

**MICROFILTRATION WITH RAPID BACKPULSING  
AND SURFACE-MODIFIED MEMBRANES**

**Robert H. Davis and Christopher N. Bowman  
Department of Chemical Engineering  
University of Colorado  
Boulder, CO 80309-0424**

**Contract No. 1425-98-FC-81-0062**

**Desalination Research and Development Program Report No. 58**

**December 1999**

**U.S. DEPARTMENT OF THE INTERIOR  
Bureau of Reclamation  
Denver Office  
Technical Service Center  
Environmental Resources Team  
Water Treatment Engineering and Research Group**

*Bureau of Reclamation  
Mission Statement*

The mission of the Bureau of Reclamation is to manage, develop, and protect water and related resources in an environmentally and economically sound manner in the interest of the American public.

*U. S. Department of the Interior  
Mission Statement*

As the Nation's principal conservation agency, the Department of the Interior has responsibility for most of our nationally-owned public lands and natural resources. This includes fostering wise use of our land and water resources; protecting our fish, wildlife, and biological diversity; preserving the environmental and cultural values of our national parks and historical places; and providing for the enjoyment of life through outdoor recreation. The Department assesses our energy and mineral resources and works to ensure that their development is in the best interests of all our people by encouraging stewardship and citizen participation in their care. The Department also has a major responsibility for American Indian reservation communities and for people who live in island territories under U.S. Administration.

*Disclaimer*

The information contained in this report regarding commercial products or firms may not be used for advertising or promotional purposes and is not to be construed as an endorsement of any product or firm by the Bureau of Reclamation.

The information contained in this report was developed for the Bureau of Reclamation: no warranty as to the accuracy, usefulness, or completeness is expressed or implied.

# TABLE OF CONTENTS

|  | <u>Page</u> |
|--|-------------|
| EXECUTIVE SUMMARY .....                            | 1           |
| 1. INTRODUCTION .....                              | 1           |
| 2. MATERIALS AND METHODS .....                     | 4           |
| 2.1 Membrane Surface Modification .....            | 4           |
| 2.2 Crossflow Filtration .....                     | 5           |
| 3. RESULTS AND DISCUSSION .....                    | 6           |
| 3.1 Photografting on Membrane Surfaces .....       | 6           |
| 3.2 Membrane Performance .....                     | 15          |
| 3.3 Fundamental Analysis of Membrane Fouling ..... | 21          |
| 3.4 Economic Analysis and Comparisons .....        | 22          |
| 4. CONCLUSIONS .....                               | 24          |
| REFERENCE LIST .....                               | 25          |
| APPENDIX: DATA RECORD .....                        | 28          |

## LIST OF FIGURES

|   |    |
|---|----|
| Figure 1. Schematic diagram of the two-step photoinduced living graft polymerization method.....  | 3  |
| Figure 2. Schematic diagram of the crossflow filtration system .....  | 6  |
| Figure 3. Grafting density versus irradiation time at different BP concentrations .....   | 8  |
| Figure 4. Average graft polymer chain length versus irradiation time at different AA concentrations.....  | 9  |
| Figure 5. Reaction rates of initiator formation versus BP concentrations.....   | 11 |
| Figure 6. Reaction rates of graft polymerization versus AA concentration .....  | 12 |
| Figure 7. Amount of surface initiator vs. BP concentration .....  | 13 |
| Figure 8. Weight gain as a function of AA concentration for graft polymerization on CA membranes .....  | 14 |
| Figure 9. Pure buffer flux at 5 psi versus the amount of grafted PEG200MA .....   | 16 |
| Figure 10. Permeate flux versus filtration time of 0.14 g/L <i>E. coli</i> without backpulsing at a forward transmembrane pressure of 5 psi .....   | 16 |
| Figure 11. Average neg flux (symbols) versus backpulse duration for crossflow filtration of 0.14 g/L <i>E. coli</i> at a forward filtration time of 4 seconds between backpulses, with forward transmembrane pressure of 5 psi and backward transmembrane pressure of 3 psi .....                 | 17 |
| Figure 12. Average net flux (symbols) versus forward filtration duration for crossflow filtration of 0.14 g/L <i>E. coli</i> at a fixed backpulse duration of 0.2 seconds, with forward transmembrane pressure of 5 psi and backward transmembrane pressure of 3 psi .....                        | 17 |
| Figure 13. Permeate volume versus filtration time for crossflow filtration of 0.14 g/L <i>E. coli</i> ..  | 18 |
| Figure 14. Long-term net flux with backpulsing and recovered flux after backwashing versus the amount of grafted PEG200MA for crossflow filtration of 0.14 g/L <i>E. coli</i> .....   | 20 |
| Figure 15: Schematic of partial cake removal by backpulsing .....   | 21 |
| Figure 16: Experimental data and model prediction of the net flux versus the duration of each backpulse for crossflow microfiltration of 1.0 g/L <i>E. coli</i> bacteria using 0.2 $\mu\text{m}$ cellulose-acetate membranes and a forward filtration period of 10 s between each backpulse ..... | 22 |
| Figure 17. Total cost of treated water as a function of the average net permeate flux for 0.5 MGD and 10 MGD membrane treatment facilities .....  | 23 |

## LIST OF TABLES

|  |    |
|--|----|
| Table 1. Weight percent gain of PP membranes and standard deviation for six repeats in air or nitrogen .....   | 7  |
| Table 2. Weight percent gain of PP membranes and standard deviation for six repeats .....  | 7  |
| Table 3. Properties of Polymeric Membranes in Two-Step Graft Polymerization .....  | 14 |
| Table 4. Effect of membrane surface chemistry on long-term flux and recovered flux after backwashing, with and without backpulsing. Shown are the average plus and minus one standard deviation for 2-6 repeats.....   | 19 |
| Table 5. Effects of <i>E. coli</i> concentration on the average net flux with backpulsing, long-term net flux with backpulsing and recovered flux after backwashing for unmodified PP membranes and modified PP membranes with a weight gain of 3.5 wt% PEG200MA. Shown are the averages plus and minus one standard deviation for 2-4 repeats ..... | 21 |
| Table 6. Long-term net flux and treatment cost for removal of 0.05 g/L bacteria from water by crossflow membrane microfiltration using unmodified and modified polypropylene membranes with and without backpulsing. PEG200MA with 3.5 wt% gain was used for the membrane surface modification .....   | 24 |

## ACRONYMS AND NOMENCLATURE

|                     |  |
|---------------------|--|
| AA                  | - acrylic acid (monomer)                                 |
| AF                  | - amortization factor                                    |
| BP                  | - benzophenone (initiator)                               |
| BPHS                | - surface initiator                                      |
| $C_{\text{mod}}$    | - the cost of single membrane module                     |
| CA                  | - cellulose acetate (membrane)                           |
| $D$                 | - grafting density                                       |
| DMAEMA              | - dimethyl aminoethyl methacrylate (monomer)             |
| $f$                 | - surface initiator formation efficiency                 |
| $G_e$               | - grafting efficiency                                    |
| $I_0$               | - intensity of UV irradiation                            |
| $\langle J \rangle$ | - net flux with backpulsing (cm/s)                       |
| $J_0$               | - water flux for unfouled membrane (cm/s)                |
| $J_s$               | - long-term flux for unfouled membrane (cm/s)            |
| $k_p$               | - propagation rate constant                              |
| $k_t$               | - termination rate constant                              |
| $N_{\text{mod}}$    | - the number of modules required                         |
| PEG200MA            | - polyethylene glycol (200) monomethacrylate (monomer)   |
| PP                  | - polypropylene (membrane)                               |
| PVDF                | - poly(vinylidene fluoride) (membrane)                   |
| $Q$                 | - volumetric treatment rate                              |
| $R_m$               | - rate of monomer consumption                            |
| $t_b$               | - backpulse duration (s)                                 |
| $t_f$               | - duration of forward filtration between backpulses (s)  |
| UV                  | - ultraviolet  |
| $\alpha$            | - ratio of backpulse and forward transmembrane pressures |
| $\beta$             | - cleaning efficiency                                    |
| $\gamma$            | - graft polymer chain length                             |
| $\phi$              | - quantum yield of polymer formation                     |
| $\phi_s$            | - quantum yield of surface initiator formation           |
| $\tau_b$            | - the time constant for cake removal                     |

## EXECUTIVE SUMMARY

A combined method of backpulsing and membrane surface modification was used for the reduction of membrane fouling in water-treatment applications. A novel photoinduced grafting method was used to render membranes hydrophilic with neutral, positively or negatively charged surfaces formed by grafting monomers of poly(ethylene glycol 200) monomethacrylate (PEG200MA), dimethyl aminoethyl methacrylate (DMAEMA), or acrylic acid (AA), respectively, onto a variety of substrates, including polypropylene (PP) and cellulose acetate (CA). Both unmodified and modified PP membranes, as well as commercial CA membranes, were evaluated in a crossflow microfiltration system with and without backpulsing in the presence of *Escherichia coli* bacterial suspensions. The grafting process on the surfaces studied was found to be controllable and reproducible. The process was modeled successfully and can be used to graft a variety of monomers with independent control of the graft density, chain length, and total amount.

For membrane studies it was found that without backpulsing the resulting permeate volume is nearly unchanged for a variety of different membranes. With backpulsing, however, the permeate volume for one hour of filtration with 0.14 g/L *E. coli* using the unmodified PP membranes is almost two times that without backpulsing, and it is significantly higher for the modified membranes. The optimal membrane process was found to be one which involved both backpulsing and modification with a neutral, hydrophilic surface graft. The permeate volume for such a PP membrane is almost three times that of the base case. Additionally, after cleaning, the recovered clean water flux of the modified membranes is twice as high as those for the unmodified membranes and even more improved when compared to unmodified membranes with backpulsing.

## 1. INTRODUCTION

Membrane systems have recently received increased attention for water treatment and other applications. However, a major obstacle to further incorporation of membrane processes in industrial operations is flux decline resulting from fouling. Membrane replacement, required because of fouling, is the single largest operating cost when membranes are used in water treatment applications (Wiesner et al., 1994). Generally, two distinct types of fouling phenomena are considered (Zeman and Zydney, 1996): (1) macrosolute adsorption, which refers to the specific intermolecular interactions between the macrosolute and the membrane that occur even in the absence of filtration, and (2) filtration-induced macrosolute or particle deposition, which is over and above that observed in a static (nonflowing) system.

Filtration-induced macrosolute or particle deposition is usually reversible, nonadhesive fouling. A variety of methods has been reported to reduce this type of fouling for a wide range of different applications:

- (1) addition of coagulants to cause the molecules or the particle to form larger particles which are readily swept off the membrane surface (Al-Malack and Anderson, 1996),
- (2) use of a dispersed phase to disrupt concentration polarization (Parvatiyar, 1996),
- (3) introduction of flow instability by low-frequency axial pressure and velocity pulsing (Si-Hassen et al., 1996; Zahka and Leary, 1985), or by injecting air into the feed stream (Cabassud et al., 1997),
- (4) crossflushing by periodically stopping the permeate flow (Kuruzovich and Piergiovanni, 1996) or forward rinsing with a rinse solution at zero transmembrane pressure (Nakanishi and Kessler, 1985),

- (5) backwashing using fluid or gas (Kroner et al., 1984; Nikolov et al., 1993),
- (6) forward and backward pressure pulsing to remove part of the adsorbed cake (Su et al., 1993),
- (7) imposing a pulsed electric field to remove particulate foulants when the membrane and particles have like charges (Bowen and Sabuni, 1992),
- (8) using curved channel to produce Taylor or Dean vortices (Parnham and Davis, 1995; Chung et al., 1993), and
- (9) rapid backpulsing (Rodgers and Sparks, 1991, 1992, 1993; Wenton, 1995; Redkar and Davis, 1995).

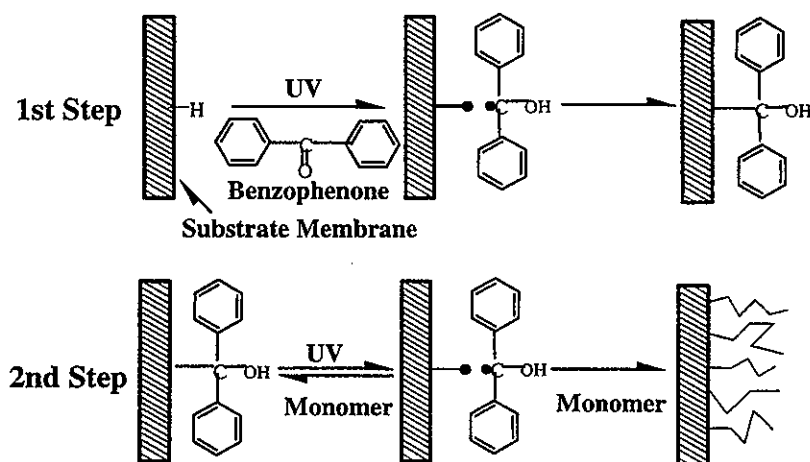
As described by Kuberkar et al. (1998), rapid backpulsing in crossflow filtration involves reversing the transmembrane pressure for approximately 0.1-1.0 second once every few seconds. This reversal results in hydraulic cleaning of the membrane by forcing permeate back through the membrane in the reverse direction; foulants are lifted off the membrane by the backpulse and then swept to the filter exit by the crossflow. Crossflow filtration with rapid backpulsing has been studied extensively by a number of groups in various membrane/foulant systems, and has been reported as an effective technology for controlling fouling and improving permeate flux for nonadhesive foulants exhibiting reversible fouling (Rodgers and Sparks, 1993; Wenton, 1995; Redkar and Davis, 1995). Unfortunately, rapid backpulsing is much less effective in reducing adhesive fouling (Kroner et al., 1984; Kuberkar et al., 1998; Parnham and Davis, 1996).

Macrosolute adsorption is generally irreversible, adhesive fouling (Zeman and Zydney 1996). In water treatment applications involving colloids, microbes, and undissolved hydrocarbons, the foulants are often adhesive and exhibit irreversible fouling, due to hydrophobic interactions, ionic interactions, hydrogen bonding, van der Waals attractions, extracellular macromolecules, and other effects. Several methods have been reported for reducing or eliminating adhesive fouling by changing the membrane surface chemistry. These methods include: (1) physically coating water soluble polymers or charged surfactants onto the membrane surface for temporary surface modification (Kim et al., 1988; Jonsson and Jonsson, 1991), (2) forming ultrathin films on the membrane using the Langmuir-Blodgett (LB) technique (Kim et al., 1989), (3) coating hydrophilic polymers on the membrane using heat curing (Stengaard, 1988; Hvid et al., 1990), (4) grafting monomers to the membranes by electron beam irradiation (Kim et al., 1991; Keszler et al., 1991), and (5) photografting monomers to the membrane using UV irradiation (Yan et al., 1988; Nystrom and Jarvinen, 1991; Yamagishi et al., 1995; Ulbricht et al., 1996).

Photoinduced grafting is a particularly useful technique for the modification and functionalization of polymeric materials due to its significant advantages: low cost of operation, mild reaction conditions, selectivity to absorb UV light without affecting the bulk polymer, and permanent alteration of the membrane surface with facile control of the chemistry. Several researchers (Ulbricht et al., 1996; Yamagishi et al., 1995) have reported the reduction of irreversible protein (BSA) fouling when membrane surfaces are modified by photografting. However, simultaneous photografting (with photoinitiator and monomer present together) may result in production of significant amounts of homopolymer and crosslinked polymer, for cases where the photoinitiator abstracts hydrogen from either the monomer or reacted polymer. The undesired homopolymer wastes expensive starting materials, and crosslinked polymer is detrimental to membrane filtration since the membrane pores may become blocked. Moreover, the grafting density (number of grafting sites per area) and graft polymer chain length can not be determined independently, much less controlled, in the previously developed process.



A novel photografting technique was designed and developed as part of this work and is currently awaiting publication in *Macromolecules* (Ma et al., 1999). With this technique, homopolymer and crosslinked polymer can be significantly reduced, linear polymer chains are preferred, and the grafting density and graft polymer chain length are controlled independently. The schematic reaction mechanism for the grafting reaction is shown in Figure 1. In the first step, benzophenone abstracts hydrogen from the substrate to generate surface radicals and semipinacol radicals, which combine to form surface photoinitiators in the absence of monomer solutions. The unreacted benzophenone is then washed off by a good solvent. In the subsequent step(s), the monomer solutions are added onto the active substrate, and the surface initiators initiate the graft polymerization upon exposure to UV irradiation. Both homopolymer and crosslinked polymer are reduced in the novel grafting method, since benzophenone is not present at the same time with monomer or grafted polymer.



**Figure 1. Schematic diagram of the two-step photoinduced living graft polymerization method.**

Both reversible and irreversible fouling are reduced by the combination of backpulsing and membrane surface modification as demonstrated by the following results. Results are presented for detailed studies on the grafting reaction, modeling of the grafting, and evaluation of membrane performance for both modified and unmodified membranes. Both unmodified and modified PP membranes, as well as commercial cellulose acetate (CA) membranes, were tested in a crossflow microfiltration system with and without backpulsing in the presence of *Escherichia coli* bacterial suspensions.

In the first study of fouling reduction in wastewater treatment funded by the Bureau of Reclamation, it was found that rapid backpulsing was quite effective in maintaining high permeate fluxes when treating suspensions of nonadhesive matter. However, for highly adhesive foulant suspensions, rapid backpulsing is much less effective in reducing membrane fouling. Therefore, in the second study of the subject, a combined method of rapid backpulsing and membrane surface modification was proposed to reduce both nonadhesive and adhesive fouling. The original objectives of the project were met, and an extra effort was required for developing a novel grafting method to modify membrane surface chemistry. In the current study of the subject, the novel photografting method was investigated using commercial photopolymerization equipment. The membrane surface chemistry, grafting density, and graft chain length were well controlled. Most of the fouling characterization and backpulsing studies were performed with the modified polypropylene membranes, and the interactions between foulant and membrane surface were examined.

## 2. MATERIALS AND METHODS

### 2.1. Membrane Surface Modification

The base membranes used in the experiments are commercial porous disk polypropylene microfiltration membranes with a diameter of 47 mm, thickness of approximately 110  $\mu\text{m}$ , porosity of 40 %, and pore diameter of 0.22  $\mu\text{m}$  (Micron Separations Inc., M02WP04700), and cellulose acetate microfiltration membranes with a diameter of 47 mm, thickness of approximately 120  $\mu\text{m}$ , and pore diameter of 0.22  $\mu\text{m}$  (Sartorius, Cat. 11127-047N). Acrylic acid (AA) (Aldrich, cat. 14,723-0), poly(ethylene glycol 200) monomethacrylate (PEG200MA) (Polyscience, Inc., cat. 16712), and dimethyl aminoethyl methacrylate (DMAEMA) (Aldrich, cat. 23,490-7) were used as the monomers. All three monomers are hydrophilic. AA is negatively charged, DMAEMA is positively charged, and PEG200MA is neutral. Unmodified PP and CA membranes are hydrophobic and hydrophilic, respectively, and they are both neutral. Benzophenone (BP) (Aldrich, Cat. No. B930-0) was used as the initiator. Benzene, acetone, and deionized water were used as solvents. All chemicals were used without purification.

