

## APPENDIX 8. SAMPLE CASE

A sample case is included with the description of the program for three reasons. First, it demonstrates the use of the program. Second, it illustrates the three types of output available (printout, punched cards, and ray path plots). Finally, it serves as a test case to verify that the user's copy of the program is running correctly. This last point is especially important if the user has had to make many modifications in converting the program to run on a computer other than a CDC 3800.

Although the ionospheric models in the sample case demonstrate the use of the program, they don't give realistic absorption for the radio waves. The absorption in the sample case is too low for two reasons. First, although the Chapman layer has a realistic electron density for the F region, it has much too low an electron density for the D region, where most of the absorption occurs. Second, the collision frequency profile in the sample case is designed for use with the Sen-Wyller formula for refractive index rather than the Appleton-Hartree formula used in the sample case. Multiplying the collision frequency profile in the sample case by 2.5 gives an effective collision frequency profile for use with the Appleton-Hartree formula that will give nearly the correct absorption for HF radio waves (Davies, 1965, p. 89).

### Appendix 8a. Input Parameter Forms for the Sample Case

Filled-out input parameter forms are included to describe the sample case (i. e., show what ray paths are requested for which ionospheric models and what type of output is wanted). Furthermore, comparing them with Appendix 8b illustrates the relationship between the forms and the input data cards.

INPUT PARAMETER FORM FOR THREE-DIMENSIONAL RAY PATHS

Name \_\_\_\_\_ Project No. \_\_\_\_\_ Date \_\_\_\_\_

Ionospheric ID (3 characters) X01

Title (75 characters) Test Case

Models:	Electron density	<u>CHAPX</u>
	Perturbation	<u>WAVE</u>
	Magnetic field	<u>DIPOLY</u>
	Ordinary	(W1 = + 1.)
	Extraordinary	<u>✓</u> (W1 = - 1.)
	Collision frequency	<u>EXPZ2</u>
Transmitter:	Height	<u>0</u> km, nautical miles, feet (W3)
	Latitude	<u>40</u> rad, <u>deg</u> km (W4)
	Longitude	<u>-105</u> rad, <u>deg</u> km (W5)
	Frequency, initial	<u>6</u> MHz (W7)
	final	(W8)
	step	(W9)
	Azimuth angle, initial	<u>45</u> rad, <u>deg</u> clockwise of north (W11)
	final	(W12)
	step	(W13)
	Elevation angle, initial	<u>0</u> rad, <u>deg</u> (W15)
	final	<u>90</u> (W16)
	step	<u>15</u> (W17)
Receiver:	Height	<u>200</u> km, nautical miles, feet (W20)
Penetrating rays:	Wanted	<u>✓</u> (W21 = 0.)
	Not wanted	<u>      </u> (W21 = 1.)
Maximum number of hops		<u>3</u> (W22)
Maximum number of steps per hop		<u>1000</u> (W23)
Maximum allowable error per step		<u>10<sup>-4</sup></u> (W42)
Additional calculations:		= 1. to integrate = 2. to integrate and print
Phase path		<u>2</u> (W57)
Absorption		<u>2</u> (W58)
Doppler shift		<u>      </u> (W59)
Path length		<u>      </u> (W60)
Other		<u>      </u>
		<u>      </u>
		<u>      </u>

Printout: Every 5 steps of the ray trace (W71)

Punched cards (raysets): ✓ (W72 = 1.)

INPUT PARAMETER FORM FOR PLOTTING THE PROJECTION  
OF THE RAY PATH ON A VERTICAL PLANE

Coordinates of the left edge of the graph:

Latitude = 40. rad  
(deg) north (W83)  
km

Longitude = -105. rad  
(deg) east (W84)  
km

Coordinates of the right edge of the graph:

Latitude = 52.12 rad  
(deg) north (W85)  
km

Longitude = -81.8 rad  
(deg) east (W86)  
km

Height above the ground of the bottom of the graph = 0. km (W88)

Distance between tic marks = 100. rad  
deg (W87)  
km

(W81 = 1.)

INPUT PARAMETER FORM FOR PLOTTING THE PROJECTION  
OF THE RAY PATH ON THE GROUND

Coordinates of the left edge of the graph:

Latitude = 40. rad  
(deg)  
km

Longitude = -105. rad  
(deg)  
km

Coordinates of the right edge of the graph:

Latitude = 52.12 rad  
(deg)  
km

Longitude = -81.8 rad  
(deg)  
km

Factor to expand lateral deviation scale by = 200. (W82)

Distance between tic marks on range scale = 100. rad  
deg  
(km) (W87)

(W81 = 2.)

## INPUT PARAMETER FORM FOR SUBROUTINE CHAPX

An ionospheric electron density model consisting of a Chapman layer with tilts, ripples, and gradients

$$\begin{aligned} f_N^2 &= f_c^2 \exp \left( \alpha (1 - z - e^{-z}) \right) \\ z &= \frac{h - h_{\max}}{H} \\ f_c^2 &= f_{co}^2 \left( 1 + A \sin \left( 2\pi \left( \theta - \frac{\pi}{2} \right) / B \right) + C \left( \theta - \frac{\pi}{2} \right) \right) \\ h_{\max} &= h_{\max_0} + E \left( \theta - \frac{\pi}{2} \right) R_0 \end{aligned}$$

$f_N$  is the plasma frequency

$h$  is the height above the ground

$R_0$  is the radius of the earth in km

and  $\theta$  is the colatitude in radians.

Specify:

Critical frequency at the equator,  $f_{co} = \underline{6.5}$  MHz (W101)

Height of the maximum electron density at the equator,  $h_{\max_0} = \underline{300}$  km (W102)

Scale height,  $H = \underline{62.}$  km (W103)

$\alpha = \underline{0.5}$  (W104, 0.5 for an  $\alpha$  Chapman layer, 1.0 for a  
g Chapman layer)

Amplitude of periodic variation of  $f_c^2$  with latitude,  $A = \underline{0.}$  (W105)

Period of variation of  $f_c^2$  with latitude,  $B = \underline{0.}$  rad  
deg (W106)  
km

Coefficient of linear variation of  $f_c^2$  with latitude,  $C = \underline{0.}$  rad $^{-1}$  (W107)

Tilt of the layer,  $E = \underline{0.}$  rad (W108)  
deg

INPUT PARAMETER FORM FOR SUBROUTINE WAVE

A perturbation to an ionospheric electron density model consisting of a "gravity-wave" irregularity traveling from north pole to south pole

$$N = N_0(1 + \Delta)$$

$$\Delta = \delta \exp - [(R - R_0 - z_0)/H]^2 .$$

$$\cos 2\pi \left[ t' + (\pi/2 - \theta) \frac{R_0}{\lambda_x} + (R - R_0)/\lambda_z \right]$$

$$\frac{\partial N}{\partial t} = \frac{-2\pi}{\lambda_x} V_x N_0 \delta \exp - [(R - R_0 - z_0)/H]^2 .$$

$$\sin 2\pi \left[ t' + (\pi/2 - \theta) \frac{R_0}{\lambda_x} + (R - R_0)/\lambda_z \right]$$

$R_0$  is the radius of the earth.

$R, \theta, \varphi$  are the spherical (earth-centered) polar coordinates  
 $(\Delta$  is independent of  $\varphi$ ).

$N_0(R, \theta, \varphi)$  is any electron density model.

Specify:

the height of maximum wave amplitude,  $z_0 = \underline{250}$  km (W151)

wave-amplitude "scale height,"  $H = \underline{100}$  km (W152)

wave perturbation amplitude,  $\delta = \underline{0.1}$  [0. to 1.] (W153)

horizontal trace velocity,  $V_x = \underline{\quad}$  km/sec (W154)  
 (needed only if Doppler shift is calculated)

horizontal wavelength,  $\lambda_x = \underline{100}$  km (W155)

vertical wavelength,  $\lambda_z = \underline{100}$  km (W156)

time in wave periods,  $t' = \underline{0.}$  [0. to 1.] (W157)

## INPUT PARAMETER FORM FOR SUBROUTINE DIPOLY

An ionospheric model of the earth's magnetic field consisting of an earth centered dipole

The gyrofrequency is given by:

$$f_H = f_{H_0} \left( \frac{R_0 + h}{R_0} \right)^3 \left( 1 + 3 \cos^2 \lambda \right)^{\frac{1}{2}}$$

The magnetic dip angle, I, is given by

$$\tan I = 2 \cot \lambda$$

h is the height above the ground

$R_0$  is the radius of the earth

$\lambda$  is the geomagnetic colatitude

Specify:

the gyrofrequency at the equator on the ground,  $f_{H_0} = \underline{0.8}$  MHz (W201)

the geographic coordinates of the north magnetic pole

latitude = 78.5 radians degrees north (W24)

longitude = 291. radians degrees east (W25)

## INPUT PARAMETER FORM FOR SUBROUTINE EXPZ 2

An ionospheric collision frequency model consisting of a double exponential profile

$$\nu = \nu_1 e^{-a_1(h-h_1)} + \nu_2 e^{-a_2(h-h_2)}$$

where  $h$  is the height above the ground.

