

TERRESTRIAL PLANET FINDER INTERFEROMETER

TECHNOLOGY MILESTONE #2 WHITE PAPER

**FORMATION CONTROL PERFORMANCE
DEMONSTRATION**

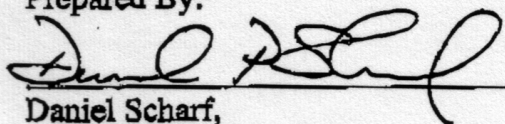
May 25, 2007

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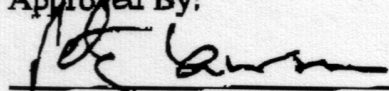
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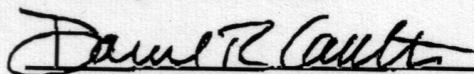
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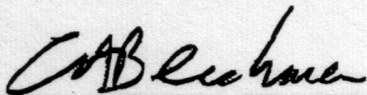
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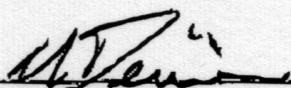
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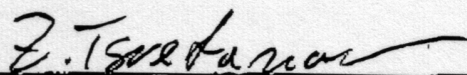
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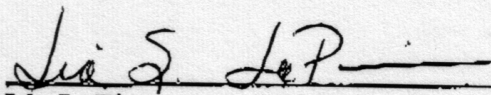
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TPF-I Technology Milestone #2 White Paper: Formation Control Performance Demonstration

1. Objective

In support of the Terrestrial Planet Finder Interferometer (TPF-I) pre-phase-A development program, this white paper explains the purpose of TPF-I Technology Milestone #2, specifies the methodology for computing the milestone metric, and establishes the success criteria against which the metric will be evaluated. See (Beichman et al. 1999) for a general discussion of the science and mission design of TPF-I.

This technology milestone was established in the TPF-I Technology Plan (Lawson & Dooley 2005) to gauge the developmental progress of the TPF-I project and its readiness to proceed from pre-Phase A to Phase A. Completion of this milestone is to be documented by the project, reviewed by the EIRB, and approved by NASA HQ. The formation control performance milestone described here addresses precision range and bearing control. The milestone is stated in the Technology Plan as follows.

Milestone #2: Formation Flying (Multiple Robot Demonstration)

Using the Formation Control Testbed as an end-to-end system-level hardware testbed, demonstrate that a formation of multiple robots can autonomously initialize, maneuver and operate in a collision free manner. A key maneuver, representative of TPF-I science will be demonstrated by rotating through greater than 90° at ten times the flight rotation rate while maintaining a relative position control to 5 cm 1σ per axis. This is the first step in a full validation the formation control architecture and algorithms and the testbed models developed by the Formation Algorithms & Simulation Testbed while physically demonstrating a scaled version of the approach to achieving the angular resolution required for the detection of terrestrial planets. Milestone TRL 4.

The goal of this milestone is to demonstrate that the developed formation algorithms can execute a scaled, two-spacecraft version of the most precise maneuver for TPF-I – a formation rotation – in an end-to-end, flight-like environment with performance traceable to flight. An end-to-end environment is required so that all sub-system interactions and algorithm and software interfaces that affect formation performance are included. As an example of such a sub-system interaction, consider that each TPF-I spacecraft will have its own flight computer and clock. Therefore, on start-up or after re-boot, the control cycles of each spacecraft will have arbitrary skew: one spacecraft may be firing its thrusters while another is reading its sensors. This skew introduces significant delay in the communication of formation control data between spacecraft, thereby degrading performance. To avoid this delay, an algorithm was developed as part of this task to synchronize the control cycles of multiple spacecraft to the millisecond level via inter-

spacecraft communication. An end-to-end testbed that includes such interactions is needed to fully validate formation algorithms.

The ability to precision formation fly depends on sensors, communication, actuators and formation guidance, estimation, and control algorithms and the interactions of these sub-systems with each other and the environment. These algorithms are collectively referred to as formation algorithms or the Formation and Attitude Control System – FACS. The purpose of the FCT and the FAST, an associated distributed real-time simulation environment, is to demonstrate the technological maturity of FACS, that is, to demonstrate the formation algorithms in a realistic system-of-systems environment.

To do so, several milestones are planned. In each milestone the exact same formation algorithms are used. The formation algorithms do have their parameters tuned to the specific system they are being demonstrated on (e.g., the thruster configuration in the FCT is different from flight, which changes the input file, but the same thrust allocator code is run), but again, the algorithms are the same.

The planned milestones are: 1) Demonstrate precision formation flying in the FCT with 2 Robots (this shows the basic ability to precision formation fly), 2) Simulate the 2-Robot FCT in FAST with Comparable Performance (this validates the FAST simulation environment), 3) Demonstrate precision formation flying in the FCT with 3 Robots (this shows more complex formations can be controlled), 4) Simulate 5 Spacecraft TPF-I in FAST (this is the highest-fidelity ground emulation of TPF-I flight performance using a validated simulation environment and hardware-tested formation algorithms). Additional milestones address robustness to faults.

Given formation algorithms, the more capable sensors, communication, and actuators are, the greater the precision that can be achieved. Error budgets, modeling, and analysis provide the link between sub-system capabilities and system-level performance resulting from formation algorithms.

For the FCT, performance requirements must be sufficiently precise that flight-relevant system interactions that affect formation performance are exercised (e.g., if a communication packet is dropped, will it affect performance?). For this milestone, the performance requirements are a factor of 15 looser than flight due to testbed constraints, principally larger disturbances and sensor noise. However, the FCT requirements are shown to be sufficiently aggressive via error budgets (i.e., a dropped packet will have an effect). Finally, the exact same formation algorithms running on the FCT robots have been shown capable of achieving flight performance in stand-alone, non-real-time simulations with flight sensor noise and disturbances levels (Scharf et al. 2004b).

Summarizing, the purpose of the above series of milestones is to demonstrate formation algorithms – shown to be capable of flight performance in lower-fidelity simulations – in both a high-fidelity, realistic (in terms of system interactions) hardware testbed and a distributed, real-time, and validated simulation environment. The traceability to flight for

this milestone is provided through analyses and error budgets that are part of the milestone success criteria.

This milestone for precision formation flying will show that, consistent with the FCT sensor precision and disturbance level, formation algorithms and software have been integrated seamlessly with flight-like communication, sensor, and actuator sub-systems to execute a scaled-version of the most precise formation maneuver needed for TPF-I. The principal investigator for the Formation Performance Milestone is Daniel Scharf at NASA’s Jet Propulsion Laboratory.

2. The Formation Control Testbed

The Formation Control Testbed (FCT) is a system-of-systems, robotic environment for ground validation of the formation algorithms being developed for TPF-I (Regehr et al., 2004). The FCT consists of two robots with flight-like hardware and dynamics, a precision flat floor for the robots to operate on, ceiling-mounted artificial stars for robot attitude sensing and navigation, and a “ground control” room for commanding the robots and receiving telemetry. The robots and part of the flat floor are shown in Figure 1. A detailed view of a robot with specific hardware identified is given in Figure 2. Each robot has a lower translational platform and an upper attitude platform. The attitude platform is the “spacecraft” and is completely disconnected from the translational platform. The attitude platform/spacecraft houses the avionics, actuators, sensors, inter-robot and



Figure 1: The Formation Control Testbed (FCT). Shown are the two robots on the flat floor with Jason Keim, the FCT Operations Lead. The floor is flat to 0.002 in., level to 120 μ rad, and spans a 7.3 m x 8.5 m area. The robots’ attitude platforms (shown tilted for each robot) also float on spherical air bearings. As a result, the attitude platforms have extremely low-friction 5DOF motion. The final, vertical degree of freedom will be provided by retrofitted vertical stages that can translate 0.5 m. The robots serve as the system-level testing ground for flight software developed for space applications in formation flying.