Both sequential and simultaneous photoinduced graft polymerization methods were used in the present work. First, the commercial PP membranes were soaked in benzene and dried to constant weight. Then, the membranes were weighed using an analytical balance which has an accuracy of 0.01 mg. For the sequential method, in the first step, the presoaked and preweighed membranes were saturated with benzene solutions of BP (3 g of solution was added to the membrane) and then placed in a quartz reaction vessel, which was subsequently purged with nitrogen or air. The quartz vessel is an empty cylinder with a diameter of 25 cm and a height of 2.5 cm. UV irradiation was carried out in a commercial ultraviolet processor (model QC120244ANIRDR, manufactured by RPC Industries), which was donated by 3M. The processor is equipped with 2 UV bulbs; each bulb is 400 W with a wavelength range of 232 nm to 500 nm. An optical multi-layer dielectric interference filter ( $365 \pm 5$  nm), from Edmund Scientific (Stock No. F43155), was used in the kinetic experiments. The quartz vessel was put on the conveyor, which carried the quartz vessel under the UV lamps. After irradiation for a selected number of passes, the substrates were removed from the quartz vessel, and the residual, unreacted solutions were extracted by soaking and washing the membrane in acetone and drying the membrane at room temperature in air until constant weight. In the subsequent step, the procedures in the first step were repeated, except that monomer solutions were used instead of BP solutions and that the membrane was put in a vacuum oven at 127 mm Hg and 50  $^{\circ}\text{C}$  to evaporate the residual, unreacted solutions. The nongrafted poly(acrylic acid) was removed by soaking the membranes in deionized water for 24 hours. Finally, the membranes were washed in acetone and dried to constant weight. For the simultaneous method, the procedures are similar to the procedures of the second step in the sequential method, except that both BP and monomer are present in the benzene solution.

The percent graft of BP, percent graft of monomer, grafting density, graft polymer chain length, and grafting efficiency are calculated by the following formulae:

$$\text{Percent graft of BP} = (W_1 - W_0)/W_0 \times 100\%, \quad (1)$$

$$\text{Percent graft of monomer} = (W_2 - W_1)/W_0 \times 100\%, \quad (2)$$

$$\text{Grafting density, } D = (W_1 - W_0)/MW_{\text{BP}}/V, \quad (3)$$

$$\text{Graft polymer length, } \gamma = [(W_2 - W_1)/MW]/[(W_1 - W_0)/MW_{\text{BP}}], \quad (4)$$

$$\text{Grafting efficiency, } G_E = (W_2 - W_1)/(W_3 - W_0) \times 100\%, \quad (5)$$

where  $W_0$  is the weight of the blank membrane,  $W_1$  is the weight of the membrane after the first step, obtained by weighing after extraction of unreacted BP solutions with proper solvents,  $W_2$  is the weight of the membrane after the second step, obtained by weighing after extraction of

homopolymer with proper solvents,  $V$  is the volume of the membrane pores,  $MW_{BP}$  and  $MW$  are the molecular weight of BP and monomer, respectively, and  $W_3$  is the weight of the membrane with both ungrafted and grafted polymer, obtained by weighing after vaporization of residual monomer and solvent solutions. The weight gain measurements were made using an analytical balance (Denver Instrument Company, A-200DS), which has an accuracy of 0.01 mg.

## 2.2. Crossflow Filtration

The original *E. coli* strain RB791 sample was obtained from the lab of Dr. George Georgiou at the University of Texas, Austin. Subsequent cultures were grown for 24 hours in a shaker water bath at 37°C and 200 rpm using M9 medium (Sambrook et al., 1989) and then centrifuged using a Beckman GPR Centrifuge at 2500 rpm for 30 minutes. Dry cell weights of 0.05-0.6 g/L *E. coli* resuspended in a buffer solution were used for the microfiltration experiments. The *E. coli* concentration was measured using a Diode Array Spectrophotometer (Hewlett 8452A). The buffer solution consists of 80 g NaCl, 14.4 g NaHPO<sub>4</sub>, 2.4 g KH<sub>2</sub>PO<sub>4</sub>, and 2.0 g KCl in 10 liters of deionized water. All of these chemicals were obtained from Fisher Scientific. The *E. coli* cells are approximately 2 μm long and 0.5 μm wide.

A schematic diagram of the crossflow microfiltration system is shown in Figure 2. The feed flows from the pressurized feed tank to the crossflow module, which was fabricated in our instrument shop. A disk membrane with a diameter of 47 mm is used. The filtration area is 30 mm wide by 23 mm long, and the thickness of silicon gaskets between the membrane and the top plate of the module is 0.4 mm. The retentate flows from the module back to the feed tank. To keep the suspension concentration constant, buffer is pumped from a second tank to the feed tank at the rate at which permeate is removed. The permeate flows to a computer-interfaced balance which records the mass. During backpulsing, buffer from a third tank is sent through permeate channel up through the membrane in the direction opposite that of forward flow. The entire system is pressurized using a nitrogen tank. A QuickBasic program is used to monitor the solenoid valves, control the rate of fluid flow from the second tank to the feed tank, and record the balance readings. The program is run on a Data Stor 386-20D computer.

All experiments were run at room temperature (22-25°C). The PP membrane was wetted using ethanol just before each filtration experiment. The pure buffer flux was determined with plain buffer at a forward transmembrane pressure of 5 psi for five minutes. Then, *E. coli* filtration with or without backpulsing was performed for one hour. A new membrane was used for each experiment. For crossflow filtration with backpulsing, the forward transmembrane pressure was 5 psi and the backward transmembrane pressure was 3 psi. The specified duration of each backpulse was 0.1-0.5 seconds, and the forward filtration between each backpulse was for a specified duration of 2-14 seconds. After obtaining the average net flux (over the one-hour filtration period) and the long-term net flux (over the last 5 minutes of filtration, during which the flux remained steady), the backpulsing was stopped and the system was immediately backwashed for at least five minutes (which we found sufficient to remove all reversible foulants) at a reverse transmembrane pressure of 3 psi while still running buffer over the membrane. Finally, plain buffer was run through the membrane at 5 psi forward transmembrane pressure for five minutes to determine the recovered permeate flux.

For crossflow filtration without backpulsing, forward filtration was performed at a transmembrane pressure of 5 psi for one hour. The long-term flux was determined over the last five minutes in the filtration process (during which the flux remained steady). The backwashing process and recovered flux measurements were performed in the same way as those with backpulsing.

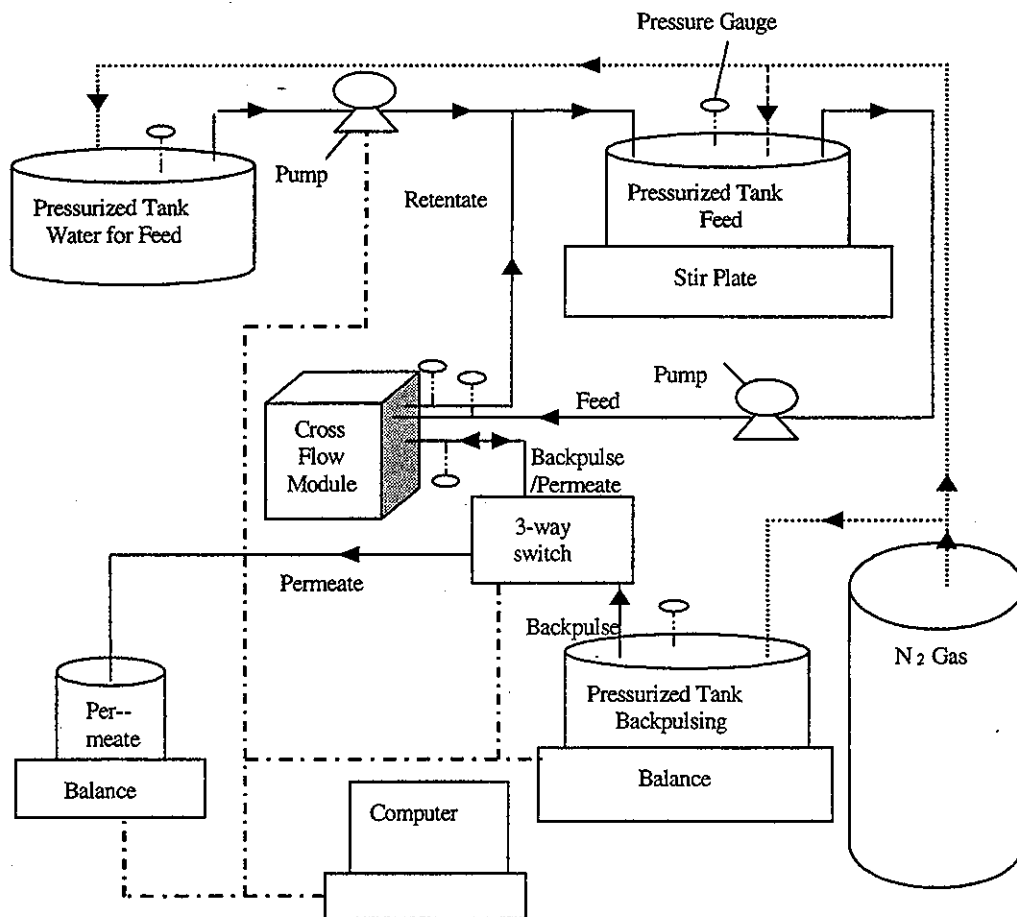


Figure 2. Schematic diagram of the crossflow filtration system. The solid lines depict liquid flows, the dotted lines depict gas flows, and the dashed-dotted lines depict electronic connections from the computer to a pump, the solenoid valve, and two balances (from Mores et al. (1999)).

### 3. RESULTS AND DISCUSSION

#### 3.1 Photografting on Membrane Surfaces

It is well recognized that simultaneous photoinduced graft polymerization onto substrates occurs *via* hydrogen abstraction (Ulbricht et al., 1996; Yang and Ranby, 1996; Li et al., 1997). This principle suggests that excited benzophenone can abstract hydrogen in the absence of monomer to form the surface initiator, as proposed in Figure 1. A series of experiments has been conducted to provide evidence of the surface initiator formation in the first step of the process. The results are listed in Table 1. It is shown that the weight of the membranes did not change significantly without BP or without UV. However, the weight of the membranes did increase with BP coating and UV irradiation, and higher weight gain was obtained in nitrogen than in air. These results indicate that the reaction proceeded as desired and that the benzophenone (BP) was chemically bound to the substrate upon UV irradiation. Otherwise, the BP would be washed off from the substrate in a good solvent. There are two possible reasons for the weight gain. One reason is the formation of peroxide (Ulbricht et al., 1996; Uchida et al., 1993; Uyama and Ikada,

1988). the other is the formation of graft BP through hydrogen abstraction. The formation of peroxide is excluded in our experiments, since oxygen is an inhibitor. Additional evidence about surface initiator formation is provided in subsequent sections of this report.

**Table 1. Weight percent gain of PP membranes and standard deviation for six repeats in air or nitrogen. 'Without BP' means that blank membranes without BP were irradiated 26.6 seconds (20 passes  $\times$  1.33 s.). 'Without UV' indicates that membranes were soaked in 5 wt% BP in benzene solution, without irradiation, and then soaked and washed in acetone and dried until constant weight. 'With BP and UV' means that the membranes were modified under the following conditions: 5 wt% BP in benzene, 26.6 seconds UV irradiation.**

|                   | Without BP      | Without UV      | With BP and UV  |
|-------------------|-----------------|-----------------|-----------------|
| In Air            | 0.01 $\pm$ 0.02 | 0.02 $\pm$ 0.03 | 0.17 $\pm$ 0.03 |
| In N <sub>2</sub> | 0.03 $\pm$ 0.03 | 0.02 $\pm$ 0.02 | 0.34 $\pm$ 0.02 |

*Verification of initiative ability of surface initiator and living graft polymerization*

From Table 2, significant weight gain in the second step of the process was obtained on the membrane with surface initiator and UV irradiation in nitrogen. The weight change is relatively small or not significantly different from zero at all other conditions. These results indicate that the oligomer or polymer was indeed grafted on the membranes. Homopolymerization of AA can occur with or without surface initiator in the presence of UV irradiation. However, the homopolymer formed in the absence of surface initiator is washed off in a good solvent. Thus, the weight gain of the membrane is caused by graft polymerization that was initiated by the surface radicals. The membrane weight was nearly unchanged when the UV irradiation was performed in the presence of air. This result suggests that oxygen is a strong inhibitor of the second step of the graft polymerization process, as expected, since oxygen is an inhibitor of free radical polymerizations.

As mentioned earlier, the semipinacol radicals prefer to combine with growing polymeric chain radicals. So, the termination pattern produces a grafted copolymer that is rooted on the surface of the polymer substrates and carries end groups which were also found to be able to reinitiate polymerization as reported by Yang and Ranby (1996). In fact, numerous experiments in our work also demonstrate that the growing chain radicals terminate the semipinacol radicals and then split-off to initiate polymerization to increase the graft polymer chain length.

**Table 2. Weight percent gain of PP membranes and standard deviation for six repeats. The monomer solution for all membranes was 25 wt% AA in ethanol. UV irradiation time was 9.31 seconds (7 passes  $\times$  1.33 s). The grafted BP in the first step was 0.34 wt% of the blank PP membrane under the conditions of 5 wt% in BP in benzene and 26.6 s UV irradiation.**

|                   | Blank Membranes |                 | Membranes with Surface Initiator |                 |
|-------------------|-----------------|-----------------|----------------------------------|-----------------|
|                   | Without UV      | With UV         | Without UV                       | With UV         |
| In Air            | 0.00 $\pm$ 0.00 | 0.02 $\pm$ 0.07 | 0.01 $\pm$ 0.01                  | 0.01 $\pm$ 0.00 |
| In N <sub>2</sub> | 0.01 $\pm$ 0.02 | 0.06 $\pm$ 0.04 | 0.02 $\pm$ 0.04                  | 2.78 $\pm$ 0.32 |

### Control of grafting density and average graft polymer chain length

Figure 3 shows the relationship between grafting density (mole of surface initiators per volume) and UV irradiation time at different BP solution concentrations. As expected, grafting density increases with increasing UV irradiation time and has a maximum value with increasing

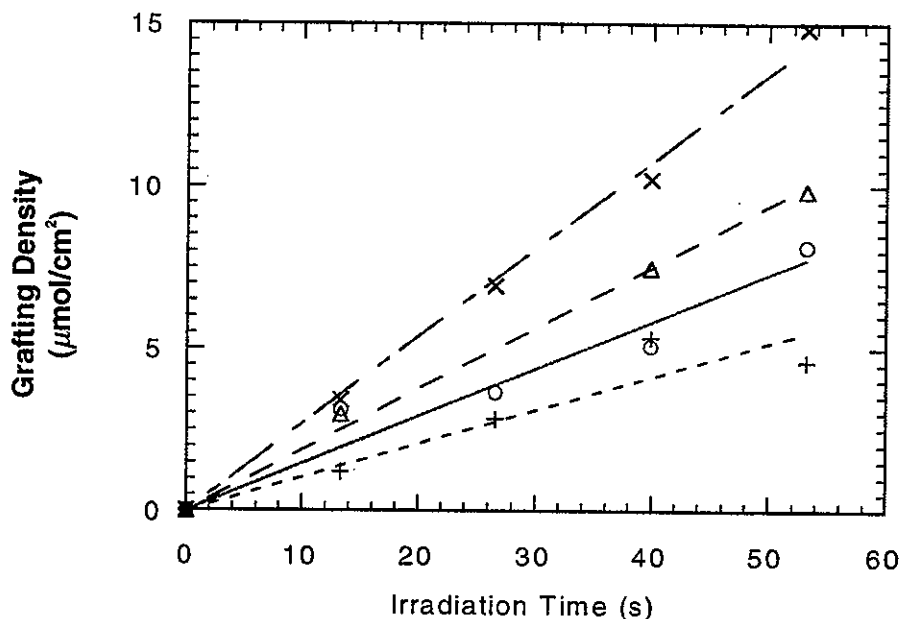
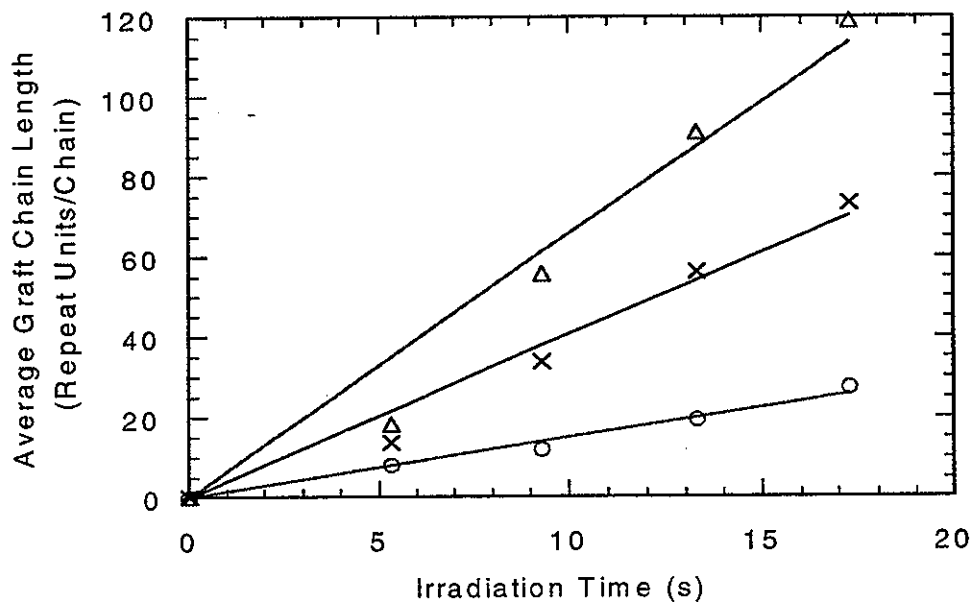


Figure 3. Grafting density versus irradiation time at different BP concentrations (o) 0.5 wt% BP; (x) 10 wt% BP; (Δ) 30 wt% BP; (+) 70 wt% BP.

BP concentration for a given UV irradiation time. Very low BP concentrations are undesired due to low surface initiation, whereas very high BP concentrations are undesired because BP absorbs the UV radiation. The results of Figure 3 indicate that the grafting density of the surface initiator can be controlled by controlling UV irradiation time and BP concentration.

In the second step of the novel photografting process, it is reasonable to assume that each surface initiator formed in the first step initiates polymerization to form one graft polymer chain since the surface initiator concentration is very low (0.34 wt% of the substrate) and the photoinitiation is very rapid. So, the average graft polymer chain length is calculated by equation (4). The results in Figure 4 demonstrate that the graft polymer chain length increases linearly with increasing UV irradiation time for a given grafting density and a given AA concentration. The graft polymer chain length also increases with increasing AA concentration in the ethanol solution. These results indicate that the graft polymer chain length can be controlled by adjusting irradiation time and monomer concentration, which is expected to have potential advantages in the membrane surface modification for controlling membrane fouling.



