

Paradigm Shift for Resonance-Region Uncertainties

**Nancy Larson
Herve Derrien
Luiz Leal
Dorothea Wiarda
Goran Arbanas**
Oak Ridge National Lab

CSEWG, Nov 6-8, 2007

Two issues for resonance covariances

- **File 32 is difficult to deal with**
 - **Size is often very large**
 - **Calculating the evaluated cross section covariance matrix from File 32 is complicated**

Save this topic for the end of the talk

- **The resonance parameter covariance matrix cannot convey complete information**

The main topic for this talk

Synopsis of the issue

- R-matrix analysis automatically produces a **resonance parameter covariance matrix** = RPCM
- From the resonance parameters, we reconstruct point-wise cross sections
 - Also multigroup cross sections
- From the RPCM, we construct the **covariance matrix for the evaluated cross sections** = ECM
- The ECM constructed using only the RPCM is generally regarded as “too small”

Why is the ECM too small?

- It is not possible for RPCM to convey **complete** information concerning ECM

Reasons will be discussed separately...

- **Several reasons for this**
 - Computation of RPCM is based on assumptions which are not fully valid
 - Bayes' equations (or least-squares equations) contain **no** information about goodness-of-fit
 - Experimental data base is not unique

Assumptions on which RPCM is based:

1. R-matrix theory is correct

- **All resonances are included**
 - Even very small invisible resonances
- **All spin assignments are correct**
 - No ambiguity
- **No direct components or other extensions exist**
- **Everything is calculated correctly**
 - No bugs in the code

These assumptions are all reasonable but imperfect

Assumptions, continued:

2. All experimental conditions are properly understood and included in the analysis

- Corrections are accurately made for
 - Doppler and resolution broadening
 - Multiple-scattering corrections
 - Normalization and background
 - Etc.
- Everything is calculated correctly
 - No bugs in computer codes, no omissions in theory
- All experimental uncertainties are described correctly
- No discrepancies exist between data sets

These assumptions are reasonable but imperfect

Conjecture: Why is the ECM too small?

- It is not possible for RPCM to convey complete information concerning ECM
- **Several reasons for this**
 - Computation of RPCM is based on assumptions which are not fully valid
 - **Bayes' equations (or least-squares equations) contain no information about goodness-of-fit**
 - Experimental data base is not unique

Bayes' Equations for RPCM

$$M' = \left(G^t V^{-1} G + M^{-1} \right)^{-1}$$

New RPCM

Data covariance matrix

Sensitivities or partial derivatives

Initial RPCM⁻¹,
0 for least squares

Appearing nowhere in this equation: the difference between theory and measurement

Conjecture: Why is the ECM too small?

- It is not possible for RPCM to convey complete information concerning ECM
- **Several reasons for this**
 - Computation of RPCM is based on assumptions which are not fully valid
 - Bayes' equations (or least-squares equations) contain no information about goodness-of-fit
 - **Experimental data base is not unique**

Experimental data base

- **Evaluator constructs a “consistent” experimental data base**
 - Based on results of preliminary analyses
 - Normalization = 1, background = 0
 - uncertainties included as SAMMY PUPs
- **This data base is not unique**
 - Depends on ability of evaluator to extract information from publications (often incomplete)
 - Systematic uncertainties should reflect this fact

Logical conclusion

- **The resonance parameter covariance matrix alone cannot provide complete information regarding the uncertainty on the evaluated cross sections**
- **Something else is needed**
- **It is not obvious how one quantizes the effects described above**

What can be done?

- **Historically**
 - Increase the RPCM in rather arbitrary fashion
- **Currently**
 - Still doing something like that
- **Future**
 - Add realistic components to the ECM
 - One component from RPCM
 - Other components from other effects

Other components

- **Two important and easy-to-implement possibilities**
 - **Normalization**
 - Value $a = 1$, uncertainty $\Delta a \sim 0.03$
 - **Background**
 - value $b = 0$, uncertainty Δb , perhaps energy-dependent
- **These may not directly represent the effects described earlier, but they should be a good first approximation**

One option for inclusion in ENDF

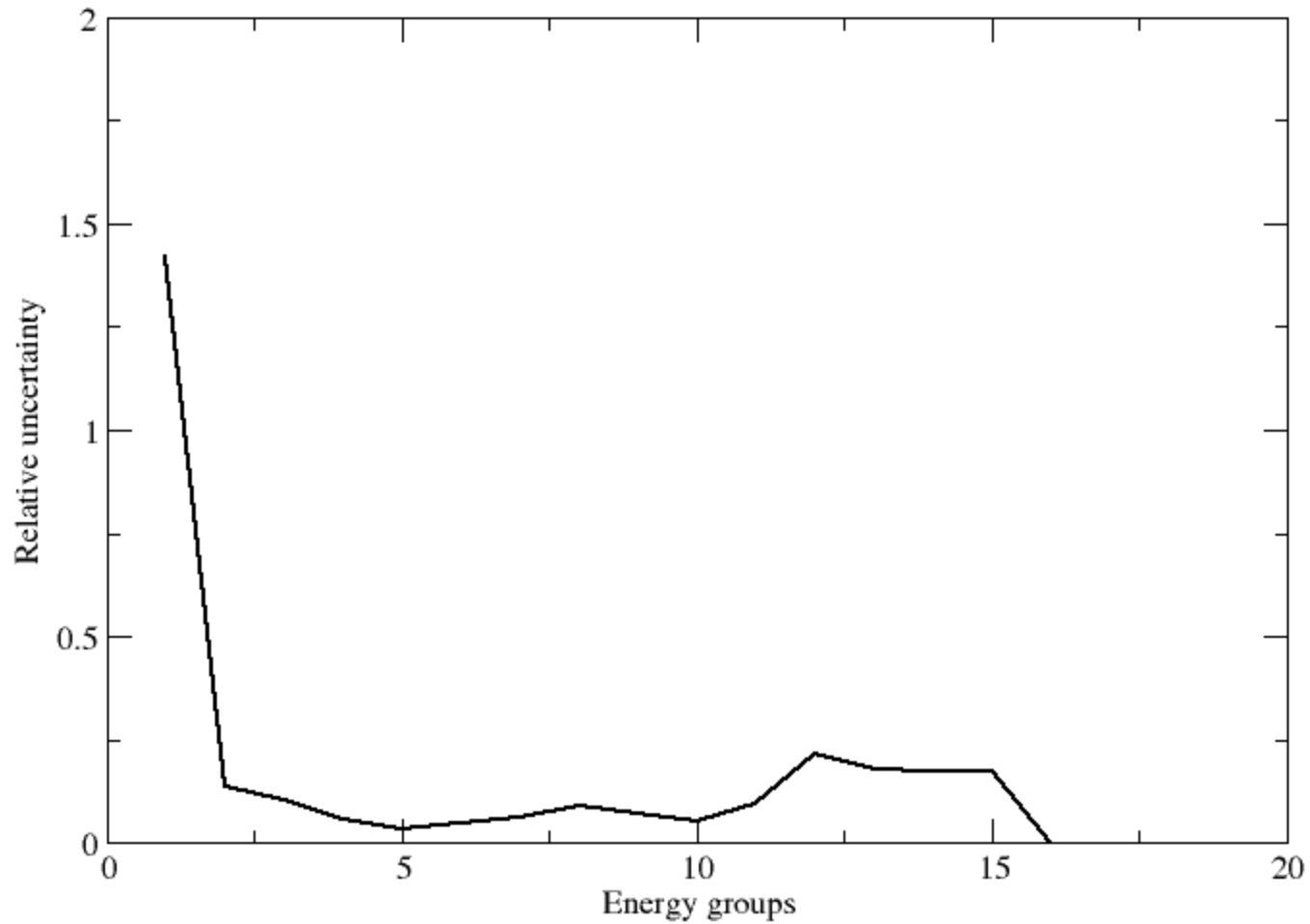
- **Use File 33 to introduce normalization and background uncertainty**
 - **No format changes required**
 - **Doro Wiarda is working on this possibility**
 - **Preliminary results are promising**
 - **Potential problems exist because of derived quantities (elastic = total – everything else)**