“ground”-to-robot wireless communication antennae, and the spacecraft processors. The translational platform provides both translational and rotational degrees of freedom to the attitude platform via (i) linear air bearings (the black, circular pads at the base of each robot) that allow the entire robot to float freely on the flat floor, and (ii) a spherical air bearing at the top of the vertical stage (the black, vertical cylinders). As a result, each robot currently has five degrees-of-freedom (DOF): two in translation and three in rotation. For the final, vertical translational degree of freedom, telescoping vertical stages with 0.5 m of travel are being retrofitted this year. The robots will then have all 6 DOFs. The formation algorithms are designed for all six degrees-of-freedom.

The FCT is housed in the former Celestarium, which had been used to calibrate star trackers. As a result, the FCT has a 12.2 m diameter circular floor space and a 7.6 m high, dome-like ceiling. See Figure 3. This ceiling is ideal for mounting artificial stars, as discussed subsequently. The precision flat floor that the robots operate on is fit within the 12.2 m diameter floor space. During FCT design, several types of flat floor were considered (e.g., granite and epoxy). The final flat floor consists of fourteen 1.2 m x 3.7 m metal panels ground to a flatness of 0.002 in. Each panel is mounted on a support structure that has coarse and vernier leveling screws. Periodic laser surveys of the floor are used to ensure that steps between panels are less than 0.001 in. (25.4 μm) and floor slope is less than 120 μrad . The resulting 7.3 m x 8.5 m flat floor was part of the FCT Technology Critical Design Review (CDR) and is sufficient to demonstrate nominal TPF-I formation maneuvers, such as formation rotations and collision avoidance.

To be as flight-like as possible, each robot is equipped with a typical single-spacecraft attitude control suite of reaction wheels, gyros, and a star tracker. Thrusters, which are necessary for formation flying,¹ are also available for attitude control. In particular, star trackers require stars. To provide artificial stars, down-looking infrared LEDs are mounted on the ceiling of the FCT. See Figure 4. The star tracker measures the direction (two angles) to at least three stars, giving six pieces of information. From this information, the attitude *and position* of a robot can be determined with respect to the “inertial” Room Frame. The position of a robot can also be determined since the stars are in the near-field, and hence, the direction to an LED changes as a robot moves.

For TPF-I, the spacecraft will know their absolute positions to no better than several kilometers. All precision formation flying will be performed using output from on-board inter-spacecraft sensors. For the FCT, a direct inter-robot sensor that consists of a fast steering mirror, corner cube, and laser range finder is in development and will be installed on the robots in June 2007. The fast steering mirror on one robot is used to track the retro-reflector on the other robot as they maneuver. This direct sensor is referred to as the Optical Pointing Loop (OPL) and will be accurate to ~ 2 mm 1σ . Once installed, the OPL will be used for formation flying, and the star tracker position measurements will serve as an independent confirmation.

¹ Thrusters are necessary to provide translational forces. Alternate translational actuation schemes utilizing, for example, electromagnets, charged spacecraft, or solar pressure, would still require a back-up set of minimally capable thrusters.