**Figure 4. Average graft polymer chain length versus irradiation time at different AA concentrations; (o) 5 wt% AA; (x) 15 wt% AA; (Δ) 25 wt% AA. The amount of grafted BP in the first step was 0.34 wt% of the blank PP membrane under the conditions of wt% BP in benzene and 26.6 s UV irradiation for all experiments.**

#### *Comparison of sequential and simultaneous grafting methods*

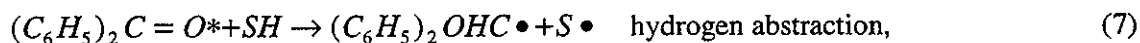
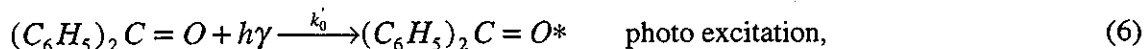
The simultaneous and novel sequential photoinduced grafting polymerization methods were both used to modify PP membranes and then compared. With 0.34 wt% BP grafted in the first step and 50 wt% AA in ethanol used in the second step, the grafting efficiency after 13.3 seconds of UV irradiation is  $18 \pm 3$  % for the simultaneous method and  $83 \pm 6$  % for the sequential method, at the 90% confidence level for three repeats. The conditions used for these experiments are ones which exaggerate the effects of lower efficiency in the simultaneous grafting case. Poly(acrylic acid) and monomeric acrylic acid both are very capable of hydrogen abstraction. When other monomers with less labile hydrogens are grafted or are grafted under different grafting conditions, the grafting efficiency may be much higher for the simultaneous grafting method (Yang and Ranby, 1996; Ranby et al., 1988).

For these studies, the grafting efficiency represents the percentage of grafted polymer relative to the total amount of polymer. It has been recognized that semipinacol radicals themselves rarely initiate bulk homopolymerization (Li et al., 1997). The significant percentage of homopolymer in the simultaneous method is attributed to the excited BP abstracting hydrogen from monomer to form monomer radicals, resulting in the formation of ungrafted homopolymer. Further, hydrogen abstraction from the graft polymer chain will result in the formation of branched or/and crosslinked polymer. In the novel sequential method, however, the homopolymer can be reduced significantly, and the formation of linear polymer chains is preferred, since there is no BP on the membrane surface or in the monomer solutions. The proposed reaction mechanism is confirmed by the fact that the grafting efficiency of the novel sequential method is 4-fold greater than that of the simultaneous method when AA was grafted to PP membranes in the present work. It is worth mentioning that the simultaneous grafting method is preferable when the hydrogen in the substrate is more readily abstracted by BP than is the

hydrogen in the monomer and in the newly formed grafted polymer or homopolymer. Under these conditions, the polymerization can be more efficient and simpler for the simultaneous method. Clearly, the photoefficiency in the simultaneous graft polymerization will be dramatically higher than the overall photoefficiency in the proposed process. Thus, the proposed process is particularly useful only for monomers (and graft copolymers) which readily abstract hydrogen, such as those studied in this work.

*Reactions of a novel sequential photoinduced living graft polymerization*

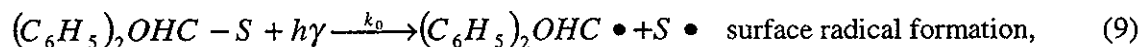
In this novel sequential photoinduced graft polymerization method, the grafting process can be divided into two steps: (1) synthesis of surface initiator, and (2) graft polymerization of monomers. In the first step, a BP molecule absorbs a photon and then abstracts a hydrogen atom from the substrate. This abstraction process creates surface radicals and semipinacol radicals. Because there is no monomer present in this step, the recombination of the surface radicals and semipinacol radicals takes place readily, and generates the surface initiators. The proposed reactions are described in equations (6)-(8):



where SH represents the substrate with hydrogen on the surface, \* represents the excited state, and • stands for the radical.

In the second step, the substrate with the surface initiators grafted on its surfaces is exposed to the solution of monomer to be grafted and UV irradiation. The UV light cleaves the carbon-carbon bond of the surface initiator to form surface radicals and semipinacol radicals. The monomer reacts with surface radicals preferentially because of steric effects. Thus, the desired polymer chains can be grafted onto the substrate. The proposed reactions are listed in equations (9)-(12):

Photo excitation:



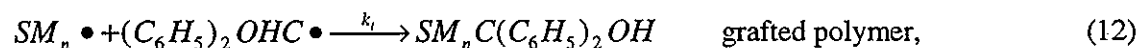
Initiation:



Propagation:



Termination:



where • stands for the radical and M represents monomer.



### Kinetics of surface initiator formation

In terms of equations (6)-(8) and the Lambert-Beer law, the kinetic equation of surface initiator formation is written as

$$d_{[\text{BPHS}]} / dt = f\phi_s I_0 e^{-\epsilon c[\text{BP}]} (1 - e^{-\epsilon b[\text{BP}]}) \quad (13)$$

where BPHS represents  $(\text{C}_6\text{H}_5)_2\text{OHC-S}$  (the surface initiator formed in the hydrogen abstraction),  $f$  is surface initiator formation efficiency,  $\phi_s$  is the quantum yield of surface initiator formation,  $I_0$  is the intensity of incident UV irradiation,  $c$  is the thickness of a BP solution layer through which UV irradiation must pass to reach the substrate surface, and  $b$  is the thickness of the membrane where the hydrogen abstraction reaction occurs.

To determine the parameters in equation (13), experiments were performed using different BP concentrations at different irradiation times. The surface initiator formation rate can be obtained by taking the derivative of the amount of grafted BP with respect to irradiation time. It was found that the reaction rate is a constant for a given initial BP concentration. This behavior is predicted by equation (13) because the conversion of BP is very low and the BP concentration can be considered to be nearly constant.

The relationship between reaction rate and BP concentration is shown in Figure 5. There is an optimum BP concentration which maximizes the reaction rate, due to the reduction in UV transmittance to the membrane surface at high BP concentrations. The circles represent the experimental data while the solid line represents the best-fit of equation (13). The maximum likelihood estimate of the model parameters is obtained using KaleidaGraph™ based on the Levenberg-Marquardt (Press et al., 1992) method by minimizing the sum of the squared errors. The confidence intervals for the model parameters were calculated based on the work of Donaldson and Schnabel (1987), as suggested by Young et al. (1997). The best-fit model parameters and their 90% confidence intervals are  $f\phi_s I_0 = 0.020 \pm 0.001$  mol/L·s,  $\epsilon c = 0.26 \pm 0.01$  l/mol, and  $\epsilon b = 34 \pm 10$  L/mol.

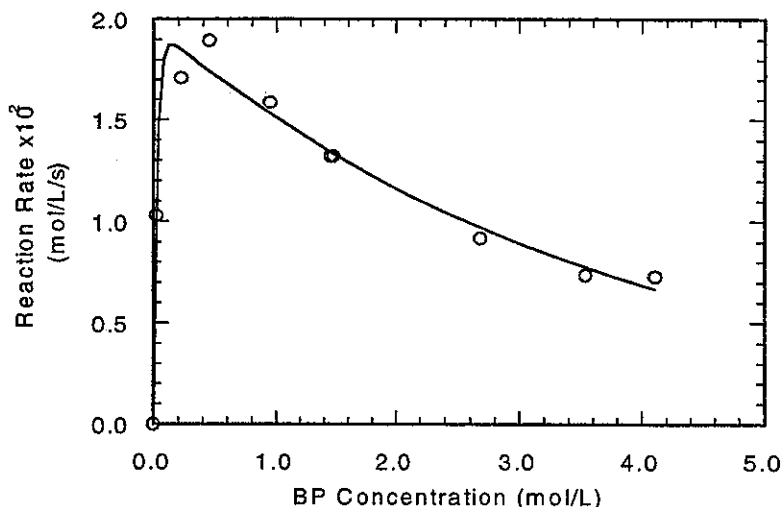
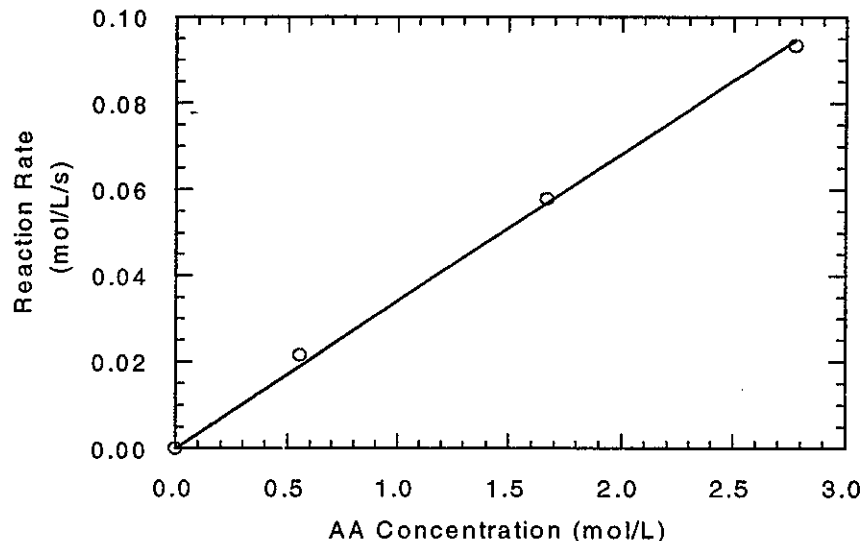


Figure 5. Reaction rates of initiator formation versus BP concentrations: (o) experimental data; (—) model curve. UV irradiation time is 26.6 s for all experiments.



**Figure 6.** Reaction rates of graft polymerization versus AA concentration: (o) experimental data; (—) model curve. UV irradiation time is 26.6 s for all experiments. The amount of grafted BP in the first step was 0.34 wt% of the blank PP membrane under the conditions of 5 wt% BP in benzene and 26.6 s UV irradiation for all experiments.

#### *Kinetics of living graft polymerization*

According to equations (9)-(12), the kinetic equation for the second step can be written as

$$R_m = k_p[M] \left\{ \phi I_0 (1 - e^{-\epsilon b [\text{BPHS}]}) / k_t \right\}^{1/2}, \quad (14)$$

where  $R_m$  represents the rate of monomer consumption,  $\phi$  is the number of grafting chains produced per light photon absorbed,  $k_p$  and  $k_t$  are reaction rate constants, and  $[M]$  stands for the monomer solution concentration. To determine the quantitative relationship between reaction rate and monomer concentration, different monomer concentrations were used at different irradiation times. The monomer consumption rate was obtained by taking the derivative of the amount of grafted AA with respect to irradiation time. It was found that the reaction rate is a constant for each initial AA concentration. This behavior is predicted by equation (14), because the conversion of AA is very low, and the AA concentration can be considered to be nearly constant. The linear relationship between monomer consumption and reaction time further verifies the living graft polymerization.

The relationship between reaction rate and AA concentration is shown in Figure 6. The linear relationship of reaction rate and AA concentration confirms the proposed kinetic equation (14). The parameters in the graft polymerization rate equation were obtained using linear regression in KaleidaGraph™. Confidence intervals for the model parameters were calculated using the method reported by Walpole and Myers (1985). The best-fit slope and intercept as well as their 90% confidence intervals are  $0.033 \pm 0.002 \text{ s}^{-1}$  and  $0.001 \pm 0.003 \text{ mol/L}\cdot\text{s}$ , respectively. As expected, the intercept is not significantly different from zero.

The parameters in equation (14) were obtained using the following method. The value of  $\epsilon b$  is 34 L/mol from the surface initiator formation kinetics, and  $[\text{BPHS}]$  is 0.014 mol/L in the

kinetic study of graft polymerization. The value of  $k_p\{\phi I_0(1-e^{-\epsilon b[\text{BPHS}]})/k_t\}^{1/2}$  is  $0.033 \text{ s}^{-1}$  from the slope of the best-fit line in Figure 5. Therefore,  $k_p\{\phi I_0/k_t\}^{1/2}$  is  $0.054 \text{ s}^{-1}$  and the final kinetic equation for graft polymerization is  $R_m = 0.054(1-e^{-34[\text{BPHS}]})^{1/2}[\text{M}]$ , with  $[\text{BPHS}]$  and  $[\text{M}]$  having units of mol/L and  $R_m$  having units of mol/L·s.

#### *Grafting on various polymer membranes*

The two-step photoinduced grafting method was originally developed using PP microfiltration membrane as substrate and acrylic acid as monomer. To examine the effect of substrates on the graft polymerization, commercial cellulose acetate and polyvinylidene fluoride polymeric membranes were used in the experiments.

For the cellulose acetate (CA) microfiltration membrane, the results showing the effect of BP concentration on the surface initiator formation (1<sup>st</sup> step) are shown in Figure 7. As for the PP membrane, there is a maximum weight gain at an optimal BP concentration due to a competition between increased reaction rate and increased light attenuation with increasing BP concentration.

In the AA graft polymerization step (2<sup>nd</sup> step), the membranes with surface initiator weight gain from the first step of  $0.27 \pm 0.04 \text{ wt}\%$  were used at different AA concentrations. It was found that the membranes stuck to the glass plate and quartz disks when the AA concentration was 25 wt% or greater and the irradiation exposure was 10 passes or greater. The weight gains of the CA membrane were  $(5.8 \pm 0.1)$  and  $(15.0 \pm 0.2) \text{ wt}\%$ , respectively, for 5 wt% and 15 wt% AA in ethanol solutions at 10 passes. These results, shown in Figure 8, are likely caused by the large weight gains achieved when grafting to CA.

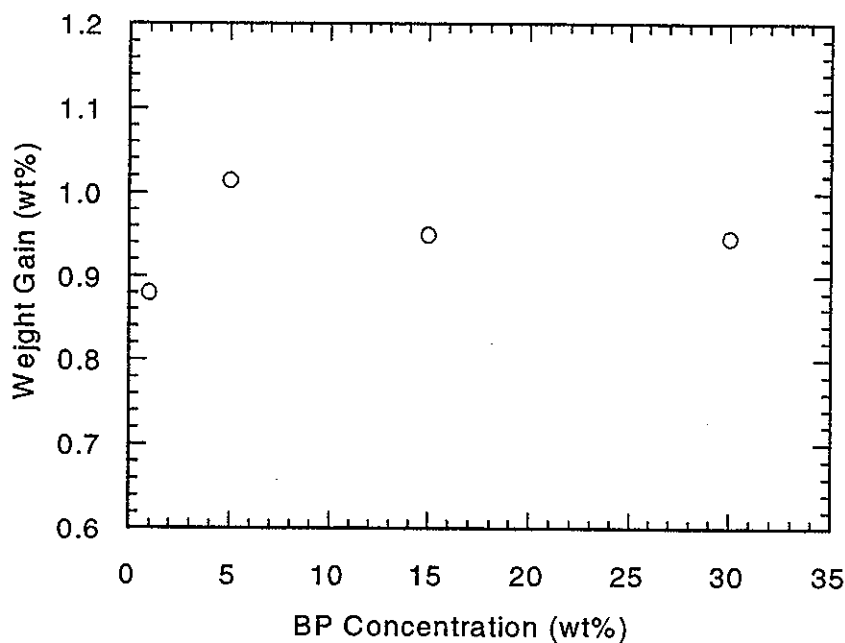
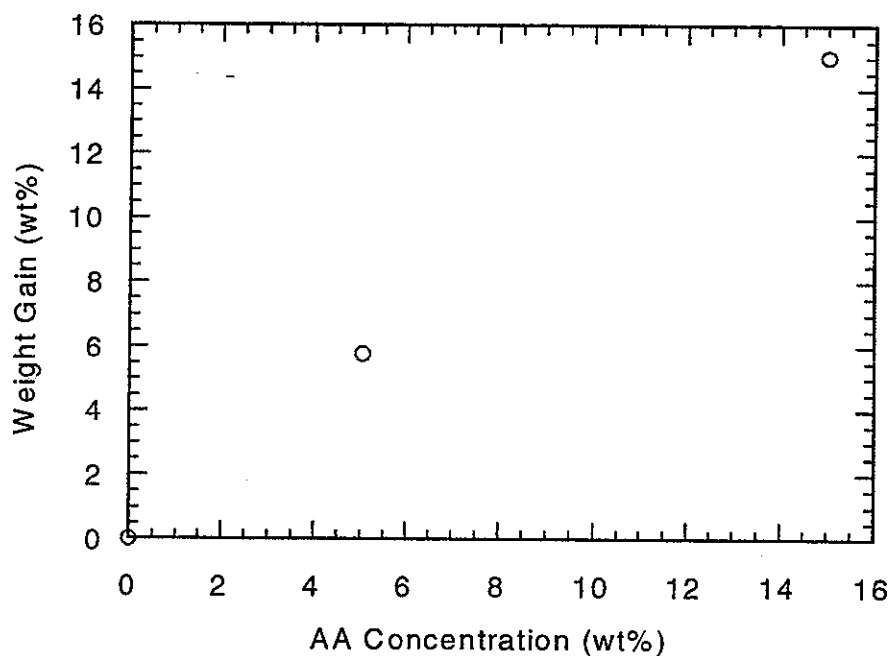


Figure 7. Amount of surface initiator vs. BP concentration. Average weight of CA membrane, 0.08 g. Irradiation time 10.6 seconds (8 passes).



**Figure 8.** Weight gain as a function of AA concentration for graft polymerization on CA membranes. The amount of surface initiator formed in the first step was  $0.27 \pm 0.04$  wt% and the UV irradiation time was 13 seconds.

For the polyvinylidene fluoride (PVDF) membranes, BP concentrations of 1–30 wt% in benzene and irradiation time of 20 passes were used in the surface initiator formation step. However, the weight change of modified PVDF was not large, and the second step was not performed.

For comparison, the results for all three membranes are presented in Table 3.

**Table 3. Properties of Polymeric Membranes in Two-step Graft Polymerization**

| Substrates | Chemical Structure   | Surface Initiator formation |                 | Monomer Graft Polymerization |                |
|------------|--|-----------------------------|-----------------|------------------------------|----------------|
|            |  | Irradiation Time (s)        | Wt% Gain*       | Irradiation Time (s)         | Wt% Gain*      |
| CA         | $\left[ \begin{array}{c} \text{---} \text{---} \text{---} \\   \\ \text{CH}_2\text{OOCCH}_3 \end{array} \right]_n$ * | 11                          | $1.01 \pm 0.14$ | 13                           | $15.0 \pm 0.2$ |
| PP         | $\text{---}(\text{CH}_2\text{CH})_n\text{---}$ $ $ $\text{CH}_3$   | 13                          | $0.16 \pm 0.02$ | 13                           | $7.3 \pm 0.5$  |
| PVDF       | $\text{---}(\text{CH}_2\text{CF}_2)_n\text{---}$   | 106                         | $0.08 \pm 0.05$ | n/a                          | n/a            |

\* Weight percent gain plus and minus one standard deviation for three repeats. BP solution was 5 wt% BP in benzene in the first step for all the membranes. In the second step, the monomer solution was 15 wt% AA in ethanol for all the membranes, and the amounts of grafted BP were 0.30 wt% and 0.27 wt% for PP and CA, respectively.

