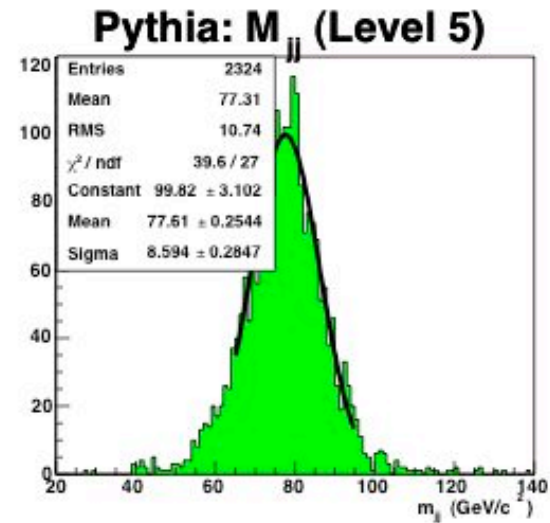
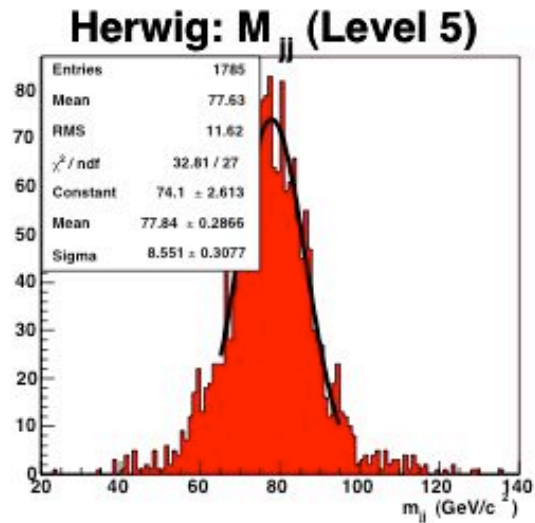
Photon+jets events



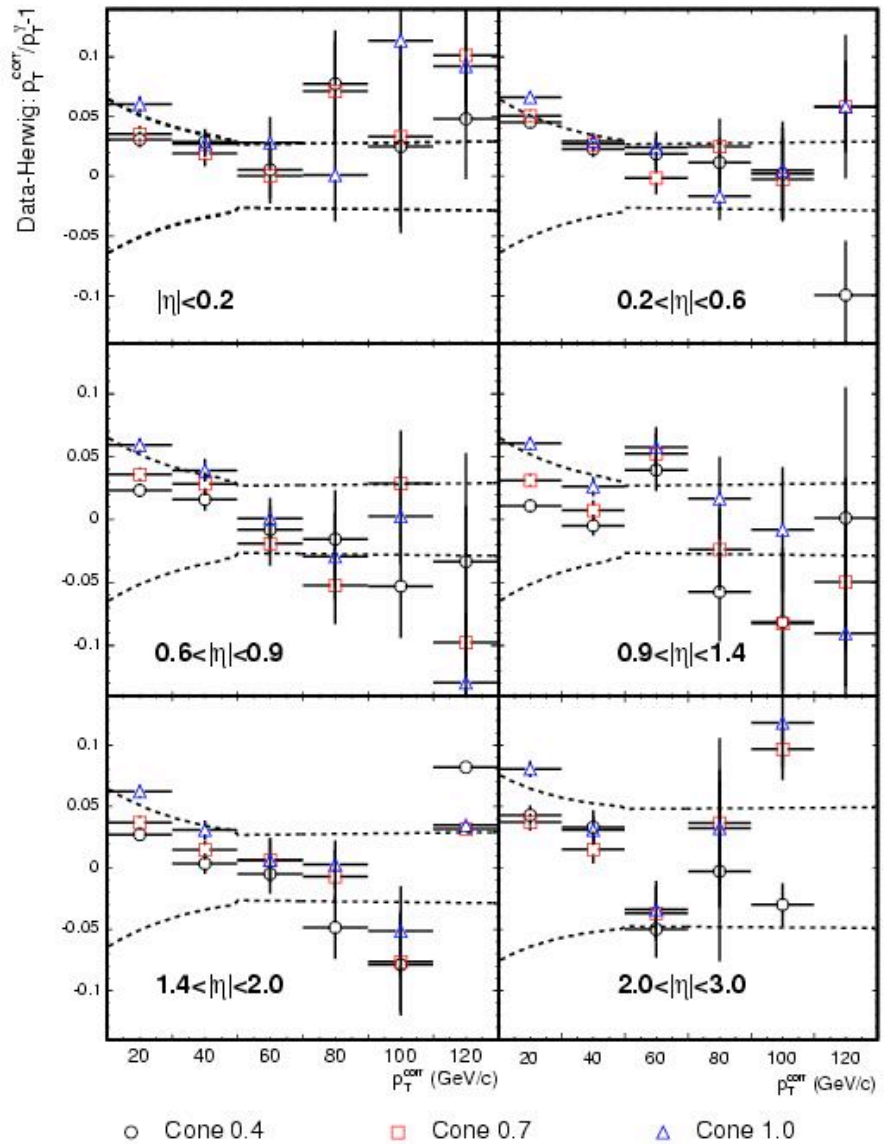
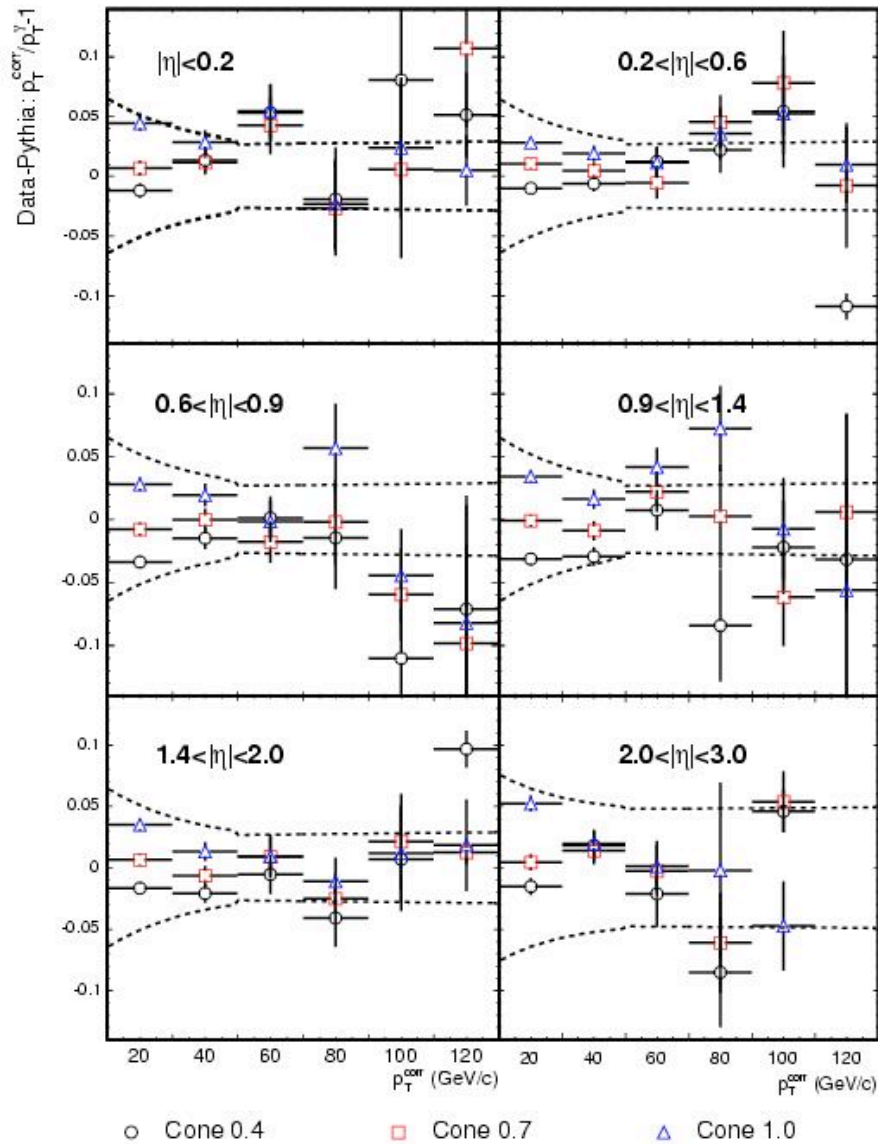
- Data
- Pythia
- - Herwig