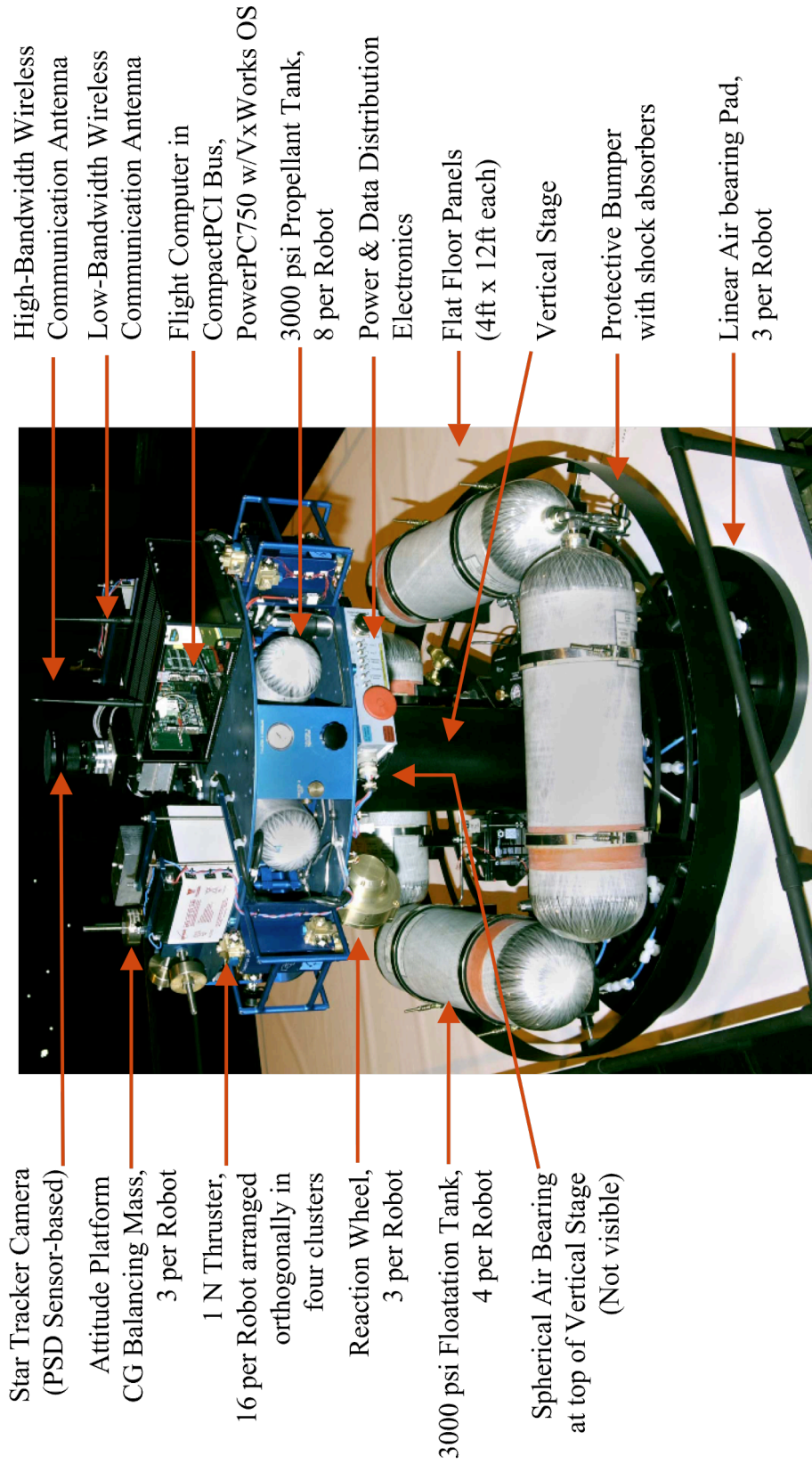


Figure 2. Detailed View of an FCT Robot

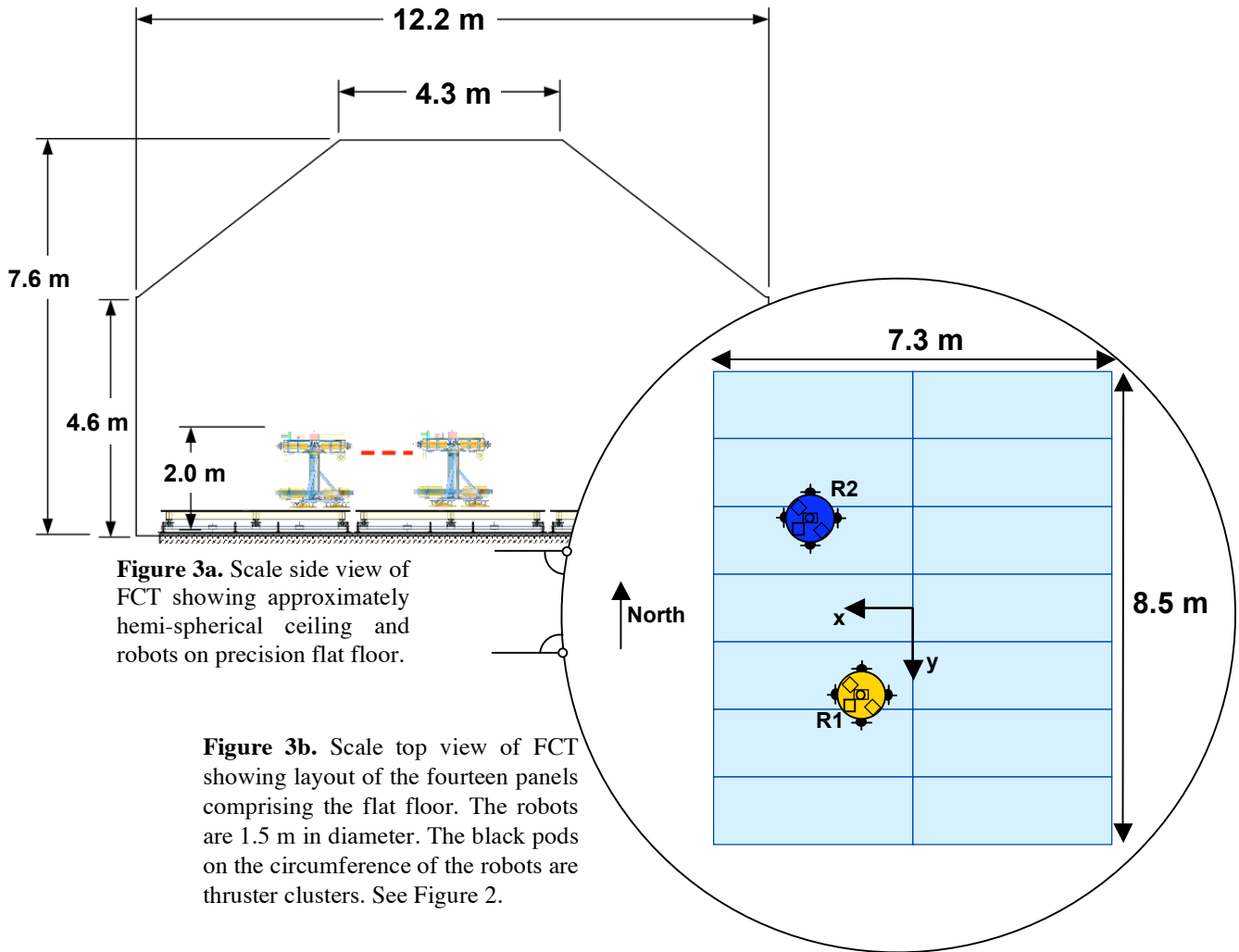


Figure 3. Scale Side- and Top-Views of the FCT.

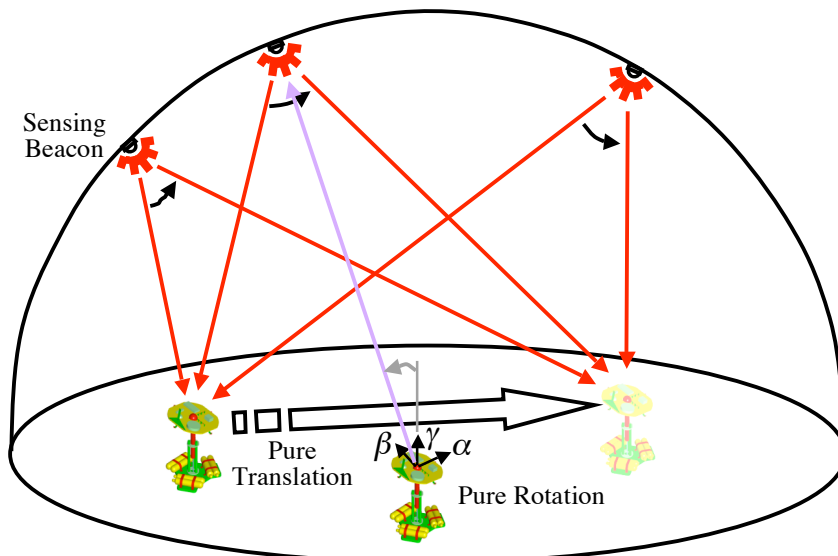


Figure 4. Illustration of Star Tracker Measurement Concept. The star tracker measures the direction to three beacons. These directions change both as a robot translates and as its attitude platform rotates.

For the milestone demonstrations, the inter-robot position is determined by differencing Room Frame positions as measured by the star trackers. This approach is similar to differencing GPS position measurements in LEO, for example, as was done during the pre-terminal rendezvous stage of the DART mission. To ensure traceability to flight, the Room Frame positions are communicated between robots and differenced *before* being passed to the Formation and Attitude Control System (FACS) software. That is, the formation algorithms only have access to the inter-robot position measurement, as will be the case for TPF-I.

The precision of the FCT star tracker is 6 arcmin 1σ in attitude and 0.9 cm 1σ in Room Frame position. Since inter-robot position is determined by differencing two Room Frame position measurements, the effective inter-robot position measurement precision is $\sqrt{2} * 0.9 \text{ cm} = 1.3 \text{ cm } 1\sigma$. Regarding attitude, a robot's attitude estimator uses gyro measurements to improve the precision of attitude knowledge to 2 arcmin 1σ .

The FCT star trackers have been calibrated by placing them on a Physik Instrumente M-85 hexapod, which has a 6 DOF repeatability of $\pm 2 \mu\text{m}$ and $\pm 1 \text{ arcsec}$ in translation and rotation, respectively. For calibration, a laser surveyor was used to accurately determine the position and attitude of the hexapod in the FCT Room Frame. Then, a star tracker was translated and rotated on the hexapod to several poses, and star tracker data was taken. This data was used to fit Zernike polynomials for lens aberrations. Details of this calibration and the algorithm that processes star tracker measurements into position and attitude are given in (Shields 2005).

There is currently no secondary truth sensor in the FCT. Several COTS truth sensors were considered (as opposed to in-house developed sensors that were deemed too expensive) as part of the FCT design process. These sensors were reviewed in technology preliminary and critical design reviews. The only viable candidate was a laser scanning system by ArcSecond, Inc. However, this system has not yet been within budget constraints of the FCT. See Appendix B for further details.

2.1. Formation Control Overview

Details of the FACS are given in (Scharf et al. 2004b). At the very highest level, the formation algorithms have the following architecture. The control architecture is Leader-Follower: one robot is designated the Leader and one the Follower. The Leader robot only applies feedforward translational forces to effect maneuvers. The Follower applies both feed-forward and feedback translational forces to maintain the desired inter-robot (i.e., relative) position. In particular, the Follower runs its own translational controller to maintain the relative position based on relative position and velocity commands from the Leader and the Follower-estimated relative position and velocity. Both robots control their attitudes independently. However, formation estimation does depend on attitude knowledge (Scharf et al. 2004b). The guidance architecture is hybrid: each robot has its own attitude guidance and the relative, translational path-planning occurs on the Leader. The Leader communicates the desired relative position and velocity to the Follower each time-step for control, as well as feedforward translational accelerations and high-level

attitude commands for the Follower’s attitude guidance algorithm. Each robot has its own formation estimator. All measurements (currently one inter-robot position in the FCT) are communicated between robots each time-step for estimation. Each robot maintains its own estimate of the formation state for collision avoidance and fault responses.

Having presented the FCT, the milestone performance requirements are discussed in detail.

3. Milestone Requirements

The FCT milestone goal is to demonstrate on the ground an end-to-end, system-level precision formation flying capability that is scaleable to flight. First, the performance requirements for the milestone and their relation to TPF-I flight requirements are discussed, and then the formation rotation maneuver to be demonstrated is specified.