In the surface initiator formation (1<sup>st</sup> step), cellulose acetate (CA) has the highest reactivity due to the activating effect of the adjacent O atoms. Polypropylene contains a large number of tertiary hydrogen atoms which are easily abstracted by BP, and it has, therefore, a higher reactivity than that of poly(vinylidene fluoride) (PVDF) but a lower reactivity than that of CA. In the graft polymerization (2<sup>nd</sup> step), the carbon-carbon bond of the surface initiator in CA is more easily cleaved to form surface radicals and semipinacol radicals due to the activating effect of adjacent O atoms and so CA shows higher reactivity than does PP.

### 3.2 Membrane Performance

Figure 9 shows the pure buffer flux, plus and minus one standard deviation, for unmodified PP membranes, commercial CA membranes, and modified PP membranes with different amounts of grafted PEG200MA. The higher buffer flux for CA membranes ( $3100 \pm 200 \text{ L/m}^2 \text{ h}$ ) than that for the unmodified PP membranes ( $1100 \pm 100 \text{ L/m}^2 \text{ h}$ ) reflects the difference in membrane morphologies. The buffer flux is nearly the same for unmodified and modified PP membranes, which suggests that the bulk structure of PP membranes was not greatly altered by the surface modification process in the weight gain range (2-10 wt%) used in the experiments. However, there is a small but statistically significant (at the 95% confidence level) increase in the buffer flux at small weight gains (2-5%), suggesting that making the membrane surface hydrophilic improves wetting and helps eliminate microbubbles which inhibit flow. The buffer flux declines slightly at larger weight gains, most likely due to partial blockage of the membrane pores by the grafted polymer. The average buffer flux for the PP membranes modified with AA (7 repeats; weight gain  $4 \pm 0.2 \text{ wt}\%$ ) and DMAEMA (8 repeats; weight gain  $4 \pm 1 \text{ wt}\%$ ) are, respectively,  $1130 \pm 100 \text{ L/m}^2 \text{ h}$  and  $1200 \pm 120 \text{ L/m}^2 \text{ h}$ . These values are similar to those for unmodified PP and modified PP with PEG200MA.

Membranes were then tested in the crossflow filtration system without backpulsing using 0.14 g/L *E. coli* bacterial suspensions. As shown in Figure 10, the flux decreased quickly for all the membranes due to fouling. Although the flux for the CA membrane is initially more than twice that for the unmodified and modified PP membranes, it drops the most rapidly and becomes comparable to that of the other membranes within 1-2 minutes. For all membranes, the long-term flux after 60 min without backpulsing is only approximately  $70 \text{ L/m}^2 \text{ h}$ . It is expected that the fouling is primarily due to physical deposition of the bacterial cells on the membrane surfaces, which is not strongly dependent on the membrane surface chemistry. For the unmodified PP membrane, the recovered flux after backwashing is seven times greater than long-term flux after one hour of filtration. For the modified PP membrane and the commercial CA membrane, the recovered fluxes are 10 times greater than long-term flux. These results indicate the potential for the membranes to be cleaned *in situ* using backpulsing.

Backpulsing experiments were then conducted at different backward and forward filtration durations, using unmodified PP membranes and 0.14 g/L bacteria. The results in Figure 11 for a fixed forward filtration duration of 4 sec show that the average net flux is maximized at a backpulse duration of approximately 0.15-0.20 sec. Longer backpulse durations are undesired due to unnecessary permeate loss, whereas shorter backpulse durations are undesired because the backpulse may be too short to effectively remove the foulants (Mores et al., 1999). The maximum average net flux with backpulsing in Figure 11 is about two-fold greater than that without backpulsing.

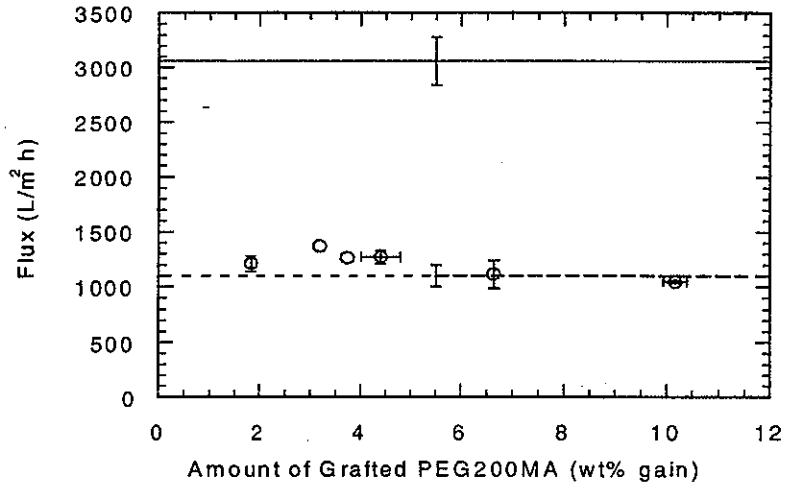


Figure 9. Pure buffer flux at 5 psi versus the amount of grafted PEG200MA. The symbols are the pure buffer flux for PP membranes modified with PEG200MA (3-6 repeats). The dashed and solid lines show the pure buffer flux for the unmodified PP membrane (26 repeats) and CA membrane (7 repeats), respectively. The error bars represent plus and minus one standard deviation.

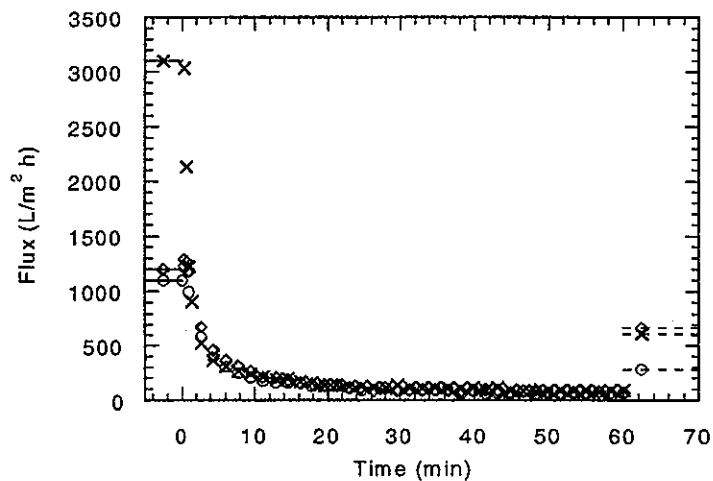


Figure 10. Permeate flux versus filtration time of 0.14 g/L *E. coli* without backpulsing at a forward transmembrane pressure of 5 psi: (o) unmodified PP membranes (∅) PP membranes modified with 5 wt% weight gain of PEG200MA, and (x) commercial CA membranes. Also shown are the pure buffer fluxes for 5 minutes before filtration (solid lines) and 5 minutes after filtration and backwashing (dashed lines).

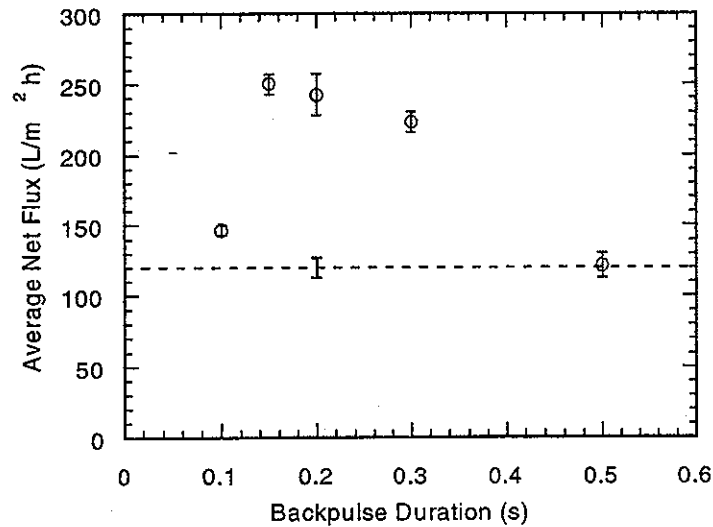


Figure 11. Average net flux (symbols) versus backpulse duration for crossflow filtration of 0.14 g/L *E. coli* at a forward filtration time of 4 seconds between backpulses, with forward transmembrane pressure of 5 psi and backward transmembrane pressure of 3 psi. The dashed line is the corresponding result without backpulsing. The error bars represent plus and minus one standard deviation for two or three repeats.

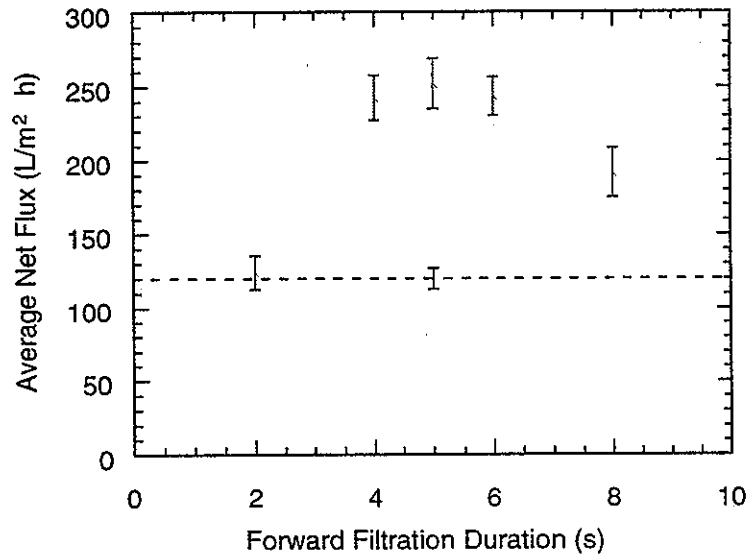
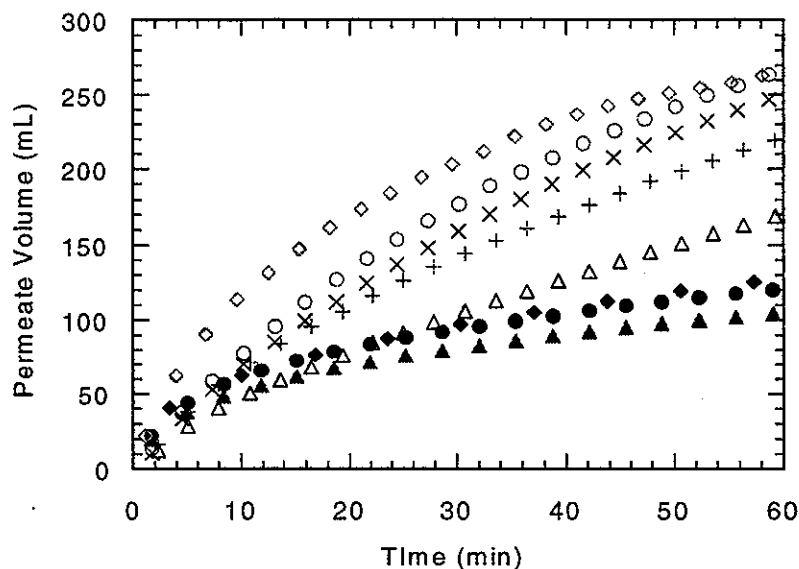


Figure 12. Average net flux (symbols) versus forward filtration duration for crossflow filtration of 0.14 g/L *E. coli* at a fixed backpulse duration of 0.2 seconds, with forward transmembrane pressure of 5 psi and backward transmembrane pressure of 3 psi. The dashed line is the corresponding result without backpulsing. The error bars represent plus and minus one standard deviation for two or three repeats.

The effects of varying forward filtration duration on the average net flux are shown in Figure 12 for a fixed backpulse duration of 0.2 sec. There is an optimum backpulsing frequency of once every 4-6 sec to maximize the average net flux. As reported by Redkar and Davis (1995), higher backpulse frequencies cause more permeate loss relative to that collected during the short periods of forward filtration. For lower backpulse frequencies, on the other hand, the average net flux decreases due to cake formation or fouling during the relatively long period of forward filtration.

The combination of surface modification and backpulsing was then tested to determine its effectiveness in reducing membrane fouling. Figure 13 shows the permeate volume versus filtration time with and without backpulsing for an unmodified PP membrane, PP membranes modified with different monomers, and an unmodified CA membrane. As discussed previously, the performance without backpulsing is nearly independent of the membrane surface chemistry and morphology, as it is primarily controlled by the bacterial cake which is deposited on the membrane surface. A very different result is observed with backpulsing, however. For the unmodified PP membrane (which is hydrophobic and neutral), the total permeate volume after 60 min of filtration with backpulsing is 1.7 times that obtained without backpulsing. In contrast, the total mass of the permeate after 60 min of filtration with backpulsing using the PP membrane modified with PEG200MA (which is hydrophilic and neutral) is 2.6 times that obtained without modification and backpulsing. The higher flux enhancement obtained for the modified PP membrane demonstrates that the membrane fouling is reduced further by an effective combination of backpulsing and surface modification. These results suggest that the adhesive



**Figure 13.** Permeate volume versus filtration time for crossflow filtration of 0.14 g/L *E. coli*: (o), (x), (+) backpulsing results for PP membranes modified with weight gain of 4.4 wt% PEG200MA graft, 4.4 wt% AA graft, and 3.7 wt% DMAEMA graft, respectively; ( $\Delta$ ), ( $\blacktriangle$ ) unmodified PP membranes with and without backpulsing, respectively; ( $\bullet$ ) PP membrane modified with weight gain of 5.8 wt% PEG200MA and without backpulsing; ( $\diamond$ ), ( $\blacklozenge$ ) unmodified CA membranes with and without backpulsing, respectively. Backpulsing experiments were performed at backward transmembrane pressure of 3.0 psi for 0.2 seconds after every 4 seconds of forward filtration at a transmembrane pressure of 5.0 psi.



hydrophobic interactions are stronger than the hydrophilic ones (Marshall, 1985) between the bacteria and the membrane surfaces, so that the bacteria are more easily lifted off the modified membrane during each backpulse. The relatively high permeate collection for the CA membrane (which is hydrophilic and neutral) with backpulsing supports this observation.

Figure 13 also shows that the permeate collection for the PP membranes modified with AA (hydrophilic, negatively charged) and DMAEMA (hydrophilic, positively charged) is greater than that for the unmodified PP membrane (hydrophobic, neutral), but less than that for the PP membrane modified with PEG200MA (hydrophilic, neutral) and the unmodified CA membrane (hydrophilic, neutral). Since *E. coli* has both negatively and positively charged surface groups (Brock and Madigan, 1991), it is not surprising that the neutral hydrophilic membrane surfaces are the most effective in reducing *E. coli* fouling.

Table 4 shows the long-term flux without backpulsing, the long-term net flux with backpulsing, and the recovered flux after backwashing for unmodified PP membranes, PP membranes modified with different monomers, and commercial CA membranes. The long-term flux values without backpulsing are nearly the same for all the membranes, indicating that physical deposition of bacteria on the membrane is the dominant fouling mechanism and that the membrane surface chemistry is then of less importance. On the other hand, the recovered fluxes for the modified PP membranes and the CA membrane are higher than that for the unmodified PP membrane, providing further evidence that the adhesive interactions of the bacteria with the hydrophilic membrane surfaces are weaker than those with a hydrophobic surface.

**Table 4. Effect of membrane surface chemistry on long-term flux and recovered flux after backwashing, with and without backpulsing. Shown are the average plus and minus one standard deviation for 2-6 repeats.**

| Membrane              | Without Backpulsing                 |                                     | With Backpulsing                        |                                     |
|-----------------------|-------------------------------------|-------------------------------------|---|-------------------------------------|
|                       | Long-term Flux (L/m <sup>2</sup> h) | Recovered Flux (L/m <sup>2</sup> h) | Long-term Net Flux (L/m <sup>2</sup> h) | Recovered Flux (L/m <sup>2</sup> h) |
| Unmodified PP         | 64 ± 5                              | 280 ± 50                            | 130 ± 20                                | 210 ± 10                            |
| Unmodified CA         | 77 ± 5                              | 610 ± 70                            | 160 ± 10                                | 400 ± 40                            |
| PP + 5.0 wt% PEG200MA | 67 ± 4                              | 670 ± 40                            | 150 ± 20                                | 380 ± 20                            |
| PP + 4.4 wt% AA       | 64 ± 5                              | 610 ± 50                            | 140 ± 10                                | 320 ± 10                            |
| PP + 3.7 wt% DMAEMA   | 66 ± 5                              | 620 ± 70                            | 130 ± 10                                | 310 ± 30                            |

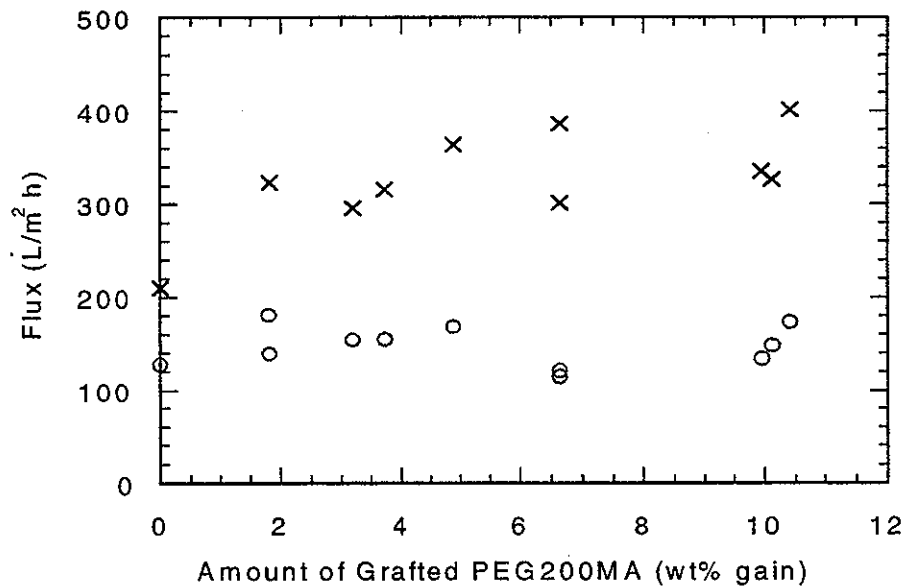
The long-term net flux values with backpulsing in all cases are about twice those without backpulsing. However, the increase in the long-term fluxes with surface modification is relatively small. Apparently, surface modification in combination with backpulsing is most effective for short filtration times (see Figure 13) when the membrane surfaces are relatively clean, but by one hour the membranes are sufficiently fouled that the resulting long-term flux is controlled more by the foulant deposition than by the clean membrane surface properties. Nevertheless, the foulant is most easily removed by backpulsing from the neutral hydrophilic surfaces, leading to higher recovered fluxes than for the hydrophobic unmodified PP membrane or for the modified membranes with negative (AA) and positive (DMAEMA) charges.

Another result shown in Table 4 is that the recovered fluxes for the PP membranes fouled without backpulsing are greater than those with backpulsing. The fouling without backpulsing is expected to be primarily in the form of a cake layer of rejected *E. coli* cells. The cake layer on the membrane surface may then play the role of a secondary membrane to capture smaller particles, such as extracellular proteins and broken cells, and prevent them from blocking the membrane pores (Kuberkar et al., 1998). For filtration with backpulsing, however, the

backpulsing lifts a portion of the deposit off the membrane with high frequency. After each backpulse, with the cake removed from parts of the membrane surface, the small particles may then enter the membrane pores and cause internal fouling which may not be subsequently removed by backwashing.