Specify for the first exponential:

Collision frequency at height  $h_1$ ,  $\nu_1 = \underline{3.65 \times 10^4}$  collisions per second (W251)

Reference height,  $h_1 = \underline{100}$  km (W252)

Exponential decrease of  $\nu$  with height,  $a_1 = \underline{0.148}$   $\text{km}^{-1}$  (W253)

Specify for the second exponential:

Collision frequency at height  $h_2$ ,  $\nu_2 = \underline{30}$  collisions per second (W254)

Reference height,  $h_2 = \underline{140}$  km (W255)

Exponential decrease of  $\nu$  with height,  $a_2 = \underline{0.0183}$   $\text{km}^{-1}$  (W256)

## Appendix 8b. Listing of Input Cards for the Sample Case

```

1 0.          OF DUPLICATE W CARDS, THE LAST ONE DOMINATES
1 -1.          EXTRAORDINARY RAY
3 0.          TRANSMITTER HEIGHT, KM
4 40.          1  TRANSMITTER LATITUDE, DEG NORTH
5 -105.        1  TRANSMITTER LONGITUDE, DEG EAST
7 6.0          INITIAL FREQUENCY, MC/S
9 0.          DONT STEP FREQUENCY
11 45.0        1  INITIAL AZIMUTH ANGLE, DEGS CLOCKWISE FROM NORTH POLE
13 0.          DONT STEP AZIMUTH ANGLE
15 0.          1  INITIAL ELEVATION ANGLE, DEG
16 90.0        1  FINAL ELEVATION ANGLE, DEG
17 15.0        1  STEP IN ELEVATION ANGLE, DEG
20 200.        RECEIVER HEIGHT ABOVE THE EARTH, KM
22 3.          NUMBER OF HOPS
57 2.          INTEGRATE AND PRINT PHASE PATH
58 2.          INTEGRATE AND PRINT ABSORPTION
71 5.0          NUMBER OF STEPS FOR EACH PRINTING
72 1.          PUNCH RAYSETS
81 1.          PLOT PROJECTION OF RAY PATH ON A VERTICAL PLANE
83 40.0        1  LEFT LATITUDE OF PLOT, DEG
84 -105.        1  LEFT LONGITUDE OF PLOT, DEG
85 52.12        1  RIGHT LATITUDE OF PLOT, DEG
86 -81.8         1  RIGHT LONGITUDE OF PLOT, DEG
87 100.0        1  DISTANCE BETWEEN TIC MARKS, KM
101 6.5          CRITICAL FREQUENCY, MC/S
102 300.0        HMAX, KM
103 62.          SCALE HEIGHT, KM
104 0.5          ALPHA CHAPMAN LAYER
150 1.          CALL PERTURBATION SUBROUTINE
151 250.          Z0, KM
152 100.          SH, SCALE HEIGHT, KM
153 0.1          DELTA
155 100.          LAMBDA_X, HORIZONTAL WAVELENGTH, KM
156 100.          LAMBDA_Z, VERTICAL WAVELENGTH, KM
201 0.8          GYROFREQUENCY ON THE GROUND AT THE EQUATOR, MHZ
24 78.5          1  ACCEPTED STANDARD LAT. OF NORTH MAGNETIC POLE, DEG NORTH
25 291.          1  ACCEPTED STANDARD LONG. OF NORTH MAGNETIC POLE, DEG EAST
251 3.65          E4  COLLISION FREQUENCY AT H1, /SEC
252 100.0        H1, REFERENCE HEIGHT, KM
253 .148         A1, EXPONENTIAL DECREASE OF NU WITH HEIGHT, /KM
254 30.           COLLISION FREQUENCY AT H2, /SEC
255 140.          H2, REFERENCE HEIGHT, KM
256 .0183        A2, EXPONENTIAL DECREASE OF NU WITH HEIGHT, /KM
                  (A BLANK IN COL. 1-3 ENDS THE CURRENT W ARRAY)

X01 TEST CASE
71 0.          NO PERIODIC PRINTOUT
72 0.          DO NOT PUNCH RAYSETS
81 2.          PLOT PROJECTION OF RAY PATH ON THE GROUND
82 10.0         LATERAL DEVIATION EXPANSION FACTOR
                  (A BLANK IN COL. 1-3 ENDS THE CURRENT W ARRAY)

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Col. 1-3 Identification number

Col. 4-17 Data in E14.6 format

Col. 18 A 1 indicates an angle in degrees

Col. 19 A 1 indicates a central earth angle in kilometers

Col. 20 A 1 indicates a distance in nautical miles

Col. 21 A 1 indicates a distance in feet

Col. 22-24 Left for other conversions

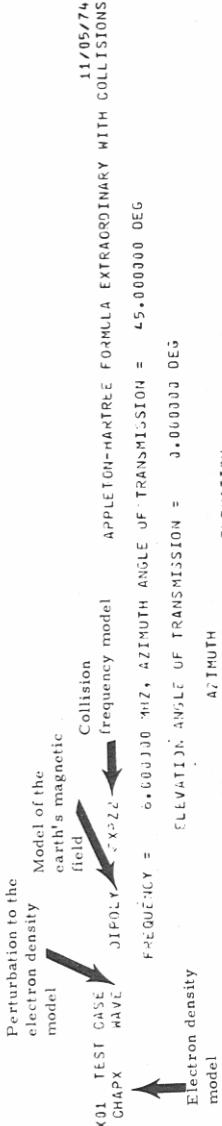
Col. 25-80 Description of the data

## Appendix 8c. Sample Printout

11/05/74

APPLETON-HARTREE FORMULA EXTRAORDINARY WITH COLLISIONS

X01 TEST CASE	CHAPX	CASE	WAVE	DIPOLY	FXPZ2	INITIAL VALUES FOR THE W ARRAY -- ALL ANGLES IN RADIANS, ONLY NONZERO VALUES PRINTED
1	-1.00000000000+000					
2	6.37000050000+003					
4	6.33131700803+001					
5	-1.33253571460+001					
7	6.00000000000+000					
11	7.83390103590-001					
10	1.570736326794000					
17	2.1793387791-001					
20	2.00000000000+002					
22	3.00000000000+000					
23	1.00000000000+003					
24	1.3700346280+000					
25	5.07890812331+000					
41	3.00000000000+000					
42	1.00000000000-004					
43	5.00000000000+000					
44	1.00000000000+001					
45	1.00000000000+002					
46	1.00000000000-008					
47	5.00000000000-001					
57	2.00000000000+000					
58	2.00000000000+000					
71	5.00000000000+000					
72	1.00000000000+000					
81	1.00000000000+000					
83	6.33131700803-001					
84	-1.33253571460-001					
85	9.09065605124-001					
86	-1.427619326134+000					
87	1.5598871273-002					
101	6.50000000000+000					
102	3.00000000000+002					
103	6.139999999995+001					
104	5.00000000000-001					
150	1.00000000000+000					
151	2.50000000000+002					
152	1.00000000000+002					
153	1.00000000000-001					
155	1.00000000000+002					
156	1.00000000000+002					
201	8.00000000000-J01					
251	3.650000000002+004					
252	1.00000000000J02					
253	1.46000000001-001					
254	3.00000000000-001					
255	1.339999999999-002					
256	1.833000000002-J02					



APPLETION-MARTRE FORMULA EXTRAORDINARY WITH COLLISIONS  
11/05/74

Collision frequency model

ELEVATION ANGLE OF TRANSMISSION = 3.060300 DEG

Height KM	Range KM	DEVIATION LOCAL DEG	ELEVATION XHQ LOCAL DEG	AZIMUTH		POLARIZATION REAL IMAG	GROUP PATH KM	PHASE PATH KM	ABSORPTION DB
				XHQ	LOCAL DEG				
0+000 XMTR TGN	0.0000	0.0000	0.000	0.000	-0.000	7.364	0.000	-1.000	0.0000
-3-011 F-UTR TGN	52.737	-1.87210	0.006	0.000	-0.000	7.797	0.513	-1.427	823.2593
53.4425	66.0000	-0.0000	-0.000	-0.000	0.000	7.797	0.513	-1.427	822.2563
54.1916	56.0962	-0.0000	-0.000	-0.000	0.000	7.6150	0.230	-2.386	912.2593
54.7839	24.52543	0.0000	-0.000	0.000	0.000	8.502	0.141	-2.599	952.2593
55.4755	10.3834	0.000	-0.000	-0.000	0.000	9.345	0.021	-3.200	104.2593
56.1675	8.5470	0.000	-0.000	0.000	0.000	10.039	0.004	-4.060	1128.2584
39.1450	11.16.8760	0.000	-0.000	-0.000	0.000	10.683	0.001	-5.656	1208.2593
-2-008	11.34.94	0.000	-0.000	-0.000	0.000	10.683	0.001	-5.656	1208.2567
-1-008	11.94.0737	0.000	-0.000	-0.000	0.000	10.683	0.001	-5.656	1208.2567