3.1. Performance Requirements

Table 1 summarizes the top-level flight requirements for TPF-I. These requirements depend on operating mode, of which there are four: safe stand-off, reconfiguration, hand-off, and observation. These modes are based on operational needs. For each mode, requirements are listed separately for knowledge and control of (i) position (ii) attitude, and (iii) the time-rate-change of these three quantities. The attitude requirement is with respect to an inertial frame and the position requirement is with respect to the Combiner spacecraft. The knowledge requirements are 1σ values for sensor precision in each axis. For example, the requirement in Table 1, Line 9, Observation Column, means that the sensor will measure the position of one spacecraft with respect to another to 0.1 cm 1σ in each Cartesian axis. The control requirements are plus/minus bounds in each axis. For example, the requirement in Table 1, Line 10, Observation Column, means that a spacecraft must remain within ± 1 cm in each Cartesian axis of its commanded position with respect to another spacecraft. That is, it must remain within a cube with a side length of 2 cm that is centered on the commanded relative position. See Appendix C for a discussion of specifying formation flying requirements as “cubes” rather than range/bearing volumes.

For TPF-I, the highest precision formation flying requirements are during science observations. Nulling requires sub-nanometer optical path-length control. There are also path-length rate control requirements derived from the capabilities of the fringe-tracking system. Focusing on the path-length control requirements for exposition, it is not possible to control inter-spacecraft positions to the sub-nanometer level. Hence, the control approach for the TPF-I distributed interferometer has two levels. In the first level, inter-spacecraft positions, which are directly related to path-lengths, are controlled via formation flying. In the second level, adaptive optics, fast steering mirrors, and optical delay lines (ODLs) cancel the residual path-length errors to the sub-nanometer level. As a result, formation flying requirements are driven by stroke and rate limitations of the optics and fringe-tracking system.

Given ODL stroke limits of ± 10 cm, performing a geometrical analysis of the science configuration, and adding margin, the inter-spacecraft positions are required to be controlled to ± 1 cm in all axes. Based on the TPF-I flight requirements of Table 1, specific requirements are levied on the ground technology development during pre-Phase A efforts. See Tables 2 and 3 (Table 3 is on page 13). The formation requirements for the FCT are relaxed from TPF-I requirements due to increased sensor noise and disturbance level. However, the formation algorithms used to control the FCT robots have been shown in lower-fidelity simulations to be capable of flight performance when flight sensor and environmental characteristics are applied.

Table 2 gives select requirements from the FCT Technology-CDR. *The principal relaxation is of the precision formation control requirement from ± 1 cm to 5 cm 1σ .* The FCT performance requirement can be approximated as an absolute bound by taking the 3-sigma value, that is, as ± 15 cm.

Table 1. Flight Requirements for Formation Flying with the TPF Interferometer.
Knowledge requirements are 1σ per axis and control requirements are \pm bounds per axis.

Ref	Parameter	TPF-I Formation Flying Requirements per Operating Mode				Observation
		Units	Safe- Standoff	Reconfig- uration	Hand- off	
1	Operating Envelope					
2	Formation Sensor		Acquisition Sensor	Acquisition Sensor	Medium Sensor	Fine Sensor
3	Inter-S/C Range	m	20–200	20–10,000	20–80	20–80
4	Inter-S/C Bearing	–	4π sr	4π sr	10° cone	10 arcmin cone
5	Inter-S/C Range Rate	< cm/s	200	200	5	0.2
6	Inter-S/C Bearing Rate	< arcmin/s	60	60	10	2.5
7	Max. Acquisition Time	s	5	30	10	10
8	Relative Position					
9	Knowledge	cm	100	50	1	0.1
10	Control	cm	500	250	5	1
11	Relative Velocity					
12	Knowledge	cm/s	1	0.1	0.1	0.005
13	Control	cm/s	5	0.5	0.5	0.050
14	Inertial Attitude					
15	Knowledge	arcmin	1	1	0.1	0.1
16	Control	arcmin	60	60	3.0	1.0
17	Inertial Attitude Rate					
18	Knowledge	arcsec/s	1	1	1	1
19	Control	arcsec/s	5	5	5	5

Table 2. Select FCT Requirements from Technology-CDR.

REFERENCE	REQUIREMENT
2.01	The total relative translation motion error between the Combiner Robot Frame and any Collector Robot Frame shall not exceed 5.0 cm (per axis, 1σ).
5.02	FCT shall be able to execute two corners of a polygonal array rotation with 1/4 chord at both ends (for a total of 1-1/2 chords), at 10 times the TPF flight rate of 1 revolution/12 hours, with the number of sides of the polygon defined by the radius of rotation and the size of the control deadband in translation.

Considering attitude, the TPF-I precision attitude requirement is ± 1 arcmin with a sensor precision of 0.1 arcmin 1σ . Given the FCT attitude estimator precision of 2 arcmin 1σ (Shields et al. 2007) and this 10-to-1 of control to sensor requirement, the FCT attitude requirement is derived as ± 20 arcmin. However, as discussed in the next paragraph, the FCT attitude control requirement is stated as a 1σ value, specifically, 6.7 arcmin 1σ .

The FCT requirements have been specified in terms of 1σ statistical bounds instead of absolute bounds. The reason for this is that absolute bounds are an approximation when disturbances, sensor noise, and actuator saturations are non-trivial. Figure 6 shows an example of simulated formation control errors from the FCT Error Budget with $\sigma_{\text{sensor}} = 1.3$ cm, thruster saturation, and a varying floor slope disturbance due to robot motion. The statistics for this example are shown in Table 4, that is, the percentage of time-steps with control errors of greater than one, two, and three times σ_{sensor} . As can be seen from the statistics, these time histories are a favorable example since more than the expected amount time-steps have an error of less than $1\sigma_{\text{sensor}}$. However, this example illustrates that there is statistically a non-zero fraction of control errors that will exceed a given absolute bound.

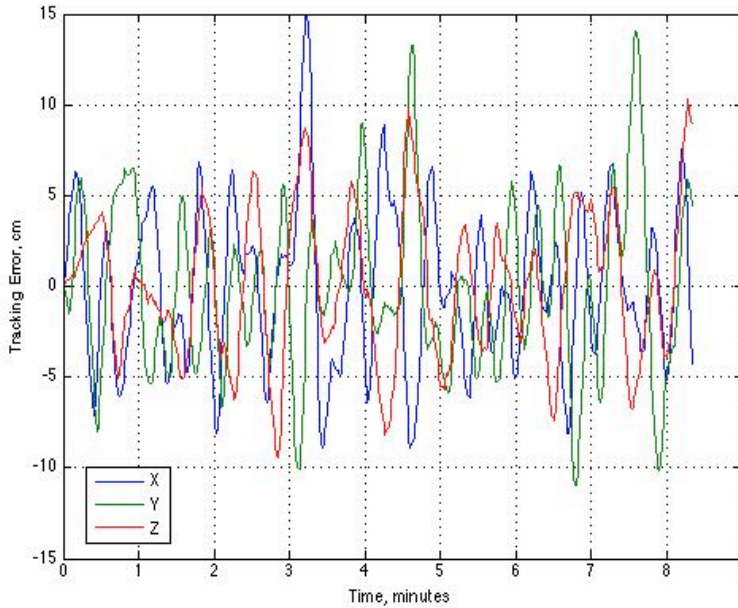


Figure 6. Example Simulated Time Histories of Formation Control Errors by Axis from the FCT Error Budget. By axis, the standard deviations of the control errors are [4.4 4.6 4.0] cm.

Table 4. Statistics for Formation Control Example of Figure 6.

Axis	% of Time Steps with Control Error...		
	$> 1\sigma_{\text{sensor}}$	$> 2\sigma_{\text{sensor}}$	$> 3\sigma_{\text{sensor}}$
X	16.6	2.0	1.0
Y	17.4	3.2	0.40
Z	18.8	3.6	0
Expected %	31.7	4.6	0.28

3.2. Formation Maneuver Specification

The maneuver to be demonstrated is a synchronized formation rotation, in which a formation rotates as a virtual rigid body. This maneuver will be used for science observations. A key aspect is that spacecraft attitudes must remain synchronized with their relative positions. This synchronization is needed to maintain the interferometric links between spacecraft. We first review the formation rotation requirements for flight and then scale it to the FCT per the ground demonstration requirements.