The effects of the amount of grafted PEG200MA on the permeate fluxes were also examined. As shown in Figure 14, the long-term flux and the recovered flux for modified PP membranes do not change significantly with the amount of grafted PEG200MA in the weight gain range of 1.8 –10 wt%. Apparently, the increased hydrophilicity of the membrane with increased graft is offset by slight pore constriction from the grafted polymer.

Finally, different concentrations of *E. coli* were used in the backpulsing experiments for both unmodified and modified PP membranes, and the results are summarized in Table 5. The average net flux, long-term net flux with backpulsing, and the recovered flux after backwashing decreased with increasing *E. coli* concentration, as expected (Parnham and Davis, 1995; Kuberkar et al., 1998). The enhancement of the net flux due to the surface modification is most significant at low concentrations of foulant. At higher concentrations, a thicker cake layer forms and so the membrane surface chemistry is less important. However, the recovered flux is always higher for the modified membranes, indicating that backpulsing is able to lift the deposit more easily off the hydrophilic membrane than off the hydrophobic membrane.



**Figure 14.** Long-term net flux with backpulsing (o) and recovered flux after backwashing (x) versus the amount of grafted PEG200MA for crossflow filtration of 0.14 g/L *E. coli*. These experiments were performed at a backward transmembrane pressure of 3.0 psi for 0.2 seconds after every 4 second of forward filtration at a transmembrane pressure of 5.0 psi.

**Table 5. Effects of *E. coli* concentration on the average net flux with backpulsing, long-term net flux with backpulsing and recovered flux after backwashing for unmodified PP membranes and modified PP membranes with a weight gain of 3.5 wt% PEG200MA. Shown are the averages plus and minus one standard deviation for 2-4 repeats.**

| <i>E. coli</i><br>(g/L) | Average Net Flux<br>(L/m <sup>2</sup> h) |          | Long-term Net Flux<br>(L/m <sup>2</sup> h) |          | Recovered Flux (L/m <sup>2</sup> h) |          |
|-------------------------|--|----------|--|----------|-------------------------------------|----------|
|                         | PP                                       | PP + PEG | PP   | PP + PEG | PP                                  | PP + PEG |
| 0.05                    | 270 ± 20                                 | 440 ± 40 | 160 ± 10                                   | 280 ± 30 | 310 ± 30                            | 480 ± 60 |
| 0.14                    | 240 ± 15                                 | 330 ± 15 | 130 ± 20                                   | 150 ± 20 | 210 ± 10                            | 380 ± 20 |
| 0.62                    | 90 ± 10                                  | 120 ± 10 | 70 ± 10                                    | 70 ± 10  | 170 ± 10                            | 310 ± 30 |

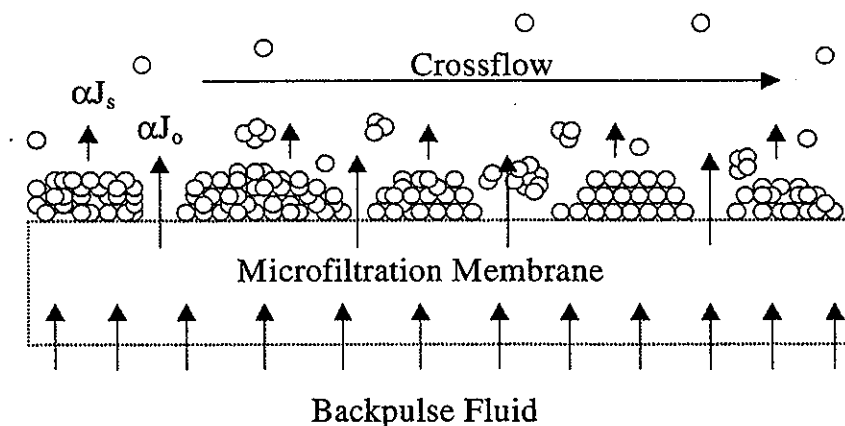
### 3.3 Fundamental Analysis of Membrane Fouling

To obtain a more fundamental understanding of backpulsing and membrane-foulant interactions, experiments were completed to examine how the reverse flow during each backpulse is able to remove the nonadhesive foulants from the membrane surface. In the first type of experiment, bacteria were deposited on commercial cellulose-acetate membranes, and then a single backpulse of a specified strength and duration was imposed. The flux recovery was then measured to determine how much of the foulant was removed. It was found that the fractional flux recovery increased with backpulse duration and strength and then saturated at a maximum value. The fraction  $\beta$  of the foulant cake removed versus time during a backpulse is well-described by a single exponential rise:

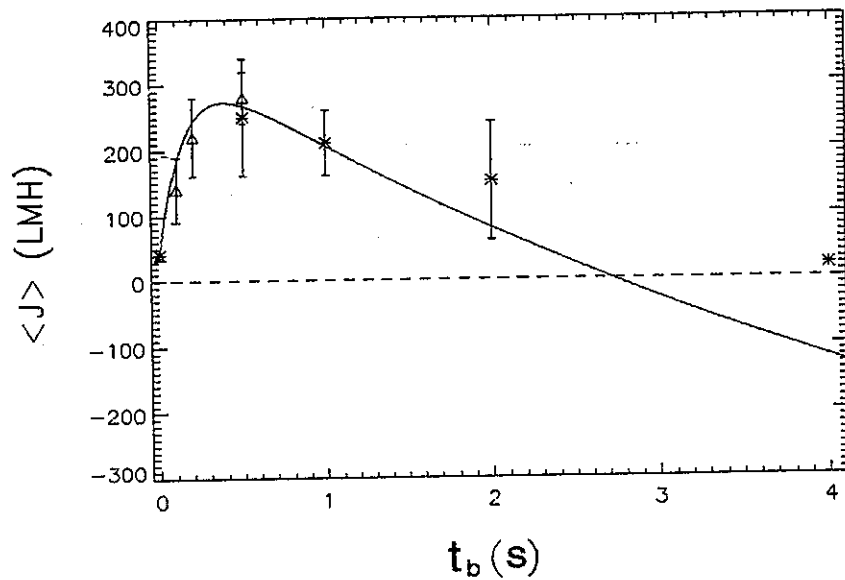
$$\beta(t) = \beta_{\max} (1 - e^{-t/\tau_b}), \quad (15)$$

where  $\beta_{\max}$  is the nonadhesive foulant fraction and  $\tau_b$  is the time constant for cake removal during reverse filtration. A model was then developed for the cyclic process of forward and reverse filtration and shown to provide good agreement with the net flux for rapid backpulsing experiments and to predict the optimal backpulse duration and frequency (Mores et al., 1999).

Figure 15 below shows a schematic of the partial membrane cleaning during a backpulse, and Figure 16 shows the model prediction and experimental verification of an optimum duration



**Figure 15: Schematic of partial cake removal by backpulsing;  $J_o$  is the clean membrane flux,  $J_s$  is the fouled membrane flux, and  $\alpha$  is the ratio of transmembrane pressures during backpulse and forward filtration.**



**Figure 16:** Experimental data and model prediction of the net flux versus the duration of each backpulse for crossflow microfiltration of 1.0 g/L *E. coli* bacteria using 0.2  $\mu\text{m}$  cellulose-acetate membranes and a forward filtration period of 10 s between each backpulse.

whereas too much fluid is lost from the permeate side to the feed side if the backpulses are too long. Only 19% of the bacterial fouling was found to be reversible.

Experiments on commercial cellulose-acetate membranes were also completed with complex mixtures containing multiple foulants which led to simultaneous internal fouling (pore plugging) and external fouling (cake formation). Using yeast cells and protein as a model mixture, microfiltration was performed using both deadend and crossflow filtration devices (Güell et al., 1999; Kuberkar and Davis, 1999a). In both cases, the internal fouling by protein aggregates was reduced by the formation of the external fouling layer. A model of simultaneous internal and external fouling was developed, with the external cake layer of large particles serving as a dynamic secondary membrane or deep-bed filter that captures the smaller particles which would otherwise foul the pores of the primary membrane (Kuberkar and Davis, 1999b).

### 3.4 Economic Analysis and Comparisons

The economic analysis is adapted from the work of Ramirez and Davis (1998) for the removal of fine particles and microorganisms from wastewater. The total costs include both capital and operating costs.

The annualized capital costs per unit treated volume are calculated from an expression developed by (Wiesner et al., 1994):

$$cc = \left( C_{\text{mod}} N_{\text{mod}} + \$1.50 \times 10^5 N_{\text{mod}}^{0.74} \right) (AF / Q) \quad , \quad (16)$$

where  $AF = 0.10 \text{ year}^{-1}$  is the amortization factor,  $Q$  is the volumetric treatment rate,  $N_{\text{mod}}$  is the number of modules required, and  $C_{\text{mod}} = \$14,600$  is the cost of a single membrane module. The first term in the numerator is the membrane-related cost (housing and initial membranes), and the second term is the nonmembrane cost (pumps, valves, piping, etc.).

The primary operating costs include power (for pumping feed, recycling retentate, and backpulsing), membrane replacement, maintenance, and labor. These costs were determined from Pickering and Wiesner (1993) and Peters and Timmerhaus (1991).

Both capital and operating costs depend strongly on the number of membrane modules, which is directly related to the amount of membrane surface area required. The latter is given by

$$A = Q / \langle J \rangle \quad , \quad (17)$$

where  $\langle J \rangle$  is the average net permeate flux. Figure 17 shows the total cost of membrane-treated water versus the net membrane flux for small ( $Q = 0.5$  million gallons per day, MGD) and large ( $Q = 10$  MGD) treatment facilities. When the net flux is less than approximately  $200 \text{ L/m}^2\text{-h}$ , the cost becomes noncompetitive with conventional treatment, for which the total cost is approximately  $\$0.8/\text{m}^3$  for a 0.5 MGD facility (Owen et al., 1995). When the net flux is increased, the total costs decrease due to the reduced amount of membranes required. The total costs for systems employing backpulsing and membrane surface modification will be lower because of the higher net flux achieved. The additional capital costs to implement backpulsing are small, since normal installations have the necessary pumps and piping for reverse flow for cleaning purposes. Also, modified membranes are expected to have similar or lower price per area as compared to current commercial membranes, because inexpensive base membrane materials such as polypropylene may be used.

From Tables 4 and 5, the long-term flux for bacteria in our studies varies from about  $70 \text{ L/m}^2\text{-h}$  without backpulsing to as much as  $280 \text{ L/m}^2\text{-h}$  with surface modification and backpulsing. The greatest improvement occurs for dilute suspensions which are typical of wastewater. Table 6 shows the approximate flux values and associated cost for a 0.5 MGD membrane facility using  $0.05 \text{ g/L E. coli}$  as the foulant. Compared to the estimated cost of  $\$0.8/\text{m}^3$  for conventional treatment, the modified membrane with backpulsing saves approximately  $\$0.25/\text{m}^3$  ( $\$1/1000$  gallons). Higher net fluxes may be obtained by optimizing the transmembrane pressure, since increasing transmembrane pressure increases the driving force for both filtration and fouling. The commercial cellulose acetate membrane performs almost the same as the modified polypropylene membrane, but the latter is expected to have lower raw materials costs.

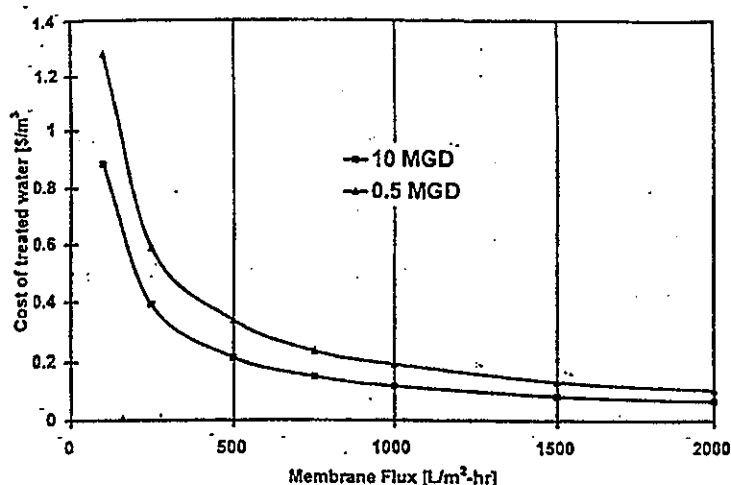


Figure 17. Total cost of treated water as a function of the average net permeate flux for 0.5 MGD and 10 MGD membrane treatment facilities.

**Table 6. Long-term net flux and treatment cost for removal of 0.05 g/L bacteria from water by crossflow membrane microfiltration using unmodified and modified polypropylene membranes with and without backpulsing. PEG200MA with 3.5 wt% gain was used for the membrane surface modification.**

|                               | Flux (L/m <sup>2</sup> -h) | Cost (\$/m <sup>3</sup> ) |
|-------------------------------|----------------------------|---------------------------|
| Unmodified PP w/o Backpulsing | 100                        | 1.25                      |
| Unmodified PP w/Backpulsing   | 160                        | 0.95                      |
| Modified PP w/Backpulsing     | 280                        | 0.55                      |

#### **4 CONCLUSIONS**

The combination of backpulsing and surface modification provides an effective method for reducing membrane fouling. A novel sequential photografting technique was developed for membrane surface modification. Desired membrane surface characteristics such as hydrophilicity and varied ionic charges were obtained by grafting different monomers to polypropylene base membranes using the novel grafting method. The experiments demonstrated that other membranes can also be modified using the novel grafting method with different monomers. For filtering 0.14 g/L *E. coli* using polypropylene membranes, 1.7-fold and 2.6-fold enhancements in the permeate volume collected over one hour were obtained using backpulsing alone and a combination of backpulsing and surface modification, respectively.

## REFERENCE LIST

- Al-Malack, M.H., and G.K. Anderson, Coagulation-crossflow Microfiltration of Domestic Wastewater, *J. Mem. Sci.* **121** (1996) 59-70.
- Bowen, W.R., and H.A. Sabuni, Pulsed Electrochemical Cleaning of Cellulose Nitrate Microfiltration Membrane, *Ind. Eng. Chem. Res.* **31** (1992) 515-523.
- Brock, T.D. and M.T. Madigan, *Biology of Microorganisms*, 6<sup>th</sup> Prentice Hall, Inc., New Jersey, 1991.
- Cabassud, C., S. Laborie, and J.M. Laine, How Slug Flow Can Enhance the Ultrafiltration Flux in Organic Hollow Fibres, *J. Mem. Sci.* **128** (1997) 93-101.
- Chung, K.Y., R. Bates, and G. Belfort, Dean Vortices with Wall Flux in a Curved Channel Membrane System, *J. Mem. Sci.* **81** (1993) 139-150.
- Donaldson, J.R. and R.B. Schnabel, *Technometrics* **29** (1987) 67.
- Güell, C., P. Czekaj, and R.H. Davis, Microfiltration of Protein Mixtures and the Effects of Yeast on Membrane Fouling, *J. Mem. Sci.* **155** (1999) 113-122.
- Hvid, K.B., P.S. Nielsen, and F.F. Stengaard, Preparation and Characterization of a New Ultrafiltration Membrane, *J. Mem. Sci.* **53** (1990) 189-202.
- Jonsson, A., and B. Jonsson, The Influence of Nonionic Surfactants on Hydrophobic and Ultrafiltration Membranes, *J. Mem. Sci.* **56** (1991) 49-76.
- Keszler, B., G. Kovacs, A. Toth, I. Bertoti, and M. Hegyi, Modified Polyethersulfone Membranes, *J. Mem. Sci.* **62** (1991) 201-210.
- Kim, K.J., A.G. Fane, and C.J.D. Fell, The Effect of Langmuir-Blodgett Layer Pretreatment on the Performance of Ultrafiltration Membranes, *J. Mem. Sci.* **43** (1989) 187-204.
- Kim, K.J., A.G. Fane, and C.J.D. Fell, The Performance of Ultrafiltration Membranes Pretreated by Polymers, *Desalination* **70** (1988) 229-249.
- Kim, M., K. Saito, and S. Furusaki, Water Flux and Protein Adsorption of a Hollow Fiber Modified with Hydroxyl Groups, *J. Mem. Sci.* **56** (1991) 289-302.
- Kroner, K.H., H. Schutte, H. Hustedt, and M.R. Kula, Cross-flow Filtration in the Downstream Processing of Enzymes, *Proc. Biochem.* **19** (1984) (4) 67-74.
- Kuberkar, V., P. Czekaj, and R.H. Davis, Flux Enhancement for Membrane Filtration of Bacterial Suspensions Using High-frequency Backpulsing, *Biotech. Bioeng.* **60** (1998) 77-87.
- Kuberkar, V.T. and R.H. Davis, Modeling of Fouling Reduction by Secondary Membranes, *J. Mem. Sci.* (1999b, in press).
- Kuberkar, V.T. and R.H. Davis, Effects of Added Yeast on Protein Transmission and Flux in Crossflow Membrane Microfiltration, *Biotech. Prog.* **15** (1999a) 472-479.
- Kuruzovich, J.N., and P.R. Piergiovanni, Yeast Cell Microfiltration: Optimization of Backwashing for Delicate Membranes, *J. Mem. Sci.* **112** (1996) 241-247.
- Li, Y., J.M. Desimone, C.D. Poon, and E. Samulski, *J. Appl. Polym. Sci.* **64** (1997) 883.
- Ma, H., R.H. Davis, and C.N. Bowman, A Novel Sequential Photoinduced Living Graft Polymerization, *Macromolecules*, in press (1999).