1.28.6479	1.27.11.132	0.000	-0.000	-0.000	0.000	10.999	0.001	-7.942	1288.2593
-1-008	1.28.6479	0.000	-0.000	-0.000	0.000	10.999	0.001	-7.942	1288.2593
-4-006	14.3.7556	1.34.7.7763	0.000	0.000	-0.078	9.958	0.003	-5.444	1368.2593
-7-006	15.3.1536	1.41.6.564	0.001	0.012	-0.269	6.649	0.000	-2.873	1440.2593
-9-006	12.7.2.033	1.54.4.683	0.011	0.051	-0.473	3.399	0.000	-2.083	1480.2593
-3-011 MIN DIST	1.91.1561	0.002	-0.029	-0.029	-0.000	0.000	-1.720	1518.9022	1512.7786
-3-011 4IN DIST	1.98.1469	0.002	-0.029	-0.029	-0.000	0.000	-1.720	1518.9022	1512.7786
-3-011 4IN DIST	1.98.1469	1.91.1561	0.002	-0.029	-0.029	0.000	-1.720	1518.9022	1512.7786
-6-011 WAVE REV	1.58.1177	1.93.4.9559	0.003	-0.030	-0.030	-0.736	-0.341	-1.695	1516.5009
-6-011 WAVE REV	1.51.1.539	1.53.3.3795	0.000	0.028	-1.756	-7.550	0.000	-1.385	1615.9022
-2-005	1.33.2.239	1.69.7.2028	0.007	0.024	-2.782	-10.588	0.003	-1.318	1684.9017
-3-005	1.68.1.392	1.61.3.4452	0.006	0.016	-4.736	-16.483	0.003	-1.341	1855.9022
-6-005	6.0.6837	1.59.0.039	0.004	0.015	-6.536	-9.113	0.003	-1.403	2015.9022
-8-119 EXIT ION	4.9.2235	21.86.5.2521	0.002	0.013	-8.572	-7.138	0.005	-1.093	2339.0.022
-8-003 EXIT ION	4.9.2235	2.30.0.4932	0.000	0.010	-13.042	0.738	0.001	-1.000	2955.+9.92
0+000 GND RRF	0.0000	4.18.0.8051	-0.003	0.008	-15.566	7.401	-0.001	-1.636	3688.5475
0+000 GND RRF	3.2.3936	3.34.0.6051	-0.003	0.008	-15.566	7.401	-0.001	-1.636	3688.5475
0+000 EXIT ION	53.4.395	3.54.0.738d	-0.003	0.008	-15.577	7.436	-0.001	-1.636	3700.+7.907
0+000 EXIT ION	31.11.954	3.92.1.3515	-0.003	0.008	-16.214	9.661	-0.004	-1.984	3957.7907
-9-008 MAX LAT	1.07.4072	3.38.1.1998	-0.003	0.008	-16.435	10.475	-0.000	-1.335	4053.7907
-1-006 WAVE REV	1.07.9.072	3.38.1.1358	-0.003	0.008	-16.576	10.907	-0.000	-1.765	4103.+5.117
-4-006	1.13.7.975	4.14.6.9652	-0.003	0.008	-16.914	9.263	-0.000	-1.668	4261.7907
-5-105	1.08.3.609	4.18.5.0294	-0.004	0.008	-17.169	4.688	-0.003	-2.901	4322.8067
-5-003	1.56.1.196	4.22.1.1682	-0.006	0.014	-17.169	4.688	-0.003	-2.901	4341.7907
3-000 MIN DIST	1.57.9.9516	4.335.0.842	-0.007	0.076	-17.366	-0.000	-0.000	-0.000	4369.8059

This ray calculation took 12.342 SEC

v<sup>\*</sup>

where v part (n<sup>2</sup>)

vector.

This quantity would be zero if there were no errors in the numerical integration.

v<sup>\*</sup> is the magnitude of the complex phase refractive index.

in degrees angle from great circle between transmitter and ray point.

Azimuth angle of current ray path point at the transmitter.

Angle of the wave normal with the local horizontal.

Elevation angle of current ray path point at the transmitter.

Azimuth angle of the wave normal between transmitter and ray point.

Azimuth angle of the wave normal along the ground.

Between circle distance between great circle between transmitter and ray point.

Great circle distance between ray point and the transmitter.

Angle of the wave normal with the local horizontal.

Polarization = ± means the electric field vector is rotating counter clockwise along the ray.

Polarization = ± means the electric field vector is rotating counter clockwise along the ray looking along the ray.

Angle of the wave normal with the local horizontal.

X01 TEST CASE  
CHAPX DIPOLY EXP72  
FREQUENCY = b.60000 MHZ, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG

ELEVATION ANGLE OF TRANSMISSION = 15.00000 DEG  
AZIMUTH DEVIATION ELEVATION POLARIZATION GROUP PATH PHASE PATH ABSORPTION  
HEIGHT XMTR LOCAL XMTR LOCAL REAL IMAG KM KM DB

	HEIGHT KM	RANGE KM	XMTR DEG	LOCAL DEG	ELEVATION DEG	POLARIZATION	GROUP KM	PATH KM	PHASE KM	PATH KM	ABSORPTION DB
0+000 XMTR	0.0000	186.0044	-0.0000	-0.0000	15.0000	16.0000	0.0001	-1.0000	0.0000	0.0000	0.0000
0+000 ENTR ION	32.0032	211.6243	-0.0000	-0.0000	15.0000	16.0000	3.1113	-3.3662	194.1401	194.1401	0.0000
0+000	60.7739	230.5627	-0.0000	-0.0000	15.0000	16.0000	2.3233	-7.4474	221.1401	221.1401	0.0000
0+000	66.5275	272.1042	-0.0000	-0.0000	15.0000	17.0074	1.297	-9.793	241.1401	241.1401	0.0000
-5+010	79.6832	309.7220	-0.0000	-0.0000	15.0000	17.447	0.369	-18.918	285.1401	285.1401	0.0001
-7+009	91.7830	347.1979	-0.0000	-0.0000	15.0000	17.785	0.355	-11.0019	325.1401	325.1401	0.0004
-2+008	104.1175	414.2867	-0.0000	-0.0000	15.0000	18.116	-0.015	29.1112	365.1401	365.1401	0.0111
-1+006	126.0616	433.2483	-0.0000	-0.0001	14.9930	18.525	-0.0000	10.310	437.1401	437.1401	0.0031
-3+005	151.4725	524.9617	-0.0000	-0.0012	14.841	16.907	-0.0001	-59.192	517.1401	517.1401	0.0049
-3+006	161.0111	561.6061	-0.0001	-0.0002	14.559	16.512	-0.0000	-4.495	557.1401	557.1401	0.0057
-1+005	169.1102	598.0253	-0.0006	-0.0078	14.015	8.049	0.0003	-2.160	597.1401	597.1401	0.0067
-3+005 MIN DIST	172.1418	604.1034	0.0015	0.0155	13.155	1.378	0.0000	-1.537	637.1401	637.1401	0.0079
-3+011 MIN DIST	172.1332	604.1034	0.015	0.134	12.975	0.000	0.000	-1.481	643.8528	643.8528	0.0081
-3+011 MIN DIST	172.1332	604.1034	0.015	0.164	12.975	0.000	0.000	-1.481	643.8528	643.8528	0.0081
2+010 WAVE REV	172.0659	607.7222	0.015	0.190	12.866	-0.320	0.000	-1.452	647.8528	647.8528	0.0083
-3+005	172.0827	706.9599	0.026	-0.078	8.942	-15.755	0.000	-1.173	756.8528	756.8528	0.0116
130.0051	750.9017	0.033	-0.036	5.835	-18.205	0.000	-1.154	836.8528	836.8528	0.0133	
105.0151	855.5089	0.037	-0.032	3.033	-17.862	0.000	-1.162	891.8528	891.8528	0.0160	
-3+005 EXIT ION	91.0547	330.6930	0.039	-0.030	0.752	-17.194	0.003	-1.174	996.8528	996.8528	0.0173
-3+005 EXIT ION	48.0333	1036.6779	0.042	-0.027	-1.943	-16.239	0.076	-1.037	1108.8528	1108.8528	0.0174
0+000 GRND REF	0.0000	1212.9251	0.046	-0.023	-5.455	14.656	-0.002	1.000	1292.1934	1292.1934	0.0174
-3+011 ENTR ION	52.0985	1+03.0+08	0.049	-0.020	-4.165	16.366	-1.306	1.085	1467.2614	1467.2614	0.0174
-3+011	54.0113	140.68464	0.049	-0.020	-4.142	16.400	-1.105	2.005	1490.3081	1490.3081	0.0174
-9+011	110.0072	1565.1016	0.052	-0.018	-3.213	17.986	-0.000	2.362	1683.3081	1683.3081	0.0191
-1+006	134.0337	1559.5945	0.052	-0.018	-2.890	18.138	-0.000	2.221	1763.3081	1763.3081	0.0214