Formation rotations for TPF-I include a modification to account for pulse-width modulated thrusters. When such thrusters fire to provide centripetal acceleration, the resulting impulse can cause fringe-loss. Hence, all pulse-width thrusters are restricted to firing in a 6 second window out of every 60 seconds. During the remaining 54 seconds, the fringe is re-acquired (if necessary) and a science measurement of the fringe is taken. Since the thrusters can only fire periodically to provide centripetal acceleration, the TPF-I spacecraft actually travel on a polygonal approximation to a circle. See Figure 6. Per requirement 5.10 of Table 2, a full TPF-I flight rotation takes 12 hours.² Hence, the angular chord length θ is 0.5 deg and the rotation rate is 0.5 arcmin/s.

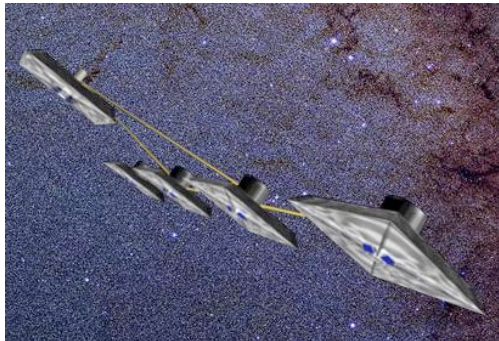


Figure 6a. Linear array of four Collector spacecraft with Combiner spacecraft offset.

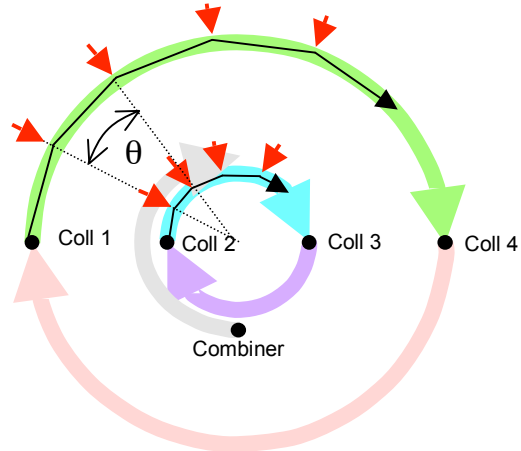


Figure 6b. Formation rotation schematic for TPF-I showing half rotation about center of linear array and, for two of the Collectors, the polygonal paths taken. All spacecraft follow an appropriately-sized polygon with angular chord length θ . Red arrows indicate the 6-second thruster firing windows to turn corners

Figure 6. TPF-I Science Configuration and Formation Rotation Schematic.

² The current TPF-I rotational period is 50,000 s (13.9 hrs). The requirements for the FCT were derived from TPF-I requirements frozen at the earlier value of 12 hrs. This freeze was done to prevent the FCT from chasing smaller variations in the evolving TPF-I design.

Table 3. Requirements of the Formation Control Testbed vs Flight Requirements

Parameter	Flight Performance	Formation Control Testbed	Comments
Number of spacecraft	5	3	FCT has 2 as of FY07
Operational capability			
Standalone operations	5 yrs	36 min	Total FCT floatation time
Mission duration	5 yrs	5+ yrs	
Observational duration	~14 hrs	~15 min	“Observation on the fly”
Availability	Continuous	8 hrs/day	Ground testbed facility
Motion DOFs	6	5+1	FCT has 1 articulated DOF
Operating envelope	3D space	2D plane	Limited out-of-plane FCT motion
Control			
Relative Position	±1 cm	≤±15 cm (5 cm 1σ)	FCT med. sensor 13x noisier than flight fine sensor, larger disturbance
Absolute Attitude	±1 arcmin	±20 arcmin (6.7 arcmin 1σ)	FCT attitude knowledge 20x noisier than flight
Fault recovery	Active and passive	In development	FCT fault scope TBD
Flight capability			
Sensor			
Inertial	Gyro/accel	Gyro/accel	
Celestial	Star tracker	Pseudo-star tracker	
Relative	Coarse, Med., Fine	Medium	Fine FCT sensor being developed
Actuator	Thrusters, RWA	Thrusters, RWA	
Control Architecture	Distributed	Distributed	
Control Algorithms	Flight	Flight	Developed by FAST
Dynamic DOFs	6	5	FCT: +1 articulated DOF
Range of motion			
Attitude In-plane	360°	360°	
Attitude Out-of-plane	± 45°	± 30°	
Linear-in-plane	Limited by sensor	Limited by lab	
Linear-out-of-plane	Limited by sensor	± 0.25 m	Emulate science deadbands
Maneuvers			
Acquisition	3D space	2D space	
Array rotation in-plane	Yes	Yes	
Array re-sizing	Yes	Yes	
Array re-targeting	Yes	Yes	
Collision Avoidance	3D space	2D space	

The FCT robots are not required to drift thrust-free for 54 seconds since the ratio of control-authority to disturbance-level is 150 for TPF-I (the thrusters are sized for centripetal acceleration), but only 6 for the FCT.³ However, the FACS is capable of meeting thrust window constraints in lower-disturbance environments (Lurie 2003, Scharf 2004b). The TPF-I design is continually evolving and so For example, even though the FCT demonstrations will not have “thrust-free” periods, the formation guidance algorithms incorporate functionality from an earlier “snapshot” of TPF-I and so generate the polygonal trajectories of Figure 6b.

The parameters that must be specified for a formation rotation are given in Table 5. Included are the TPF-I parameter values, the FCT parameter values, and the requirements the FCT parameter values are derived from. From these parameters, the formation demonstration will take approximately 18 minutes (the time to rotate through 90 deg. at 5 arcmin/s).

Table 5. Formation Rotation Parameters for TPF-I and the FCT.

#	Parameters	Unit	TPF-I	FCT	Requirement Traceability
1	Rotation Axis, λ	N/A	Within 45 deg. of anti-Sunline	Vertical axis of FCT	FCT currently 2D in translation. With retrofit of Vertical Stage, vectors within 15 deg. of vertical can be used.
2	Rotation Rate, ω	arcmin/s	0.5	5.0	Table 2, Requirement 5.02: 10 x Flight
3	Rotation Angle, ϕ	deg.	360	90	TPF-I Technology Plan, pg. 58.
4	Vehicle Separation, b	m	20-80	≥ 3.44	No governing requirement. Selected minimum separation results in speed of 0.0025 m/s, consistent with disturbance frequency and control bandwidth. ⁴
5	Angular Chord Length, θ	deg.	0.5	40, 20	Table 2, Requirement 5.02: 1 side of polygon plus $\frac{1}{4}$ chord on either side. A $\frac{3}{4}$ chord is allocated to “spin-up” for a total of 2.25 chords in 90 deg. (Line 3). ⁵
6	Formation Control	\pm cm per axis	1	15	Table 2, Requirement 2.01.
7	Attitude Control	\pm arcmin per axis	1	20	Derived from 10-to-1 ratio of Table 1, Lines 16 and 15 and the FCT attitude knowledge of 2 arcmin.

³ The principal translational disturbance to the TPF-I formation will be differential solar pressure. Using the latest baseline TPF design, the disturbance acceleration due to solar pressure is $\sim 2e-8$ m/s². TPF-I thrusters will be capable accelerating the spacecraft at $\sim 3e-6$ m/s². The FCT floor has a residual flatness error, which is variation about mean floor slope, of ~ 51 μ m (Regehr 2004). Since the distance between air-bearings is 1 m, this flatness error results in a maximum acceleration of $5e-4$ m/s² on each robot. Further, since each robot is subject to different flatness errors, the maximum differential acceleration on the robots is 1 mm/s². The FCT thrusters are capable of accelerating the robots at 6 mm/s².