Corrections in $t\bar{t}$ Events

➔ Hadronic W mass after all corrections were applied to the jets

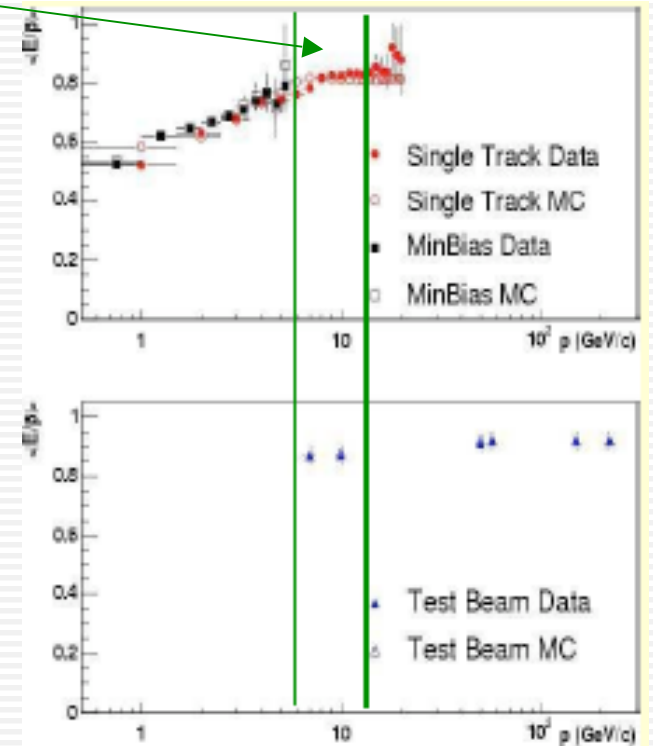


Are the uncertainties large enough?