- Marshall, K.C., *Bacterial Adhesion: Mechanism and Physiological Significance: Mechanisms of Bacterial Adhesion at Solid-Water Interfaces*, Editors: D.C. Savage and M. Fletcher, Plenum Press, New York, 1985.
- Matsumoto, K., S. Katsuyama, and H. Ohya, Cross-flow Filtration of Yeast by Microporous Ceramic Membrane with Backpulsing, *J. Ferment. Technol.* **66** (1988) 199-205.
- Matsumoto, K., S. Katsuyama, and H. Ohya, Separation of Yeast by Cross-flow Filtration with Backpulsing, *J. Ferment. Technol.* **65** (1987) 77-83.
- Mores, W.D., C.N. Bowman, and R.H. Davis, Theoretical and Experimental Flux Maximization by Optimization of Backpulsing, *J. Mem. Sci.* in press (1999).
- Nakanishi, K., and H.G. Kessler, Stability and Rinsing Behavior of Deposited Layers, *J. Food Sci.* **50** (1985) 1726.
- Nikolov, N.D., V. Mavrov, and J.D. Nikolova, Ultrafiltration in a Tubular Membrane under Simultaneous Action of Pulsating Pressures in Permeate and Feed Solution, *J. Mem. Sci.* **83** (1993) 167-172.
- Nipkow, A., J.G. Zeikus, and P. Gerhardt, Microfiltration Cell-recycle Pilot System for Continuous Thermoanaerobic Production of Exo- $\alpha$ -amylase, *Biotech. Bioeng.* **34** (1989) 1075-1084.
- Nystrom, M., and P. Jarvinen, Modification of Polysulfone Ultrafiltration Membranes with UV Irradiation and Hydrophilicity Increasing Agents, *J. Mem. Sci.* **60** (1991) 275-296.
- Owen, G., M. Bandi, J.A. Howell, and S.J. Churchouse, Economic Assessment of Membrane Processes for Water and Wastewater Treatment, *J. Mem. Sci.* **102** (1995) 77.
- Parnham, C.S., and R.H. Davis, Protein Recovery from Bacterial Cell Debris Using Crossflow Microfiltration with Backpulsing, *J. Mem. Sci.* **118** (1996) 259-268.
- Parnham, C.S., and R.H. Davis, Protein Recovery from Cell Debris Using Rotary and Tangential Crossflow Microfiltration, *Biotech. Bioeng.* **47** (1995) 155-164.
- Parvatiyar, M.G., Interaction of Dispersed Phase with Concentration Polarization, *J. Mem. Sci.* **115** (1996) 121-127.
- Peters, M.S. and K.D. Timmerhaus, *Plant Design and Economics for Chemical Engineers*, 4<sup>th</sup> ed., McGraw-Hill, New York, 1991, p. 198.
- Pickering, K.D. and M.R. Wiesner, Cost Model for Low-pressure Membrane Filtration, *J. Environ. Eng.* **199** (1993) 772.
- Press, W.H., S.A. Teukdsky, W.T. Vetterling, and B.P. Plannery, in *Numerical Recipes in C*, 2<sup>nd</sup> ed., Cambridge University Press: Cambridge, 1992.
- Ramirez, J.A. and R.H. Davis, Application of Cross-Flow Microfiltration with Rapid Backpulsing to Wastewater Treatment, *J. Haz. Mat.* **63** (1998) 179-197.
- Ranby, B., Z.M. Gao, and P.Y. Zhang, *Polym. Prep. Am. Chem. Soc.* **27** (1988) 38.
- Redkar, S.G., and R.H. Davis, Cross-flow Microfiltration with High-frequency Reverse Filtration, *AIChE J.* **41** (1995) 501-508.
- Rodgers, V.G.J., and R.E. Sparks, Effects of Solution Properties on Polarization Redevelopment and Flux in Pressure Pulsed Ultrafiltration, *J. Mem. Sci.* **78** (1993) 163-180.
- Rodgers, V.G.J., and R.E. Sparks, Effects of Transmembrane Pressure Pulsing on Concentration Polarization, *J. Mem. Sci.* **68** (1992) 149-168.



- Rodgers, V.G.J., and R.E. Sparks, Reduction of Membrane Fouling in the Ultrafiltration of Binary Protein Mixtures, *AIChE J.* **37** (1991) 1517-1528.
- Sambrook, J., E.F. Fritsch, and T. Maniatis, *Molecular Cloning-A Laboratory Manual*, Second Edition Cold Spring Harbor Laboratory Press, 1989.
- Si-Hassen, D., A. Ould-Dris, M.Y. Jaffrin, and Y.K. Benkahla, Optimisation of an Intermittent Cross-flow Filtration Process of Mineral Suspensions, *J. Mem. Sci.* **118** (1996) 185-198.
- Stengaard, F.F., Characteristics and Performance of New Types of Ultrafiltration Membranes with Chemically Modified Surfaces, *Desalination* **70** (1988) 207-224.
- Su, S.K., J.C. Liu, and R.C. Wiley, Cross-flow Microfiltration with Gas Backwash of Apple Juice, *J. Food Sci.* **58** (1993) 639-641.
- Uchida, E., Y. Uyama, and Y. Ikada, *J. Appl. Polym. Sci.* **47** (1993) 417.
- Ulbricht, M., H. Matuschewski, A. Oechel, and H.G. Hicke, Photo-Induced Graft Polymerization Surface Modification for the Preparation of Hydrophilic and Low-protein-adsorbing Ultrafiltration Membranes, *J. Mem. Sci.* **115** (1996) 31-47.
- Uyama, Y. and Y. Ikada, *J. Appl. Polym. Sci.* **36** (1988), 1087.
- Walpole, R.E. and R.H. Myers, In *Probability and Statistics for Engineers and Scientists*, 3<sup>rd</sup> ed., Macmillan Publishing Co., Inc.: New York, 1985.
- Wenten, I.G., Mechanism and Control of Fouling in Crossflow Microfiltration, *Filt. Sep.* March issue (1995) 252-253.
- Wiesner, M.R., J. Hackey, S. Sandeep, J.G. Jacangelo, and J.M. Laine, Cost Estimates for Membrane Filtration and Conventional Treatment, *J. Am. Water Work Assoc.* **86** (1994) (12) 33-41.
- Wiesner, M.R., J. Hackney, S. Sethi, J.G. Jacangelo, and J.M. Laine, Cost Estimates for Membrane Filtration and Conventional Treatment, *J. A WAA* **85** (1994) 33.
- Yamagishi, H., J.V. Crivello, and G. Belfort, Development of a Novel Photochemical Technique for Modifying Poly(arylsulfone) Ultrafiltration Membranes, *J. Mem. Sci.* **105** (1995) 237-247.
- Yamagishi, H., J.V. Crivello, and G. Belfort, Evaluation of Ultrafiltration Membranes, *J. Mem. Sci.* **105** (1995) 249-259.
- Yan, W., P. Yang, and Y. Wang, UV-Radiation Grafting of Acrylamide onto Cellulose Acetate Reverse Osmosis Membrane, *Shuichuli Jishu* (in Chinese) **14** (1988) 213-222.
- Yang, W. and B. Ranby, *J. Appl. Polym. Sci.* **62** (1996) 533.
- Yang, W. and B. Ranby, *Macromolecules* **29** (1996) 3308.
- Young, J.S., W.F. Ramirez, and R.H. Davis, *Biotech. Bioeng.* **56** (1997) 214.
- Zahka, J., and T.J. Leary, Practical Aspects of Tangential Flow Filtration in Cell Separations, Purification of Fermentation Products, *ACS Symposium Series* **271** (1985) 51-69.
- Zeman, L.J., and A. Zydney, *Microfiltration and Ultrafiltration: Principles and Applications*, Marcel Dekker, Inc., New York, 1996.

## APPENDIX: DATA RECORD

**Data for Figure 3**

| Time | 0.5 wt% | 10 wt% | 30 wt% | 70 wt% |
|------|---------|--------|--------|--------|
| 0    | 0       | 0      | 0      | 0      |
| 13.3 | 3.1229  | 3.4179 | 2.9732 | 1.1966 |
| 26.6 | 3.6549  | 6.9269 |        | 2.847  |
| 39.9 | 5.07    | 10.212 | 7.4958 | 5.3451 |
| 53.2 | 8.1562  | 14.852 | 9.8726 | 4.5873 |

**Data for Figure 4**

| Time  | 5 wt%  | 15 wt% | 25 wt% |
|-------|--------|--------|--------|
| 0     | 0      | 0      | 0      |
| 5.32  | 7.9554 | 13.702 | 18.22  |
| 9.31  | 11.957 | 33.641 | 55.712 |
| 13.3  | 19.392 | 56.186 | 91.073 |
| 17.29 | 27.426 | 73.379 | 118.93 |

**Data for Figure 5**

| BP Conc. | Rate    |
|----------|---------|
| 0        | 0       |
| 0.02199  | 1.0289  |
| 0.22354  | 1.7097  |
| 0.45495  | 1.895   |
| 0.94771  | 1.5853  |
| 1.4551   | 1.3234  |
| 1.476    | 1.3234  |
| 2.6796   | 0.92052 |
| 3.534    | 0.73804 |
| 4.1086   | 0.72881 |

**Data for Figure 6**

| AA Conc. | Rate    |
|----------|---------|
| 0        | 0       |
| 0.55509  | 0.02138 |
| 1.6653   | 0.05780 |
| 2.7755   | 0.09351 |

**Data for Figure 7**

| BP Conc. | Wt Gain |
|----------|---------|
| 1        | 0.88002 |
| 5.03     | 1.0142  |
| 15.01    | 0.94939 |
| 30.05    | 0.94562 |

**Data for Figure 8**

| AA Conc. | Wt Gain |
|----------|---------|
| 0        | 0       |
| 5.05     | 5.77074 |
| 15       | 15.0245 |

**Data for Figure 9**

| Wt Gain | PEG    | Stdev | PP   | Stdev | CA     | Stdev |
|---------|--------|-------|------|-------|--------|-------|
| 3.19    | 1369.4 |       | 1100 |       | 3.59.2 |       |
| 3.73    | 1263.4 |       | 1100 | 100   | 3059.2 | 219.7 |
| 4.4     | 1271.2 | 61.3  | 1100 |       | 3059.2 |       |
| 10.17   | 1046   | 15.7  | 1100 |       |        |       |
| 1.82    | 1209.9 | 71.8  | 1100 |       |        |       |
| 6.64    | 1111.2 | 128.8 | 1100 |       |        |       |

**Data for Figure 10**

| Pure Buffer Flux |        |        |        |
|------------------|--------|--------|--------|
| Time             | PP     | PEG    | CA     |
| Baseline         | 1100   | 1200   | 3100   |
|                  |        |        |        |
| Fouled Flux      |        |        |        |
| Time             | PP     | PEG    | CA     |
| 0.34688          | 1222.3 | 1289.9 | 3034.9 |
| 0.68568          | 1094.7 | 1266.5 | 2132.3 |
| 1.0243           | 997.69 | 1184.6 | 1220.5 |
| 1.3604           | 949.9  | 1104   | 908.19 |
| 1.699            | 821.32 | 950.31 | 737.63 |
| 2.035            | 721.71 | 832.99 | 642.31 |
| 2.3737           | 650.21 | 747.61 | 568.61 |
| 2.7124           | 579.14 | 676.54 | 523.85 |
| 3.051            | 539.65 | 608.09 | 485.56 |
| 3.387            | 485.56 | 557.31 | 431.72 |
| 3.7257           | 434.35 | 515.96 | 421.88 |
| 4.0617           | 419.23 | 501.39 | 368.54 |
| 4.4003           | 392.31 | 458.22 | 361.77 |
| 4.7363           | 360.85 | 440.37 | 350.11 |
| 5.0742           | 329.82 | 408.97 | 329.01 |
| 5.4102           | 334.38 | 395.42 | 321.16 |
| 5.7488           | 308    | 363.27 | 297.18 |
| 6.0848           | 305.13 | 368.89 | 305.36 |
| 6.4235           | 281.67 | 350.11 | 289.21 |
| 6.7595           | 265.34 | 320.99 | 284.36 |
| 7.0982           | 273.77 | 310.63 | 260.61 |
| 7.4368           | 244.82 | 310.63 | 255.35 |
| 7.7755           | 242.18 | 313.26 | 265.33 |
| 8.1115           | 236.15 | 281.31 | 263.24 |
| 8.4502           | 231.65 | 281.67 | 236.15 |
| 8.7862           | 209.61 | 262.63 | 240.15 |
| 9.1249           | 229.02 | 257.98 | 228.19 |
| 9.46             | 207.48 | 262.73 | 239.55 |
| 9.7987           | 205.33 | 248.02 | 206.96 |
| 10.135           | 188.39 | 249.46 | 236.92 |

| Time   | PP     | PEG    | CA     |
|--------|--------|--------|--------|
| 10.473 | 205.33 | 236.92 | 212.27 |
| 10.809 | 188.39 | 241.41 | 207.96 |
| 11.148 | 179.01 | 202.7  | 212.27 |
| 11.487 | 176.37 | 233.54 | 207.96 |
| 11.825 | 186.94 | 215.05 | 189.54 |
| 12.161 | 156.55 | 209.57 | 205.33 |
| 12.5   | 184.27 | 209.66 | 188.39 |
| 12.836 | 161.85 | 205.33 | 186.94 |
| 13.175 | 155.31 | 193.66 | 204.31 |
| 13.511 | 169.81 | 202.7  | 184.7  |
| 13.849 | 166.26 | 191.08 | 167.16 |
| 14.185 | 145.93 | 184.27 | 179.04 |
| 14.523 | 155.31 | 183.05 | 196.35 |
| 14.859 | 159.2  | 184.34 | 168.48 |
| 15.198 | 134.25 | 185.7  | 175.12 |
| 15.534 | 156.55 | 166.23 | 163.21 |
| 15.873 | 136.89 | 188.42 | 186.9  |
| 16.211 | 157.95 | 157.95 | 168.48 |
| 16.55  | 134.25 | 183.12 | 156.55 |
| 16.886 | 137.98 | 163.21 | 152.68 |
| 17.225 | 128.99 | 161.82 | 159.2  |
| 17.561 | 140.63 | 127.3  | 165.85 |
| 17.899 | 128.99 | 143.28 | 156.54 |
| 18.235 | 138    | 134.25 | 168.9  |
| 18.573 | 131.92 | 137.98 | 145.94 |
| 18.909 | 111.44 | 134.26 | 151.32 |
| 19.248 | 139.55 | 138    | 163.12 |
| 19.584 | 124.7  | 137.2  | 135.4  |
| 19.922 | 118.46 | 140.63 | 160.49 |
| 20.258 | 130.01 | 134.28 | 137.98 |
| 20.597 | 118.46 | 111.44 | 155.34 |
| 20.936 | 102.66 | 134.26 | 139.52 |
| 21.274 | 128.99 | 137.98 | 139.52 |
| 21.61  | 114.09 | 110.56 | 137.97 |
| 21.946 | 111.44 | 134.25 | 136.89 |
| 22.285 | 113.19 | 110.56 | 135.32 |
| 22.621 | 92.867 | 132.67 | 147.42 |
| 22.96  | 115.83 | 115.83 | 127.36 |
| 23.296 | 108.79 | 122.05 | 137.23 |
| 23.634 | 110.84 | 128.99 | 135.32 |

| Time   | PP     | PEG    | CA     |
|--------|--------|--------|--------|
| 23.97  | 111.44 | 111.44 | 139.52 |
| 24.308 | 107.93 | 110.84 | 132.66 |
| 24.644 | 87.559 | 108.79 | 128.99 |
| 24.983 | 115.82 | 134.26 | 124.71 |
| 25.319 | 103.48 | 95.521 | 136.89 |
| 25.658 | 94.769 | 115.83 | 110.56 |
| 25.996 | 107.95 | 111.44 | 139.52 |
| 26.335 | 92.136 | 86.871 | 114.09 |
| 26.671 | 108.79 | 118.48 | 134.25 |
| 27.01  | 86.872 | 107.92 | 108.81 |
| 27.346 | 111.44 | 87.562 | 137.21 |
| 27.683 | 89.726 | 113.2  | 119.4  |
| 28.019 | 103.48 | 114.09 | 110.58 |
| 28.358 | 92.136 | 86.868 | 135.32 |
| 28.694 | 90.211 | 114.09 | 115.83 |
| 29.033 | 105.3  | 87.091 | 103.48 |
| 29.369 | 92.869 | 111.44 | 115.82 |
| 29.707 | 84.239 | 89.499 | 134.25 |
| 30.043 | 87.555 | 108.79 | 118.46 |
| 30.382 | 107.93 | 92.136 | 111.44 |
| 30.721 | 89.503 | 95.521 | 110.56 |
| 31.059 | 86.868 | 105.29 | 114.09 |
| 31.395 | 92.867 | 92.136 | 113.2  |
| 31.734 | 86.872 | 107.93 | 114.09 |
| 32.07  | 87.562 | 87.559 | 110.84 |
| 32.408 | 87.086 | 89.501 | 114.09 |
| 32.744 | 87.559 | 106.13 | 113.2  |
| 33.083 | 86.872 | 92.154 | 111.44 |
| 33.418 | 87.579 | 93.08  | 89.503 |
| 33.757 | 86.868 | 86.872 | 122.05 |
| 34.093 | 82.254 | 92.867 | 107.93 |
| 34.432 | 89.503 | 106.19 | 107.95 |
| 34.771 | 89.505 | 92.1   | 115.83 |
| 35.109 | 89.499 | 90.249 | 87.562 |
| 35.445 | 76.948 | 84.206 | 113.19 |
| 35.784 | 73.709 | 92.138 | 111.44 |
| 36.12  | 82.256 | 86.866 | 89.503 |
| 36.459 | 92.132 | 90.215 | 111.44 |
| 36.795 | 87.562 | 110.56 | 92.363 |
| 37.132 | 65.977 | 87.562 | 108.79 |

| Time   | PP     | PEG    | CA     |
|--------|--------|--------|--------|
| 37.468 | 84.903 | 94.764 | 105.3  |
| 37.807 | 92.136 | 87.562 | 100.83 |
| 38.143 | 61.028 | 79.172 | 107.93 |
| 38.482 | 89.503 | 92.863 | 90.213 |
| 38.818 | 82.25  | 92.138 | 97.402 |
| 39.156 | 65.812 | 82.254 | 100.03 |
| 39.495 | 89.505 | 71.076 | 92.134 |
| 39.834 | 84.251 | 90.215 | 114.09 |
| 40.17  | 68.988 | 89.499 | 89.503 |
| 40.508 | 84.239 | 81.608 | 90.215 |
| 40.844 | 66.334 | 97.415 | 110.58 |
| 41.183 | 86.87  | 82.256 | 90.213 |
| 41.519 | 66.331 | 92.136 | 87.073 |
| 41.857 | 87.091 | 92.867 | 111.44 |
| 42.193 | 63.68  | 57.915 | 89.523 |
| 42.532 | 84.235 | 92.863 | 87.562 |
| 42.868 | 63.682 | 87.091 | 90.249 |
| 43.206 | 65.812 | 87.562 | 113.15 |
| 43.542 | 87.559 | 86.866 | 90.213 |
| 43.881 | 63.178 | 68.988 | 84.239 |
| 44.22  | 81.606 | 81.606 | 89.505 |
| 44.558 | 68.445 | 87.562 | 89.499 |
| 44.894 | 63.68  | 65.809 | 90.215 |
| 45.233 | 84.235 | 94.769 | 92.136 |
| 45.569 | 68.988 | 89.503 | 84.908 |
| 45.905 | 63.68  | 68.988 | 113.48 |
| 46.243 | 63.335 | 86.868 | 92.867 |
| 46.579 | 79.649 | 84.908 | 84.239 |
| 46.917 | 71.034 | 68.445 | 82.256 |
| 47.253 | 66.334 | 84.924 | 94.764 |
| 47.592 | 68.455 | 89.706 | 84.908 |
| 47.928 | 61.028 | 66.347 | 78.973 |
| 48.267 | 65.812 | 92.136 | 79.602 |
| 48.603 | 63.68  | 63.67  | 89.516 |
| 48.941 | 68.445 | 89.499 | 84.239 |
| 49.28  | 63.176 | 61.04  | 92.138 |
| 49.619 | 57.915 | 92.136 | 87.555 |
| 49.955 | 66.334 | 65.809 | 86.872 |
| 50.293 | 63.176 | 92.136 | 90.215 |
| 50.629 | 68.988 | 63.668 | 89.724 |

| Time               | PP     | PEG    | CA     |
|--------------------|--------|--------|--------|
| 50.967             | 58.06  | 65.838 | 63.68  |
| 51.303             | 55.72  | 66.318 | 86.872 |
| 51.642             | 52.646 | 63.181 | 87.562 |
| 51.978             | 61.028 | 74.482 | 89.503 |
| 52.317             | 65.812 | 78.969 | 71.638 |
| 52.653             | 63.68  | 66.347 | 84.239 |
| 52.991             | 65.809 | 63.181 | 86.872 |
| 53.33              | 65.812 | 68.972 | 89.499 |
| 53.668             | 60.56  | 63.181 | 71.64  |
| 54.005             | 63.677 | 66.344 | 84.241 |
| 54.343             | 65.812 | 60.546 | 84.908 |
| 54.679             | 39.801 | 73.709 | 65.809 |
| 55.018             | 63.179 | 60.545 | 90.231 |
| 55.354             | 63.68  | 82.237 | 89.713 |
| 55.692             | 65.974 | 73.711 | 63.68  |
| 56.028             | 66.334 | 66.347 | 92.15  |
| 56.366             | 60.548 | 60.683 | 66.334 |
| 56.702             | 42.451 | 74.309 | 81.606 |
| 57.041             | 60.548 | 60.548 | 84.908 |
| 57.377             | 66.334 | 66.321 | 76.338 |
| 57.716             | 63.179 | 63.176 | 86.872 |
| 58.054             | 65.809 | 63.693 | 60.548 |
| 58.393             | 42.121 | 66.374 | 90.213 |
| 58.729             | 66.334 | 71.628 | 71.072 |
| 59.068             | 57.912 | 58.383 | 84.91  |
| 59.404             | 63.68  | 66.321 | 60.546 |
| 59.742             | 44.752 | 65.812 | 68.988 |
| 60.078             | 63.68  | 68.443 | 92.363 |
| 60.416             | 65.974 | 66.344 |        |
|                    |        |        |        |
| Recover<br>ed Flux |        |        |        |
| Time               | PP     | PEG    | CA     |
|                    | 280    | 670    | 610    |