-5+005	156.0113	1726.0642	0.052	-0.021	-2.688	15.432	-0.000	3.028	1835.3081	1835.3081	0.0226
-1+005	165.02114	1762.7028	0.051	-0.021	-2.675	11.173	-0.000	14.89	1875.3081	1875.3081	0.0237
-7+005	170.7731	1799.2958	0.054	-0.023	-2.779	5.562	0.003	-3.471	1935.3081	1935.3081	0.0248
0+000 MIN DIST	171.9566	1+26.6204	0.059	-0.065	-2.959	-0.000	0.003	-1.952	1947.4107	1947.4107	0.0258
THIS RAY CALCULATION TOOK 11.2+7 SEC											

X01 TEST CASE  
CHAPX WAVE DIPOLY EXPZ2  
FREQUENCY = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
ELEVATION ANGLE OF TRANSMISSION = 30.00000 DEG

APPLETON-HARRTREE FORMULA EXTRAORDINARY WITH COLLISIONS									
11/05/74									
AZIMUTH		DEVIATION		ELEVATION		POLARIZATION		PHASE PATH	
HEIGHT	RANGE	XMTX	LOCAL	XMTX	LOCAL	REAL	IMAG	GROUP PATH	PHASE PATH
KM	KM	DEG	DEG	DEG	DEG	0.0000	1.0000	KM	KM
3-011 XMTR ENTR ION	52.9739	0.0000	0.0000	-0.300	-0.000	30.000	-0.000	0.0000	0.0000
0+0.03 ENTR ION	52.9739	0.0000	0.0000	-0.300	-0.000	30.000	-0.000	104.6686	104.6686
-3-011 60.6694	102.6627	-0.000	-0.000	30.000	30.000	-0.332	-0.213	1.562	119.6686
0+0.00	111.1525	-0.000	-0.000	30.000	30.000	-0.000	-0.213	1.614	129.6686
-2-010 71.2077	131.4761	-0.000	-0.000	30.000	30.000	-0.110	-0.017	1.609	153.6686
-2-009 88.5857	148.3519	-0.000	-0.000	30.000	30.000	-0.004	-0.004	1.592	173.6686
-1-007 107.7766	178.5914	-0.000	-0.000	30.000	30.000	-0.000	-0.000	1.562	209.6686
-1-006 128.3954	211.9816	-0.000	-0.000	29.993	31.773	-0.000	-0.000	1.539	209.6686
5-005 149.2460	245.1205	-0.002	-0.009	29.935	31.083	-0.000	-0.000	1.574	249.6686
-2-005 168.5912	277.9003	-0.111	-0.168	27.599	29.657	-0.000	-0.000	1.895	289.6686
2-005 164.0395	310.3608	-0.016	-0.029	28.909	19.956	-0.000	-0.000	7.331	329.6686
1-005 191.3569	342.2014	-0.027	0.444	27.306	5.952	-0.000	-1.911	4.911	369.6686
0+0.00 MIN JIST	191.5641	354.9408	-0.023	0.219	26.398	-0.000	-0.000	4.25	390.0049
0+0.00 MIN JIST	191.5641	354.9408	-0.023	0.219	26.398	-0.000	-0.000	4.25	400.9514
0-0.00 HAVE REV	191.5641	358.1065	-0.020	0.137	26.154	-1.395	-0.000	-0.530	425.7924
4-006 172.2694	426.8860	0.135	-0.735	19.783	-23.513	-0.000	-1.475	429.7924	403.6919
2-005 135.6960	493.7148	0.235	-0.521	12.986	-29.961	-0.000	-0.113	514.7924	0.0125
2-005 95.7801	561.2775	0.298	-0.455	7.074	-29.718	-0.000	-1.076	594.7924	0.1477
2-005 56.5019	630.5940	0.348	-0.405	2.057	-29.100	-0.039	-1.062	674.7924	0.0172
2-005 46.7356	644.6611	0.357	-0.397	1.406	-28.375	-0.035	-1.017	754.7924	0.0177
-3-011 GND REF	73.3606	0.405	-0.349	-3.239	28.173	-0.000	-1.000	872.6850	822.6850
0+0.00 ENTR ION	52.9781	830.3382	0.446	-0.308	-0.104	29.043	-0.277	1.223	98.3256
-4-007 92.6896	930.1376	0.470	-0.284	1.779	29.671	-0.002	1.497	1064.4256	1014.0788
-2-005 132.5904	368.2234	0.490	-0.266	3.349	30.046	-0.000	1.461	1144.4256	1093.9864
-1-005 163.3870	1621.9170	0.501	-0.223	4.356	26.978	-0.000	1.628	1208.3256	1156.1125
-2-005 179.0552	1655.0139	0.507	-0.452	4.735	20.718	-1.003	2.556	124.8.3256	1191.4144
-9-006 186.6742	1C87.7704	0.511	0.102	4.784	9.433	-0.000	-4.108	128.8.2256	1222.7505
0+0.00 MIN DIST	103.8217	0.515	0.454	4.531	0.000	-0.000	-1.771	1312.8736	1240.1070
THIS RAY CALCULATION TOOK 8.642 SEC									

X01 TEST CASE  
CHAPX WAVE DIPOLY RXPZ2  
FREQUENCY = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
ELEVATION ANGLE OF TRANSMISSION = 45.00000 DEG

	HEIGHT	DANGE	DEVIATION	ELEVATION	POLARIZATION	GROUP PATH	PHASE PATH	ABSORPTION
	KM	XMTR LOCAL	XMTR LOCAL	DEG	REAL	KM	KM	DB
0+000 XMTR	0.0000	0.0000	-0.101	-0.000	45.000	-0.113	1.100	0.0000
0+000 ENTR ION	52.9759	52.3466	-0.101	-0.000	45.471	-0.153	1.207	0.0000
3-011 RCVR	62.2499	61.3530	-0.101	-0.000	45.552	-0.021	1.119	87.6128
6-000 ENTR ION	69.5926	68.2802	-0.101	-0.000	45.614	-0.002	1.217	97.6128
-3-009 RCVR	65.1331	63.4659	-0.100	-0.000	45.751	-0.000	1.199	119.6128
-4-008 APOGEE	39.4743	37.2070	-0.100	-0.000	45.873	-0.000	1.213	139.6125
-1-007 WAVE REV	113.433	110.8663	-0.100	-0.000	45.386	-0.000	1.209	159.6128
5-005 RCVR	142.4506	138.0429	-0.002	0.003	44.980	0.557	-0.000	0.0009
-2-005 RCVR	170.1037	164.7256	-0.111	-0.006	44.789	0.268	-0.000	1.0024
6-005 RCVR	193.2703	180.6257	-0.171	0.369	44.104	34.673	-0.000	237.3102
-3-011 RCVR	200.0000	200.2014	-0.132	0.607	43.622	28.430	-0.000	279.6128
2-006 APOGEE	209.8843	233.2593	-0.160	-1.930	40.436	4.780	-0.000	295.1649
-2-006 APOGEE	203.6634	235.8629	-0.046	-1.746	40.109	3.110	-0.000	278.4398
3-003 WAVE REV	209.4300	201.0959	0.921	-1.982	39.431	-0.266	-0.000	304.3962
3-037 RCVR	205.3618	259.5133	3.244	-2.015	36.819	-12.492	-0.000	352.1649
3-011 RCVR	200.0000	274.0000	3.3768	0.985	34.427	-23.456	-0.000	324.3166
1-005 RCVR	172.6329	311.8736	3.547	-0.183	27.233	-41.318	-0.000	41.042
4-005 RCVR	117.6520	366.4860	3.568	0.833	16.021	45.154	-0.000	41.041
6-005 RCVR	89.5472	394.2843	3.573	-0.833	11.932	-44.327	-0.000	54.776
6-005 RCVR	38.3026	444.9524	3.574	-0.527	2.976	-44.472	-0.000	58.7843
6-005 EXIT ION	36.3026	-44.9524	0.574	-0.027	2.978	-44.472	-0.000	49.9453
0+00 GRND REF	0.0000	484.7060	0.575	-0.125	-2.180	44.114	-0.000	1.119
0+000 ENTR ION	52.9177	538.6662	0.578	-0.322	3.168	44.599	-9.105	1.694
-6-007 RCVR	110.1068	535.3574	0.581	-0.120	7.705	45.103	-0.000	1.196
-6-007 RCVR	138.4237	622.5739	0.581	-0.016	9.586	45.095	-0.000	1.194
-4-006 RCVR	165.81750	650.1889	0.579	-0.068	11.199	42.389	-0.000	1.230
7-005 RCVR	189.935	576.6832	0.572	0.557	12.376	35.011	-0.000	1.434
-3-011 RCVR	200.0000	531.5163	0.548	0.996	12.769	26.353	-0.000	2.159
THIS RAY CALCULATION TOOK 10.310 SEC								
THIS RAY CALCULATION TOOK 1015.8617 SEC								

XJ1 TEST CASE  
CHApx WAVE VIPOLY FREQZ2  
FREQUENCY = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
ELEVATION ANGLE OF TRANSMISSION = 60.00000 DEG

APPLETON-HARTREE FORMULA EXTRAGORDINARY WITH COLLISIONS  
11/05/74

HEIGHT KM	RANGE KM		AZIMUTH DEVIATION XMTX LOCAL DEG		ELEVATION XMTX LOCAL DEG		POLARIZATION REAL IMAG	GROUP PATH KM	PHASE PATH KM	ABSORPTION DB
	XMTR	DEG	XMTR	DEG	XMTR	DEG				