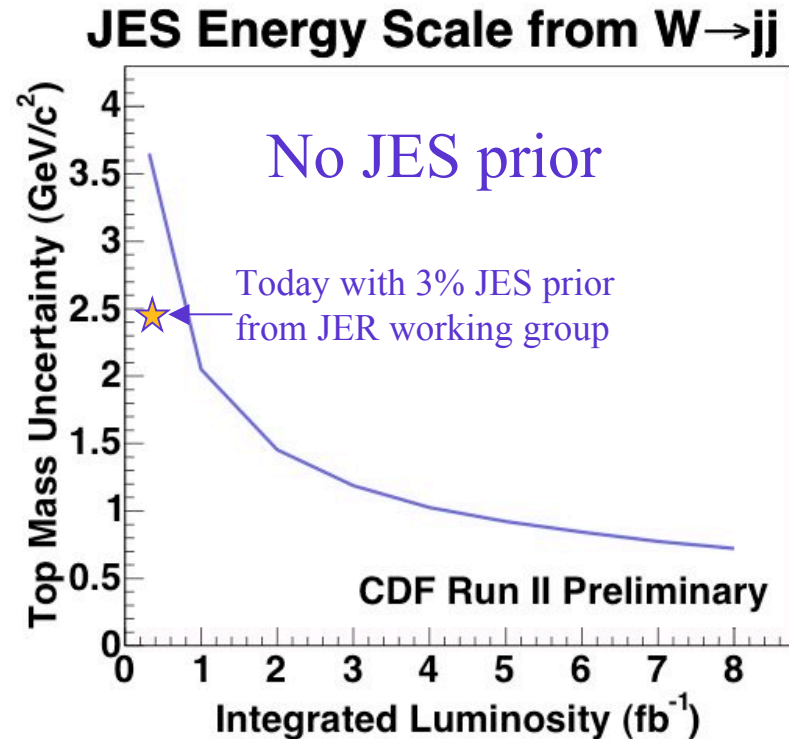
Future Improvements

- ➔ Improve calorimeter simulation:
 - ➔ Lateral profile
 - ➔ Statistical precision of central calorimeter (medium p)
 - ➔ Extend tuning to higher p to avoid the use of test beam data
 - ➔ Measurement of single particle response in the plug calorimeter
 - ➔ Electron response in ϕ -boundaries
- ➔ Improve performance of physics generators:
 - ➔ better understanding of the underlying event, gluon radiation effects
 - ➔ tuning of Pythia, Herwig (Jimmy)
- ➔ Improve jet resolution
- ➔ Will $Z \rightarrow b\bar{b}$ help with the JES in the near future?



Conclusions

- ➔ CDF has a set of corrections and uncertainties that are very solid
- ➔ The main component consist of tuning the calorimeter simulation to single particle response
- ➔ Uncertainties are about 3% and we are working on decreasing them as well improving our means
- ➔ Besides decreasing JES uncertainties, Improvements in JES benefit many analysis: better simulation, missing ET resolution, better physics models
- ➔ At 320pb^{-1} , the top mass in the golden channel, the JES plays an very important role reducing the error from $W \rightarrow jj$. In the future, as more data is accumulated, the impact of JES will be limited in this channel comparing to $W \rightarrow jj$



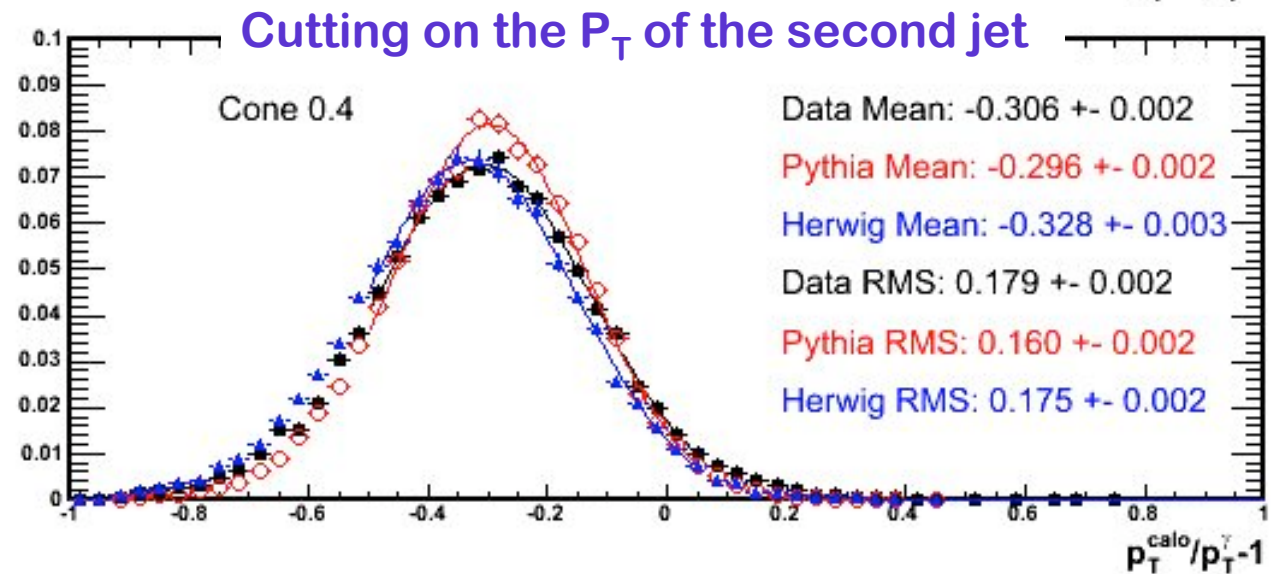
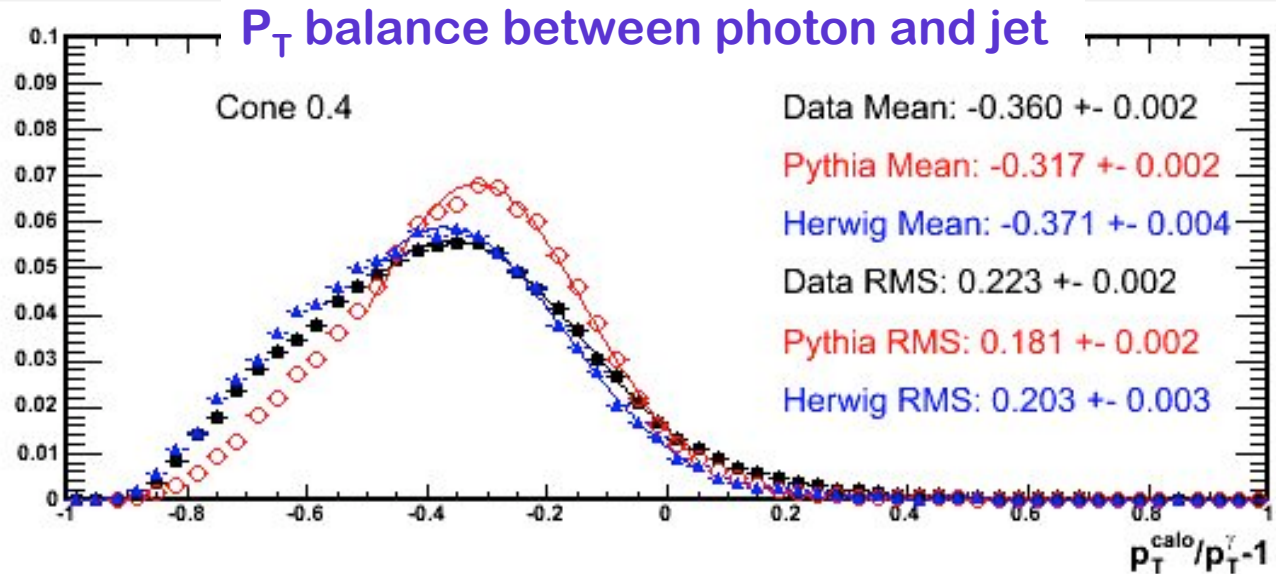
- ➔ Moreover, there are other analyses for which the JES will soon be an important uncertainty (if not yet)