⁴ The primary disturbance to the FCT formation is residual floor unevenness. This disturbance varies with the location of the robot air-bearing pads. Hence, the speed of a robot determines how quickly the disturbance varies. The formation control algorithms include an integrator to overcome the largest flatness variations. The integrator can take up to ~ 100 s to reach maximum force. This “rise time” is typical for 1 Hz control loops such as are implemented in the FCT and in flight mission designs such as for ST-

The FCT demonstration maneuver is illustrated in Figure 7. The first portion of the 90 deg. rotation is referred to as the Spin-Up Regime (the red, dotted lines) and allows initial

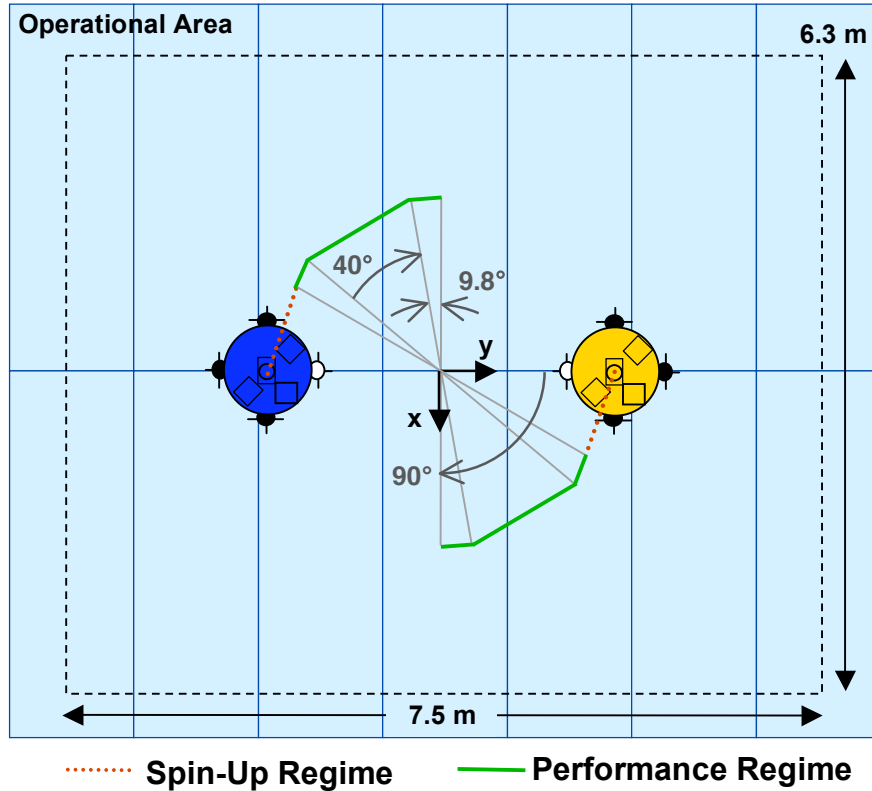


Figure 7. Illustration of the Precision Synchronized Formation Rotation Maneuver for the FCT as Specified in Table 5. In the Spin-Up Regime initial maneuver transients decay. Precision formation control is required in the Performance Regime. The entire maneuver is directly scalable to TPF-I, where inter-spacecraft separations vary from 20 m to 80 m. The maneuver is synchronized in that the robot attitudes rotate to maintain the white thruster clusters (colored for emphasis) pointed along the inter-spacecraft vector. This synchronization allows inter-spacecraft pointing loops for the TPF-I interferometer to remain locked. For a maximum baseline demonstration, the robot starting positions would be rotated 45 deg.

3/StarLight and ST-9. For highest precision, the disturbance should vary no faster than the integrator can respond. The air-bearing pads have a span of 1 m, and the disturbance is approximated as varying when the pads have moved a quarter span, or 0.25 m. At 0.0025 m/s, the disturbance varies no faster than $0.25 \text{ m} / 0.0025 \text{ m/s} = 100 \text{ s}$, as desired. Maneuvers at larger robot separations will be performed when the OPL is installed on the robots. The OPL is a formation sensor 10 times more precise than the current formation sensor, and it will enable a shorter integrator rise time (by reducing sensor noise, the control bandwidth can be increased, and rise time is inversely proportional to bandwidth).

The maximum separation in the FCT compatible with a 90 deg. rotation is 6.78 m, which includes a margin of 1.0 m for mean floor slope. Mean floor slope causes the formation as a whole to drift. The robot separation will be increased as much as possible above the minimum specified.

⁵ Requirement 5.02 in Table 2 states the FCT formation rotation will follow a polygon with the “number of sides of the polygon defined by the radius of rotation and the size of the control deadband in translation.” This requirement was clarified by the TPF-I Design Team as: determine the two-dimensional regular polygon with the fewest sides that can fit within a torus with overall diameter equal to b and tube radius equal to the two times the control bound. Applying this criterion, the number of polygonal sides is given by the rounded value of $\pi / \arccos[1 - 2(\text{control bound}) / b]$. For the FCT control requirement and $b = 3.44 \text{ m}$, the polygon has 8 sides, which gives a θ of 45 deg. This value is consistent with Table 5, Line 5. An angular chord length of 20 deg was also selected, since this corresponds to a linear chord length of 1.2 m, which will be distinguishable with the FCT formation performance.

maneuver transients to decay. Then precision formation control will be demonstrated in the Performance Regime (the green, solid lines) for 1.5 chords as required by Table 2. Each chord is 2.35 m long. Hence, the quarter chords are 0.59 m long and subtend 9.8 deg. The Operational Area is shown for reference. It includes a 0.5 m margin to account for mean floor slope. Mean slope does not affect formation performance, but it can cause the formation as a whole to drift.

4. Computation of the Metric

4.1. Definitions

The TPF-I Formation Control Milestone 2 demonstration requires measurement and control of inter-robot position and absolute robot attitudes. In the following paragraphs we define the terms involved in this process, enumerate the measurement steps, and specify the data products.

- 4.1.1 Formation and Attitude Control System (FACS).** The C-code software module that runs in real-time on each robot and contains the formation and attitude estimation, guidance, and control algorithms. The FACS is discussed in detail in (Scharf et al. 2004b).
- 4.1.2 Room Frame.** The reference frame of the FCT. The origin is at a reference block in the center of the FCT. The X and Y axes are defined by fixed posts (a second post for each axis was installed using a laser surveyor since the reference block has since been covered by the flat floor). The Z axis is defined by the cross product of the X and Y axes.
- 4.1.3 Robot Body Frame.** The reference frame of a robot. The origin is at the center of curvature of the spherical air bearing. The axes are defined by reference posts affixed to the attitude platform.
- 4.1.4 Absolute Position.** The position vector, r_i , $i = 1, 2$, of the origin of a robot's Body Frame in the Room Frame as determined by the star tracker and represented in the Room Frame.
- 4.1.5 Relative Position.** The position of Robot 2 (R2) with respect to R1 as determined by differencing Absolute Positions, $r = r_2 - r_1$.
- 4.1.6 Desired Relative Position.** The commanded relative position, r^d , as calculated by the formation guidance algorithm. See Figure 8 for an example as generated by the C-coded algorithm running on the robots. In this example, three successive synchronized rotations are commanded about different axes with different rotation angles and angular chord lengths.