0+000 XMTR ION	0.0000	30.936	-0.1100	-0.300	0.0000	60.272	-0.003	1.000	0.0000	0.0000
0+000 ENTR ION	52.9788	34.2236	-0.0500	-0.000	0.0000	60.308	-0.035	1.049	61.0908	61.0908
0+000 ENTR ION	59.9272	38.6347	-0.1000	-0.000	0.0000	60.348	-0.012	1.092	69.0908	69.0908
0+000 ENTR ION	67.7470	48.5990	-0.0500	-0.000	0.0000	60.388	-0.001	1.103	78.0908	78.0908
-7-019 35.1354	58.1107	-0.500	-0.0000	0.0000	50.435	-0.001	1.103	98.0908	98.0908	
-1-017 102.5337	67.7696	-0.0000	-0.0000	0.0000	60.522	-0.000	1.101	118.0904	118.0904	
-4-017 119.9525	85.6342	-0.0000	-0.0000	0.0000	60.592	-0.000	1.100	138.0820	138.0820	
-4-016 136.1635	105.2175	-0.007	-0.005	59.957	60.149	-0.000	1.103	177.0563	177.0563	
4+015 200.0000	114.4162	-0.094	0.088	59.897	55.830	-0.000	1.158	218.0908	211.9329	
9-015 224.6062	137.5936	-0.157	-0.851	59.325	50.578	-0.003	1.250	239.2552	235.6343	
-1-014 APOGEE	225.8382	146.6930	-0.234	0.797	57.441	24.698	-0.000	5.656	248.1596	
-1-014 WAVE REV	225.8382	146.6930	-0.354	5.402	55.872	-5.298	-0.000	324.2552	253.2681	
-1-014 WAVE REV	225.8382	146.6930	-0.354	5.402	55.872	-5.298	-0.000	324.2552	253.2681	
-1-014 WAVE REV	221.4155	153.9714	-0.522	9.624	54.028	-33.727	-0.000	324.2552	253.2681	
-3-005 20+2335	166.0800	-1.210	16.099	49.687	-60.227	-0.000	1.188	348.2552	347.1925	
0+000 RCVR	166.1639	-1.383	16.376	48.744	-62.499	-0.000	1.030	388.2552	269.8039	
-1-005 153.9530	185.8715	-3.275	16.994	38.460	-59.419	-0.000	1.025	395.1225	273.3158	
-4-005 116.7265	198.8446	-4.206	15.804	29.230	-68.701	-0.003	1.013	452.1225	318.1391	
-2-015 73.2276	212.0602	-5.215	14.796	19.415	-69.586	-0.000	1.013	492.1225	357.6180	
-2-015 EXIT ION	236.9190	-0.447	13.564	5.561	-69.411	-0.000	1.000	532.1225	397.6124	
0+000 GRND REF	0.0000	240.7118	-7.005	13.003	-1.003	69.320	-0.000	1.000	588.1225	453.6124
-3-011 ENTR ION	52.9836	260.0662	-7.392	12.021	10.239	69.499	-0.020	1.025	616.7330	482.2229
-3-011 ENTR ION	56.7354	261.4245	-8.355	11.957	11.015	69.511	-0.023	1.038	677.3376	538.8275
-3-015 113.9101	281.9769	-8.339	11.075	20.549	69.695	-0.000	1.050	738.3376	542.8275	
6-005 151.2131	295.2551	-3.446	10.601	25.546	69.477	-0.000	1.051	603.8243	603.8243	
-4-005 105.7563	308.0424	-9.310	9.231	29.355	66.600	-0.000	1.071	778.3376	643.4278	
0+000 RCVR	210.0000	313.9111	-10.115	8.555	30.682	63.564	-0.000	1.093	837.7013	678.2033
										691.0808
										0.0271

X01 TEST CASE EXP22  
 CHAPX DIFOLY ELEVATION = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
 FREQUENCY = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
 ELEVATION ANGLE OF TRANSMISSION = 75.00000 DEG

	HEIGHT	RANGE	AZIMUTH	DEVIATION	ELEVATION	POLARIZATION	GROUP PATH	PHASE PATH	ABSORPTION
	KM	KM	XMT	LOCAL	XMT	REAL	KM	KM	OB
	0.0000	0.0000	DEG	DEG	DEG	IMAG	0.0000	0.0000	0.0000
0+000 XMTR	52.9446	14.0759	-0.0000	-0.0000	75.000	1.000	54.8374	54.8374	0.0000
0+000 ENTR ION	52.7161	16.1100	-0.0000	-0.0000	75.000	1.044	62.3374	62.3374	0.0000
-3+011	65.5439	11.3768	-0.0000	-0.0000	75.000	1.044	67.8374	67.8374	0.0000
-3+011	67.7850	23.1909	-0.0000	-0.0000	75.000	1.047	67.8374	67.8374	0.0000
-2+006	147.1237	28.2124	-0.0000	-0.0000	75.000	1.048	90.8374	90.8374	0.0001
-1+007	145.4556	33.2025	-0.0001	-0.0000	75.000	1.047	110.8365	110.8365	0.0005
-9+007	145.6921	38.1498	-0.0007	-0.012	74.934	1.046	130.8374	130.8374	0.0013
4+007	178.7737	44.6081	-0.062	-0.321	74.922	1.047	150.8374	150.8374	0.0019
3+005 RCVR	226.1016	52.6875	-0.362	1.334	74.783	1.057	183.5011	183.5011	0.0030
6+005	224.94+0	60.4669	-1.077	1.370	74.379	1.057	213.9181	213.9181	0.0046
1+004 APOGEE	230.7936	66.1625	-1.711	-7.396	73.332	1.058	266.9181	266.9181	0.0091
9+002 WAVE REV	230.2593	70.7664	-9.322	-11.181	73.111	1.058	220.0213	220.0213	0.0127
5+005	222.0226	4.2620	1.343	14.206	72.307	1.057	314.9181	314.9181	0.0134
0+000 RCVR	200.0000	10.6297	5.511	-13.543	72.307	1.050	330.9181	330.9181	0.0147
2+005	161.6693	13.46131	3.542	-11.276	49.256	1.057	228.5798	228.5798	0.0187
-2+005	129.015	155.6964	10.092	-9.754	38.661	1.057	24.2747	24.2747	0.0232
-3+006	35.3732	177.1805	1.1285	-8.562	27.405	1.057	434.9673	434.9673	0.0263
-1+006 EXIT ION	62.4974	199.9503	12.225	-7.620	16.463	1.057	491.9673	491.9673	0.0275
*1+006 GRNL REF	29.3420	220.9908	12.292	-6.356	6.551	1.057	531.9673	531.9673	0.0275
0+000 ENTR ION	52.9836	244.7569	13.557	-8.291	-1.083	1.050	571.9673	571.9673	0.0292
-8+003	67.0257	239.8465	14.370	-5.473	9.365	1.064	631.9673	631.9673	0.0293
-6+006	120.3197	320.5884	15.12P	-4.721	18.948	1.130	632.4263	632.4263	0.0303
2+005	153.3776	344.0624	15.42	-4.425	22.353	1.135	672.4963	672.4963	0.0314
4+005	183.3941	362.9372	15.675	-4.214	24.915	1.195	705.8795	705.8795	0.0327
-3+011 RCVR	200.0006	375.3567	15.94	-3.64	25.987	1.374	937.9577	937.9577	0.0343
					45.376	-0.000			
					9.624 SEC		THIS RAY CALCULATION TOOK		

X01 TEST CASE  
 CHAPX JIPJLY RX2Z2  
 FREQUENCY = 1.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
 ELEVATION ANGLE OF TRANSMISSION = 90.00000 DEG

AZIMUTH DEVIATION	ELEVATION			POLARIZATION REAL IMAG	GROUP PATH KM	PHASE PATH KM	ABSORPTION DB
	XMR KM	LOCAL DEG	XMR DEG				
0+0.000 YMTR	0.00066		90.00000	-6.0003	0.0000	0.0000	0.0000
-3-0.11 ENTR ION	52.1938	+0.000	90.00000	-0.0009	1.009	52.9908	52.9908
-3-0.11 MAX LAT	54.1938	+0.000	90.00000	-0.0003	1.012	54.9908	54.9908
-3-0.11	50.1938	+0.000	90.00000	-0.0003	1.012	56.9908	56.9908
-6-0.11	62.1938	+0.000	90.00000	-0.0004	1.018	62.4908	62.4908
-9-0.11	64.1938	+0.000	90.00000	-0.0003	1.018	64.9908	64.9908
-6-0.11	67.1938	+0.000	90.00000	-0.0002	1.018	67.4908	67.4908
-6-0.11 WAVE REV	69.1938	+0.000	90.00000	-0.0002	1.019	69.2408	69.2408
-6-0.11	69.1408	+0.000	90.00000	-0.0002	1.019	69.2408	69.2408
-6-0.11	71.1408	+0.000	90.00000	-0.0001	1.019	71.1408	71.1408
-3-0.11	74.2408	+0.000	90.00000	-0.0001	1.019	74.2408	74.2408
-3-0.11	76.7408	+0.000	90.00000	-0.0001	1.019	76.7408	76.7408
-6-0.11	79.1408	+0.000	90.00000	-0.0001	1.019	79.2408	79.2408
-9-0.11	84.1408	+0.000	90.00000	-0.0001	1.019	84.2408	84.2408