Preliminary results ...

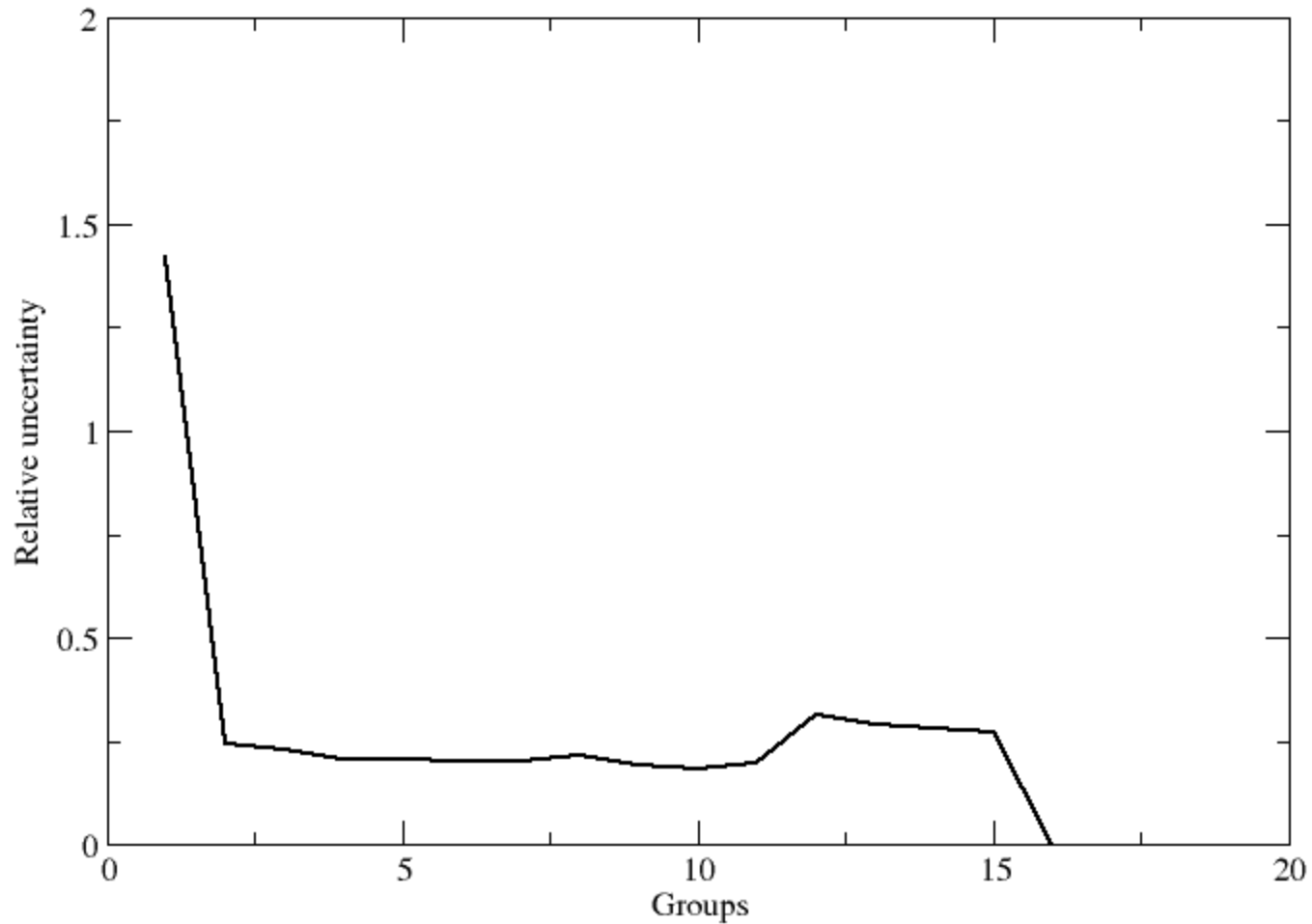
- **^{55}Mn capture cross section, expressed in arbitrary group structure**
- **Two versions**
 - **With only RPCM**
 - **With combination of**
 - **RPCM**
 - **Normalization uncertainty = 0.03**
 - **Background uncertainty varies with energy**
 - **Lowest = 0.8 % of average cross section**
 - **Highest = 15 %**
- **(No higher-energy information is included in these plots)**