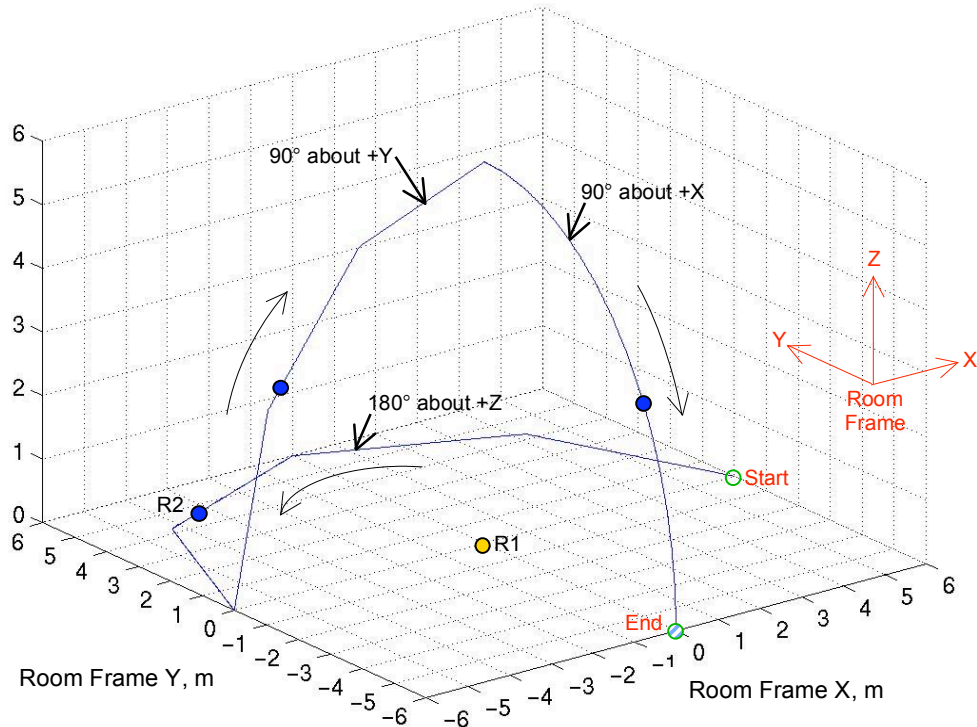


Figure 8. Example Desired Relative Positions as Output by Formation Guidance Algorithm to Demonstrate Algorithm Capabilities. The robots will not actually follow these paths. The guidance algorithm can rotate a formation about an arbitrary axis with arbitrary chord length (subject to geometrical constraints and vehicle capabilities). The desired relative positions are shown with respect to the Leader, which in this case is Robot 1 (R1). As shown in Figure 7, both robots actually rotate about the geometric center of the formation. The rotations correspond to a 180 deg. rotation about the Z-axis with 45 deg. chords, a 90 deg. rotation about the Y-axis with 30 deg. chords, and a 90 deg. rotation about the X-axis with 6 deg. chords. For the last rotation, the linear chord length is 10 cm, and so at the scale of the plot the rotation looks continuous.

4.1.7 Attitude Estimator. The element of the FACS that combines star tracker attitude measurements with gyroscope outputs to obtain an estimate of the orientation of a robot Body Frame with respect to the Room Frame.

4.1.8 Absolute Attitude. The rotation that takes the Room Frame to the Robot Body Frame as determined by the output of a robot's attitude estimator and represented as a proper quaternion, $q_{RB,i}$, $i = 1, 2$.

4.1.9 Desired Absolute Attitude. The commanded rotation that takes the Room Frame to the Robot Body Frame as calculated by the formation guidance algorithm that synchronizes absolute attitude with the desired relative position. The rotation is represented by a proper quaternion, $q_{RB,i}^d$, $i = 1, 2$.

4.1.10 Translational Control Error. The relative position minus the desired relative position, $r_e = r - r^d$. An example is shown in Figure 6.

4.1.11 Rotational Control Error. The rotation that takes the Desired Absolute Attitude to the Absolute Attitude as represented by the proper quaternion

$q_{e,i} = \text{prop}(\text{conj}(q_{RB,i}^d) * q_{RB,i})$, where $\text{conj}(\cdot)$ is conjugates a quaternion, $\text{prop}(\cdot)$ properizes a quaternion, and $*$ is the quaternion multiplication operator.

4.1.12 Angular Control Error. The representation of $q_{e,i}$ via a vector of angles, g_i , corresponding to the axis/angle rotation parameterization. That is, a rotation may be equivalently represented by the vector $\phi\lambda$, where ϕ is the angle to turn and λ is the unit vector to turn about. When ϕ is small, this vector of angles gives the “small angle” approximation to a rotation. For example, an angular control error of $g_i = [3 \ -2 \ 4]$ arcmin means that to match the absolute attitude and the desired absolute attitude, the Robot Body Frame must be rotated -3 arcmin about the positive x-axis of the Robot Body Frame, 2 arcmin about the positive y-axis of the Robot Body Frame, and -4 arcmin about the positive z-axis of the Robot Body Frame.

4.1.13 Performance Interval. The interval of time when the Desired Relative Position is commanding the green portion of the robot trajectories in Figure 7.

4.1.14 Translational Control Performance. The by axis standard deviations, p_i , of the Translational Control Error during the Performance Interval. An example is given in the caption of Figure 6.

4.1.15 Rotational Control Performance. The by axis standard deviations, $p_{r,i}$, $i = 1, 2$, of an Angular Control Error during the Performance Interval.

4.2. Formation Control Milestone 2 Demonstration Procedure

This section describes the procedure that will be followed to collect data for the milestone validation review. The robots are given high-level commands over a wireless connection from the FCT “Ground” Console. The commands are high-level in that they specify the desired outcome and the detailed path-planning and execution is performed on-board the robots by the FACS. Example commands are given below.

4.2.1 Initial Robot Positioning. The robots will be manually placed in their approximate initial conditions. A command script will be sent to the robots for them to position themselves at the initial conditions for the demonstration. After the robots have converged, they will be shut-down and their computers reset. These actions ensure repeatability from run to run and that the individual “flight” computers on each robot have arbitrary skew in their control cycles. An example command for positioning a robot in the Room Frame (not formation flying) is:

```
facts_cmd ATS_ABS_OFFSET time {20} OffsetVec {0, 1.72, 0}
```

which commands the Absolute Translation System (ATS) to go to the position specified in the offset vector (OffsetVec) in the Room Frame when the on-board clock is at 20 s.

4.2.2 Demonstration Run via Command Script. The robots will be started with a command script that contains all the commands for the demonstration. The robots go through their autonomous check-out modes in 15 seconds. Synchronizing control cycles can take up to 100 s (the need for synchronization is discussed at the bottom of Page 2). At 110 s, the robots will begin formation initialization as specified in the command script uploaded at the beginning of the demonstration. Initialization, during which the attitudes are aligned and formation flying begins, takes 50 s in this scenario. At 170 s, the synchronized formation rotation command activates. The rotation is actually commanded for 100 deg. so that the formation will stop rotating beyond the Performance Interval. At 5 arcmin/s, this rotation takes 20 minutes. The robots are commanded to quit and download telemetry. An example command script for R1 is:

```
fac_cmd BEGIN_FORMINIT time {110}
fac_cmd SYNCH_ROT time {170} Rotation {0, 0, 1.7453} Duration
{1200} LinArcLen {0.6981}
```

The Rotation vector is similar to the g vector in Section 4.1.12 and specifies a 100 deg. rotation about the Room Frame z-axis. The Duration of 1200 s results in a rotation rate of 100 deg. / 1200 s = 5 arcmin/s. Finally, LinArcLen is the length of a chord.

4.2.3 Telemetry Processing. Upon receiving the shut-down command from the FCT Ground Console, the robots de-float their air-bearings and download telemetry to the Ground Console. The telemetry contains all the data necessary to calculate the Translational Control Performance and Rotational Control Performance. These performances are then compared to the required values given in Section 3.1 and reiterated in Section 5.

5. Success Criteria

The following is a statement of the three elements that must be demonstrated to close the TPF-I Formation Control Milestone 2. Each element includes a brief rationale.

5.1.1 Formation Guidance Verification. The time history of r^d and $q_{RB,i}^d$ in telemetry must agree to ± 5 mm and ± 1 arcmin, respectively, with the trajectory specified in Table 5 and shown in Figure 7 for the actual value of inter-robot separation b at the start of the synchronized formation rotation.

Rationale: Since the Translational and Rotational Control Performances are based on the desired relative position and desired absolute attitude, these values are double-checked for correctness. The accuracy specified is a factor of 10 smaller than the performance requirements and ensures the robots are following the proper trajectories.

5.1.2 Translational Control Performance. The per-axis Translational Control Performance must be less than or equal to 5 cm 1σ .

Rationale: *This performance shows that the formation algorithms in FACS and the flight-like sensing, actuation, and communication sub-systems have functioned together to achieve the highest formation performance consistent with sensing precision.*

5.1.3 Rotational Control Performance. The per-axis Rotational Control Performance must be less than or equal to 6.7 arcmin 1σ .