**Data for Figure 11**

| Duration | Net flux | Stdev | Flux No BK |  | Stdev |
|----------|----------|-------|------------|--|-------|
| 0.1      | 146.6    | 3.2   |            |  |       |
| 0.15     | 250      | 7.1   |            |  |       |
| 0.2      | 242.5    | 15    | 120        |  | 7     |
| 0.3      | 223      | 7.3   |            |  |       |
| 0.5      | 121.5    | 8.9   |            |  |       |

**Data for Figure 12**

| Duration | Net Flux | Stdev | Flux No Bk |  | Stdev |
|----------|----------|-------|------------|--|-------|
| 2        | 124.1    | 11.4  |            |  |       |
| 4        | 242.5    | 15    |            |  |       |
| 5        | 252      | 16.9  | 120        |  | 7     |
| 6        | 243.5    | 13.2  |            |  |       |
| 8        | 191.6    | 16.3  |            |  |       |

**Data for Figure 13**

| Time    | PEG   | Time    | AA    | Time   | DMA   | Time   | PP    |
|---------|-------|---------|-------|--------|-------|--------|-------|
| 0.58503 | 0.44  | 0.58952 | 0.67  | 1.1553 | 4.65  | 1.1553 | 4.82  |
| 1.1544  | 6.96  | 1.1617  | 5.82  | 1.7265 | 10.47 | 1.7255 | 9.15  |
| 1.7238  | 13.28 | 1.7292  | 10.5  | 2.2969 | 16.18 | 2.2932 | 12.44 |
| 2.294   | 18.34 | 2.3005  | 15.22 | 2.8672 | 21.29 | 2.8617 | 16.2  |
| 2.8617  | 23.44 | 2.8707  | 20.01 | 3.4357 | 25.8  | 3.432  | 19.5  |
| 3.4328  | 29.16 | 3.4383  | 24.58 | 4.0061 | 30.45 | 3.9995 | 22.65 |
| 4.0032  | 33.04 | 4.0095  | 28.99 | 4.5762 | 34.64 | 4.5698 | 25.72 |
| 4.5707  | 37.65 | 4.5798  | 33.48 | 5.1439 | 37.93 | 5.141  | 28.41 |
| 5.142   | 42.4  | 5.1502  | 37.77 | 5.715  | 42.3  | 5.7113 | 31.16 |
| 5.7124  | 46.36 | 5.7187  | 41.81 | 6.2854 | 45.48 | 6.2789 | 33.62 |
| 6.2825  | 50.55 | 6.289   | 45.61 | 6.8529 | 49.04 | 6.8501 | 35.99 |
| 6.851   | 56.12 | 6.8592  | 49.28 | 7.4242 | 52.6  | 7.4206 | 38.25 |
| 7.4214  | 58.67 | 7.4268  | 53    | 7.9945 | 56.01 | 7.9898 | 40.38 |
| 7.9917  | 62.64 | 7.998   | 56.54 | 8.562  | 59.06 | 8.5591 | 42.54 |
| 8.5639  | 66.54 | 8.5684  | 60.02 | 9.1332 | 62.48 | 9.1296 | 44.55 |
| 9.1332  | 70.37 | 9.1359  | 63.4  | 9.7046 | 65.29 | 9.6971 | 46.47 |
| 9.7035  | 74.11 | 9.7072  | 66.74 | 10.274 | 68.21 | 10.268 | 48.45 |
| 10.274  | 77.79 | 10.278  | 69.94 | 10.846 | 71.2  | 10.839 | 50.33 |
| 10.842  | 81.49 | 10.848  | 73.27 | 11.415 | 73.62 | 11.409 | 52.22 |

| Time   | PEG    | Time   | AA     | Time   | DMA    | Time   | PP     |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 11.413 | 85.12  | 11.415 | 76.28  | 11.988 | 76.24  | 11.977 | 54.06  |
| 11.983 | 88.71  | 11.986 | 79.19  | 12.558 | 79.14  | 12.549 | 55.7   |
| 12.551 | 92.11  | 12.557 | 82.32  | 13.127 | 81.27  | 13.119 | 57.46  |
| 13.122 | 95.57  | 13.124 | 85.11  | 13.699 | 83.83  | 13.689 | 59.2   |
| 13.693 | 98.93  | 13.696 | 87.98  | 14.268 | 86.52  | 14.261 | 60.94  |
| 14.263 | 102.14 | 14.266 | 91.07  | 14.835 | 88.51  | 14.831 | 62.64  |
| 14.835 | 105.43 | 14.835 | 93.55  | 15.407 | 90.98  | 15.4   | 64.28  |
| 15.406 | 108.57 | 15.404 | 96.22  | 15.977 | 93.57  | 15.971 | 65.96  |
| 15.974 | 111.75 | 15.975 | 99.05  | 16.546 | 95.34  | 16.542 | 67.7   |
| 16.543 | 114.86 | 16.545 | 101.53 | 17.116 | 96.19  | 17.112 | 69.48  |
| 17.114 | 117.85 | 17.117 | 104.17 | 17.686 | 98.48  | 17.682 | 71.03  |
| 17.682 | 120.85 | 17.687 | 106.74 | 18.255 | 100.53 | 18.253 | 72.57  |
| 18.252 | 123.76 | 18.255 | 109.38 | 18.824 | 102.93 | 18.824 | 74.19  |
| 18.823 | 126.58 | 18.826 | 111.96 | 19.395 | 105.13 | 19.393 | 75.81  |
| 19.393 | 129.5  | 19.395 | 114.69 | 19.964 | 107.12 | 19.963 | 77.44  |
| 19.962 | 132.26 | 19.964 | 116.9  | 20.532 | 109.7  | 20.533 | 78.99  |
| 20.531 | 134.96 | 20.535 | 119.38 | 21.102 | 111.85 | 21.102 | 80.39  |
| 21.101 | 137.74 | 21.104 | 122.35 | 21.672 | 113.88 | 21.671 | 81.96  |
| 21.67  | 140.48 | 21.674 | 124.31 | 22.24  | 116    | 22.24  | 84.77  |
| 22.24  | 143.07 | 22.243 | 126.8  | 22.81  | 118.09 | 22.81  | 85.03  |
| 22.812 | 145.64 | 22.812 | 129.32 | 23.379 | 120.07 | 23.38  | 86.58  |
| 23.383 | 148.26 | 23.383 | 131.51 | 23.948 | 122.07 | 23.949 | 88.56  |
| 23.951 | 150.8  | 23.952 | 133.85 | 24.518 | 123.96 | 24.517 | 89.54  |
| 24.521 | 153.33 | 24.522 | 136.65 | 25.088 | 125.84 | 25.086 | 90.97  |
| 25.09  | 155.78 | 25.092 | 138.47 | 25.656 | 127.52 | 25.656 | 92.46  |
| 25.659 | 158.28 | 25.663 | 140.85 | 26.226 | 129.53 | 26.226 | 93.95  |
| 26.229 | 160.86 | 26.232 | 143.45 | 26.795 | 131.31 | 26.795 | 95.53  |
| 26.8   | 163.03 | 26.802 | 145.38 | 27.365 | 133.36 | 27.364 | 97.07  |
| 27.372 | 165.42 | 27.371 | 147.79 | 27.935 | 135.12 | 27.934 | 98.38  |
| 27.941 | 167.82 | 27.941 | 149.95 | 28.505 | 137.1  | 28.504 | 99.75  |
| 28.513 | 170.06 | 28.511 | 152.2  | 29.074 | 138.73 | 29.074 | 101.81 |
| 29.084 | 172.33 | 29.08  | 154.4  | 29.644 | 140.46 | 29.643 | 102.71 |
| 29.653 | 175.46 | 29.65  | 156.78 | 30.214 | 142.24 | 30.213 | 104.17 |
| 30.223 | 176.88 | 30.22  | 158.84 | 30.784 | 143.89 | 30.782 | 105.48 |
| 30.792 | 179.13 | 30.789 | 161.05 | 31.354 | 145.61 | 31.352 | 106.75 |
| 31.362 | 181.28 | 31.361 | 163.27 | 31.923 | 147.4  | 31.923 | 108.09 |
| 31.932 | 183.39 | 31.931 | 165.33 | 32.492 | 149    | 32.491 | 109.5  |
| 32.502 | 185.57 | 32.501 | 167.41 | 33.062 | 150.61 | 33.061 | 110.85 |
| 33.071 | 188.59 | 33.071 | 169.99 | 33.632 | 152.37 | 33.631 | 112.37 |
| 33.644 | 189.91 | 33.641 | 171.61 | 34.201 | 153.84 | 34.2   | 113.72 |

| Time   | PEG    | Time   | AA     | Time   | DMA    | Time   | PP     |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 34.214 | 191.85 | 34.208 | 173.7  | 34.773 | 155.62 | 34.771 | 114.97 |
| 34.784 | 194.43 | 34.78  | 175.93 | 35.342 | 157.33 | 35.342 | 116.45 |
| 35.355 | 196.01 | 35.349 | 177.72 | 35.91  | 158.91 | 35.912 | 118.55 |
| 35.923 | 197.96 | 35.919 | 179.85 | 36.48  | 160.56 | 36.482 | 118.97 |
| 36.493 | 200.26 | 36.49  | 182.43 | 37.05  | 162.18 | 37.053 | 120.42 |
| 37.064 | 201.95 | 37.061 | 183.85 | 37.62  | 163.8  | 37.624 | 121.72 |
| 37.634 | 203.97 | 37.629 | 185.79 | 38.189 | 165.4  | 38.193 | 123.13 |
| 38.206 | 205.88 | 38.2   | 188    | 38.759 | 166.9  | 38.762 | 124.45 |
| 38.776 | 207.76 | 38.77  | 189.75 | 39.329 | 168.3  | 39.333 | 125.74 |
| 39.345 | 209.7  | 39.339 | 191.64 | 39.898 | 169.85 | 39.903 | 126.97 |
| 39.915 | 211.58 | 39.908 | 194.18 | 40.468 | 171.37 | 40.474 | 128.39 |
| 40.485 | 213.46 | 40.479 | 195.55 | 41.039 | 172.99 | 41.044 | 129.67 |
| 41.058 | 215.21 | 41.049 | 197.34 | 41.608 | 174.48 | 41.612 | 130.98 |
| 41.628 | 217.18 | 41.621 | 199.06 | 42.178 | 176.02 | 42.183 | 132.26 |
| 42.198 | 219.06 | 42.19  | 200.86 | 42.748 | 177.63 | 42.753 | 133.59 |
| 42.77  | 220.65 | 42.76  | 202.48 | 43.317 | 179.28 | 43.323 | 134.78 |
| 43.341 | 222.45 | 43.33  | 204.29 | 43.887 | 180.78 | 43.895 | 136.21 |
| 43.91  | 224.16 | 43.899 | 206.01 | 44.456 | 182.45 | 44.466 | 137.35 |
| 44.48  | 225.74 | 44.468 | 207.65 | 45.026 | 184.08 | 45.036 | 138.62 |
| 45.05  | 227.42 | 45.039 | 209.25 | 45.597 | 185.49 | 45.607 | 139.94 |
| 45.618 | 229.03 | 45.608 | 210.85 | 46.164 | 186.82 | 46.179 | 141.19 |
| 46.188 | 230.69 | 46.177 | 212.62 | 46.735 | 188.48 | 46.748 | 142.47 |
| 46.758 | 232.28 | 46.747 | 214.23 | 47.307 | 190    | 47.319 | 143.65 |
| 47.328 | 234.01 | 47.317 | 215.99 | 47.875 | 191.49 | 47.89  | 144.94 |
| 47.897 | 235.48 | 47.888 | 217.61 | 48.446 | 193.07 | 48.46  | 146.48 |
| 48.465 | 237.14 | 48.458 | 219.23 | 49.017 | 194.49 | 49.03  | 147.47 |
| 49.034 | 238.7  | 49.026 | 220.91 | 49.587 | 195.9  | 49.601 | 148.71 |
| 49.603 | 240.3  | 49.598 | 222.42 | 50.155 | 197.47 | 50.168 | 149.98 |
| 50.172 | 241.89 | 50.168 | 224.22 | 50.727 | 198.7  | 50.739 | 151.03 |
| 50.743 | 243.48 | 50.74  | 225.67 | 51.297 | 199.52 | 51.31  | 152.4  |
| 51.312 | 244.9  | 51.311 | 227.3  | 51.865 | 201.17 | 51.88  | 154.06 |
| 51.882 | 246.63 | 51.88  | 228.86 | 52.437 | 202.41 | 52.452 | 154.83 |
| 52.452 | 248.02 | 52.448 | 230.42 | 53.007 | 204.05 | 53.021 | 156.05 |
| 53.021 | 249.46 | 53.018 | 231.92 | 53.574 | 205.53 | 53.593 | 157.23 |
| 53.591 | 250.9  | 53.589 | 233.38 | 54.143 | 206.91 | 54.163 | 158.5  |
| 54.161 | 252.34 | 54.159 | 234.94 | 54.713 | 208.33 | 54.734 | 159.64 |
| 54.729 | 253.8  | 54.729 | 236.42 | 55.281 | 209.66 | 55.305 | 160.7  |
| 55.3   | 255.23 | 55.299 | 237.9  | 55.851 | 211.02 | 55.875 | 161.85 |
| 55.869 | 256.59 | 55.869 | 239.38 | 56.423 | 212.5  | 56.442 | 163.08 |
| 56.437 | 258.05 | 56.439 | 240.86 | 56.993 | 213.88 | 57.014 | 164.3  |

| Time    | PEG         | Time    | AA           | Time    | DMA    | Time    | PP          |
|---------|-------------|---------|--------------|---------|--------|---------|-------------|
| 57.006  | 259.56      | 57.009  | 242.34       | 57.56   | 215.18 | 57.584  | 165.3       |
| 57.575  | 260.96      | 57.579  | 243.82       | 58.131  | 216.54 | 58.152  | 166.61      |
| 58.143  | 262.38      | 58.149  | 245.3        | 58.702  | 217.76 | 58.723  | 167.75      |
| 58.713  | 264         | 58.719  | 246.78       | 59.269  | 218.99 | 59.293  | 168.83      |
|         |             | 59.289  | 248.26       | 59.841  | 220.46 | 59.861  | 169.95      |
|         |             | 59.859  | 249.74       |         |        |         |             |
|         |             |         |              |         |        |         |             |
| Time    | PP No<br>BK |         | PEG No<br>BK |         | CA     |         | CA No<br>BK |
| 0.34688 | 4.63        | 0.34779 | 4.9          | 0.01914 | 0      | 0.34798 | 11.5        |
| 0.68568 | 8.79        | 0.68568 | 9.7          | 0.59134 | 10.01  | 0.68665 | 19.6        |
| 1.0243  | 12.58       | 1.0243  | 14.2         | 1.1625  | 21.74  | 1.0227  | 24.2        |
| 1.3604  | 16.16       | 1.3603  | 18.36        | 1.7301  | 31.64  | 1.3613  | 27.65       |
| 1.699   | 19.28       | 1.699   | 21.97        | 2.3013  | 40.43  | 1.6973  | 30.43       |
| 2.035   | 22          | 2.035   | 25.11        | 2.8716  | 48.27  | 2.036   | 32.87       |
| 2.3737  | 24.47       | 2.3737  | 27.95        | 3.4391  | 55.48  | 2.3747  | 35.03       |
| 2.7124  | 26.67       | 2.7124  | 30.52        | 4.0105  | 61.85  | 2.7133  | 37.02       |
| 3.051   | 28.72       | 3.051   | 32.83        | 4.5807  | 68.11  | 3.0493  | 38.85       |
| 3.387   | 30.55       | 3.387   | 34.93        | 5.151   | 74.1   | 3.388   | 40.49       |
| 3.7257  | 32.2        | 3.7257  | 36.89        | 5.7195  | 79.68  | 3.724   | 42.08       |
| 4.0617  | 33.78       | 4.0617  | 38.78        | 6.2898  | 85.18  | 4.0627  | 43.48       |
| 4.4003  | 35.27       | 4.4003  | 40.52        | 6.861   | 90.19  | 4.3979  | 44.84       |
| 4.7363  | 36.63       | 4.7363  | 42.18        | 7.4313  | 95.06  | 4.7365  | 46.17       |
| 5.0742  | 37.88       | 5.0742  | 43.73        | 8.0016  | 99.89  | 5.0725  | 47.41       |
| 5.4102  | 39.14       | 5.4102  | 45.22        | 8.572   | 104.14 | 5.4112  | 48.63       |
| 5.7488  | 40.31       | 5.7488  | 46.6         | 9.1395  | 108.43 | 5.7472  | 49.75       |
| 6.0848  | 41.46       | 6.0848  | 47.99        | 9.7108  | 113.3  | 6.0859  | 50.91       |
| 6.4235  | 42.53       | 6.4234  | 49.32        | 10.281  | 116.49 | 6.4219  | 52          |
| 6.7595  | 43.53       | 6.7595  | 50.53        | 10.852  | 120.37 | 6.7605  | 53.08       |
| 7.0982  | 44.57       | 7.0982  | 51.71        | 11.422  | 124.7  | 7.0992  | 54.07       |
| 7.4368  | 45.5        | 7.4368  | 52.89        | 11.993  | 127.5  | 7.4378  | 55.04       |
| 7.7755  | 46.42       | 7.7755  | 54.08        | 12.565  | 130.96 | 7.7738  | 56.04       |
| 8.1115  | 47.31       | 8.1115  | 55.14        | 13.136  | 134.37 | 8.1125  | 57.04       |
| 8.4502  | 48.19       | 8.4501  | 56.21        | 13.707  | 137.66 | 8.4485  | 57.93       |
| 8.7862  | 48.98       | 8.7862  | 57.2         | 14.278  | 140.93 | 8.7863  | 58.84       |
| 9.1249  | 49.85       | 9.1249  | 58.18        | 14.848  | 143.98 | 9.1223  | 59.7        |
| 9.46    | 50.63       | 9.4608  | 59.17        | 15.416  | 147.02 | 9.461   | 60.61       |
| 9.7987  | 51.41       | 9.7987  | 60.11        | 15.986  | 150.01 | 9.797   | 61.39       |
| 10.135  | 52.12       | 10.135  | 61.05        | 16.557  | 152.9  | 10.136  | 62.29       |
| 10.473  | 52.9        | 10.473  | 61.95        | 17.127  | 155.66 | 10.472  | 63.09       |