Proof-of-principal only,
not a realistic case

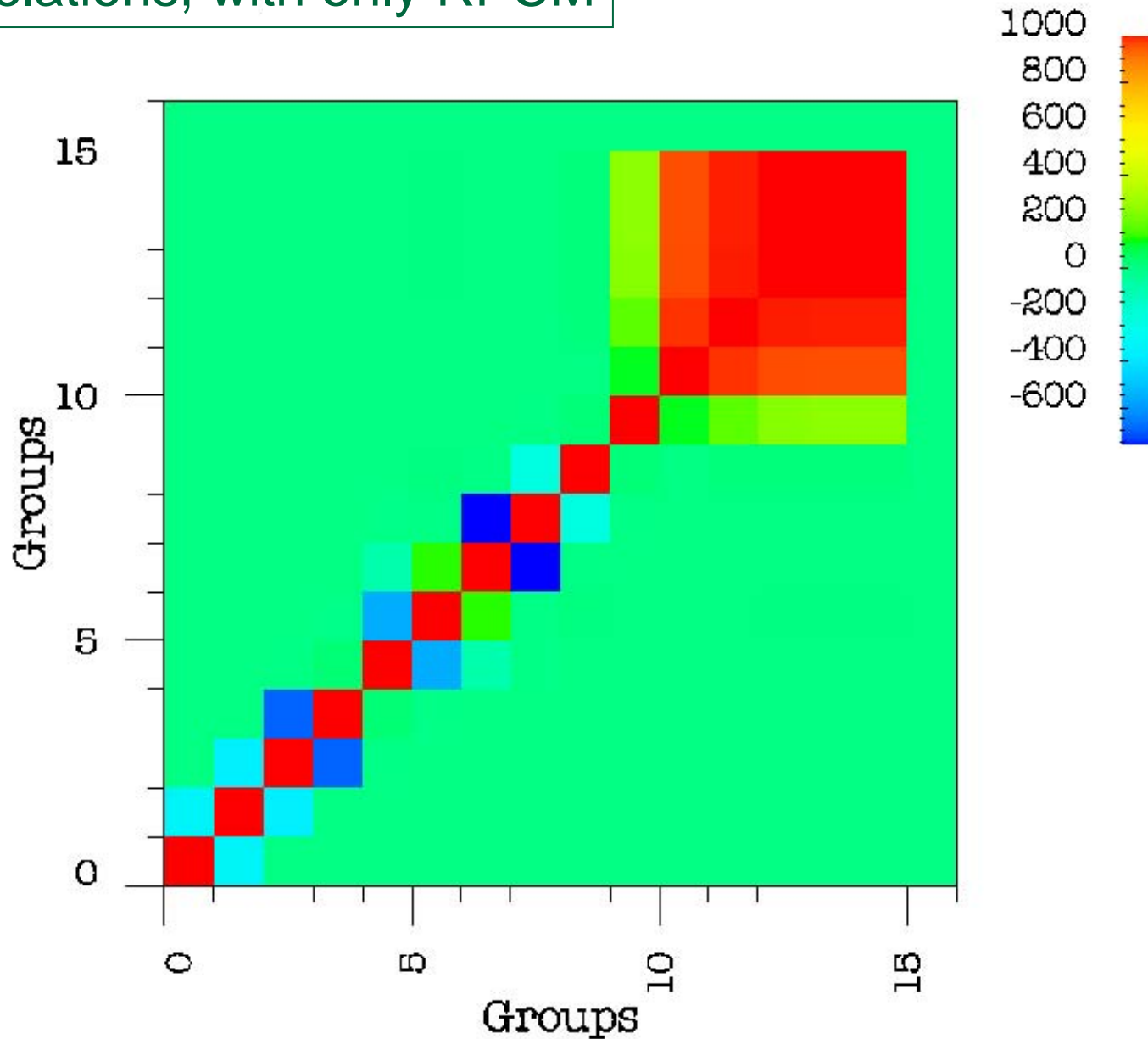
Relative uncertainty, with only RPCM



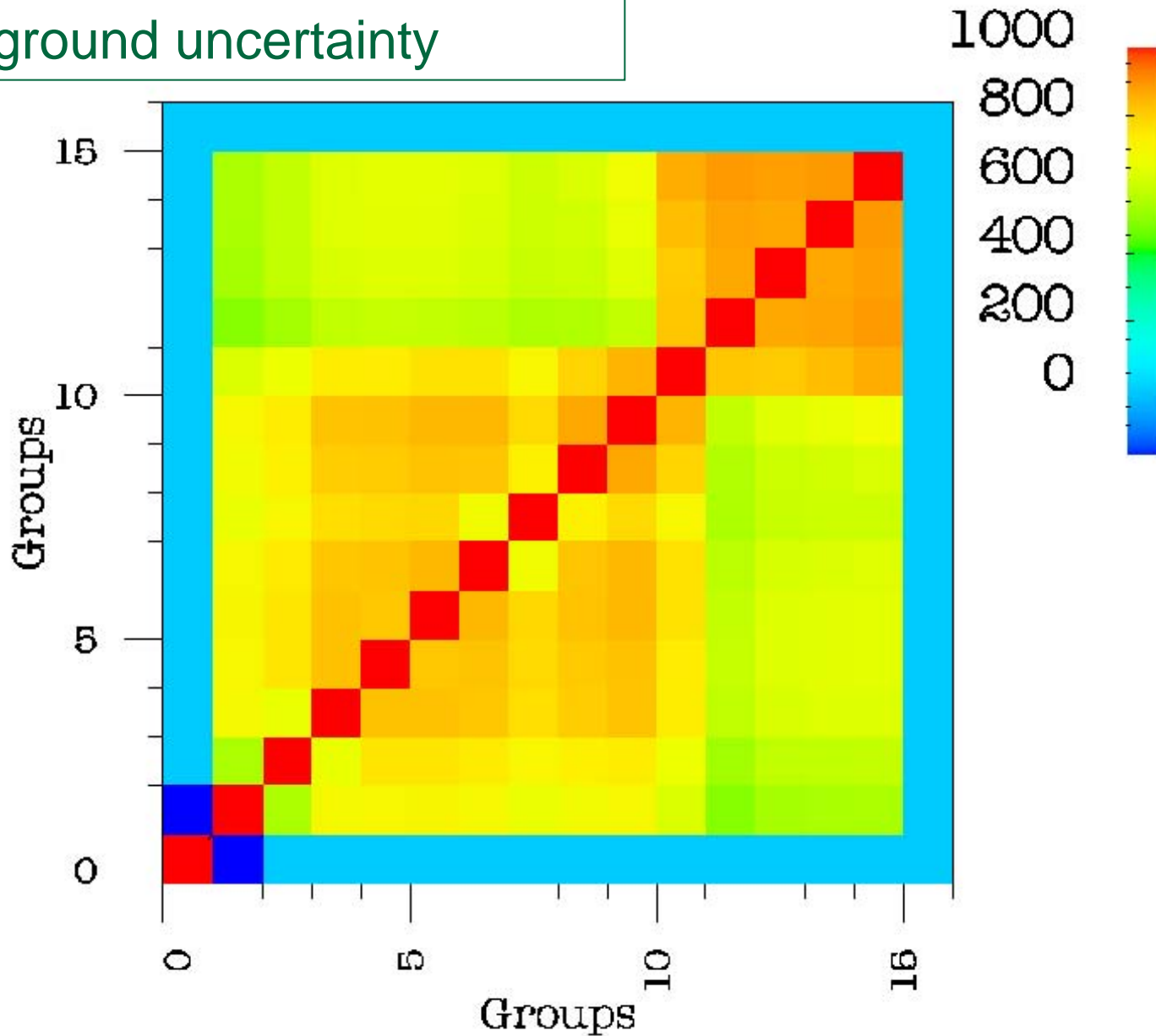
Relative uncertainty, with RPCM + norm + background unc.