More ! More !

Improvements - Monte Carlo

→ Our understanding of the differences between data and MC in photon+jet is about 3%

→ Decreasing the jet energy scale uncertainty means improve the Monte Carlo generators



Improvements - Simulation

➔ Central:

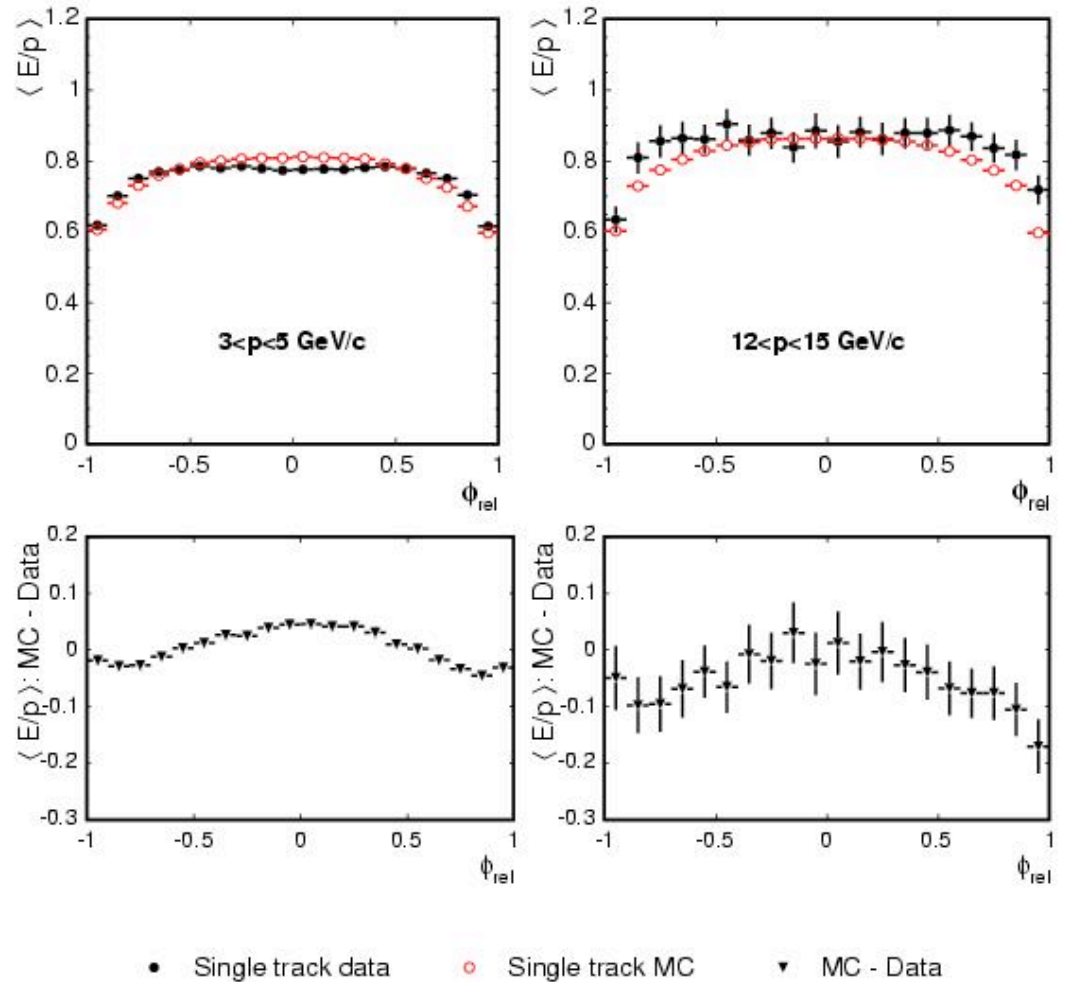
- ➔ For $p < 20$ GeV
 - ➔ more statistics to evaluate E/p uncertainty
 - ➔ if the discrepancy is large, tune the Monte Carlo
- ➔ For $p > 20$ GeV
 - ➔ replace test beam measurement for in situ calibration
 - ➔ special trigger
- ➔ Lateral profile:
 - ➔ could improve the calorimeter showering, decrease out-of-cone uncertainty
- ➔ Need to tune simulation in ϕ cracks