| Time   | PP No<br>BK |        | PEG No<br>BK |        | CA     |        | CA No<br>BK |
|--------|-------------|--------|--------------|--------|--------|--------|-------------|
| 10.809 | 53.61       | 10.809 | 62.86        | 17.697 | 158.34 | 10.81  | 63.88       |
| 11.148 | 54.29       | 11:148 | 63.63        | 18.267 | 160.9  | 11.146 | 64.68       |
| 11.487 | 54.96       | 11.484 | 64.51        | 18.837 | 163.48 | 11.485 | 65.47       |
| 11.825 | 55.67       | 11.82  | 65.32        | 19.407 | 166.01 | 11.824 | 66.19       |
| 12.161 | 56.26       | 12.156 | 66.11        | 19.975 | 168.51 | 12.162 | 66.97       |
| 12.5   | 56.96       | 12.492 | 66.9         | 20.545 | 170.92 | 12.498 | 67.68       |
| 12.836 | 57.57       | 12.83  | 67.68        | 21.114 | 173.23 | 12.837 | 68.39       |
| 13.175 | 58.16       | 13.167 | 68.41        | 21.684 | 175.5  | 13.173 | 69.16       |
| 13.511 | 58.8        | 13.505 | 69.18        | 22.253 | 177.75 | 13.511 | 69.86       |
| 13.849 | 59.43       | 13.841 | 69.9         | 22.821 | 179.95 | 13.847 | 70.49       |
| 14.185 | 59.98       | 14.18  | 70.6         | 23.391 | 182.07 | 14.185 | 71.17       |
| 14.523 | 60.57       | 14.516 | 71.29        | 23.96  | 184.12 | 14.521 | 71.91       |
| 14.859 | 61.17       | 14.854 | 71.99        | 24.532 | 186.24 | 14.86  | 72.55       |
| 15.198 | 61.68       | 15.19  | 72.69        | 25.1   | 188.25 | 15.196 | 73.21       |
| 15.534 | 62.27       | 15.528 | 73.32        | 25.669 | 190.22 | 15.535 | 73.83       |
| 15.873 | 62.79       | 15.864 | 74.03        | 26.239 | 192.26 | 15.874 | 74.54       |
| 16.211 | 63.39       | 16.203 | 74.63        | 26.809 | 194.16 | 16.212 | 75.18       |
| 16.55  | 63.9        | 16.539 | 75.32        | 27.378 | 196.05 | 16.548 | 75.77       |
| 16.886 | 64.42       | 16.878 | 75.94        | 27.95  | 197.8  | 16.887 | 76.35       |
| 17.225 | 64.91       | 17.214 | 76.55        | 28.517 | 199.69 | 17.223 | 76.95       |
| 17.561 | 65.44       | 17.557 | 77.04        | 29.088 | 201.49 | 17.562 | 77.58       |
| 17.899 | 65.93       | 17.893 | 77.58        | 29.657 | 203.23 | 17.898 | 78.17       |
| 18.235 | 66.45       | 18.232 | 78.09        | 30.227 | 204.87 | 18.235 | 78.81       |
| 18.573 | 66.95       | 18.568 | 78.61        | 30.797 | 206.66 | 18.571 | 79.36       |
| 18.909 | 67.37       | 18.906 | 79.12        | 31.367 | 208.23 | 18.907 | 79.93       |
| 19.248 | 67.9        | 19.242 | 79.64        | 31.935 | 209.83 | 19.246 | 80.55       |
| 19.584 | 68.37       | 19.58  | 80.16        | 32.505 | 211.64 | 19.582 | 81.06       |
| 19.922 | 68.82       | 19.916 | 80.69        | 33.075 | 213.63 | 19.921 | 81.67       |
| 20.258 | 69.31       | 20.255 | 81.2         | 33.644 | 215.62 | 20.257 | 82.19       |
| 20.597 | 69.76       | 20.591 | 81.62        | 34.214 | 217.74 | 20.595 | 82.78       |
| 20.936 | 70.15       | 20.929 | 82.13        | 34.785 | 219.75 | 20.934 | 83.31       |
| 21.274 | 70.64       | 21.265 | 82.65        | 35.354 | 221.68 | 21.273 | 83.84       |
| 21.61  | 71.07       | 21.604 | 83.07        | 35.923 | 223.56 | 21.609 | 84.36       |
| 21.946 | 71.49       | 21.943 | 83.58        | 36.493 | 225.29 | 21.947 | 84.88       |
| 22.285 | 71.92       | 22.281 | 84           | 37.063 | 227.04 | 22.283 | 85.39       |
| 22.621 | 72.27       | 22.617 | 84.5         | 37.632 | 228.34 | 22.622 | 85.95       |
| 22.96  | 72.71       | 22.956 | 84.94        | 38.205 | 229.81 | 22.958 | 86.43       |
| 23.296 | 73.12       | 23.292 | 85.4         | 38.775 | 231.31 | 23.296 | 86.95       |
| 23.634 | 73.54       | 23.631 | 85.89        | 39.344 | 232.7  | 23.632 | 87.46       |

| Time   | PP No<br>BK |        | PEG No<br>BK |        | CA     |        | CA No<br>BK |
|--------|-------------|--------|--------------|--------|--------|--------|-------------|
| 23.97  | 73.96       | 23.967 | 86.31        | 39.913 | 234.04 | 23.971 | 87.99       |
| 24.308 | 74.37       | 24.305 | 86.73        | 40.484 | 235.31 | 24.307 | 88.49       |
| 24.644 | 74.7        | 24.64  | 87.14        | 41.053 | 236.55 | 24.645 | 88.98       |
| 24.983 | 75.14       | 24.979 | 87.65        | 41.624 | 237.84 | 24.981 | 89.45       |
| 25.319 | 75.53       | 25.315 | 88.01        | 42.193 | 239.02 | 25.32  | 89.97       |
| 25.658 | 75.89       | 25.654 | 88.45        | 42.763 | 240.18 | 25.659 | 90.39       |
| 25.996 | 76.3        | 25.99  | 88.87        | 43.331 | 241.25 | 25.997 | 90.92       |
| 26.335 | 76.65       | 26.329 | 89.2         | 43.901 | 242.41 | 26.333 | 91.35       |
| 26.671 | 77.06       | 26.667 | 89.65        | 44.472 | 243.44 | 26.672 | 91.86       |
| 27.01  | 77.39       | 27.006 | 90.06        | 45.042 | 244.51 | 27.008 | 92.27       |
| 27.346 | 77.81       | 27.342 | 90.39        | 45.613 | 245.58 | 27.346 | 92.79       |
| 27.683 | 78.15       | 27.68  | 90.82        | 46.183 | 246.28 | 27.682 | 93.24       |
| 28.019 | 78.54       | 28.016 | 91.25        | 46.752 | 247.04 | 28.02  | 93.66       |
| 28.358 | 78.89       | 28.355 | 91.58        | 47.32  | 247.74 | 28.356 | 94.17       |
| 28.694 | 79.23       | 28.691 | 92.01        | 47.891 | 248.52 | 28.695 | 94.61       |
| 29.033 | 79.63       | 29.029 | 92.34        | 48.462 | 249.26 | 29.031 | 95          |
| 29.369 | 79.98       | 29.365 | 92.76        | 49.029 | 250    | 29.37  | 95.44       |
| 29.707 | 80.3        | 29.704 | 93.1         | 49.6   | 250.92 | 29.708 | 95.95       |
| 30.043 | 80.63       | 30.04  | 93.51        | 50.171 | 251.66 | 30.047 | 96.4        |
| 30.382 | 81.04       | 30.378 | 93.86        | 50.741 | 252.41 | 30.383 | 96.82       |
| 30.721 | 81.38       | 30.714 | 94.22        | 51.311 | 253.2  | 30.722 | 97.24       |
| 31.059 | 81.71       | 31.053 | 94.62        | 51.883 | 253.91 | 31.058 | 97.67       |
| 31.395 | 82.06       | 31.392 | 94.97        | 52.453 | 254.62 | 31.396 | 98.1        |
| 31.734 | 82.39       | 31.73  | 95.38        | 53.023 | 255.43 | 31.732 | 98.53       |
| 32.07  | 82.72       | 32.066 | 95.71        | 53.594 | 256.18 | 32.07  | 98.95       |
| 32.408 | 83.05       | 32.405 | 96.05        | 54.166 | 256.83 | 32.406 | 99.38       |
| 32.744 | 83.38       | 32.741 | 96.45        | 54.736 | 258.14 | 32.745 | 99.81       |
| 33.083 | 83.71       | 33.08  | 96.8         | 55.305 | 258.28 | 33.081 | 100.23      |
| 33.418 | 84.04       | 33.415 | 97.15        | 55.875 | 259.02 | 33.42  | 100.57      |
| 33.757 | 84.37       | 33.754 | 97.48        | 56.445 | 259.86 | 33.756 | 101.03      |
| 34.093 | 84.68       | 34.09  | 97.83        | 57.015 | 260.48 | 34.094 | 101.44      |
| 34.432 | 85.02       | 34.425 | 98.23        | 57.586 | 261.18 | 34.433 | 101.85      |
| 34.771 | 85.36       | 34.764 | 98.58        | 58.157 | 263.04 | 34.771 | 102.29      |
| 35.109 | 85.7        | 35.1   | 98.92        | 58.727 | 262.5  | 35.107 | 102.62      |
| 35.445 | 85.99       | 35.439 | 99.24        | 59.296 | 263.3  | 35.446 | 103.05      |
| 35.784 | 86.27       | 35.777 | 99.59        | 59.866 | 264.36 | 35.782 | 103.47      |
| 36.12  | 86.58       | 36.116 | 99.92        | 60.435 | 264.65 | 36.121 | 103.81      |
| 36.459 | 86.93       | 36.452 | 100.26       |        |        | 36.457 | 104.23      |
| 36.795 | 87.26       | 36.791 | 100.68       |        |        | 36.795 | 104.58      |

| Time   | PP No<br>BK |        | PEG No<br>BK |  | CA |        | CA No<br>BK |
|--------|-------------|--------|--------------|--|----|--------|-------------|
| 37.132 | 87.51       | 37.127 | 101.01       |  |    | 37.131 | 104.99      |
| 37.468 | 87.83       | 37.465 | 101.37       |  |    | 37.469 | 105.39      |
| 37.807 | 88.18       | 37.801 | 101.7        |  |    | 37.805 | 105.77      |
| 38.143 | 88.41       | 38.139 | 102          |  |    | 38.144 | 106.18      |
| 38.482 | 88.75       | 38.475 | 102.35       |  |    | 38.48  | 106.52      |
| 38.818 | 89.06       | 38.814 | 102.7        |  |    | 38.819 | 106.89      |
| 39.156 | 89.31       | 39.15  | 103.01       |  |    | 39.157 | 107.27      |
| 39.495 | 89.65       | 39.489 | 103.28       |  |    | 39.496 | 107.62      |
| 39.834 | 89.97       | 39.825 | 103.62       |  |    | 39.832 | 108.05      |
| 40.17  | 90.23       | 40.163 | 103.96       |  |    | 40.171 | 108.39      |
| 40.508 | 90.55       | 40.502 | 104.27       |  |    | 40.507 | 108.73      |
| 40.844 | 90.8        | 40.841 | 104.64       |  |    | 40.845 | 109.15      |
| 41.183 | 91.13       | 41.177 | 104.95       |  |    | 41.181 | 109.49      |
| 41.519 | 91.38       | 41.515 | 105.3        |  |    | 41.519 | 109.82      |
| 41.857 | 91.71       | 41.851 | 105.65       |  |    | 41.855 | 110.24      |
| 42.193 | 91.95       | 42.19  | 105.87       |  |    | 42.194 | 110.58      |
| 42.532 | 92.27       | 42.526 | 106.22       |  |    | 42.53  | 110.91      |
| 42.868 | 92.51       | 42.864 | 106.55       |  |    | 42.866 | 111.25      |
| 43.206 | 92.76       | 43.2   | 106.88       |  |    | 43.204 | 111.68      |
| 43.542 | 93.09       | 43.538 | 107.21       |  |    | 43.541 | 112.02      |
| 43.881 | 93.33       | 43.874 | 107.47       |  |    | 43.879 | 112.34      |
| 44.22  | 93.64       | 44.213 | 107.78       |  |    | 44.218 | 112.68      |
| 44.558 | 93.9        | 44.549 | 108.11       |  |    | 44.557 | 113.02      |
| 44.894 | 94.14       | 44.888 | 108.36       |  |    | 44.893 | 113.36      |
| 45.233 | 94.46       | 45.227 | 108.72       |  |    | 45.231 | 113.71      |
| 45.569 | 94.72       | 45.565 | 109.06       |  |    | 45.567 | 114.03      |
| 45.905 | 94.96       | 45.901 | 109.32       |  |    | 45.905 | 114.46      |
| 46.243 | 95.2        | 46.24  | 109.65       |  |    | 46.241 | 114.81      |
| 46.579 | 95.5        | 46.576 | 109.97       |  |    | 46.58  | 115.13      |
| 46.917 | 95.77       | 46.915 | 110.23       |  |    | 46.916 | 115.44      |
| 47.253 | 96.02       | 47.25  | 110.55       |  |    | 47.254 | 115.8       |
| 47.592 | 96.28       | 47.588 | 110.89       |  |    | 47.59  | 116.12      |
| 47.928 | 96.51       | 47.924 | 111.14       |  |    | 47.929 | 116.42      |
| 48.267 | 96.76       | 48.263 | 111.49       |  |    | 48.265 | 116.72      |
| 48.603 | 97          | 48.599 | 111.73       |  |    | 48.604 | 117.06      |
| 48.941 | 97.26       | 48.938 | 112.07       |  |    | 48.942 | 117.38      |
| 49.28  | 97.5        | 49.274 | 112.3        |  |    | 49.281 | 117.73      |
| 49.619 | 97.72       | 49.612 | 112.65       |  |    | 49.617 | 118.06      |
| 49.955 | 97.97       | 49.951 | 112.9        |  |    | 49.956 | 118.39      |

| Time    | PP No<br>BK |        | PEG No<br>BK |  | CA |        | CA No<br>BK |
|---------|-------------|--------|--------------|--|----|--------|-------------|
| 50.293  | 98.21       | 50.29  | 113.25       |  |    | 50.292 | 118.73      |
| 50.629  | 98.47       | 50.626 | 113.49       |  |    | 50.63  | 119.07      |
| 50.967  | 98.69       | 50.964 | 113.74       |  |    | 50.965 | 119.31      |
| 51.303  | 98.9        | 51.3   | 113.99       |  |    | 51.304 | 119.64      |
| 51.642  | 99.1        | 51.639 | 114.23       |  |    | 51.64  | 119.97      |
| 51.978  | 99.33       | 51.974 | 114.51       |  |    | 51.979 | 120.31      |
| 52.317  | 99.58       | 52.313 | 114.81       |  |    | 52.315 | 120.58      |
| 52.653  | 99.82       | 52.649 | 115.06       |  |    | 52.654 | 120.9       |
| 52.991  | 100.07      | 52.987 | 115.3        |  |    | 52.992 | 121.23      |
| 53.33   | 100.32      | 53.324 | 115.56       |  |    | 53.331 | 121.57      |
| 53.668  | 100.55      | 53.662 | 115.8        |  |    | 53.667 | 121.84      |
| 54.005  | 100.79      | 53.998 | 116.05       |  |    | 54.006 | 122.16      |
| 54.343  | 101.04      | 54.337 | 116.28       |  |    | 54.342 | 122.48      |
| 54.679  | 101.19      | 54.675 | 116.56       |  |    | 54.68  | 122.73      |
| 55.018  | 101.43      | 55.014 | 116.79       |  |    | 55.016 | 123.07      |
| 55.354  | 101.67      | 55.35  | 117.1        |  |    | 55.354 | 123.41      |
| 55.692  | 101.92      | 55.689 | 117.38       |  |    | 55.69  | 123.65      |
| 56.028  | 102.17      | 56.025 | 117.63       |  |    | 56.029 | 124         |
| 56.366  | 102.4       | 56.363 | 117.86       |  |    | 56.365 | 124.25      |
| 56.702  | 102.56      | 56.699 | 118.14       |  |    | 56.703 | 124.56      |
| 57.041  | 102.79      | 57.037 | 118.37       |  |    | 57.039 | 124.88      |
| 57.377  | 103.04      | 57.373 | 118.62       |  |    | 57.378 | 125.17      |
| 57.716  | 103.28      | 57.712 | 118.86       |  |    | 57.717 | 125.5       |
| 58.054  | 103.53      | 58.048 | 119.1        |  |    | 58.055 | 125.73      |
| 58.393  | 103.69      | 58.384 | 119.35       |  |    | 58.391 | 126.07      |
| 58.729  | 103.94      | 58.72  | 119.62       |  |    | 58.73  | 126.34      |
| 59.068  | 104.16      | 59.056 | 119.84       |  |    | 59.066 | 126.66      |
| 59.404  | 104.4       | 59.392 | 120.09       |  |    | 59.405 | 126.89      |
| 59.742  | 104.57      | 59.731 | 120.34       |  |    | 59.741 | 127.15      |
| /60.078 | 104.81      | 60.069 | 120.6        |  |    | 60.079 | 127.5       |
| 60.416  | 105.06      | 60.405 | 120.85       |  |    |        |             |



**Data for Figure 14**

| Wt Gain | Long-term Flux |  | Recovered Flux |  |
|---------|----------------|--|----------------|--|
| 4.88    | 168            |  | 363.2          |  |
| 3.19    | 153.6          |  | 295.6          |  |
| 3.73    | 154.4          |  | 315.8          |  |
| 10.42   | 173.6          |  | 401.8          |  |
| 10.13   | 148            |  | 326.5          |  |
| 9.96    | 134.4          |  | 335.2          |  |
| 6.64    | 121.6          |  | 386.4          |  |
| 6.64    | 115.2          |  | 301.2          |  |
| 0       | 128            |  | 210            |  |
| 1.81    | 181            |  |                |  |
| 1.83    | 139            |  | 323.4          |  |