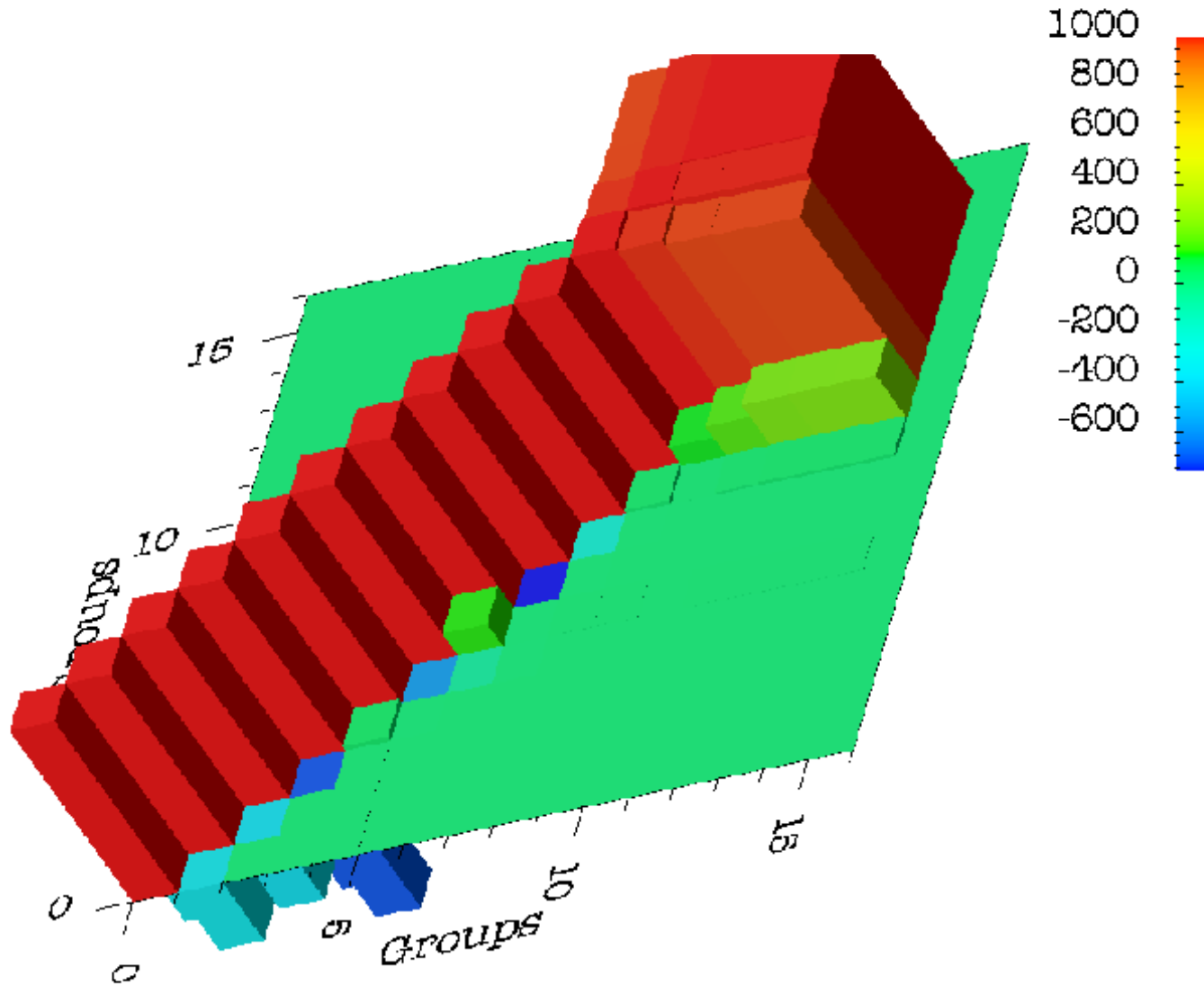
Correlations, with only RPCM



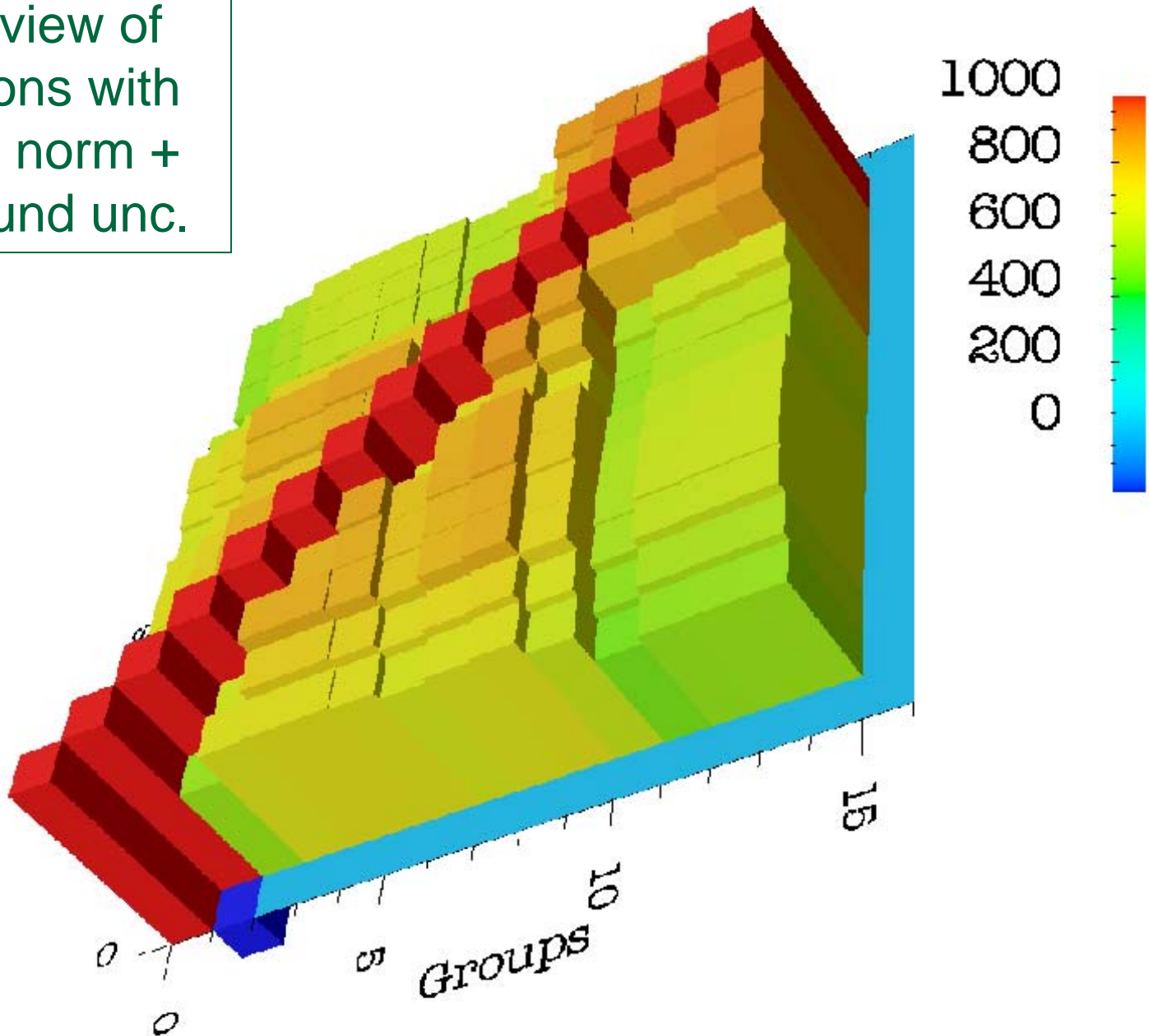
Correlations with RPCM + norm + background uncertainty



Another view of correlations with only RPCM



Another view of correlations with RPCM + norm + background unc.



Another option for inclusion in ENDF

Luiz Leal, Goran Arbanas, Doro Wiarda

- **Add RPCM plus other components prior to writing into ENDF files**
 - **Judiciously choose energy grid for storage of the complete ECM in File 33 of ENDF**
 - **Grid is chosen to convey maximum information for the nuclide – depends on level spacing, etc.**
 - **Grid must be tested to be sure that little information is lost**
 - **Test → compare to results generated using full ECM**
 - **File 32 would not be needed**
 - **This avoids the problems of storing too-large arrays**