-2-0.10	89.1408	+0.000	90.00000	-0.0001	1.019	89.2408	89.2408
-3-0.10	94.1408	+0.000	90.00000	-0.0000	1.018	94.2407	94.2407
-1-0.09	105.2405	+0.000	90.00000	-0.0000	1.018	105.2402	105.2402
-1-0.09	110.2405	+0.001	145.186-179.920	30.000	-0.0003	110.2408	110.2408
-2-0.09	110.1405	+0.000	145.186-179.920	30.000	-0.0003	110.2408	110.2408
-3-0.09	115.1405	+0.000	145.186-179.920	30.000	-0.0003	115.370	115.370
-3-0.09 WAVE REV	119.1365	+0.0003	145.262	0.0004	30.000	-0.0003	119.7048
-3-0.09	120.7358	+0.0003	145.262	0.0006	30.000	-0.0003	120.7318
-4+0.09	125.7304	+0.0007	145.269	-0.0003	30.000	-0.0000	125.7220
-4-0.09	138.6856	+0.039	145.265	0.0001	39.198	-0.0000	138.6413
-9-0.08	148.8779	+0.121	145.266	0.0000	89.198	-0.0000	148.8476
-3-0.07	158.3272	+0.318	145.266	-0.0000	39.988	-0.0000	158.7048
-3-0.07	167.8234	+0.0700	145.266	0.0000	89.970	-0.0000	157.9965
2-0.07 HAVE REV	175.1532	+0.1157	145.260-180.000	39.961	-0.0003	175.3276	175.3276
2-0.07	176.9406	+0.1263	145.266-180.000	39.957	-0.0000	176.7048	176.7048
-1-0.16	192.0775	+0.2533	145.266-180.000	89.322	-0.0000	198.6768	198.6768
0+0.00 RCVR	200.4000	+0.3028	145.266-180.000	89.411	-0.0000	207.1658	194.9665
4-0.05	218.5537	+0.318	145.266	-0.0000	89.893	-0.0000	148.7048
3-0.06	227.9866	+0.7709	145.266-180.000	39.799	-0.0000	158.7048	157.9965
4-0-06 HAVE REV	230.2098	+0.9818	145.250	0.0000	93.747	-0.0000	168.7048
-4-0-04	237.1654	+2.6623	145.266	0.0000	89.33	-0.0000	167.7048
-3-0-03 WAVE REV	238.3305	+3.6109	145.266	0.0000	89.099	-0.0000	173.0000
-2-0-03 APODEE	233.0227	+4.0332	145.266	-0.0000	88.978	-0.0000	175.573
-4-0-04	236.0571	+5.1869	145.266	0.0000	38.696	-0.0000	188.7408
-2-0-05	221.3800	+9.3361	145.266	0.0000	87.375	-0.0000	207.1658
-6-0-11 RCVR	200.0000	+15.3973	145.260	0.0000	85.460	-0.0000	236.1658
-2-0-05	151.1549	+21.7623	145.266	0.0000	80.469	-0.0000	213.0202
-1-0-05	112.0674	+32.1385	145.266	0.0000	73.720	-0.0000	215.9535
2-0-06 EXIT ION	25.6774	+39.6085	145.266	0.0000	61.133	-0.0000	322.5369
-3-0-11 GRND REF	0+0.00	+48.6937	145.266	0.0000	27.535	-0.0002	362.5365
-3-0-11 ENTR ION	52.1956	+53.7013	145.266	0.0000	-0.242	-0.0001	410.5365
-6-0-11	63.1934	+54.5266	0.0000	39.224	79.011	-0.0003	622.2176
-1-0-07	85.3955	+70.2016	-145.266	0.0000	50.073	-0.0003	436.6971
-2-0-05	121+0.623	+77.6+23	-145.256	0.0000	57.484	-0.0000	410.5365
3-0-05	103.2840	+86.+9935	-145.266	0.0000	51.819	-0.0003	563.6739
-3-0-06	197.1502	+32.0417	-145.256	0.0000	54.210	-0.0006	602.5108
0+0-06 RCVR	32.716-145.256	+0.003	-0.368	-0.0000	77.233	-0.0000	633.2002
					13.937 SEC		0.0300
					THIS RAY CALCULATION TOOK		0.0300

X01 TEST CASE      DIFOLY      RXFZ2  
 GRAPX      WAVE  
 INITIAL VALUES FOR THE WAVEFUNCTION - ALL ANGLES IN RADIANS, ONLY NONZERO VALUES PRINTED  
 11/05/74  
 APPLETON-HARTREE FORMULA EXTRAORDINARY WITH COLLISIONS

1 -1.00000000000+000  
 2 5.37000000000+003  
 4 6.381517000503+001  
 5 -1.33259571460+000  
 7 6.00000000000+000  
 11 7.85359163390+001  
 16 1.57073632679+000  
 17 2.61799367791+001  
 20 2.00000000000+002  
 22 3.00000000000+000  
 23 1.00000000000+003  
 24 1.37006369280+000  
 25 5.37893812331+001  
 41 3.00000000000+000  
 42 1.00000000000-004  
 43 5.00000000000+001  
 44 1.00000000000+000  
 45 1.00000000000-002  
 46 1.00000000000-006  
 47 5.00000000000-001  
 57 2.00000000000+000  
 58 2.00000000000+000  
 71 1.00000000000+003  
 81 2.00000000000+000  
 82 1.00000000000-001  
 83 6.98131700063-001  
 84 -1.83259571460+000  
 85 9.0366566124-001  
 86 -1.42767932613+000  
 87 1.56395581273-002  
 101 6.50000000000+000  
 102 3.00000000000+002  
 103 6.139399399395+001  
 104 5.00000000000-001  
 150 1.00000000000+000  
 151 2.50000000000+000  
 152 1.00000000000-002  
 153 1.00000000000-001  
 155 1.00000000000+002  
 156 1.00000000000+002  
 201 8.00000000000-001  
 251 3.65000000000+004  
 252 1.00000000000+002  
 253 1.48000000000-001  
 254 3.00000000000+001  
 255 1.33995999999+002  
 256 1.93000630002-002

X01 TEST CASE  
CHAPX WAVE DIFOLY FXPZ2 APPLETOM-HARTREE FORMULA EXTRAORDINARY WITH COLLISIONS

FREQUENCY = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG

ELEVATION ANGLE OF TRANSMISSION = 0.00000 DEG

	HEIGHT KM	RANGE KM	AZIMUTH DEVIATION DEG	ELEVATION XMR LOCAL DEG	POLARIZATION REAL IMAG	GROUP PATH KM	PHASE PATH KM	ABSORPTION DB
0+000 XMR ION	52.9737	518.7210	0.0000	-0.0000	0.0000	0.0000	-1.0000	0.0000
-3-011 ENTR ION	52.9737	1.91.1561	0.102	-0.029	-0.753	0.597	-1.427	823.2533
-3-011 MIN DIST	158.1469	1.91.1561	0.002	-0.029	-0.753	0.000	-1.720	1518.9022
-3-011 MIN DIST	158.1469	1.91.1561	0.003	-0.039	-0.716	-0.341	0.000	1518.9022
-6-011 WAVE REV	158.1177	1.91.9559	0.003	-0.039	-0.716	-0.341	0.000	1518.7766
8-006 EXIT ION	49.2239	218.5251	0.003	0.013	-8.572	-7.138	0.205	1522.9022
0+000 GRND REF	0.0000	2906.0482	-0.306	0.010	-13.042	-7.736	-1.093	1516.5809
0+000 ENTR ION	52.9737	3640.8051	-9.003	0.008	-15.566	7.401	-1.000	2227.6590
-1-005 MAX LAT	107.3072	3785.1998	-0.103	0.008	-16.45	10.475	1.636	2955.4329
-1-005 WAVE REV	107.3072	3785.1998	-0.002	0.008	-16.435	10.475	0.000	2943.2497
0+000 MIN DIST	157.3016	4305.0842	-0.007	0.076	-17.366	-10.475	-0.000	0.0220
			THIS RAY CALCULATION TIME	10.723 SEC				

ELEVATION ANGLE OF TRANSMISSION = 15.00000 DEG

	HEIGHT KM	RANGE KM	AZIMUTH DEVIATION DEG	ELEVATION XMR LOCAL DEG	POLARIZATION REAL IMAG	GROUP PATH KM	PHASE PATH KM	ABSORPTION DB
0+000 XMR ION	52.9737	172.1332	-0.300	-0.000	15.000	16.673	3.119	0.0000
-3-011 MIN DIST	172.1332	0.04.1034	0.015	0.184	12.975	0.000	-3.368	194.1401
-3-011 MIN DIST	172.1332	0.04.1034	0.015	0.164	12.375	0.000	-1.481	643.8528
-2-010 WAVE REV	172.0659	607.7222	0.015	0.196	12.864	-0.020	0.000	632.4672
-3-005 EXIT ION	48.0383	1036.879	0.042	-0.027	-11.983	-16.239	-1.452	0.0081
0+000 GRND REF	0.0000	1212.9251	0.046	-0.023	-5.455	14.656	-0.002	647.8328
-3-011 ENTR ION	52.9737	1403.0468	0.049	-0.020	-4.165	16.366	-1.306	1085.8358
0+000 MIN DIST	171.9560	1525.620+	0.059	-0.065	-22.559	-0.000	-1.952	1269.1466