➔ Plug:

- ➔ Having a better forward simulation will allow us to be independent of the dijet balance method
- ➔ p_T balance in dijet event is topology dependent and might create a bias
- ➔ Will improve MET resolution

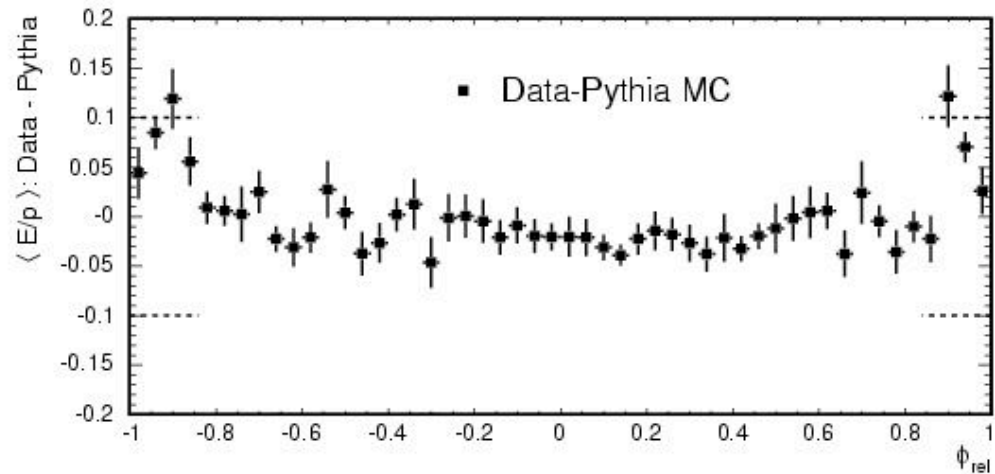
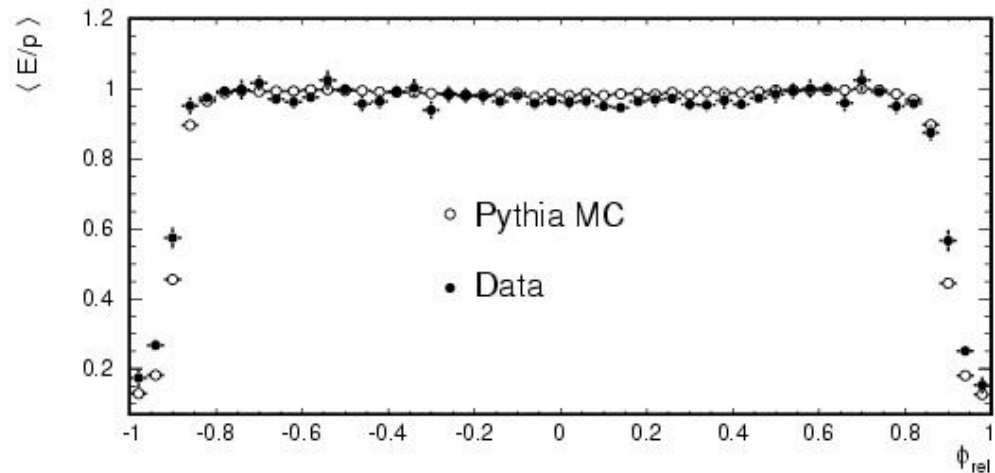
Single Particle Response - ϕ -boundaries

- ➔ **HAD particles**
- ➔ ϕ_{rel} azimuthal angle of the track impact point w.r.t. the target tower center
- ➔ Signal defined in only 81% of calorimeter HAD towers
- ➔ 10% discrepancy in 19% of the tower: 1.9% uncertainty in single particle response
- ➔ Similar effect seen at η -boundaries