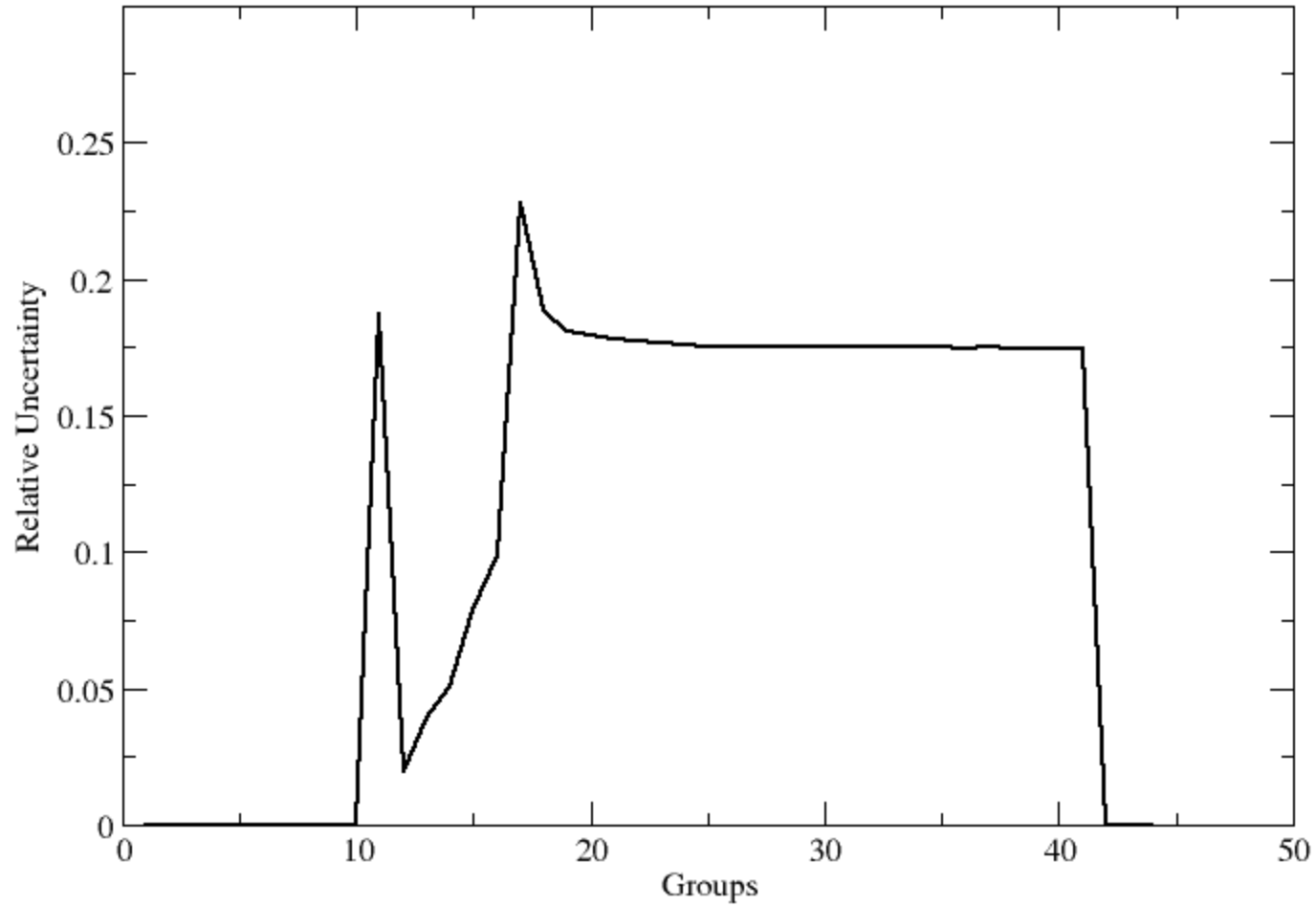
Conclusions

- **Paradigm shift may be necessary**
 - **Cannot expect the resonance parameter covariance matrix to convey all information about evaluated cross section uncertainties**
- **First-order effects should not require ENDF format changes**
- **File 33 can sometimes be used alone to convey the complete point-wise covariance matrix**
 - **When the energy grid is sufficiently fine and tailored to the specific nuclide**

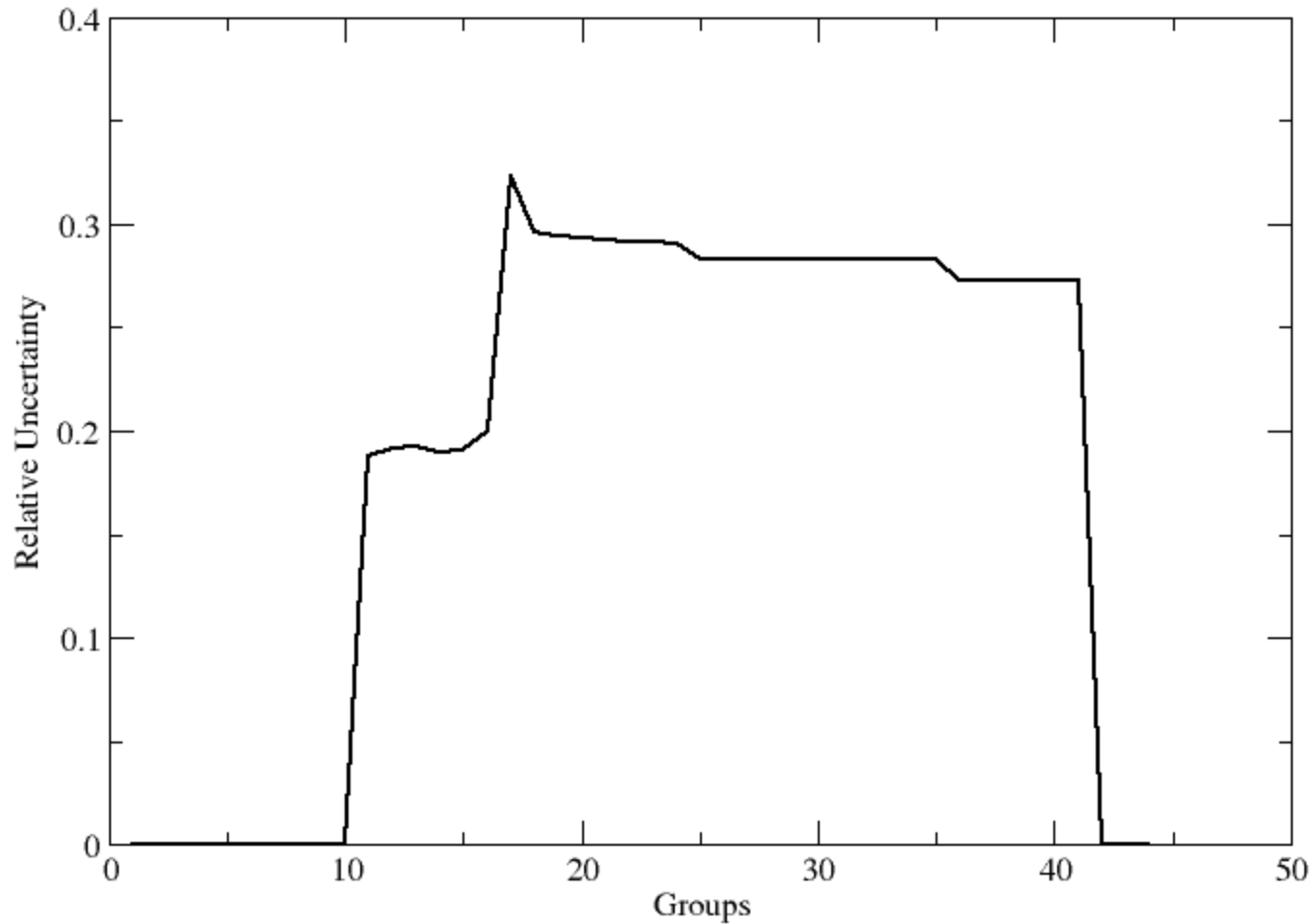
The end

The following slides show the same figures as above, but in a different group structure (AMPX standard 44-group structure)