			THIS RAY CALCULATION TIME	10.736 SEC				

X01 TEST CASE  
CHARX WAVE JIPOLY FXPZ2  
FREQUENCY = 0.00000 MHZ, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
ELEVATION ANGLE OF TRANSMISSION = 30.00000 DEG

AZIMUTH  
HEIGHT  
KM  
3-011 XMTR  
0.0000  
3-000 ENTR ION  
52.9739  
0+000 MIN DIST  
191.5641  
0+000 MIN OIST  
191.5641  
6-010 WAVE REV  
191.4065  
2-015 EXIT ION  
48.7352  
-3-011 GRND REF  
0.0000  
0+000 ENTR ION  
52.9741  
0+000 MIN DIST  
139.3217

RANGE  
KM  
89.9016  
354.9403  
354.9403  
358.1065  
44.46c1  
0.0000  
430.3562  
1107.3272  
139.3217

DEVIATION  
DEG  
-0.600  
-0.023  
-0.023  
-0.020  
0.137  
0.357  
0.405  
-0.308  
0.454  
0.454

XMT  
LOCAL  
DEG  
0.219  
0.219  
0.137  
0.397  
1.446  
-0.349  
-0.349  
-0.308  
0.581  
0.581

ELEVATION  
DEG  
30.000  
26.398  
26.398  
26.154  
1.446  
-0.349  
-0.349  
-0.308  
28.173  
28.173

POLARIZATION  
REAL  
IMAG  
-0.332  
0.000  
0.000  
-1.395  
-26.975  
-28.173  
-29.043  
0.000  
0.000

GROUP PATH  
KM  
1.000  
1.259  
1.530  
1.530  
0.000  
0.000  
0.000  
1.223  
1.223  
1.223

PHASE PATH  
KM  
104.6686  
425.7324  
425.7924  
429.7924  
770.7924  
720.5457  
872.6850  
822.3833  
933.0769  
0.0259

ABSORPTION  
DB  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000

ELEVATION ANGLE OF TRANSMISSION = 45.00000 DEG

AZIMUTH  
HEIGHT  
KM  
0.0000  
52.9759  
200.0000  
-3-011 RCVR  
209.6834  
2-015 APOGE  
209.43b0  
3-011 RCVR  
200.0000  
6-015 EXIT ION  
38.9028  
0+000 GRND REF  
3.0000  
0+000 ENTR ION  
52.9777  
-3-011 RCVR

RANGE  
KM  
52.9759  
200.2014  
0.0000  
-0.132  
0.607  
-0.146  
-1.746  
-1.746  
-1.382  
-1.415  
0.574  
0.576  
0.578  
0.542  
0.5163

DEVIATION  
DEG  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000  
-0.000

XMT  
LOCAL  
DEG  
45.000  
45.471  
3.622  
28.480  
3.110  
-0.266  
-23.456  
-44.472  
0.004  
-44.114  
44.599  
26.953  
12.7b9  
26.953  
-0.000

ELEVATION  
DEG  
-0.113  
1.100  
-0.000  
2.293  
-1.831  
-1.623  
-1.142  
-1.000  
-1.000  
1.000  
1.055  
1.094  
2.159  
0.000  
0.000

POLARIZATION  
REAL  
IMAG  
-0.000  
1.000  
-0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000  
0.000

GROUP PATH  
KM  
74.6128  
295.1649  
352.1649  
360.3649  
410.1543  
336.3372  
659.8543  
715.5626  
622.2214  
697.9980  
791.3397  
1015.3617  
905.3752

PHASE PATH  
KM  
0.0000  
74.6128  
278.4398  
306.3131  
310.1892  
410.1543  
336.3372  
566.5130  
715.5626  
622.2214  
697.9980  
791.3397  
1015.3617

ABSORPTION  
DB  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000  
0.0000

THIS RAY CALCULATION TOOK 9.813 SEC

X01 TEST CASE  
CHAPX DIPOLY FXYFZ2  
FREQUENCY = 6.00000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
ELEVATION ANGLE OF TRANSMISSION = 60.00000 DEG

APPLETON-HARTREE FORMULA EXTRAORDINARY WITH COLLISIONS  
11/05/74

	AZIMUTH	DEVIATION	ELEVATION	POLARIZATION	GROUP PATH	PHASE PATH	ABSORPTION
	XMT	XMT	XMT	REAL IMAG	KM	KM	DB
HEIGHT	KM	DEG	LOCAL DEG	LOCAL DEG	-0.000	1.000	0.0000
0+000 XMTR	0.0000	0.0000	0.0000	0.0000	60.000	1.049	61.0908
0+000 ENTR ION	52.9748	30.936	-0.000	60.000	60.272	-0.053	0.0000
0+000 RCVR	200.0000	1.14.412	-0.157	-0.851	59.325	-0.000	1.250
-1-004 APOGEE	225.8332	1.45.630	-0.354	5.402	55.872	-5.298	0.0002
-1-004 WAVE REV	225.8332	1.45.630	-0.354	5.402	55.872	-5.298	0.0002
0+000 RCVR	200.0030	1.68.1639	-1.383	1.376	48.744	-62.499	0.000
-2-005 EXIT ION	26.7751	2.30.9456	-6.447	1.3.564	5.561	-59.411	1.025
0+000 GRND REF	0.0000	240.7118	-7.009	13.033	-1.083	0.320	-0.000
-3-011 ENTR ION	52.9836	260.6662	-7.992	12.021	10.299	69.499	-0.026
0+000 RCVR	200.0030	313.9111	-10.115	8.555	10.632	03.564	-0.000
		THIS RAY CALCULATION TOOK			7.518 SEC	1.099	837.7013
		ELEVATION ANGLE OF TRANSMISSION = 75.00000 DEG					691.0808

	AZIMUTH	DEVIATION	ELEVATION	POLARIZATION	GROUP PATH	PHASE PATH	ABSORPTION
	XMT	XMT	XMT	REAL IMAG	KM	KM	DB
HEIGHT	KM	DEG	LOCAL DEG	LOCAL DEG	-0.000	1.000	0.0000
0+000 XMTR	0.0000	0.0000	0.000	-0.000	75.000	75.127	-0.024
0+000 ENTR ION	52.9846	14.0759	-0.000	75.000	71.357	-0.000	1.023
0+000 RCVR	200.0000	52.6875	-0.302	1.334	74.783	-0.000	1.023
-1-004 APOGEE	230.9183	57.9504	-1.511	-0.853	73.111	8.237	-3.876
9-005 WAVE REV	230.2533	70.7691	-0.322	-11.181	72.307	-4.474	0.000
0+000 RCVR	200.0000	106.6297	5.511	-13.543	61.084	-45.475	0.000
-1-006 EXIT ION	29.3420	220.9308	12.392	-6.856	6.551	-55.885	0.000
0+000 GRND REF	0.0000	240.7589	13.557	-0.291	-1.083	55.706	-0.000
0+000 ENTR ION	52.9836	276.4663	14.370	-5.479	9.565	56.027	-0.063
-3-011 RCVR	200.0000	375.3507	15.794	-3.644	25.987	45.376	-0.000
		THIS RAY CALCULATION TOOK			9.049 SEC	1.374	937.9577
		ELEVATION ANGLE OF TRANSMISSION = 75.00000 DEG					722.8911

X01 TEST CASE  
 CHAPX  
 WAVE DIPOLY EXPZZ  
 FREQUENCY = 0.60000 MHz, AZIMUTH ANGLE OF TRANSMISSION = 45.00000 DEG  
 ELEVATION ANGLE OF TRANSMISSION = 90.00000 DEG  
 APPLETON-HARTREE FORMULA EXTRAORDINARY WITH COLLISIONS  
 11/05/74

	HEIGHT	RANGE	AZIMUTH	ELEVATION	POLARIZATION	GROUP	PATH	PHASE	PATH	ABSORPTION
	KM	KM	XMTR LOCAL DEG	XMTR LOCAL DEG	REAL IMAG	KM	KM	PHASE	PATH	DB
0+0.00 XMTR	3.0000	0.0000	90.000 90.000	-0.003 1.009	0.0000 0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
-3-0.11 ENTR ION	52.9935	0.0000	90.000 90.000	-0.003 1.009	5.9908 5.9908	52.9908	52.9908	5.9908	5.9908	0.0000
-3-0.11 MAX LAT	54.9935	0.0000	90.000 90.000	-0.003 1.009	54.9908 54.9908	54.9908	54.9908	54.9908	54.9908	0.0000
-6-0.11 WAVE REV	6.2408	0.0000	90.000 90.000	-0.002 1.019	69.2408 69.2408	69.2408	69.2408	69.2408	69.2408	0.0000
-3-0.09 WAVE REV	1.197335	0.0003	-145.262 0.004	30.000 30.000	-0.000 1.018	119.7408	119.7408	119.7408	119.7408	0.0010
2-0.07 WAVE REV	1.751532	0.1157	-145.265-180.000	89.361 89.361	-0.003 1.021	173.9276	173.9276	173.9276	173.9276	0.0029
0+0.00 RCVR	2.00010	0.3028	-145.266-180.000	59.911 59.911	-0.000 1.030	207.1658	194.9665	194.9665	194.9665	0.0047