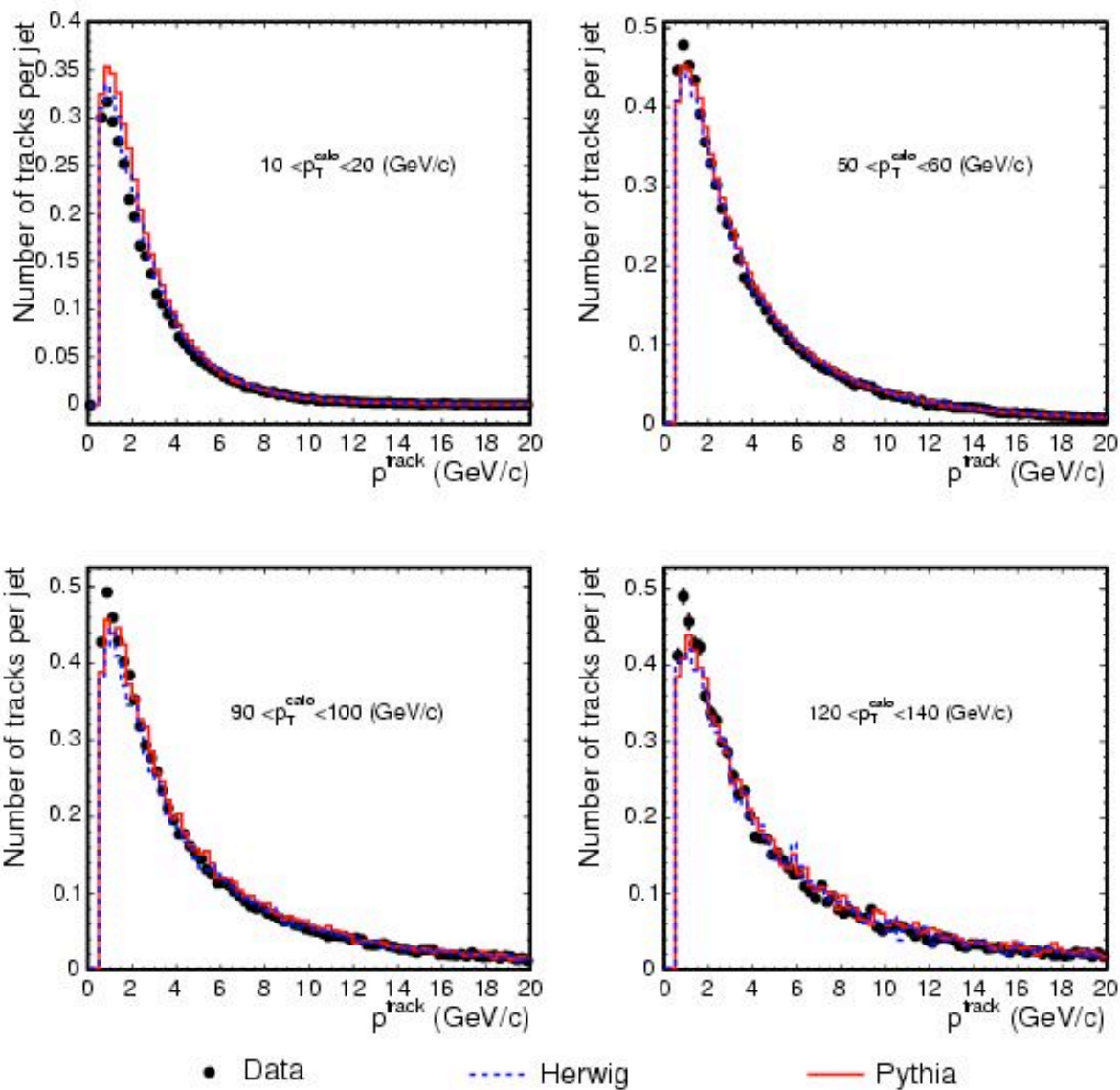
Single Particle Response - ϕ -boundaries

- ➔ **EM particles**
- ➔ ϕ_{rel} azimuthal angle of the track impact point w.r.t. the target tower center
- ➔ Signal defined in 84% of calorimeter EM towers
- ➔ 10% discrepancy in 16% of the tower: 1.6% uncertainty in single particle response
- ➔ Similar effect seen at η -boundaries



Particle Multiplicity

- p_T spectrum of particles inside a jet depends on fragmentation details
- Spectrum corrected for track inefficiencies and underlying event contribution
- Good agreement between MC and data for all jet p_T bins



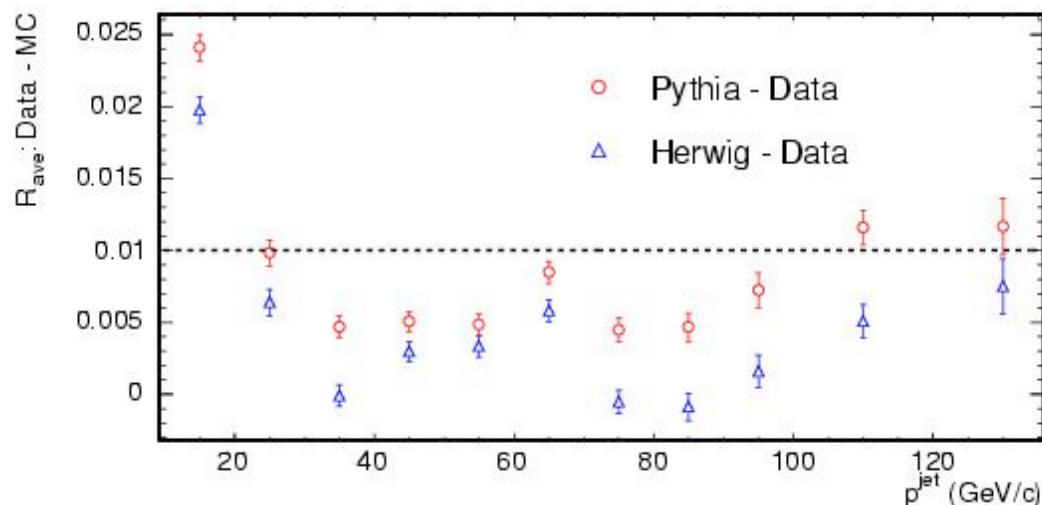
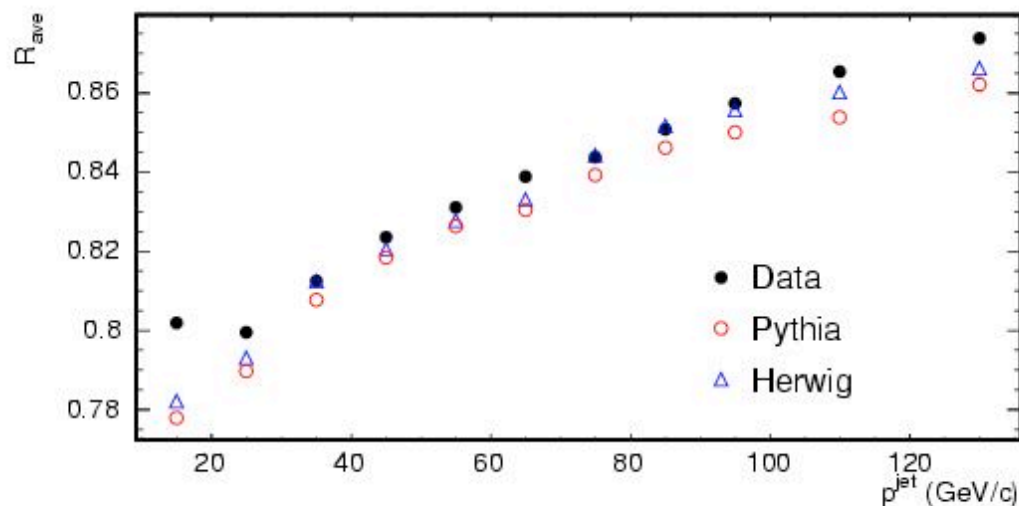
Particle Multiplicity Uncertainties