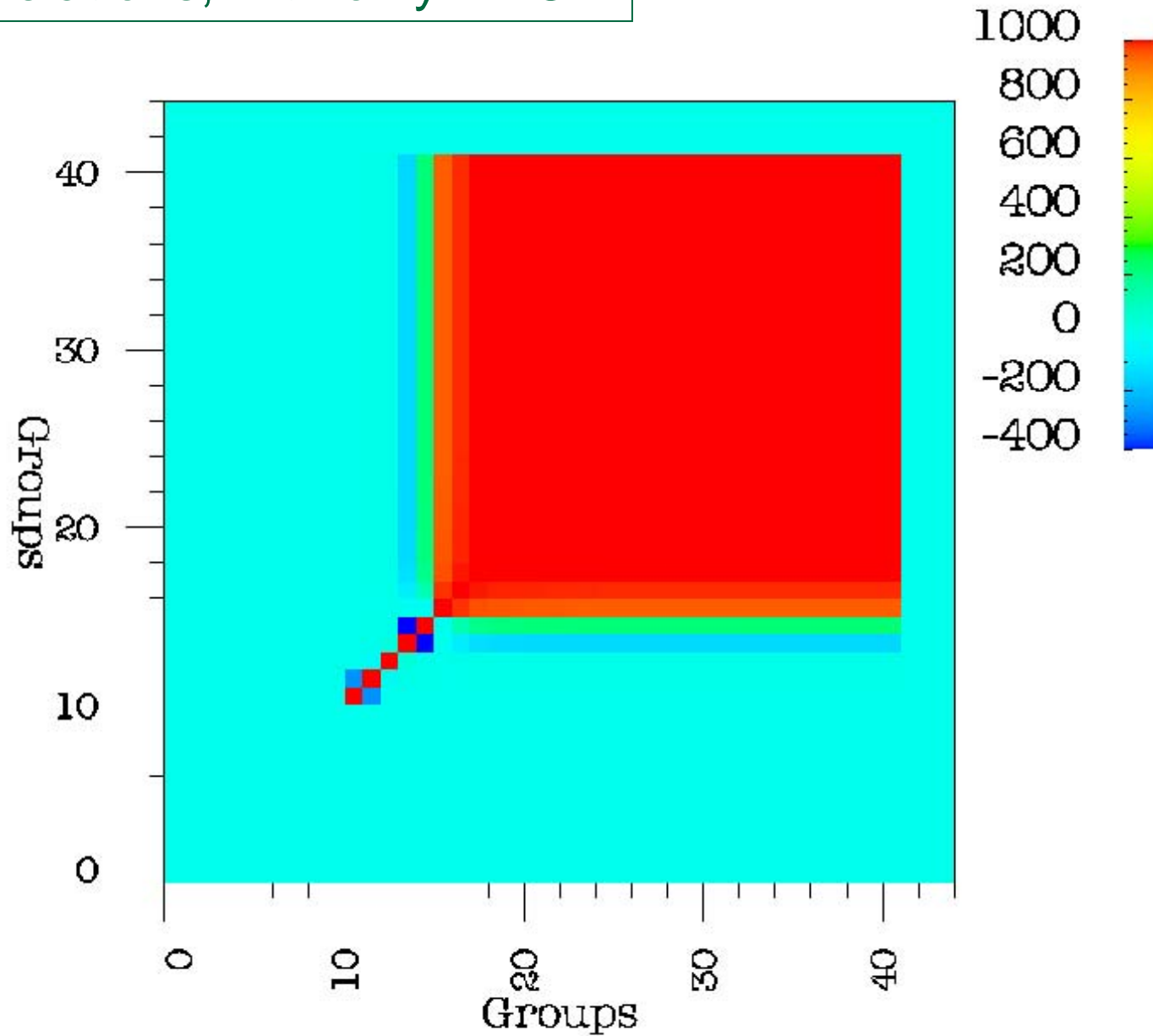
Relative uncertainty, with only RPCM



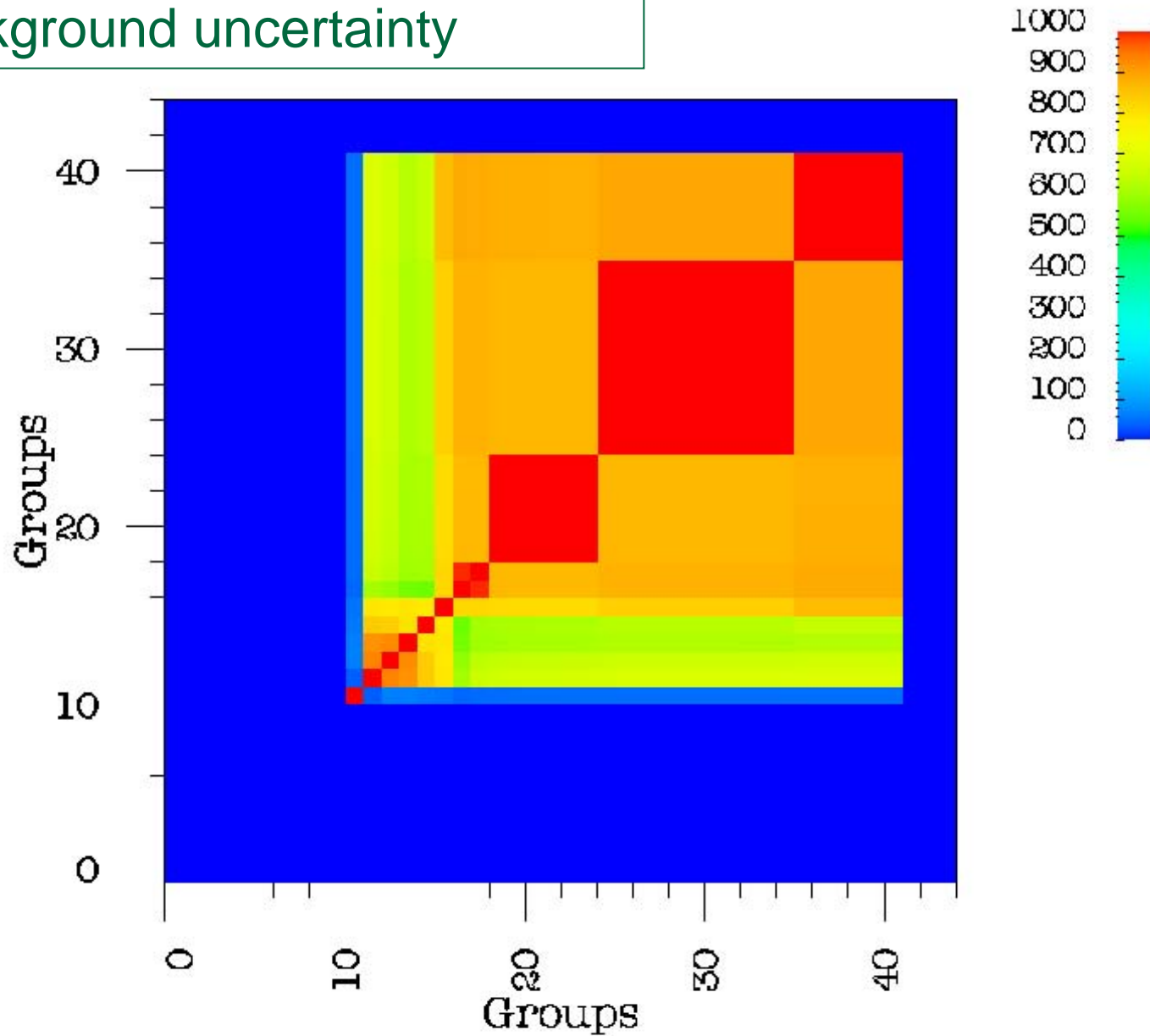
Relative uncertainty, with RPCM + norm + background unc.



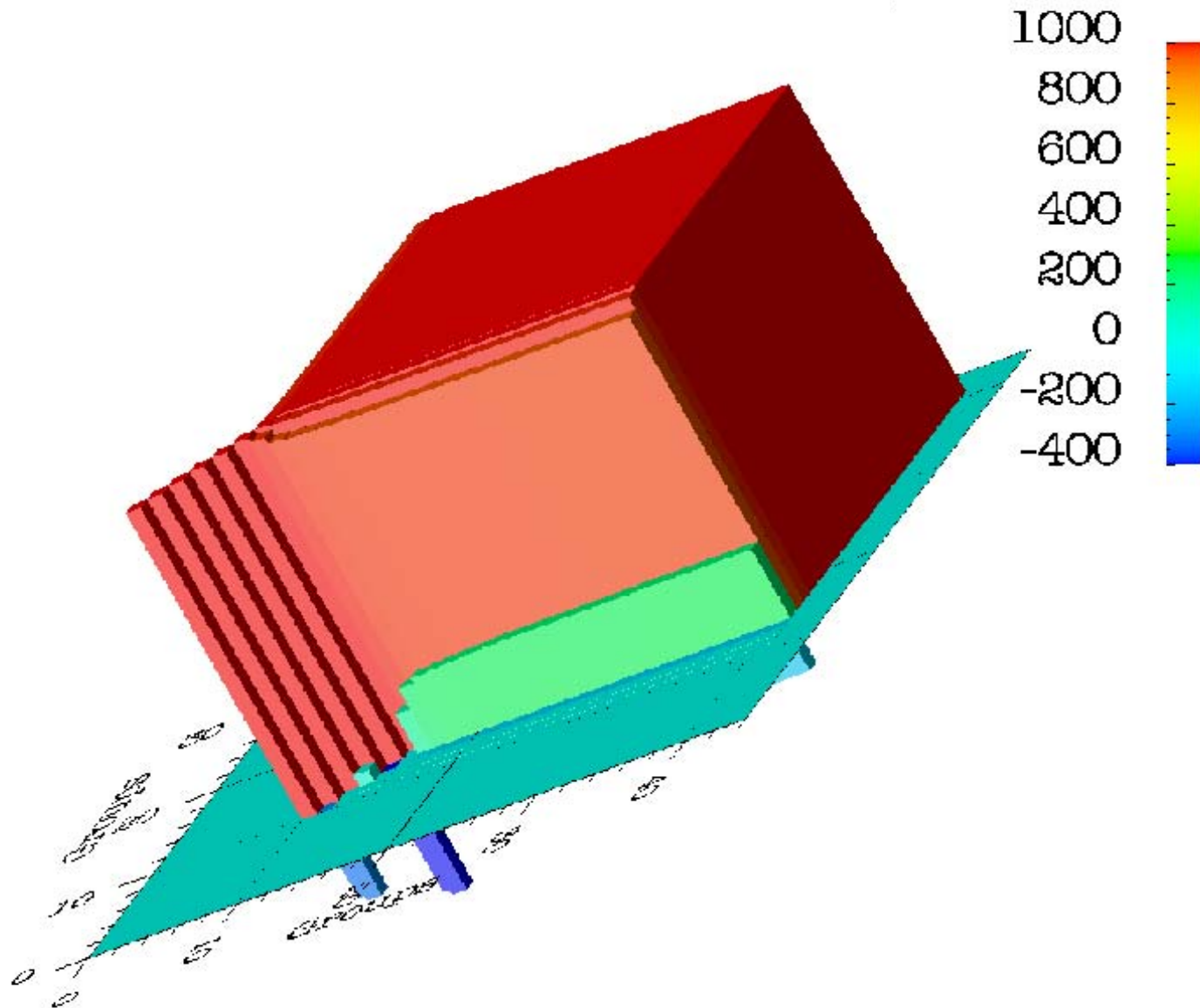
Correlations, with only RPCM



Correlations with RPCM + norm + background uncertainty



Another view of correlations with only RPCM



Another view of correlations with
RPCM + norm + background unc.