Rationale: *This performance shows that the formation algorithms in FACS and the flight-like sensing, actuation, and communication sub-systems have functioned together to achieve the highest synchronized attitude performance consistent with sensing precision.*

5.1.4 Multiple Guidance Profiles. The 90 deg rotation must be performed with an angular chord width of 40 deg and 20 deg.

Rationale: *TPF-I will tailor its rotations to specific target stars. By demonstrating rotations with two different angular chord widths, the flexibility of the formation guidance algorithm is demonstrated.*

5.1.5 Repeatability. The entire demonstration for both angular chord widths must be repeated three times while meeting criteria 5.1.1-4 with at least two days between demonstrations. Demonstrations of different angular chord widths may occur on the same day.

Rationale: *This repeatability shows the Precision Formation Control capability is robust to variations in the testbed environment.*

5.1.6 Formation Timing. During all demonstrations, timing information for each formation mode and maneuver will be recorded. There is no performance requirement on timing.

Rationale: *Since TPF-I will have cryogenic operating temperatures, maneuver times are critical to telescope design and overall observational efficiency. Future milestones will more completely address timing. However, the process is being initiated as part of this milestone, and documentation of maneuver times will be part of future milestone success criteria.*

5.1.7 Traceability to Flight via Error Budgets. Provide analyses and error budgets showing that the FACS demonstrated in the FCT can achieve flight performance given flight-level spacecraft and environment properties.

Rationale: *Since exact flight performance is not being demonstrated, the performance of the FCT formation in this milestone must be shown to provide a path forward to flight.*

6. Certification Process

The TPF-I Project will assemble a milestone certification data package for review by the EIRB. If the success criteria are determined to have been met, the Project will submit the finding of the review board, together with the certification data package, to NASA HQ for official certification of milestone compliance. In the event of disagreement between the Project and the EIRB, NASA HQ will determine whether to accept the data package and certify compliance or request additional work.

The milestone certification data package will include a discussion of how each element of the milestone was met, an explanation of each plot, appropriate tables and summary charts, and a narrative summary of the overall milestone achievement.

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Appendix A: Table of Acronyms and Abbreviations

ATS	Absolute Translation System
CDR	Critical Design Review
COTS	Commercial Off The Shelf
DART	Demonstrator for Autonomous Rendezvous Technology
DOF	Degree Of Freedom
FACS	Formation and Attitude Control System
FCT	Formation Control Testbed
GPS	Global Positioning System
LED	Light Emitting Diode
ODL	Optical Delay Line
OPL	Optical Pointing Loop
RWA	Reaction Wheel Assembly
TPF-I	Terrestrial Planet Finder Interferometer

Appendix B: Further Details on COTS Truth Sensors

The principal challenge in a truth sensor for the FCT is to obtain 6DOF information with sub-centimeter and arcminute-level accuracy over a dynamic range of 7 meters. If the robots remained in the same positions with only tens of centimeters variations, a test-stand as is used for JWST would be applicable. Other, 3DOF formation flying testbeds with appreciable dynamic ranges have used GPS pseudo-lites and ceiling-mounted camera systems. These two systems are significantly simplified by the 3DOF nature of these testbeds: they only need to sense planar position and scalar attitude, which makes the, say, colored LEDs in the camera frame a straightforward transformation of their pixel position.

Camera systems were ruled-out since the achievable accuracy for a given complexity/cost was not feasible for our 6 DOF application; consider MSFC's AVGS and StarVision's VisNav products which achieve ~1 cm position but only 1 degree in attitude. The accuracy of RF-based sensing systems (including pseudo-lites) is limited in the FCT due to multi-path from the metallic floor. Ultrasound-based systems are corrupted by thruster firings. Capacitive sensing is clearly not applicable. Hence, a laser-based system must be used.

There are two general types of laser-based distance measuring equipment: point-to-point interferometers such as the HP 5527A and point cloud-producing laser surveyors such as the Reigl Laser Radar (see Figure B.1). Estimating position and attitude from point

clouds is a complex machine vision problem. Point-to-point interferometers do not have an appreciable FOV, and so steering mirrors and control loops to track retro-reflectors on the robots would have to be added. Additionally, there would still be the machine-vision problem of differentiating the retro-reflector returns.

These are all solvable problems, but in-house development would become prohibitively expensive. Candidate commercial systems included (i) a scanning laser head with retro-reflectors and proprietary machine vision software by ArcSecond, Inc., (ii) an infrared LED-based system similar to the current star tracker by 3rd Tech, and (iii) another scanning laser head with multiple detectors as opposed to retro-reflectors by MacLeod Technologies, Inc. As of the FCT CDR, the 3rd Tech system was still maturing and the MacLeod Technologies, Inc. scanner was for planar applications. While it could be extended to 6DOF in principle, it would become another in-house development. The cost of the ArcSecond system lowered its priority.

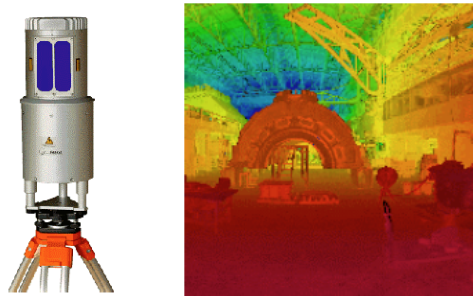


Figure B.1. Reigl scanning laser radar and example point-cloud data.

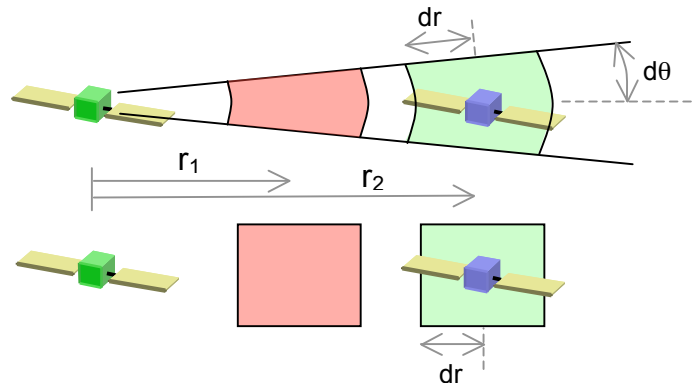
Appendix C: Specification of Formation Flying Requirements

Specifying formation flying requirements in terms of range and bearing is an inherited method that is misleading since a reference range is needed. The formation flying requirements are derived from stroke-limitations of adaptive optics that modify the optical path lengths in the interferometric payload. There are two sets of optics that bear on the formation requirements: optical delay lines (ODLs) and fast-steering mirrors (FSMs). The FSMs route light between spacecraft, and the ODLs correct for pathlength differences down to the sub-nanometer level. The ODLs require spacecraft to remain in a fixed volume with respect to neighboring spacecraft. See Figure C.1. This volume does not need to change with inter-spacecraft range because the ODLs stroke-limits remain constant. However, in specifying this volume as range and bearing, which is more intuitive to some, a confusion is introduced. The primary flight requirement is that each spacecraft remains in a cube with sides of 2 cm with respect to a specified neighbor spacecraft. Since planned spacecraft separations vary from 20 m to 200 m, the tightest *apparent* bearing requirement is $2 \text{ cm} / 200 \text{ m} = 20.6 \text{ arcsec}$, which is the value

maintained in previous TPF-I requirement tables. However, at 20 m the 2 cm-requirement translates into a bearing requirement of 206 arcsec. The 20 arcsec number was adopted as a requirement because it is the tightest bearing if you specify requirements by range and bearing. However, *it is not an actual requirement*.

There is a caveat: the FSMs must have sufficient stroke to cover the range of inter-spacecraft bearings derived from the ODL stroke-limits. If the bearing performance resulting from ODL-derived requirements were large, then an additional bearing requirement would be needed so that FSM stroke-limits are not exceeded. FSMs are available with several degree fields-of-regard whereas only ~ 5 arcmin is needed.

Formation requirement stated imprecisely in terms of range and bearing results in different “control volumes” as spacecraft separation varies.



Formation requirement stated precisely gives “control volume” that is independent of spacecraft separation.

Figure C.1. Illustration of Formation Control Requirements. Only dr is needed.