- ➔ Uncertainty derived from calculating

$$R_{\text{jet}} = \frac{\sum_{i=1}^{\text{Ntracks}} p_{T,i} R_{\text{single-particle}}(p_{T,i})}{\sum_{i=1}^{\text{Ntracks}} p_{T,i}}$$

fixing the single particle response

- ➔ Pythia and data agree within 1% for 20-220 GeV jets, take as uncertainty
- ➔ Herwig and Pythia agree within <1%, not added to total uncertainty

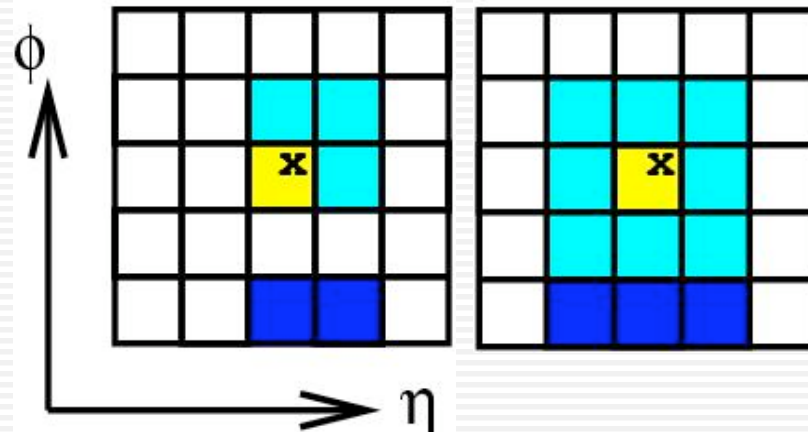


Single Particle Response - Signal Definition

Signal definition for hadron response

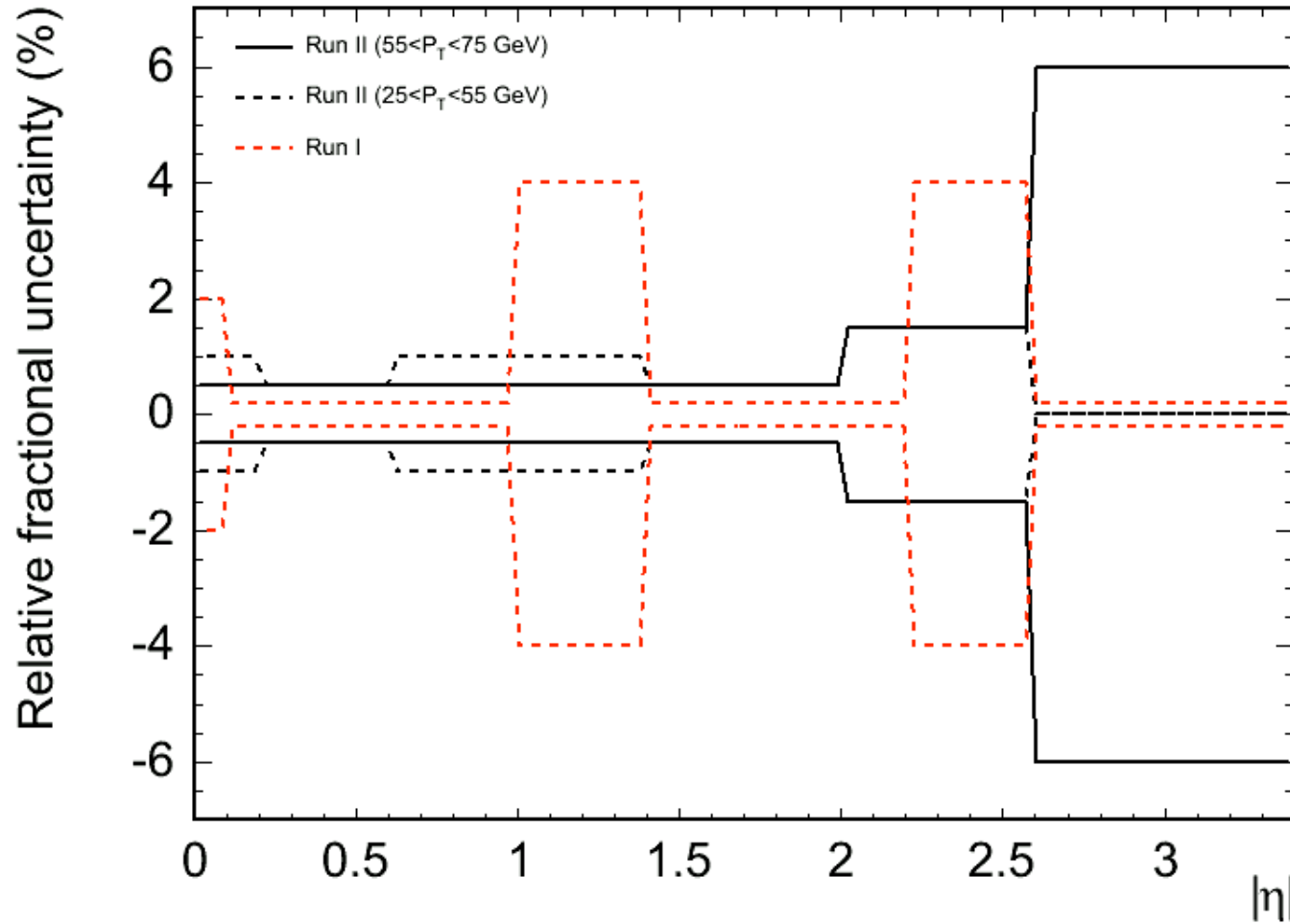
EM: 2x2

HAD: 3x3



Target tower
Signal region
Background region

η -dependent Uncertainties Run I vs Run II





Gflash in a Nutshell

Parametrization of single particle response:

$$\propto a + b \tanh(c \ln E_{\text{inc}} + d)$$

← simple model for incident energy dependence

fraction of deposited energy | relative sampling fractions

energy deposit

$$dE_{\text{vis}}(r) = E_{\text{inc}} f_{\text{dep}} \tilde{m} \left[\frac{\tilde{e}}{\tilde{m}} c_e f_e(r) + \frac{\tilde{h}}{\tilde{m}} c_h f_h(r) \right] dr$$

shower profile

$$f(r) \propto L(z) T(r)$$

z: shower depth
r: radial distance from shower center

longitudinal part:

- photons, electrons:

2 parameters: α, β

$$L(z) = \frac{(\beta z)^{\alpha-1} e^{-\beta z}}{\Gamma(\alpha)}$$

- hadrons: sum of three subprofiles (all Γ functions):

$$L \propto c_h H(x)_h + c_f H_f(y) + c_l H_l(z)$$

pure hadronic shower

π^0 produced in first interaction

π^0 produced in later interactions

3x6 parameters: $\langle \alpha \rangle, \langle \beta \rangle, \sigma_\alpha, \sigma_\beta, \langle f_{\text{dep}} \rangle, \sigma(f_{\text{dep}})$
mean and widths of 2 shower class fractions

lateral part:

$$T(r) = \frac{2r R_0^2}{(r^2 + R_0^2)^2}$$

- R_0 : log-normal distribution in units of Moliere radius
- photons, electrons: $n=2$
- hadrons: $n=1$

$$\langle R_0(E_{\text{inc}}, z) \rangle = [R_1 + (R_2 - R_3 \ln E_{\text{inc}}) z]^n$$

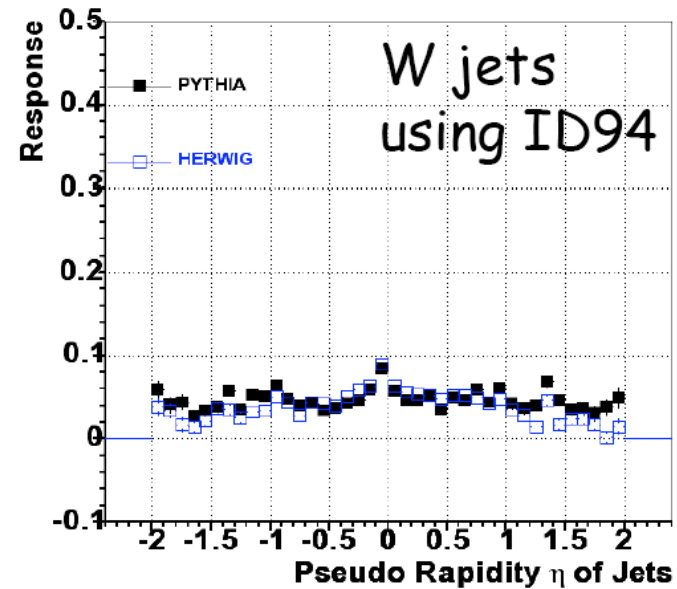
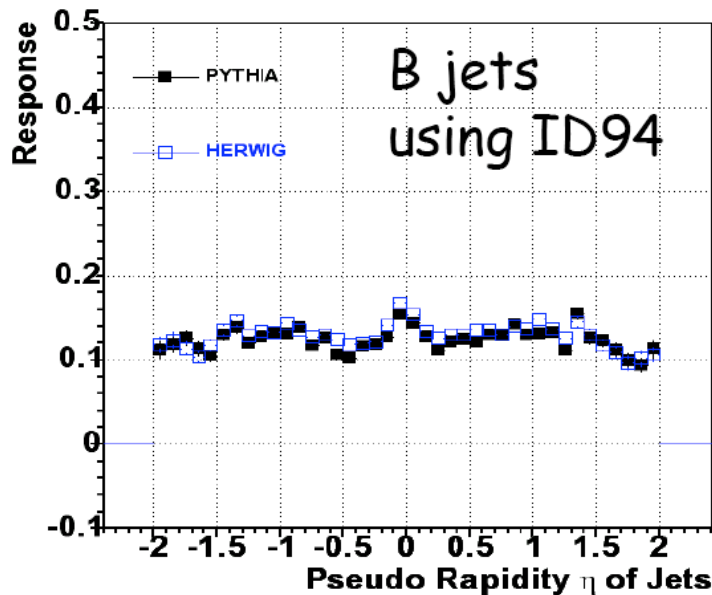
$$\frac{\sigma_{R_0}(E_{\text{inc}}, z)}{\langle R_0(E_{\text{inc}}, z) \rangle} = [(S_1 - S_2 \ln E_{\text{inc}})(S_3 + S_4 z)]^2$$

7 parameters: $R_1, R_2, R_3, S_1, S_2, S_3, S_4$

Corrections for b Jets

➔ The scale of b jets is different:

➤ Taken into account when using top specific corrections or transfer functions



➔ But b and light jets seem to share similar characteristics:

➤ In top analyses, we assign an small uncertainty of 0.6 GeV