4-0.06 WAVE REV	2.332036	0.9313	-145.266 0.000	59.747 69.207	-0.000 1.052	262.1658	213.5202	213.5202	213.5202	0.0089
-3-0.03 WAVE REV	2.352305	3.6109	-145.266 0.000	99.099 -11.160	-0.003 4.505	310.1658	215.7522	215.7522	215.7522	0.0127
-2-0.03 APOGEE	2.380027	4.0933	-145.265 0.000	98.978 -33.291	0.003 -5.605	318.1658	215.8346	215.8346	215.8346	0.0134
-6-0.11 RCVR	2.33.0027	15.3973	-145.265 0.000	55.450 75.213	3.003 -1.080	411.0570	238.1693	238.1693	238.1693	0.0205
2-0.05 EXIT ION	25.667+0	48.6937	-145.266 0.000	27.353 -78.363	0.001 -1.009	59.6.0570	410.5365	410.5365	410.5365	0.0252
-3-0.11 GRND REF	0.00000	53.7019	-145.266 0.000	-0.242 78.918	-0.003 1.009	622.2176	436.6971	436.6971	436.6971	0.0252
-3-0.11 ENTR ION	52.9935	63.9944	-145.266 0.000	39.224 79.011	-0.003 1.003	676.2116	430.6911	430.6911	430.6911	0.0252
0+3.00 RCVR	2.33.0027	92.7123	-145.266 0.000	64.368 77.233	-0.003 1.006	833.2790	635.5670	635.5670	635.5670	0.0300
THIS DAY CALCULATION TOOK 13.161 SEC										

Appendix 8d. Listing of Punched Card Output (ray sets)  
for Sample Case

X01	TEST CASE						
CHAPX	6.500+000	3.000+002	6.200+001	5.000-001	0.000+000	0.000+000	0.000+000
WAVE	2.500+002	1.000+002	1.000-001	0.000+000	1.000+002	1.000+002	0.000+000
DIPOLY	8.000-001	0.000+000	0.000+000	0.000+000	0.000+000	0.000+000	0.000+000
EXPZ2	3.650+004	1.000+002	1.480-001	3.000+001	1.400+002	1.830-002	0.000+000
X01X	0	40000255000	2000000	60000	4500000	0	0 -1003T
1581469	14911561	2	-29	0	1514389	4513 -1610	11 0 0 -1721M
1581469	14911561	2	-29	0	1514389	4513 -1610	11 0 0 -1722M
1581469	29000482	-0	10	738	2875068	80425 68182	22 0 0 -1003G
1579016	43050842	-7	76	-0	4278561109482	91246	33 0 -0 9323M
X01X	0	40000255000	2000000	60000	4500000	1500000	0 -1003T
1721392	6041034	15	184	0	635731	8122 -3264	8 0 0 -1481M
1721392	6041034	15	184	0	635731	8122 -3264	8 0 0 -1482M
1721418	12129251	46	-23	14656	1211094	81100 58053	17 0 -0 1003G
1719566	18286204	59	-65	-0	1854769	92641 58123	26 0 0 -1953M
X01X	0	40000255000	2000000	60000	4500000	3000000	-0 1003T
1915641	3549408	-23	219	0	407964	17828 -7003	8 0 0 -1531M
1915641	3549408	-23	219	0	407964	17828 -7003	8 0 0 -1532M
1916346	7336080	405	-349	28173	733203139482	89236	18 0 -0 1003G
1898217	11075272	514	454	0	1138430174444101677		26 0 0 -1773M
X01X	0	40000255000	2000000	60000	4500000	4500000	-0 1003T
0	2002014	-132	607	28480	285194	9971 -6754	6 0 -0 2291R
2096843	2743788	389	-1415-23456	342980	67874	-6143	14 0 0 -1142R
2096843	4847060	576	-25	44114	484589230974137632		21 0 -0 1003G
0	6915163	548	796	26953	729880285982175495		27 0 -0 2163R
X01X	0	40000255000	2000000	60000	4500000	6000000	-0 1003T
0	1144182	-157	-851	50578	231305	7950 -5671	5 0 -0 1251R
2258382	1681639	-1383	16876-62499	262993132130	10323		17 0 0 -1032R
2258382	2407118	-7009	13003	69320	240697376036241525		22 0 -0 1003G
0	3139111-10115	8555	63564		376316461386314765		27 0 -0 1103R
X01X	0	40000255000	2000000	60000	4500000	7500000	-0 1003T
0	526875	-302	1334	71357	207034	6884 -4906	5 0 -0 1091R
2309183	1066297	5511-13543-46475			227435207533	21840	23 0 0 -1022R
2309183	2407589	13557	-6291	55706	240745446701245294		29 0 -0 1003G
0	3753507	15794	-3644	45376	430430507528292462		34 0 -0 1373R
X01X	0	40000255000	2000000	60000	4500000	9000000	-0 1003T
0	3028214734180000	88779	200000	7166	-5034	5 0 -0 1031R	
2382305	153973214734	0-75213	200610210447	37559		20 0 0 -1082R	
2382305	537019214734	0	78918	53702568516382995		25 0 -0 1003G	
0	927180214734	0	77233	221057612222414510		30 0 -0 1013R	

The first card is the title card.

The second card contains the name of the electron density model plus parameters W101-W107.

The third card contains the name of the perturbation model plus parameters W151-W157.

The fourth card contains the name of the magnetic field model plus parameters W201-W207.

The fifth card contains the name of the collision frequency model plus parameters W251-W257.

For description of remaining cards, see figures 1 and 2.

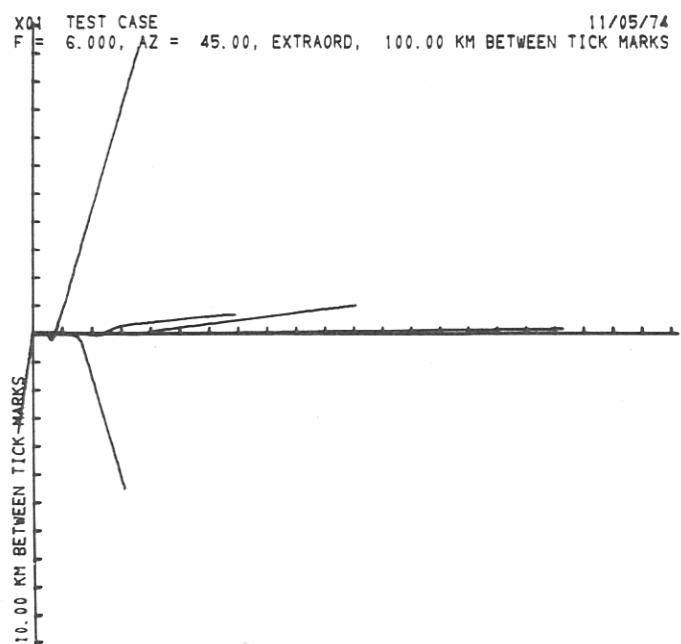
Appendix 8e. Ray Path Plots for Sample Case

Projection of raypath on vertical plane

X01 TEST CASE 11/05/74  
F = 6.000, AZ = 45.00, EXTRAORD, 100.00 KM BETWEEN TICK MARKS



Projection of raypath on ground for sample case





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7. AUTHOR(S)  R. Michael Jones and Judith J. Stephenson		9. Project/Task/Work Unit No.	
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<p>15. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here.)</p> <p>This report describes an accurate, versatile FORTRAN computer program for tracing rays through an anisotropic medium whose index of refraction varies continuously in three dimensions. Although developed to calculate the propagation of radio waves in the ionosphere, the program can be easily modified to do other types of ray tracing because of its organization into subroutine.</p> <p>The program can represent the refractive index by either the Appleton-Hartree or the Sen-Wyller formula, and has several ionospheric models for electron density perturbations to the electron density (irregularities), the earth's magnetic field and electron collision frequency.</p> <p>For each path, the program can calculate group path length, phase path length, absorption, Doppler shift due to a time-varying ionosphere, and geometrical path length. In addition to printing these parameters and the direction of the wave normal at various points along the ray path, the program can plot the projection of the ray path on any vertical plane or on the ground and punch the main characteristics of each ray path on cards.</p> <p>The documentation includes equations, flow charts, program listings with comments, definitions of program variables, deck set-ups, description of input and output, and a sample case.</p>			
<p>KEY WORDS:</p> <p>Appleton-Hartree formula; computer program; ionosphere; radio waves; ray tracing; Sen-Wyller formula; three-dimensional.</p>			
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